

Gretl User's Guide



Gnu Regression, Econometrics and Time-series Library

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Chapter 1

Introduction

1.1 Features at a glance

Gretl is an econometrics package, including a shared library, a command-line client program and a graphical user interface.

User-friendly Gretl offers an intuitive user interface; it is very easy to get up and running with econometric analysis. Thanks to its association with the econometrics textbooks by Ramu Ramanathan, Jeffrey Wooldridge, and James Stock and Mark Watson, the package offers many practice data files and command scripts. These are well annotated and accessible. Two other useful resources for gretl users are the available documentation and the [gretl-users](#) mailing list.

Flexible You can choose your preferred point on the spectrum from interactive point-and-click to complex scripting, and can easily combine these approaches.

Cross-platform Gretl's "home" platform is Linux but it is also available for MS Windows and Mac OS X, and should work on any unix-like system that has the appropriate basic libraries (see [Appendix B](#)).

Open source The full source code for gretl is available to anyone who wants to critique it, patch it, or extend it. See [Appendix B](#).

Sophisticated Gretl offers a full range of least-squares based estimators, either for single equations and for systems, including vector autoregressions and vector error correction models. Several specific maximum likelihood estimators (e.g. probit, ARIMA, GARCH) are also provided natively; more advanced estimation methods can be implemented by the user via generic maximum likelihood or nonlinear GMM.

Extensible Users can enhance gretl by writing their own functions and procedures in gretl's scripting language, which includes a wide range of matrix functions.

Accurate Gretl has been thoroughly tested on several benchmarks, among which the NIST reference datasets. See [Appendix C](#).

Internet ready Gretl can fetch materials such databases, collections of textbook datafiles and add-on packages over the internet.

International Gretl will produce its output in English, French, Italian, Spanish, Polish, Portuguese, German, Basque, Turkish, Russian, Albanian or Greek depending on your computer's native language setting.

1.2 Acknowledgements

The gretl code base originally derived from the program ESL ("Econometrics Software Library"), written by Professor Ramu Ramanathan of the University of California, San Diego. We are much in debt to Professor Ramanathan for making this code available under the GNU General Public Licence and for helping to steer gretl's early development.

We are also grateful to the authors of several econometrics textbooks for permission to package for gretl various datasets associated with their texts. This list currently includes William Greene, author of *Econometric Analysis*; Jeffrey Wooldridge (*Introductory Econometrics: A Modern Approach*); James Stock and Mark Watson (*Introduction to Econometrics*); Damodar Gujarati (*Basic Econometrics*); Russell Davidson and James MacKinnon (*Econometric Theory and Methods*); and Marno Verbeek (*A Guide to Modern Econometrics*).

GARCH estimation in gretl is based on code deposited in the archive of the *Journal of Applied Econometrics* by Professors Fiorentini, Calzolari and Panattoni, and the code to generate p -values for Dickey-Fuller tests is due to James MacKinnon. In each case we are grateful to the authors for permission to use their work.

With regard to the internationalization of gretl, thanks go to Ignacio Díaz-Emparanza (Spanish), Michel Robitaille and Florent Bresson (French), Cristian Rigamonti (Italian), Tadeusz Kufel and Pawel Kufel (Polish), Markus Hahn and Sven Schreiber (German), Hélio Guilherme and Henrique Andrade (Portuguese), Susan Orbe (Basque), Talha Yalta (Turkish) and Alexander Gedranovich (Russian).

Gretl has benefitted greatly from the work of numerous developers of free, open-source software: for specifics please see Appendix B. Our thanks are due to Richard Stallman of the Free Software Foundation, for his support of free software in general and for agreeing to “adopt” gretl as a GNU program in particular.

Many users of gretl have submitted useful suggestions and bug reports. In this connection particular thanks are due to Ignacio Díaz-Emparanza, Tadeusz Kufel, Pawel Kufel, Alan Isaac, Cri Rigamonti, Sven Schreiber, Talha Yalta, Andreas Rosenblad, and Dirk Eddebuettel, who maintains the gretl package for Debian GNU/Linux.

1.3 Installing the programs

Linux

On the Linux¹ platform you have the choice of compiling the gretl code yourself or making use of a pre-built package. Building gretl from the source is necessary if you want to access the development version or customize gretl to your needs, but this takes quite a few skills; most users will want to go for a pre-built package.

Some Linux distributions feature gretl as part of their standard offering: Debian, Ubuntu and Fedora, for example. If this is the case, all you need to do is install gretl through your package manager of choice. In addition the gretl webpage at <http://gretl.sourceforge.net> offers a “generic” package in rpm format for modern Linux systems.

If you prefer to compile your own (or are using a unix system for which pre-built packages are not available), instructions on building gretl can be found in Appendix B.

MS Windows

The MS Windows version comes as a self-extracting executable. Installation is just a matter of downloading `gretl_install.exe` and running this program. You will be prompted for a location to install the package.

Mac OS X

The Mac version comes as a gzipped disk image. Installation is a matter of downloading the image file, opening it in the Finder, and dragging `Gretl.app` to the Applications folder. However, when installing for the first time two prerequisite packages must be put in place first; details are given on the gretl website.

¹In this manual we use “Linux” as shorthand to refer to the GNU/Linux operating system. What is said herein about Linux mostly applies to other unix-type systems too, though some local modifications may be needed.

Part I

Running the program

Chapter 2

Getting started

2.1 Let's run a regression

This introduction is mostly angled towards the graphical client program; please see Chapter 51 below and the *Gretl Command Reference* for details on the command-line program, `gretlcli`.

You can supply the name of a data file to open as an argument to `gretl`, but for the moment let's not do that: just fire up the program.¹ You should see a main window (which will hold information on the data set but which is at first blank) and various menus, some of them disabled at first.

What can you do at this point? You can browse the supplied data files (or databases), open a data file, create a new data file, read the help items, or open a command script. For now let's browse the supplied data files. Under the File menu choose “Open data, Sample file”. A second notebook-type window will open, presenting the sets of data files supplied with the package (see Figure 2.1). Select the first tab, “Ramanathan”. The numbering of the files in this section corresponds to the chapter organization of [Ramanathan \(2002\)](#), which contains discussion of the analysis of these data. The data will be useful for practice purposes even without the text.

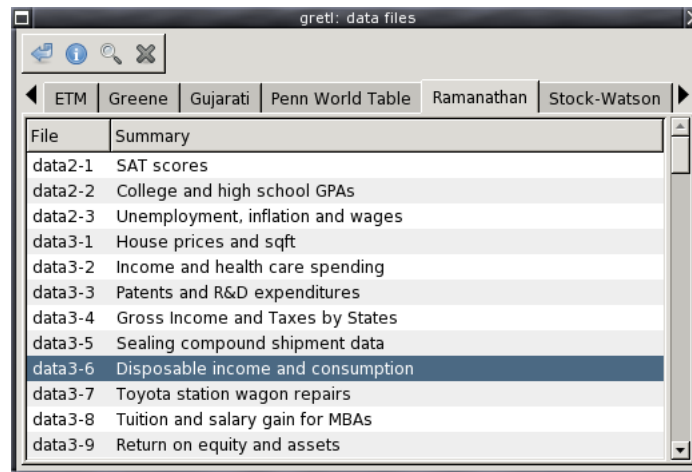



Figure 2.1: Practice data files window

If you select a row in this window and click on “Info” this opens a window showing information on the data set in question (for example, on the sources and definitions of the variables). If you find a file that is of interest, you may open it by clicking on “Open”, or just double-clicking on the file name. For the moment let's open data3-6.

 In `gretl` windows containing lists, double-clicking on a line launches a default action for the associated list entry: e.g. displaying the values of a data series, opening a file.

¹For convenience we refer to the graphical client program simply as `gretl` in this manual. Note, however, that the specific name of the program differs according to the computer platform. On Linux it is called `gretl_x11` while on MS Windows it is `gretl.exe`. On Linux systems a wrapper script named `gretl` is also installed — see also the *Gretl Command Reference*.

This file contains data pertaining to a classic econometric “chestnut”, the consumption function. The data window should now display the name of the current data file, the overall data range and sample range, and the names of the variables along with brief descriptive tags—see Figure 2.2.

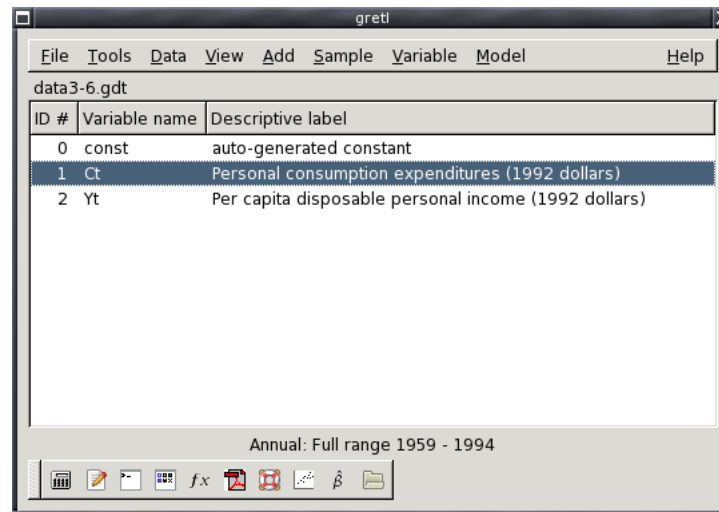


Figure 2.2: Main window, with a practice data file open

OK, what can we do now? Hopefully the various menu options should be fairly self explanatory. For now we’ll dip into the Model menu; a brief tour of all the main window menus is given in Section 2.3 below.

Gretl’s Model menu offers numerous various econometric estimation routines. The simplest and most standard is Ordinary Least Squares (OLS). Selecting OLS pops up a dialog box calling for a *model specification*—see Figure 2.3.

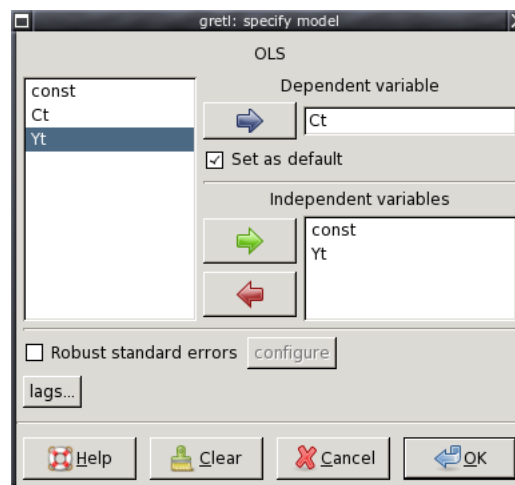


Figure 2.3: Model specification dialog

To select the dependent variable, highlight the variable you want in the list on the left and click the arrow that points to the Dependent variable slot. If you check the “Set as default” box this variable will be pre-selected as dependent when you next open the model dialog box. Shortcut: double-clicking on a variable on the left selects it as dependent and also sets it as the default. To select independent variables, highlight them on the left and click the green arrow (or right-click the

highlighted variable); to remove variables from the selected list, use the rad arrow. To select several variable in the list box, drag the mouse over them; to select several non-contiguous variables, hold down the **Ctrl** key and click on the variables you want. To run a regression with consumption as the dependent variable and income as independent, click **Ct** into the Dependent slot and add **Yt** to the Independent variables list.

2.2 Estimation output

Once you've specified a model, a window displaying the regression output will appear. The output is reasonably comprehensive and in a standard format (Figure 2.4).

	coefficient	std. error	t-ratio	p-value	
const	-384.105	151.330	-2.538	0.0159	**
Yt	0.932738	0.0106966	87.20	1.44e-41	***
Mean dependent var	12490.89	S.D. dependent var	2940.028		
Sum squared resid	1346750	S.E. of regression	199.0234		
R-squared	0.995548	Adjusted R-squared	0.995417		
F(1, 34)	7603.702	P-value(F)	1.44e-41		
Log-likelihood	-240.6161	Akaike criterion	485.2323		
Schwarz criterion	488.3993	Hannan-Quinn	486.3377		
rho	0.768301	Durbin-Watson	0.513696		

Figure 2.4: Model output window

The output window contains menus that allow you to inspect or graph the residuals and fitted values, and to run various diagnostic tests on the model.

For most models there is also an option to print the regression output in \LaTeX format. See Chapter 43 for details.

To import *gretl* output into a word processor, you may copy and paste from an output window, using its **Edit** menu (or **Copy** button, in some contexts) to the target program. Many (not all) *gretl* windows offer the option of copying in RTF (Microsoft's "Rich Text Format") or as \LaTeX . If you are pasting into a word processor, RTF may be a good option because the tabular formatting of the output is preserved.² Alternatively, you can save the output to a (plain text) file then import the file into the target program. When you finish a *gretl* session you are given the option of saving all the output from the session to a single file.

Note that on the *gnome* desktop and under MS Windows, the **File** menu includes a command to send the output directly to a printer.

☞ When pasting or importing plain text *gretl* output into a word processor, select a monospaced or typewriter-style font (e.g. Courier) to preserve the output's tabular formatting. Select a small font (10-point Courier should do) to prevent the output lines from being broken in the wrong place.

²Note that when you copy as RTF under MS Windows, Windows will only allow you to paste the material into applications that "understand" RTF. Thus you will be able to paste into MS Word, but not into notepad. Note also that there appears to be a bug in some versions of Windows, whereby the paste will not work properly unless the "target" application (e.g. MS Word) is already running prior to copying the material in question.

2.3 The main window menus

Reading left to right along the main window's menu bar, we find the File, Tools, Data, View, Add, Sample, Variable, Model and Help menus.



- File menu

- Open data: Open a native gretl data file or import from other formats. See Chapter 4.
- Append data: Add data to the current working data set, from a gretl data file, a comma-separated values file or a spreadsheet file.
- Save data: Save the currently open native gretl data file.
- Save data as: Write out the current data set in native format, with the option of using gzip data compression. See Chapter 4.
- Export data: Write out the current data set in Comma Separated Values (CSV) format, or the formats of GNU R or GNU Octave. See Chapter 4 and also Appendix D.
- Send to: Send the current data set as an e-mail attachment.
- New data set: Allows you to create a blank data set, ready for typing in values or for importing series from a database. See below for more on databases.
- Clear data set: Clear the current data set out of memory. Generally you don't have to do this (since opening a new data file automatically clears the old one) but sometimes it's useful.
- Working directory: Change the current working directory (or "workdir") and specify related options. For an explanation of the role of the workdir click the Help button in the dialog window which is presented, or refer to the documentation of the `set` command with the `workdir` option in the command reference.
- Script files: A "script" is a file containing a sequence of gretl commands. This item contains entries that let you open a script you have created previously ("User file"), open a sample script, or open an editor window in which you can create a new script.
- Session files: A "session" file contains a snapshot of a previous gretl session, including the data set used and any models or graphs that you saved. Under this item you can open a saved session or save the current session.
- Databases: Allows you to browse various large databases, either on your own computer or, if you are connected to the internet, on the gretl database server. See Section 4.2 for details.
- Function packages: Manage user-contributed function packages that extend gretl's capabilities. To learn more about such packages written in gretl's built-in matrix and scripting language "hansl", please refer to the "Packages" entry in Help menu.
- Resource from addon: Access example scripts and datafiles that are shipped as part of gretl's official "addons". (Addons are function packages that are more tightly integrated with the gretl program than standard user-contributed packages.)
- Exit: Quit the program. You'll be prompted to save any unsaved work.

- Tools menu

- Statistical tables: Look up critical values for commonly used distributions (normal or Gaussian, t , chi-square, F and Durbin-Watson).
- P-value finder: Look up p-values from the Gaussian, t , chi-square, F , gamma, binomial or Poisson distributions. See also the `pvalue` command in the *Gretl Command Reference*.

- **Distribution graphs:** Produce graphs of various probability distributions. In the resulting graph window, the pop-up menu includes an item “Add another curve”, which enables you to superimpose a further plot (for example, you can draw the t distribution with various different degrees of freedom).
 - **Test statistic calculator:** Calculate test statistics and p-values for a range of common hypothesis tests (population mean, variance and proportion; difference of means, variances and proportions).
 - **Nonparametric tests:** Calculate test statistics for various nonparametric tests (Sign test, Wilcoxon rank sum test, Wilcoxon signed rank test, Runs test).
 - **Seed for random numbers:** Set the seed for the random number generator (by default this is set based on the system time when the program is started).
 - **Command log:** Open a window containing a record of the commands executed so far.
 - **Gretl console:** Open a “console” window into which you can type commands as you would using the command-line program, `gretlcli` (as opposed to using point-and-click).
 - **Start Gnu R:** Start R (if it is installed on your system), and load a copy of the data set currently open in `gretl`. See Appendix D.
 - **Sort variables:** Rearrange the listing of variables in the main window, either by ID number or alphabetically by name.
 - **Function packages:** Handles “function packages” (see Section 14.5), which allow you to access functions written by other users and share the ones written by you.
 - **NIST test suite:** Check the numerical accuracy of `gretl` against the reference results for linear regression made available by the (US) National Institute of Standards and Technology.
 - **Preferences:** Set the paths to various files `gretl` needs to access. Choose the font in which `gretl` displays text output. Activate or suppress `gretl`’s messaging about the availability of program updates, and so on. See the *Gretl Command Reference* for further details.
- **Data menu**
 - **Select all:** Several menu items act upon those variables that are currently selected in the main window. This item lets you select all the variables.
 - **Display values:** Pops up a window with a simple (not editable) printout of the values of the selected variable or variables.
 - **Edit values:** Opens a spreadsheet window where you can edit the values of the selected variables.
 - **Add observations:** Gives a dialog box in which you can choose a number of observations to add at the end of the current dataset; for use with forecasting.
 - **Remove extra observations:** Active only if extra observations have been added automatically in the process of forecasting; deletes these extra observations.
 - **Read info, Edit info:** “Read info” just displays the summary information for the current data file; “Edit info” allows you to make changes to it (if you have permission to do so).
 - **Print description:** Opens a window containing a full account of the current dataset, including the summary information and any specific information on each of the variables.
 - **Add case markers:** Prompts for the name of a text file containing “case markers” (short strings identifying the individual observations) and adds this information to the data set. See Chapter 4.
 - **Remove case markers:** Active only if the dataset has case markers identifying the observations; removes these case markers.

- **Dataset structure:** invokes a series of dialog boxes which allow you to change the structural interpretation of the current dataset. For example, if data were read in as a cross section you can get the program to interpret them as time series or as a panel. See also section 4.4.
 - **Compact data:** For time-series data of higher than annual frequency, gives you the option of compacting the data to a lower frequency, using one of four compaction methods (average, sum, start of period or end of period).
 - **Expand data:** For time-series data, gives you the option of expanding the data to a higher frequency.
 - **Transpose data:** Turn each observation into a variable and vice versa (or in other words, each row of the data matrix becomes a column in the modified data matrix); can be useful with imported data that have been read in “sideways”.
- **View menu**
 - **Icon view:** Opens a window showing the content of the current session as a set of icons; see section 3.4.
 - **Graph specified vars:** Gives a choice between a time series plot, a regular X-Y scatter plot, an X-Y plot using impulses (vertical bars), an X-Y plot “with factor separation” (i.e. with the points colored differently depending to the value of a given dummy variable), boxplots, and a 3-D graph. Serves up a dialog box where you specify the variables to graph. See Chapter 6 for details.
 - **Multiple graphs:** Allows you to compose a set of up to six small graphs, either pairwise scatter-plots or time-series graphs. These are displayed together in a single window.
 - **Summary statistics:** Shows a full set of descriptive statistics for the variables selected in the main window.
 - **Correlation matrix:** Shows the pairwise correlation coefficients for the selected variables.
 - **Cross Tabulation:** Shows a cross-tabulation of the selected variables. This works only if at least two variables in the data set have been marked as discrete (see Chapter 12).
 - **Principal components:** Produces a Principal Components Analysis for the selected variables.
 - **Mahalanobis distances:** Computes the Mahalanobis distance of each observation from the centroid of the selected set of variables.
 - **Cross-correlogram:** Computes and graphs the cross-correlogram for two selected variables.
 - **Add menu** Offers various standard transformations of variables (logs, lags, squares, etc.) that you may wish to add to the data set. Also gives the option of adding random variables, and (for time-series data) adding seasonal dummy variables (e.g. quarterly dummy variables for quarterly data).
 - **Sample menu**
 - **Set range:** Select a different starting and/or ending point for the current sample, within the range of data available.
 - **Restore full range:** self-explanatory.
 - **Define, based on dummy:** Given a dummy (indicator) variable with values 0 or 1, this drops from the current sample all observations for which the dummy variable has value 0.
 - **Restrict, based on criterion:** Similar to the item above, except that you don’t need a pre-defined variable: you supply a Boolean expression (e.g. `sqft > 1400`) and the sample is restricted to observations satisfying that condition. See the entry for `genr` in the *Gretl Command Reference* for details on the Boolean operators that can be used.

- Random sub-sample: Draw a random sample from the full dataset.
 - Drop all obs with missing values: Drop from the current sample all observations for which at least one variable has a missing value (see Section 4.6).
 - Count missing values: Give a report on observations where data values are missing. May be useful in examining a panel data set, where it's quite common to encounter missing values.
 - Set missing value code: Set a numerical value that will be interpreted as “missing” or “not available”. This is intended for use with imported data, when gretl has not recognized the missing-value code used.
- Variable menu Most items under here operate on a single variable at a time. The “active” variable is set by highlighting it (clicking on its row) in the main data window. Most options will be self-explanatory. Note that you can rename a variable and can edit its descriptive label under “Edit attributes”. You can also “Define a new variable” via a formula (e.g. involving some function of one or more existing variables). For the syntax of such formulae, look at the online help for “Generate variable syntax” or see the *genr* command in the *Gretl Command Reference*. One simple example:

```
foo = x1 * x2
```

will create a new variable *foo* as the product of the existing variables *x1* and *x2*. In these formulae, variables must be referenced by name, not number.

- Model menu For details on the various estimators offered under this menu please consult the *Gretl Command Reference*. Also see Chapter 25 regarding the estimation of nonlinear models.
- Help menu Please use this as needed! It gives details on the syntax required in various dialog entries.

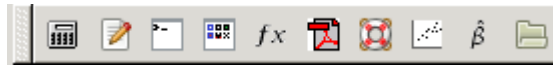
2.4 Keyboard shortcuts

When working in the main gretl window, some common operations may be performed using the keyboard, as shown in the table below.

Return	Opens a window displaying the values of the currently selected variables: it is the same as selecting “Data, Display Values”.
Delete	Pressing this key has the effect of deleting the selected variables. A confirmation is required, to prevent accidental deletions.
e	Has the same effect as selecting “Edit attributes” from the “Variable” menu.
F2	Same as “e”. Included for compatibility with other programs.
g	Has the same effect as selecting “Define new variable” from the “Variable” menu (which maps onto the <i>genr</i> command).
h	Opens a help window for gretl commands.
F1	Same as “h”. Included for compatibility with other programs.
r	Refreshes the variable list in the main window.
t	Graphs the selected variable; a line graph is used for time-series datasets, whereas a distribution plot is used for cross-sectional data.

2.5 The gretl toolbar

At the bottom left of the main window sits the toolbar.



The icons have the following functions, reading from left to right:

1. Launch a calculator program. A convenience function in case you want quick access to a calculator when you're working in gretl. The default program is `calc.exe` under MS Windows, or `xcalc` under the X window system. You can change the program under the "Tools, Preferences, General" menu, "Programs" tab.
2. Start a new script. Opens an editor window in which you can type a series of commands to be sent to the program as a batch.
3. Open the gretl console. A shortcut to the "Gretl console" menu item (Section 2.3 above).
4. Open the session icon window.
5. Open a window displaying available gretl function packages.
6. Open this manual in PDF format.
7. Open the help item for script commands syntax (i.e. a listing with details of all available commands).
8. Open the dialog box for defining a graph.
9. Open the dialog box for estimating a model using ordinary least squares.
10. Open a window listing the sample datasets supplied with gretl, and any other data file collections that have been installed.

Chapter 3

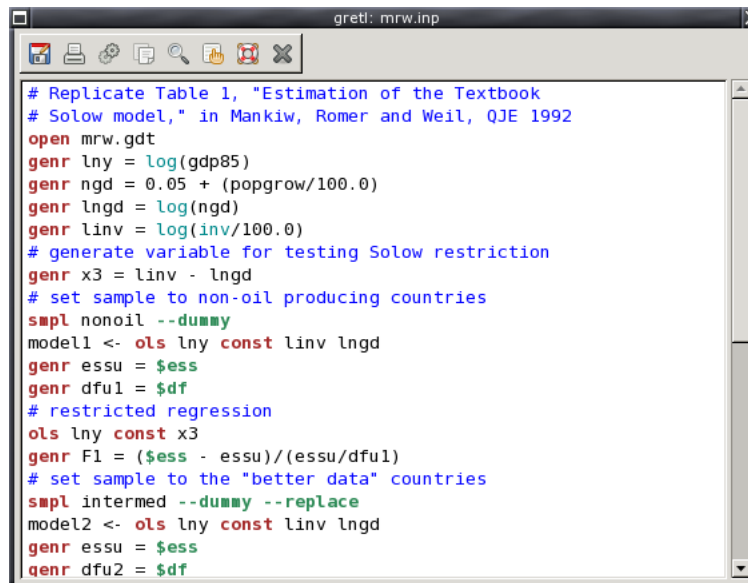
Modes of working

3.1 Command scripts

As you execute commands in gretl, using the GUI and filling in dialog entries, those commands are recorded in the form of a “script” or batch file. Such scripts can be edited and re-run, using either gretl or the command-line client, gretlcli.

To view the current state of the script at any point in a gretl session, choose “Command log” under the Tools menu. This log file is called `session.inp` and it is overwritten whenever you start a new session. To preserve it, save the script under a different name. Script files will be found most easily, using the GUI file selector, if you name them with the extension “.inp”.

To open a script you have written independently, use the “File, Script files” menu item; to create a script from scratch use the “File, Script files, New script” item or the “new script” toolbar button. In either case a script window will open (see Figure 3.1).



```
# Replicate Table 1, "Estimation of the Textbook
# Solow model," in Mankiw, Romer and Weil, QJE 1992
open mrw.gdt
genr lny = log(gdp85)
genr ngd = 0.05 + (popgrow/100.0)
genr lngd = log(ngd)
genr linv = log(inv/100.0)
# generate variable for testing Solow restriction
genr x3 = linv - lngd
# set sample to non-oil producing countries
smpl nonoil --dummy
model1 <- ols lny const linv lngd
genr essu = $ess
genr dfu1 = $df
# restricted regression
ols lny const x3
genr F1 = ($ess - essu)/($ess/dfu1)
# set sample to the "better data" countries
smpl intermed --dummy --replace
model2 <- ols lny const linv lngd
genr essu = $ess
genr dfu2 = $df
```

Figure 3.1: Script window, editing a command file

The toolbar at the top of the script window offers the following functions (left to right): (1) Save the file; (2) Save the file under a specified name; (3) Print the file (this option is not available on all platforms); (4) Execute the commands in the file; (5) Copy selected text; (6) Paste the selected text; (7) Find and replace text; (8) Undo the last Paste or Replace action; (9) Help (if you place the cursor in a command word and press the question mark you will get help on that command); (10) Close the window.

When you execute the script, by clicking on the Execute icon or by pressing Ctrl-r, all output is directed to a single window, where it can be edited, saved or copied to the clipboard. To learn more about the possibilities of scripting, take a look at the gretl Help item “Command reference,”

or start up the command-line program `gretlcli` and consult its help, or consult the *Gretl Command Reference*.

If you run the script when part of it is highlighted, `gretl` will only run that portion. Moreover, if you want to run just the current line, you can do so by pressing `Ctrl-Enter`.¹

Clicking the right mouse button in the script editor window produces a pop-up menu. This gives you the option of executing either the line on which the cursor is located, or the selected region of the script if there's a selection in place. If the script is editable, this menu also gives the option of adding or removing comment markers from the start of the line or lines.

The `gretl` package includes over 70 example scripts. Many of these relate to [Ramanathan \(2002\)](#), but they may also be used as a free-standing introduction to scripting in `gretl` and to various points of econometric theory. You can explore the example files under “File, Script files, Example scripts”. There you will find a listing of the files along with a brief description of the points they illustrate and the data they employ. Open any file and run it to see the output. Note that long commands in a script can be broken over two or more lines, using backslash as a continuation character.

You can, if you wish, use the GUI controls and the scripting approach in tandem, exploiting each method where it offers greater convenience. Here are two suggestions.

- Open a data file in the GUI. Explore the data—generate graphs, run regressions, perform tests. Then open the Command log, edit out any redundant commands, and save it under a specific name. Run the script to generate a single file containing a concise record of your work.
- Start by establishing a new script file. Type in any commands that may be required to set up transformations of the data (see the `genr` command in the *Gretl Command Reference*). Typically this sort of thing can be accomplished more efficiently via commands assembled with forethought rather than point-and-click. Then save and run the script: the GUI data window will be updated accordingly. Now you can carry out further exploration of the data via the GUI. To revisit the data at a later point, open and rerun the “preparatory” script first.

Scripts and data files

One common way of doing econometric research with `gretl` is as follows: compose a script; execute the script; inspect the output; modify the script; run it again—with the last three steps repeated as many times as necessary. In this context, note that when you open a data file this clears out most of `gretl`'s internal state. It's therefore probably a good idea to have your script start with an open command: the data file will be re-opened each time, and you can be confident you're getting “fresh” results.

One further point should be noted. When you go to open a new data file via the graphical interface, you are always prompted: opening a new data file will lose any unsaved work, do you really want to do this? When you execute a script that opens a data file, however, you are *not* prompted. The assumption is that in this case you're not going to lose any work, because the work is embodied in the script itself (and it would be annoying to be prompted at each iteration of the work cycle described above).

This means you should be careful if you've done work using the graphical interface and then decide to run a script: the current data file will be replaced without any questions asked, and it's your responsibility to save any changes to your data first.

¹This feature is not unique to `gretl`; other econometric packages offer the same facility. However, experience shows that while this can be remarkably useful, it can also lead to writing dinosaur scripts that are never meant to be executed all at once, but rather used as a chaotic repository to cherry-pick snippets from. Since `gretl` allows you to have several script windows open at the same time, you may want to keep your scripts tidy and reasonably small.

3.2 Saving script objects

When you estimate a model using point-and-click, the model results are displayed in a separate window, offering menus which let you perform tests, draw graphs, save data from the model, and so on. Ordinarily, when you estimate a model using a script you just get a non-interactive printout of the results. You can, however, arrange for models estimated in a script to be “captured”, so that you can examine them interactively when the script is finished. Here is an example of the syntax for achieving this effect:

```
Model1 <- ols Ct 0 Yt
```

That is, you type a name for the model to be saved under, then a back-pointing “assignment arrow”, then the model command. The assignment arrow is composed of the less-than sign followed by a dash; it must be separated by spaces from both the preceding name and the following command. The name for a saved object may include spaces, but in that case it must be wrapped in double quotes:

```
"Model 1" <- ols Ct 0 Yt
```

Models saved in this way will appear as icons in the gretl icon view window (see Section 3.4) after the script is executed. In addition, you can arrange to have a named model displayed (in its own window) automatically as follows:

```
Model1.show
```

Again, if the name contains spaces it must be quoted:

```
"Model 1".show
```

The same facility can be used for graphs. For example the following will create a plot of Ct against Yt, save it under the name “CrossPlot” (it will appear under this name in the icon view window), and have it displayed:

```
CrossPlot <- gnpplot Ct Yt  
CrossPlot.show
```

You can also save the output from selected commands as named pieces of text (again, these will appear in the session icon window, from where you can open them later). For example this command sends the output from an augmented Dickey-Fuller test to a “text object” named ADF1 and displays it in a window:

```
ADF1 <- adf 2 x1  
ADF1.show
```

Objects saved in this way (whether models, graphs or pieces of text output) can be destroyed using the command `.free` appended to the name of the object, as in `ADF1.free`.

3.3 The gretl console

A further option is available for your computing convenience. Under gretl’s “Tools” menu you will find the item “Gretl console” (there is also an “open gretl console” button on the toolbar in the main window). This opens up a window in which you can type commands and execute them one by one (by pressing the Enter key) interactively. This is essentially the same as gretlcli’s mode of operation, except that the GUI is updated based on commands executed from the console, enabling you to work back and forth as you wish.

In the console, you have “command history”; that is, you can use the up and down arrow keys to navigate the list of command you have entered to date. You can retrieve, edit and then re-enter a previous command. In console mode, you can create, display and free objects (models, graphs or text) as described above for script mode.

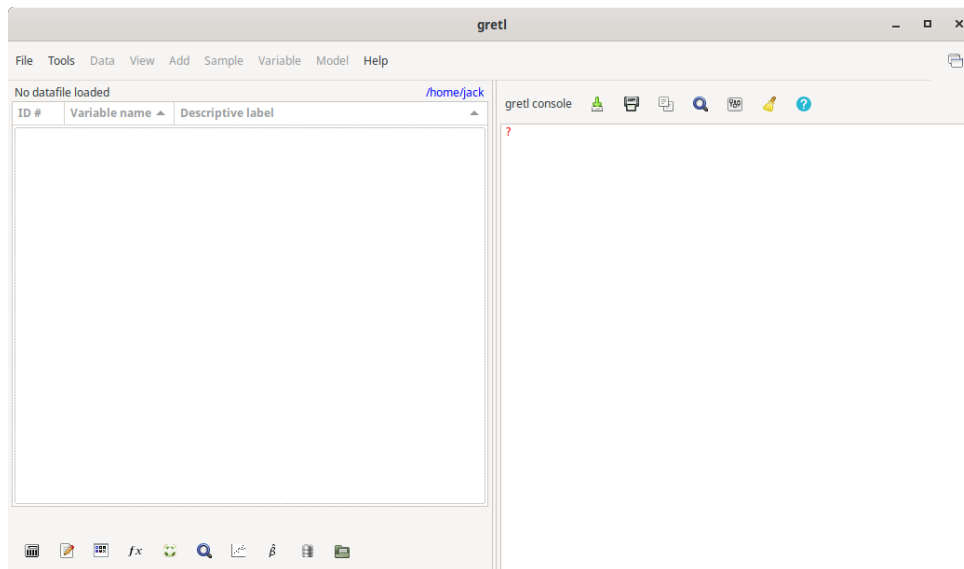


Figure 3.2: Main window including console

Optionally, the console can be shown not as a separate window, but as a side pane to the main window, as in Figure 3.2. Some people prefer this arrangement, that is vaguely reminiscent of other programs such as Rstudio or the Octave GUI interface. In order to activate the “split panes” interface, go to the Tools menu, select “Preferences” and tick the “Main window includes console” box.

3.4 The Session concept

Gretl offers the idea of a “session” as a way of keeping track of your work and revisiting it later. The basic idea is to provide an iconic space containing various objects pertaining to your current working session (see Figure 3.3). You can add objects (represented by icons) to this space as you go along. If you save the session, these added objects should be available again if you re-open the session later.

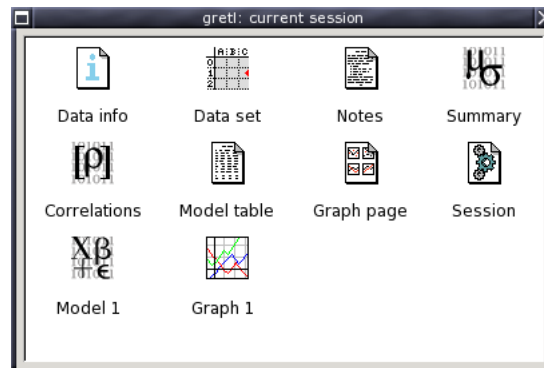


Figure 3.3: Icon view: one model and one graph have been added to the default icons

If you start gretl and open a data set, then select “Icon view” from the View menu, you should see the basic default set of icons: these give you quick access to information on the data set (if any), correlation matrix (“Correlations”) and descriptive summary statistics (“Summary”). All of these are activated by double-clicking the relevant icon. The “Data set” icon is a little more complex: double-clicking opens up the data in the built-in spreadsheet, but you can also right-click on the icon for a menu of other actions.

To add a model to the Icon view, first estimate it using the Model menu. Then pull down the File menu in the model window and select “Save to session as icon...” or “Save as icon and close”. Simply hitting the S key over the model window is a shortcut to the latter action.

To add a graph, first create it (under the View menu, “Graph specified vars”, or via one of gretl’s other graph-generating commands). Click on the graph window to bring up the graph menu, and select “Save to session as icon”.

Once a model or graph is added its icon will appear in the Icon view window. Double-clicking on the icon redisplay the object, while right-clicking brings up a menu which lets you display or delete the object. This popup menu also gives you the option of editing graphs.

The model table

In econometric research it is common to estimate several models with a common dependent variable—the models differing in respect of which independent variables are included, or perhaps in respect of the estimator used. In this situation it is convenient to present the regression results in the form of a table, where each column contains the results (coefficient estimates and standard errors) for a given model, and each row contains the estimates for a given variable across the models. Note that some estimation methods are not compatible with the straightforward model table format, therefore gretl will not let those models be added to the model table. These methods include non-linear least squares (nls), generic maximum-likelihood estimators (mle), generic GMM (gmm), dynamic panel models (dpanel), interval regressions (intreg), bivariate probit models (biprobit), AR(D)MA models (arima or arma), and (G)ARCH models (garch and arch).

In the Icon view window gretl provides a means of constructing such a table (and copying it in plain text, \LaTeX or Rich Text Format). The procedure is outlined below. (The model table can also be built non-interactively, in script mode—see the entry for `modeltab` in the *Gretl Command Reference*.)

1. Estimate a model which you wish to include in the table, and in the model display window, under the File menu, select “Save to session as icon” or “Save as icon and close”.
2. Repeat step 1 for the other models to be included in the table (up to a total of six models).
3. When you are done estimating the models, open the icon view of your gretl session, by selecting “Icon view” under the View menu in the main gretl window, or by clicking the “session icon view” icon on the gretl toolbar.
4. In the Icon view, there is an icon labeled “Model table”. Decide which model you wish to appear in the left-most column of the model table and add it to the table, either by dragging its icon onto the Model table icon, or by right-clicking on the model icon and selecting “Add to model table” from the pop-up menu.
5. Repeat step 4 for the other models you wish to include in the table. The second model selected will appear in the second column from the left, and so on.
6. When you are finished composing the model table, display it by double-clicking on its icon. Under the Edit menu in the window which appears, you have the option of copying the table to the clipboard in various formats.
7. If the ordering of the models in the table is not what you wanted, right-click on the model table icon and select “Clear table”. Then go back to step 4 above and try again.

A simple instance of gretl’s model table is shown in Figure 3.4.

gretl: model table

OLS estimates
Dependent variable: price

	Model 1	Model 2	Model 3
const	129.1 (88.30)	121.2 (80.18)	52.35 (37.29)
sqft	0.1548** (0.03194)	0.1483** (0.02121)	0.1388** (0.01873)
bedrms	-21.59 (27.03)	-23.91 (24.64)	
baths	-12.19 (43.25)		
n	14	14	14
Adj. R**2	0.7868	0.8046	0.8056

Standard errors in parentheses
* indicates significance at the 10 percent level
** indicates significance at the 5 percent level

Close

Figure 3.4: Example of model table

The graph page

The “graph page” icon in the session window offers a means of putting together several graphs for printing on a single page. This facility will work only if you have the \LaTeX typesetting system installed, and are able to generate and view either PDF or PostScript output. The output format is controlled by your choice of program for compiling \TeX files, which can be found under the “Programs” tab in the Preferences dialog box (under the “Tools” menu in the main window). Usually this should be `pdflatex` for PDF output or `latex` for PostScript. In the latter case you must have a working set-up for handling PostScript, which will usually include `dvips`, `ghostscript` and a viewer such as `gv`, `gsv` or `kgghostview`.

In the Icon view window, you can drag up to eight graphs onto the graph page icon. When you double-click on the icon (or right-click and select “Display”), a page containing the selected graphs (in PDF or EPS format) will be composed and opened in your viewer. From there you should be able to print the page.

To clear the graph page, right-click on its icon and select “Clear”.

As with the model table, it is also possible to manipulate the graph page via commands in script or console mode—see the entry for the `graphpg` command in the *Gretl Command Reference*.

Saving and re-opening sessions

If you create models or graphs that you think you may wish to re-examine later, then before quitting `gretl` select “Session files, Save session” from the File menu and give a name under which to save the session. To re-open the session later, either

- Start `gretl` then re-open the session file by going to the “File, Session files, Open session”, or
- From the command line, type `gretl -r sessionfile`, where *sessionfile* is the name under which the session was saved, or
- Drag the icon representing a session file onto `gretl`.

Chapter 4

Data files

4.1 Data file formats

Gretl has its own native format for data files. Most users will probably not want to read or write such files outside of gretl itself, but occasionally this may be useful and details on the file formats are given in Appendix A. The program can also import data from a variety of other formats. In the GUI program this can be done via the “File, Open Data, User file” menu—note the drop-down list of acceptable file types. In script mode, simply use the `open` command. The supported import formats are as follows.

- Plain text files (comma-separated or “CSV” being the most common type). For details on what gretl expects of such files, see Section 4.3.
- Spreadsheets: MS Excel, Gnumeric and Open Document (ODS). The requirements for such files are given in Section 4.3.
- Stata data files (.dta).
- SPSS data files (.sav).
- SAS “xport” files (.xpt).
- Eviews workfiles (.wf1).¹
- JMulTi data files.

When you import data from a plain text format, gretl opens a “diagnostic” window, reporting on its progress in reading the data. If you encounter a problem with ill-formatted data, the messages in this window should give you a handle on fixing the problem.

Note that gretl has a facility for writing out data in the native formats of GNU R, Octave, JMulTi and PcGive (see Appendix D). In the GUI client this option is found under the “File, Export data” menu; in the command-line client use the `store` command with the appropriate option flag.

4.2 Databases

For working with large amounts of data gretl is supplied with a database-handling routine. A *database*, as opposed to a *data file*, is not read directly into the program’s workspace. A database can contain series of mixed frequencies and sample ranges. You open the database and select series to import into the working dataset. You can then save those series in a native format data file if you wish. Databases can be accessed via the menu item “File, Databases”.

For details on the format of gretl databases, see Appendix A.

¹See http://users.wfu.edu/cottrell/eviews_format/.

Online access to databases

Several gretl databases are available from Wake Forest University. Your computer must be connected to the internet for this option to work. Please see the description of the “data” command under the Help menu.

🔗 Visit the gretl [data page](#) for details and updates on available data.

Foreign database formats

Thanks to Thomas Doan of *Estima*, who made available the specification of the database format used by RATS 4 (Regression Analysis of Time Series), gretl can handle such databases—or at least, a subset of same, namely time-series databases containing monthly and quarterly series.

Gretl can also import data from PcGive databases. These take the form of a pair of files, one containing the actual data (with suffix `.bn7`) and one containing supplementary information (`.in7`).

In addition, gretl offers ODBC connectivity. Be warned: this feature is meant for somewhat advanced users; there is currently no graphical interface. Interested readers will find more info in appendix 42.

4.3 Creating a dataset from scratch

There are several ways of doing this:

1. Find, or create using a text editor, a plain text data file and open it via “Import”.
2. Use your favorite spreadsheet to establish the data file, save it in comma-separated format if necessary (this may not be necessary if the spreadsheet format is MS Excel, Gnumeric or Open Document), then use one of the “Import” options.
3. Use gretl’s built-in spreadsheet.
4. Select data series from a suitable database.
5. Use your favorite text editor or other software tools to create a data file in gretl format independently.

Here are a few comments and details on these methods.

Common points on imported data

Options (1) and (2) involve using gretl’s “import” mechanism. For the program to read such data successfully, certain general conditions must be satisfied:

- The first row must contain valid variable names. A valid variable name is of 31 characters maximum; starts with a letter; and contains nothing but letters, numbers and the underscore character, `_`. (Longer variable names will be truncated to 31 characters.) Qualifications to the above: First, in the case of an plain text import, if the file contains no row with variable names the program will automatically add names, `v1`, `v2` and so on. Second, by “the first row” is meant the first *relevant* row. In the case of plain text imports, blank rows and rows beginning with a hash mark, `#`, are ignored. In the case of Excel, Gnumeric and ODS imports, you are presented with a dialog box where you can select an offset into the spreadsheet, so that gretl will ignore a specified number of rows and/or columns.
- Data values: these should constitute a rectangular block, with one variable per column (and one observation per row). The number of variables (data columns) must match the number of variable names given. See also section 4.6. Numeric data are expected, but in the case of

importing from plain text, the program offers limited handling of character (string) data: if a given column contains character data only, consecutive numeric codes are substituted for the strings, and once the import is complete a table is printed showing the correspondence between the strings and the codes.

- Dates (or observation labels): Optionally, the *first* column may contain strings such as dates, or labels for cross-sectional observations. Such strings have a maximum of 15 characters (as with variable names, longer strings will be truncated). A column of this sort should be headed with the string *obs* or *date*, or the first row entry may be left blank.

For dates to be recognized as such, the date strings should adhere to one or other of a set of specific formats, as follows. For *annual* data: 4-digit years. For *quarterly* data: a 4-digit year, followed by a separator (either a period, a colon, or the letter Q), followed by a 1-digit quarter. Examples: 1997.1, 2002:3, 1947Q1. For *monthly* data: a 4-digit year, followed by a period or a colon, followed by a two-digit month. Examples: 1997.01, 2002:10.

Plain text (“CSV”) files can use comma, space, tab or semicolon as the column separator. When you open such a file via the GUI you are given the option of specifying the separator, though in most cases it should be detected automatically.

If you use a spreadsheet to prepare your data you are able to carry out various transformations of the “raw” data with ease (adding things up, taking percentages or whatever): note, however, that you can also do this sort of thing easily—perhaps more easily—within gretl, by using the tools under the “Add” menu.

Appending imported data

You may wish to establish a dataset piece by piece, by incremental importation of data from other sources. This is supported via the “File, Append data” menu items: gretl will check the new data for conformability with the existing dataset and, if everything seems OK, will merge the data. You can add new variables in this way, provided the data frequency matches that of the existing dataset. Or you can append new observations for data series that are already present; in this case the variable names must match up correctly. Note that by default (that is, if you choose “Open data” rather than “Append data”), opening a new data file closes the current one.

Using the built-in spreadsheet

Under the “File, New data set” menu you can choose the sort of dataset you want to establish (e.g. quarterly time series, cross-sectional). You will then be prompted for starting and ending dates (or observation numbers) and the name of the first variable to add to the dataset. After supplying this information you will be faced with a simple spreadsheet into which you can type data values. In the spreadsheet window, clicking the right mouse button will invoke a popup menu which enables you to add a new variable (column), to add an observation (append a row at the foot of the sheet), or to insert an observation at the selected point (move the data down and insert a blank row.)

Once you have entered data into the spreadsheet you import these into gretl’s workspace using the spreadsheet’s “Apply changes” button.

Please note that gretl’s spreadsheet is quite basic and has no support for functions or formulas. Data transformations are done via the “Add” or “Variable” menus in the main window.

Selecting from a database

Another alternative is to establish your dataset by selecting variables from a database.

Begin with the “File, Databases” menu item. This has four forks: “Gretl native”, “RATS 4”, “PcGive” and “On database server”. You should be able to find the file `fedstl.bin` in the file selector that

opens if you choose the “Gretl native” option since this file, which contains a large collection of US macroeconomic time series, is supplied with the distribution.

You won’t find anything under “RATS 4” unless you have purchased RATS data.² If you do possess RATS data you should go into the “Tools, Preferences, General” dialog, select the Databases tab, and fill in the correct path to your RATS files.

If your computer is connected to the internet you should find several databases (at Wake Forest University) under “On database server”. You can browse these remotely; you also have the option of installing them onto your own computer. The initial remote databases window has an item showing, for each file, whether it is already installed locally (and if so, if the local version is up to date with the version at Wake Forest).

Assuming you have managed to open a database you can import selected series into gretl’s workspace by using the “Series, Import” menu item in the database window, or via the popup menu that appears if you click the right mouse button, or by dragging the series into the program’s main window.

Creating a gretl data file independently

It is possible to create a data file in one or other of gretl’s own formats using a text editor or software tools such as `awk`, `sed` or `perl`. This may be a good choice if you have large amounts of data already in machine readable form. You will, of course, need to study these data formats (XML-based or “traditional”) as described in Appendix A.

4.4 Structuring a dataset

Once your data are read by gretl, it may be necessary to supply some information on the nature of the data. We distinguish between three kinds of datasets:

1. Cross section
2. Time series
3. Panel data

The primary tool for doing this is the “Data, Dataset structure” menu entry in the graphical interface, or the `setobs` command for scripts and the command-line interface.

Cross sectional data

By a cross section we mean observations on a set of “units” (which may be firms, countries, individuals, or whatever) at a common point in time. This is the default interpretation for a data file: if there is insufficient information to interpret data as time-series or panel data, they are automatically interpreted as a cross section. In the unlikely event that cross-sectional data are wrongly interpreted as time series, you can correct this by selecting the “Data, Dataset structure” menu item. Click the “cross-sectional” radio button in the dialog box that appears, then click “Forward”. Click “OK” to confirm your selection.

Time series data

When you import data from a spreadsheet or plain text file, gretl will make fairly strenuous efforts to glean time-series information from the first column of the data, if it looks at all plausible that such information may be present. If time-series structure is present but not recognized, again you can use the “Data, Dataset structure” menu item. Select “Time series” and click “Forward”; select the appropriate data frequency and click “Forward” again; then select or enter the starting observation

²See www.estima.com

and click “Forward” once more. Finally, click “OK” to confirm the time-series interpretation if it is correct (or click “Back” to make adjustments if need be).

Besides the basic business of getting a data set interpreted as time series, further issues may arise relating to the frequency of time-series data. In a gretl time-series data set, all the series must have the same frequency. Suppose you wish to make a combined dataset using series that, in their original state, are not all of the same frequency. For example, some series are monthly and some are quarterly.

Your first step is to formulate a strategy: Do you want to end up with a quarterly or a monthly data set? A basic point to note here is that “compacting” data from a higher frequency (e.g. monthly) to a lower frequency (e.g. quarterly) is usually unproblematic. You lose information in doing so, but in general it is perfectly legitimate to take (say) the average of three monthly observations to create a quarterly observation. On the other hand, “expanding” data from a lower to a higher frequency is not, in general, a valid operation.

In most cases, then, the best strategy is to start by creating a data set of the *lower* frequency, and then to compact the higher frequency data to match. When you import higher-frequency data from a database into the current data set, you are given a choice of compaction method (average, sum, start of period, or end of period). In most instances “average” is likely to be appropriate.

You *can* also import lower-frequency data into a high-frequency data set, but this is generally not recommended. What gretl does in this case is simply replicate the values of the lower-frequency series as many times as required. For example, suppose we have a quarterly series with the value 35.5 in 1990:1, the first quarter of 1990. On expansion to monthly, the value 35.5 will be assigned to the observations for January, February and March of 1990. The expanded variable is therefore useless for fine-grained time-series analysis, outside of the special case where you know that the variable in question does in fact remain constant over the sub-periods.

When the current data frequency is appropriate, gretl offers both “Compact data” and “Expand data” options under the “Data” menu. These options operate on the whole data set, compacting or expanding all series. They should be considered “expert” options and should be used with caution.

Panel data

Panel data are inherently three dimensional—the dimensions being variable, cross-sectional unit, and time-period. For example, a particular number in a panel data set might be identified as the observation on capital stock for General Motors in 1980. (A note on terminology: we use the terms “cross-sectional unit”, “unit” and “group” interchangeably below to refer to the entities that compose the cross-sectional dimension of the panel. These might, for instance, be firms, countries or persons.)

For representation in a textual computer file (and also for gretl’s internal calculations) the three dimensions must somehow be flattened into two. This “flattening” involves taking layers of the data that would naturally stack in a third dimension, and stacking them in the vertical dimension.

gretl always expects data to be arranged “by observation”, that is, such that each row represents an observation (and each variable occupies one and only one column). In this context the flattening of a panel data set can be done in either of two ways:

- Stacked time series: the successive vertical blocks each comprise a time series for a given unit.
- Stacked cross sections: the successive vertical blocks each comprise a cross-section for a given period.

You may input data in whichever arrangement is more convenient. Internally, however, gretl always stores panel data in the form of stacked time series.

4.5 Panel data specifics

When you import panel data into gretl from a spreadsheet or comma separated format, the panel nature of the data will not be recognized automatically (most likely the data will be treated as “undated”). A panel interpretation can be imposed on the data using the graphical interface or via the `setobs` command.

In the graphical interface, use the menu item “Data, Dataset structure”. In the first dialog box that appears, select “Panel”. In the next dialog you have a three-way choice. The first two options, “Stacked time series” and “Stacked cross sections” are applicable if the data set is already organized in one of these two ways. If you select either of these options, the next step is to specify the number of cross-sectional units in the data set. The third option, “Use index variables”, is applicable if the data set contains two variables that index the units and the time periods respectively; the next step is then to select those variables. For example, a data file might contain a country code variable and a variable representing the year of the observation. In that case gretl can reconstruct the panel structure of the data regardless of how the observation rows are organized.

The `setobs` command has options that parallel those in the graphical interface. If suitable index variables are available you can do, for example

```
setobs unitvar timevar --panel-vars
```

where `unitvar` is a variable that indexes the units and `timevar` is a variable indexing the periods. Alternatively you can use the form `setobs freq 1:1 structure`, where `freq` is replaced by the “block size” of the data (that is, the number of periods in the case of stacked time series, or the number of units in the case of stacked cross-sections) and `structure` is either `--stacked-time-series` or `--stacked-cross-section`. Two examples are given below: the first is suitable for a panel in the form of stacked time series with observations from 20 periods; the second for stacked cross sections with 5 units.

```
setobs 20 1:1 --stacked-time-series
setobs 5 1:1 --stacked-cross-section
```

Panel data arranged by variable

Publicly available panel data sometimes come arranged “by variable.” Suppose we have data on two variables, `x1` and `x2`, for each of 50 states in each of 5 years (giving a total of 250 observations per variable). One textual representation of such a data set would start with a block for `x1`, with 50 rows corresponding to the states and 5 columns corresponding to the years. This would be followed, vertically, by a block with the same structure for variable `x2`. A fragment of such a data file is shown below, with quinquennial observations 1965–1985. Imagine the table continued for 48 more states, followed by another 50 rows for variable `x2`.

	x1				
	1965	1970	1975	1980	1985
AR	100.0	110.5	118.7	131.2	160.4
AZ	100.0	104.3	113.8	120.9	140.6

If a datafile with this sort of structure is read into gretl,³ the program will interpret the columns as distinct variables, so the data will not be usable “as is.” But there is a mechanism for correcting the situation, namely the `stack` function.

Consider the first data column in the fragment above: the first 50 rows of this column constitute a cross-section for the variable `x1` in the year 1965. If we could create a new series by stacking the

³Note that you will have to modify such a datafile slightly before it can be read at all. The line containing the variable name (in this example `x1`) will have to be removed, and so will the initial row containing the years, otherwise they will be taken as numerical data.

first 50 entries in the second column underneath the first 50 entries in the first, we would be on the way to making a data set “by observation” (in the first of the two forms mentioned above, stacked cross-sections). That is, we’d have a column comprising a cross-section for x_1 in 1965, followed by a cross-section for the same variable in 1970.

The following gretl script illustrates how we can accomplish the stacking, for both x_1 and x_2 . We assume that the original data file is called `panel.txt`, and that in this file the columns are headed with “variable names” v_1, v_2, \dots, v_5 . (The columns are not really variables, but in the first instance we “pretend” that they are.)

```
open panel.txt
series x1 = stack(v1..v5, 50)
series x2 = stack(v1..v5, 50, 50)
setobs 50 1:1 --stacked-cross-section
store panel.gdt x1 x2
```

The second and third lines illustrate the syntax of the `stack` function, which has this signature:

```
series stack(list L, scalar length, scalar offset)
```

- `L`: a list of series on which to operate.
- `length`: an integer giving the number of observations to take from each series.
- `offset`: an integer giving the offset from the top of the dataset at which to start taking values (optional, defaults to 0).

The “`..`” syntax in the example above constructs a list of the 5 contiguous series to be stacked. More generally, you can define a named list of series and pass that as the first argument to `stack` (see chapter 15). In this example we’re supposing that the full data set contains 100 rows, and that in the stacking of variable x_1 we wish to read only the first 50 rows from each column, so we give 50 as the second argument.

On line 3 we do the stacking for variable x_2 . Again we want a `length` of 50 for the components of the stacked series, but this time we want to start reading from the 50th row of the original data, and so we add a third `offset` argument of 50. Line 4 then imposes a panel interpretation on the data. Finally, we save the stacked data to file, with the panel interpretation.

The illustrative script above is appropriate when the number of variables to be processed is small. When there are many variables in the dataset it will be more convenient to use a loop to accomplish the stacking, as shown in the following script. The setup is presumed to be the same as in the previous case (50 units, 5 periods), but with 20 variables rather than 2.

```
open panel.txt
list L = v1..v5 # predefine a list of series
scalar length = 50
loop i=1..20
    scalar offset = (i - 1) * length
    series xi = stack(L, length, offset)
endloop
setobs 50 1:01 --stacked-cross-section
store panel.gdt x1..x20
```

Side-by-side time series

There’s a second sort of data that you may wish to convert to gretl’s panel format, namely side-by-side time series for a number of cross-sectional units. For example, a data file might contain separate GDP series of common length T for each of N countries. To turn these into a single stacked

time series the `stack` function can again be used. An example follows, where we suppose the original data source is a comma-separated file named `GDP.csv`, containing GDP data for countries from Austria (GDP_AT) to Zimbabwe (GDP_ZW) in consecutive columns.

```
open GDP.csv
scalar T = $nobs # the number of periods
list L = GDP_AT..GDP_ZW
series GDP = stack(L, T)
setobs T 1:01 --stacked-time-series
store panel.gdt GDP
```

The resulting data file, `panel.gdt`, will contain a single series of length NT where N is the number of countries and T is the length of the original dataset. One could insert revised variants of lines 3 and 4 of the script if the original file contained additional side-by-side per-country series for investment, consumption or whatever.

Relatively simple cases of this transformation can be handled via gretl's graphical interface. The “simplicity” requirements are:

- The dataset contains exactly $M \cdot N$ time series, arranged in $M \geq 1$ blocks each having $N \geq 2$ contiguous members.
- In each block, the N series represent measures of a single variable (e.g. GDP) for a set of N cross-sectional units, and in each block these units appear in the same order.

The relevant GUI apparatus can be accessed via the item **Dataset structure** under the **Data** menu in the main window. On selecting this item one of the options is **Panel**; choose this option and the next step offers “Convert from side-by-side time series”. This leads to steps where you specify M or N ; give a name for the panel series; then confirm that the specified transformation is what you want. The end result is the same as executing a series of commands on the pattern shown above, using the `stack` function, then executing the additional command `open panel.gdt`.

Panel data marker strings

It can be helpful with panel data to have the observations identified by mnemonic markers. A special function in the `genr` command is available for this purpose.

In the example under the heading “Panel data arranged by variable” above, suppose all the states are identified by two-letter codes in the left-most column of the original datafile. When the `stack` function is invoked as shown, these codes will be stacked along with the data values. If the first row is marked AR for Arkansas, then the marker AR will end up being shown on each row containing an observation for Arkansas. That’s all very well, but these markers don’t tell us anything about the date of the observation. To rectify this we could do:

```
genr time
series year = 1960 + (5 * time)
genr markers = "%s:%d", marker, year
```

The first line generates a 1-based index representing the period of each observation, and the second line uses the `time` variable to generate a variable representing the year of the observation. The third line contains this special feature: if (and only if) the name of the new “variable” to generate is `markers`, the portion of the command following the equals sign is taken as a C-style format string (which must be wrapped in double quotes), followed by a comma-separated list of arguments. The arguments will be printed according to the given format to create a new set of observation markers. Valid arguments are either the names of variables in the dataset, or the string `marker` which denotes the pre-existing observation marker. The format specifiers which are likely to be

useful in this context are %s for a string and %d for an integer. Strings can be truncated: for example %.3s will use just the first three characters of the string. To chop initial characters off an existing observation marker when constructing a new one, you can use the syntax marker + n, where n is a positive integer: in the case the first n characters will be skipped.

After the commands above are processed, then, the observation markers will look like, for example, AR:1965, where the two-letter state code and the year of the observation are spliced together with a colon.

Panel dummy variables

In a panel study you may wish to construct dummy variables of one or both of the following sorts: (a) dummies as unique identifiers for the units or groups, and (b) dummies as unique identifiers for the time periods. The former may be used to allow the intercept of the regression to differ across the units, the latter to allow the intercept to differ across periods.

Two special functions are available to create such dummies. These are found under the “Add” menu in the GUI, or under the `genr` command in script mode or `gretlcli`.

1. “unit dummies” (script command `genr unitdum`). This command creates a set of dummy variables identifying the cross-sectional units. The variable `du_1` will have value 1 in each row corresponding to a unit 1 observation, 0 otherwise; `du_2` will have value 1 in each row corresponding to a unit 2 observation, 0 otherwise; and so on.
2. “time dummies” (script command `genr timedum`). This command creates a set of dummy variables identifying the periods. The variable `dt_1` will have value 1 in each row corresponding to a period 1 observation, 0 otherwise; `dt_2` will have value 1 in each row corresponding to a period 2 observation, 0 otherwise; and so on.

If a panel data set has the YEAR of the observation entered as one of the variables you can create a periodic dummy to pick out a particular year, e.g. `genr dum = (YEAR==1960)`. You can also create periodic dummy variables using the modulus operator, %. For instance, to create a dummy with value 1 for the first observation and every thirtieth observation thereafter, 0 otherwise, do

```
genr index
series dum = ((index-1) % 30) == 0
```

Lags, differences, trends

If the time periods are evenly spaced you may want to use lagged values of variables in a panel regression (but see also chapter 24); you may also wish to construct first differences of variables of interest.

Once a dataset is identified as a panel, `gretl` will handle the generation of such variables correctly. For example the command `genr x1_1 = x1(-1)` will create a variable that contains the first lag of `x1` where available, and the missing value code where the lag is not available (e.g. at the start of the time series for each group). When you run a regression using such variables, the program will automatically skip the missing observations.

When a panel data set has a fairly substantial time dimension, you may wish to include a trend in the analysis. The command `genr time` creates a variable named `time` which runs from 1 to T for each unit, where T is the length of the time-series dimension of the panel. If you want to create an index that runs consecutively from 1 to $m \times T$, where m is the number of units in the panel, use `genr index`.

Basic statistics by unit

gretl contains functions which can be used to generate basic descriptive statistics for a given variable, on a per-unit basis; these are `pnoobs()` (number of valid cases), `pmin()` and `pmax()` (minimum and maximum) and `pmean()` and `psd()` (mean and standard deviation).

As a brief illustration, suppose we have a panel data set comprising 8 time-series observations on each of N units or groups. Then the command

```
series pmx = pmean(x)
```

creates a series of this form: the first 8 values (corresponding to unit 1) contain the mean of x for unit 1, the next 8 values contain the mean for unit 2, and so on. The `psd()` function works in a similar manner. The sample standard deviation for group i is computed as

$$s_i = \sqrt{\frac{\sum (x - \bar{x}_i)^2}{T_i - 1}}$$

where T_i denotes the number of valid observations on x for the given unit, \bar{x}_i denotes the group mean, and the summation is across valid observations for the group. If $T_i < 2$, however, the standard deviation is recorded as 0.

One particular use of `psd()` may be worth noting. If you want to form a sub-sample of a panel that contains only those units for which the variable x is time-varying, you can either use

```
smpl pmin(x) < pmax(x) --restrict
```

or

```
smpl psd(x) > 0 --restrict
```

4.6 Missing data values

Representation and handling

Missing values are represented internally as NaN (“not a number”), as defined in the IEEE 754 floating-point standard. In a native-format data file they should be represented as NA. When importing CSV data `gretl` accepts several common representations of missing values including `-999`, the string NA (in upper or lower case), a single dot, or simply a blank cell. Blank cells should, of course, be properly delimited, e.g. `120.6, , 5.38`, in which the middle value is presumed missing.

As for handling of missing values in the course of statistical analysis, `gretl` does the following:

- In calculating descriptive statistics (mean, standard deviation, etc.) under the `summary` command, missing values are simply skipped and the sample size adjusted appropriately.
- In running regressions `gretl` first adjusts the beginning and end of the sample range, truncating the sample if need be. Missing values at the beginning of the sample are common in time series work due to the inclusion of lags, first differences and so on; missing values at the end of the range are not uncommon due to differential updating of series and possibly the inclusion of leads.

If `gretl` detects any missing values “inside” the (possibly truncated) sample range for a regression, the result depends on the character of the dataset and the estimator chosen. In many cases, the program will automatically skip the missing observations when calculating the regression results. In this situation a message is printed stating how many observations were dropped. On the other hand, the skipping of missing observations is not supported for all procedures: exceptions include

all autoregressive estimators, system estimators such as SUR, and nonlinear least squares. In the case of panel data, the skipping of missing observations is supported only if their omission leaves a balanced panel. If missing observations are found in cases where they are not supported, gretl gives an error message and refuses to produce estimates.

Manipulating missing values

Some special functions are available for the handling of missing values. The Boolean function `missing()` takes the name of a variable as its single argument; it returns a series with value 1 for each observation at which the given variable has a missing value, and value 0 otherwise (that is, if the given variable has a valid value at that observation). The function `ok()` is complementary to `missing`; it is just a shorthand for `!missing` (where `!` is the Boolean NOT operator). For example, one can count the missing values for variable `x` using

```
scalar nmiss_x = sum(missing(x))
```

The function `zeromiss()`, which again takes a single series as its argument, returns a series where all zero values are set to the missing code. This should be used with caution—one does not want to confuse missing values and zeros—but it can be useful in some contexts. For example, one can determine the first valid observation for a variable `x` using

```
genr time
scalar x0 = min(zeromiss(time * ok(x)))
```

The function `misszero()` does the opposite of `zeromiss`, that is, it converts all missing values to zero.

If missing values get involved in calculations, they propagate according to the IEEE rules: notably, if one of the operands to an arithmetical operation is a NaN, the result will also be NaN.

4.7 Maximum size of data sets

Basically, the size of data sets (both the number of variables and the number of observations per variable) is limited only by the characteristics of your computer. Gretl allocates memory dynamically, and will ask the operating system for as much memory as your data require. Obviously, then, you are ultimately limited by the size of RAM.

Aside from the multiple-precision OLS option, gretl uses double-precision floating-point numbers throughout. The size of such numbers in bytes depends on the computer platform, but is typically eight. To give a rough notion of magnitudes, suppose we have a data set with 10,000 observations on 500 variables. That's 5 million floating-point numbers or 40 million bytes. If we define the megabyte (MB) as 1024×1024 bytes, as is standard in talking about RAM, it's slightly over 38 MB. The program needs additional memory for workspace, but even so, handling a data set of this size should be quite feasible on a current PC, which at the time of writing is likely to have at least 256 MB of RAM.

If RAM is not an issue, there is one further limitation on data size (though it's very unlikely to be a binding constraint). That is, variables and observations are indexed by signed integers, and on a typical PC these will be 32-bit values, capable of representing a maximum positive value of $2^{31} - 1 = 2,147,483,647$.

The limits mentioned above apply to gretl's "native" functionality. There are tighter limits with regard to two third-party programs that are available as add-ons to gretl for certain sorts of time-series analysis including seasonal adjustment, namely TRAMO/SEATS and X-12-ARIMA. These programs employ a fixed-size memory allocation, and can't handle series of more than 600 observations.

4.8 Data file collections

If you're using gretl in a teaching context you may be interested in adding a collection of data files and/or scripts that relate specifically to your course, in such a way that students can browse and access them easily.

There are three ways to access such collections of files:

- For data files: select the menu item “File, Open data, Sample file”, or click on the folder icon on the gretl toolbar.
- For script files: select the menu item “File, Script files, Example scripts”.

When a user selects one of the items:

- The data or script files included in the gretl distribution are automatically shown (this includes files relating to Ramanathan's *Introductory Econometrics* and Greene's *Econometric Analysis*).
- The program looks for certain known collections of data files available as optional extras, for instance the datafiles from various econometrics textbooks (Davidson and MacKinnon, Gujarati, Stock and Watson, Verbeek, Wooldridge) and the Penn World Table (PWT 5.6). (See [the data page](#) at the gretl website for information on these collections.) If the additional files are found, they are added to the selection windows.
- The program then searches for valid file collections (not necessarily known in advance) in these places: the “system” data directory, the system script directory, the user directory, and all first-level subdirectories of these. For reference, typical values for these directories are shown in Table 4.1. (Note that PERSONAL is a placeholder that is expanded by Windows, corresponding to “My Documents” on English-language systems.)

	<i>Linux</i>	<i>MS Windows</i>
system data dir	/usr/share/gretl/data	c:\Program Files\gretl\data
system script dir	/usr/share/gretl/scripts	c:\Program Files\gretl/scripts
user dir	\$HOME/gretl	PERSONAL\gretl

Table 4.1: Typical locations for file collections

Any valid collections will be added to the selection windows. So what constitutes a valid file collection? This comprises either a set of data files in gretl XML format (with the `.gdt` suffix) or a set of script files containing gretl commands (with `.inp` suffix), in each case accompanied by a “master file” or catalog. The gretl distribution contains several example catalog files, for instance the file descriptions in the `misc` sub-directory of the gretl data directory and `ps_descriptions` in the `misc` sub-directory of the scripts directory.

If you are adding your own collection, data catalogs should be named `descriptions` and script catalogs should be named `ps_descriptions` (in each case, with no suffix). The catalog file should be placed (along with the associated data or script files) in its own sub-directory (e.g. `/usr/share/gretl/data/mydata` or `c:\Program Files\gretl\data\mydata`).

The catalog files are plain text (encoded as UTF-8 if they contain any non-ASCII characters). The syntax of such files is straightforward. Here, for example, are the first few lines of gretl's “misc” data catalog:

```
# Gretl: various illustrative datafiles
"abdata","Arellano and Bond (1991) panel data","panel, T=9 N=140"
"anscombe","Anscombe's Quartet (artificial data)","cross section, n=11"
"arma","Artificial data for ARMA script example","time series, T=624"
"australia","Johansen's Australian macroeconomic data","time series, T=77"
```

The first line, which must start with a hash mark followed by a space, contains a short name (not to exceed 23 bytes)—here `Gretl`—which will appear as the label for this collection’s tab in the data browser window, terminated by a colon and optionally followed by a brief description of the collection as a whole.

Each subsequent line should contain three elements, wrapped in upright double quotes and separated by commas, as follows:

1. The name of a data file, not to exceed 23 characters (leave off the `.gdt` suffix here).
2. A short description of the content of the datafile, not to exceed 79 bytes.
3. A stylized record of the structure (cross section, time series or panel) and length of the dataset (see the examples from the Gretl collection above).

There should be one such line for each data file in the collection.

A script catalog file looks very similar. Again there are three fields in the per-file lines: a filename (without its `.inp` suffix); a brief account of the econometric point illustrated in the script; and a brief indication of the nature of the data used. Again, here are the first few lines of the supplied “misc” script catalog:

```
# Gretl: various sample scripts
"arbond91","Dynamic panel model (GMM-DIF)","UK employment data"
"armalooop","ARMA using command loop","artificial data"
"auto_arima","Automatic ARIMA model selection","artificial data"
"bbond98","Dynamic panel model (GMM-SYS)","UK employment data"
"biprobit","Bivariate probit (William Greene)","credit rating"
```

If you want to make your own data collection available to users, these are the steps:

1. Assemble the data, in whatever format is convenient.
2. Convert the data to gretl format and save as `gdt` files. It is probably easiest to convert the data by importing them into the program from plain text, CSV, or a spreadsheet format (MS Excel or Gnumeric) then saving them. You may wish to add descriptions of the individual variables (the “Variable, Edit attributes” menu item), and add information on the source of the data (the “Data, Dataset info” menu item).
3. Write a catalog file for the collection using a text editor.
4. Put the data files plus the catalog file in a subdirectory of the gretl data directory (or per-user directory).
5. If the collection is to be distributed to other people, package the data files and catalog in some suitable manner, e.g. as a zipfile.

If you assemble such a collection, and the data are not proprietary, we would encourage you to submit the collection for packaging as a gretl optional extra.

4.9 Assembling data from multiple sources

In many contexts researchers need to bring together data from multiple source files, and in some cases these sources are not organized such that the data can simply be “stuck together” by appending rows or columns to a base dataset. In gretl, the `join` command can be used for this purpose; this command is discussed in detail in chapter 7.

Chapter 5

Sub-sampling a dataset

5.1 Introduction

Some subtle issues can arise here; this chapter attempts to explain the issues.

A sub-sample may be defined in relation to a full dataset in two different ways: we will refer to these as “setting” the sample and “restricting” the sample; these methods are discussed in sections 5.2 and 5.3 respectively. In addition section 5.4 discusses some special issues relating to panel data, and section 5.5 covers resampling with replacement, which is useful in the context of bootstrapping test statistics.

The following discussion focuses on the command-line approach. But you can also invoke the methods outlined here via the items under the Sample menu in the GUI program.

5.2 Setting the sample

By “setting” the sample we mean defining a sub-sample simply by means of adjusting the starting and/or ending point of the current sample range. This is likely to be most relevant for time-series data. For example, one has quarterly data from 1960:1 to 2003:4, and one wants to run a regression using only data from the 1970s. A suitable command is then

```
smp1 1970:1 1979:4
```

Or one wishes to set aside a block of observations at the end of the data period for out-of-sample forecasting. In that case one might do

```
smp1 ; 2000:4
```

where the semicolon is shorthand for “leave the starting observation unchanged”. (The semicolon may also be used in place of the second parameter, to mean that the ending observation should be unchanged.) By “unchanged” here, we mean unchanged relative to the last `smp1` setting, or relative to the full dataset if no sub-sample has been defined up to this point. For example, after

```
smp1 1970:1 2003:4  
smp1 ; 2000:4
```

the sample range will be 1970:1 to 2000:4.

An incremental or relative form of setting the sample range is also supported. In this case a relative offset should be given, in the form of a signed integer (or a semicolon to indicate no change), for both the starting and ending point. For example

```
smp1 +1 ;
```

will advance the starting observation by one while preserving the ending observation, and

```
smp1 +2 -1
```

will both advance the starting observation by two and retard the ending observation by one.

An important feature of “setting” the sample as described above is that it necessarily results in the selection of a subset of observations that are contiguous in the full dataset. The structure of the dataset is therefore unaffected (for example, if it is a quarterly time series before setting the sample, it remains a quarterly time series afterwards).

5.3 Restricting the sample

By “restricting” the sample we mean selecting observations on the basis of some Boolean (logical) criterion, or by means of a random number generator. This is likely to be most relevant for cross-sectional or panel data.

Suppose we have data on a cross-section of individuals, recording their gender, income and other characteristics. We wish to select for analysis only the women. If we have a `male` dummy variable with value 1 for men and 0 for women we could do

```
smp1 male==0 --restrict
```

to this effect. Or suppose we want to restrict the sample to respondents with incomes over \$50,000. Then we could use

```
smp1 income>50000 --restrict
```

A question arises: if we issue the two commands above in sequence, what do we end up with in our sub-sample: all cases with income over 50000, or just women with income over 50000? By default, the answer is the latter: women with income over 50000. The second restriction augments the first, or in other words the final restriction is the logical product of the new restriction and any restriction that is already in place. If you want a new restriction to replace any existing restrictions you can first recreate the full dataset using

```
smp1 --full
```

Alternatively, you can add the `replace` option to the `smp1` command:

```
smp1 income>50000 --restrict --replace
```

This option has the effect of automatically re-establishing the full dataset before applying the new restriction.

Unlike a simple “setting” of the sample, “restricting” the sample may result in selection of non-contiguous observations from the full data set. It may therefore change the structure of the data set.

This can be seen in the case of panel data. Say we have a panel of five firms (indexed by the variable `firm`) observed in each of several years (identified by the variable `year`). Then the restriction

```
smp1 year==1995 --restrict
```

produces a dataset that is not a panel, but a cross-section for the year 1995. Similarly

```
smp1 firm==3 --restrict
```

produces a time-series dataset for firm number 3.

For these reasons (possible non-contiguity in the observations, possible change in the structure of the data), `gretl` acts differently when you “restrict” the sample as opposed to simply “setting” it. In

the case of setting, the program merely records the starting and ending observations and uses these as parameters to the various commands calling for the estimation of models, the computation of statistics, and so on. In the case of restriction, the program makes a reduced copy of the dataset and by default treats this reduced copy as a simple, undated cross-section—but see the further discussion of panel data in section 5.4.

If you wish to re-impose a time-series interpretation of the reduced dataset you can do so using the `setobs` command, or the GUI menu item “Data, Dataset structure”.

The fact that “restricting” the sample results in the creation of a reduced copy of the original dataset may raise an issue when the dataset is very large. With such a dataset in memory, the creation of a copy may lead to a situation where the computer runs low on memory for calculating regression results. You can work around this as follows:

1. Open the full data set, and impose the sample restriction.
2. Save a copy of the reduced data set to disk.
3. Close the full dataset and open the reduced one.
4. Proceed with your analysis.

Random sub-sampling

Besides restricting the sample on some deterministic criterion, it may sometimes be useful (when working with very large datasets, or perhaps to study the properties of an estimator) to draw a random sub-sample from the full dataset. This can be done using, for example,

```
smp1 100 --random
```

to select 100 cases. If you want the sample to be reproducible, you should set the seed for the random number generator first, using the `set` command. This sort of sampling falls under the “restriction” category: a reduced copy of the dataset is made.

5.4 Panel data

Consider for concreteness the Arellano–Bond dataset supplied with `gretl` (`abdata.gdt`). This comprises data on 140 firms ($n = 140$) observed over the years 1976–1984 ($T = 9$). The dataset is “nominally balanced” in the sense that the time-series length is the same for all countries (this being a requirement for a dataset to count as a panel in `gretl`), but in fact there are many missing values (NAs).

You may want to sub-sample such a dataset in either the cross-sectional dimension (limit the sample to a subset of firms) or the time dimension (e.g. use data from the 1980s only). One way to sub-sample on firms keys off the notation used by `gretl` for panel observations. The full data range is printed as 1:1 (firm 1, period 1) to 140:9 (firm 140, period 9). The effect of

```
smp1 1:1 80:9
```

is to limit the sample to the first 80 firms. Note that if you instead tried `smp1 1:1 80:4` this would provoke an error: you cannot use this syntax to sub-sample in the time dimension of the panel. Alternatively, and perhaps more naturally, you can use the `--unit` option with the `smp1` command to limit the sample in the cross-sectional dimension, as in

```
smp1 1 80 --unit
```

The firms in the Arellano–Bond dataset are anonymous, but suppose you had a panel with five named countries. With such a panel you can inform `gretl` of the names of the groups using the `setobs` command. For example, given

```
string cstr = "Portugal Italy Ireland Greece Spain"
setobs country cstr --panel-groups
```

gretl creates a string-valued series named `country` with group names taken from the variable `cstr`. Then, to include only Italy and Spain you could do

```
smp1 country=="Italy" || country=="Spain" --restrict
```

or to exclude one country,

```
smp1 country!="Ireland" --restrict
```

Sub-sampling a panel in the time dimension can be done via `--restrict`. For example, the Arellano-Bond dataset contains a variable named `YEAR` that records the year of the observations and if one wanted to omit the first two years of data one could do

```
smp1 YEAR >= 1978 --restrict
```

If a dataset does not already include a suitable variable for this purpose one can use the command `genr time` to create a simple 1-based time index.

Another way to sub-sample in the time dimension of a panel starts with a specification of time via the `setobs` command, as in

```
setobs 1 1976 --panel-time
```

This tells `gretl` that panel-time is annual (frequency 1), starting in 1976. (In fact this is already done for `abdata.gdt`.) Then to restrict the sample range to 1979–1982 you can do

```
smp1 1979 1982 --time
```

Note that if you apply a sample restriction that just selects certain units (firms, countries or whatever), or selects certain contiguous time-periods—such that $n > 1$, $T > 1$ and the time-series length is still the same across all included units—your sub-sample will still be interpreted by `gretl` as a panel.

Unbalancing restrictions

In some cases one wants to sub-sample according to a criterion that “cuts across the grain” of a panel dataset. For instance, suppose you have a micro dataset with thousands of individuals observed over several years and you want to restrict the sample to observations on employed women.

If we simply extracted from the total nT rows of the dataset those that pertain to women who were employed at time t ($t = 1, \dots, T$) we would likely end up with a dataset that doesn’t count as a panel in `gretl` (because the specific time-series length, T_i , would differ across individuals). In some contexts it might be OK that `gretl` doesn’t take your sub-sample to be a panel, but if you want to apply panel-specific methods this is a problem. You can solve it by giving the `--preserve-panel` option with `smp1`. For example, supposing your dataset contained dummy variables `gender` (with the value 1 coding for women) and `employed`, you could do

```
smp1 gender==1 && employed==1 --restrict --preserve-panel
```

What exactly does this do? Well, let’s say the years of your data are 2000, 2005 and 2010, and that some women were employed in all of those years, giving a maximum T_i value of 3. But individual 526 is a woman who was employed only in the year 2000 ($T_i = 1$). The effect of the `--preserve-panel` option is then to insert “padding rows” of NAs for the years 2005 and 2010 for individual 526, and similarly for all individuals with $0 < T_i < 3$. Your sub-sample then qualifies as a panel.

5.5 Resampling and bootstrapping

Given an original data series x , the command

```
series xr = resample(x)
```

creates a new series each of whose elements is drawn at random from the elements of x . If the original series has 100 observations, each element of x is selected with probability $1/100$ at each drawing. Thus the effect is to “shuffle” the elements of x , with the twist that each element of x may appear more than once, or not at all, in xr .

The primary use of this function is in the construction of bootstrap confidence intervals or p-values. Here is a simple example. Suppose we estimate a simple regression of y on x via OLS and find that the slope coefficient has a reported t -ratio of t_0 with ν degrees of freedom. A two-tailed p-value for the null hypothesis that the slope parameter equals zero can then be found using the $t(\nu)$ distribution. Depending on the context, however, we may doubt whether the ratio of coefficient to standard error truly follows the $t(\nu)$ distribution. In that case we could derive a bootstrap p-value as shown in Listing 5.1.

Under the null hypothesis that the slope with respect to x is zero, y is simply equal to its mean plus an error term. We simulate y by resampling the residuals from the initial OLS and re-estimate the model. We repeat this procedure a large number of times, and record the number of cases where the absolute value of the t -ratio is greater than t_0 : the proportion of such cases is our bootstrap p-value. For a good discussion of simulation-based tests and bootstrapping, see Davidson and MacKinnon (2004, chapter 4); Davidson and Flachaire (2001) is also instructive.

Listing 5.1: Calculation of bootstrap p-value [\[Download ▼\]](#)

```
nulldata 50
set seed 54321
series x = normal()
series y = 10 + x + 2*normal()
ols y 0 x
# the reported t-stat
t0 = abs($coeff[2] / $stderr[2])
# save the residuals
series u = $uhat
scalar ybar = mean(y)
# number of replications for bootstrap
scalar B = 1000
scalar tcount = 0
series ysim
loop B
  # generate simulated y by resampling
  ysim = ybar + resample(u)
  ols ysim 0 x --quiet
  scalar tsim = abs($coeff[2] / $stderr[2])
  tcount += (tsim > t0)
endloop
printf "proportion of cases with |t| > %.3f = %g\n", t0, tcount / B
```

Chapter 6

Graphics

6.1 Gnuplot graphs

A separate program, `gnuplot`, is called to generate graphs. Gnuplot is a very full-featured graphing program with myriad options. It is available from www.gnuplot.info (but note that a suitable copy of `gnuplot` is bundled with the packaged versions of `gretl` for MS Windows and Mac OS X). `Gretl` gives you direct access, via a graphical interface, to a subset of `gnuplot`'s options and it tries to choose sensible values for you; it also allows you to take complete control over graph details if you wish.

With a graph displayed, you can right-click on the graph window (or use the “hamburger” toolbar button) for a pop-up menu with the following options.

- **Save as PNG:** Save the graph in Portable Network Graphics format (the same format that you see on screen).
- **Save as postscript (EPS):** Save in encapsulated postscript format.
- **Save as PDF:** Save in PDF format.
- **Save as Windows metafile:** Save in Enhanced Metafile (EMF) format (with color and monochrome options).
- **Copy to clipboard:** with color and monochrome options.
- **Save to session as icon:** The graph will appear in iconic form when you select “Icon view” from the View menu.
- **Zoom:** Lets you select an area within the graph for closer inspection (not available for all graphs).
- **Display PDF:** view a PDF version of the graph.
- **Edit:** Opens a controller for the plot which lets you adjust many aspects of its appearance.
- **Close:** Closes the graph window.

If you select **Save as postscript** or **Save as PDF** you get a dialog box that lets you adjust several aspects of the graph, and also preview the result.

Displaying data labels

For simple X-Y scatter plots, some further options are available if the dataset includes “case markers” (that is, labels identifying each observation).¹ With a scatter plot displayed, when you move the mouse pointer over a data point its label is shown on the graph. By default these labels are transient: they do not appear in the printed or copied version of the graph. They can be removed by selecting “Clear data labels” from the graph pop-up menu. If you want the labels to be affixed permanently (so they will show up when the graph is printed or copied), select the option “Freeze data

¹For an example of such a dataset, see the Ramanathan file `data4-10`: this contains data on private school enrollment for the 50 states of the USA plus Washington, DC; the case markers are the two-letter codes for the states.

labels” from the pop-up menu; “Clear data labels” cancels this operation. The other label-related option, “All data labels”, requests that case markers be shown for all observations. At present the display of case markers is disabled for graphs containing more than 250 data points.

GUI plot editor

Selecting the Edit option in the graph popup menu opens an editing dialog box, shown in Figure 6.1. Notice that there are several tabs, allowing you to adjust many aspects of a graph’s appearance: font, title, axis scaling, line colors and types, and so on. You can also add lines or descriptive labels to a graph (under the Lines and Labels tabs). The “Apply” button applies your changes without closing the editor; “OK” applies the changes and closes the dialog.

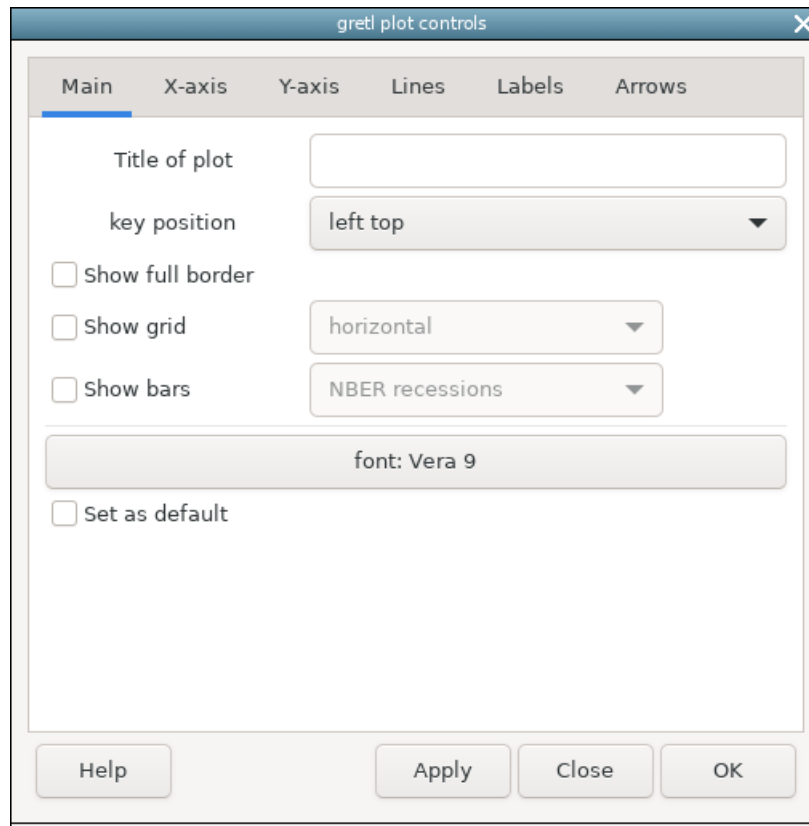


Figure 6.1: gretl’s plot controller

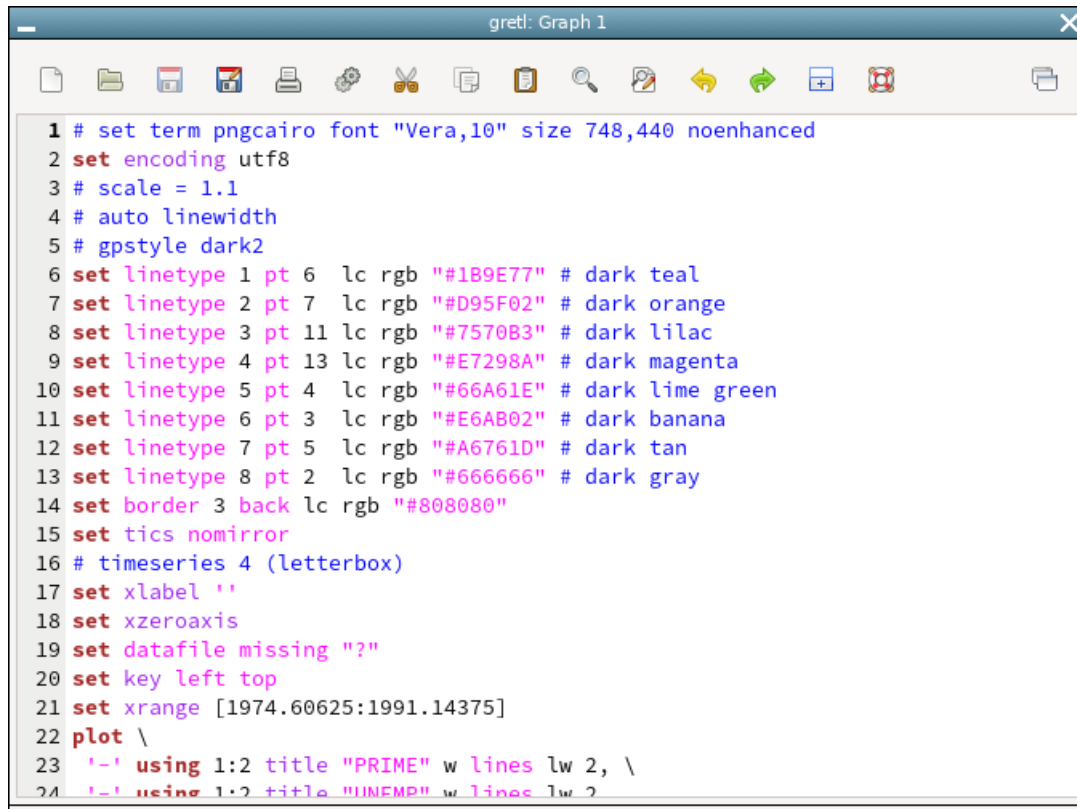
Publication-quality graphics: advanced options

The GUI plot editor has two limitations. First, it cannot represent all the myriad options that **gnuplot** offers. Users who are sufficiently familiar with **gnuplot** to know what they’re missing in the plot editor presumably don’t need much help from gretl, so long as they can get hold of the **gnuplot** command file that gretl has put together. Second, even if the plot editor meets your needs, in terms of fine-tuning the graph you see on screen, a few details may need further work in order to get optimal results for publication.

Either way, the first step in advanced tweaking of a graph is to get access to the graph command file.

- In the graph display window, right-click and choose “Save to session as icon”.

- If it's not already open, open the icon view window—either via the menu item View/Icon view, or by clicking the “session icon view” button on the main-window toolbar.
- Right-click on the icon representing the newly added graph and select “Edit plot commands” from the pop-up menu.
- You get a window displaying the plot file (Figure 6.2).



```

1 # set term pngcairo font "Vera,10" size 748,440 noenhanced
2 set encoding utf8
3 # scale = 1.1
4 # auto linewidth
5 # gpstyle dark2
6 set linetype 1 pt 6 lc rgb "#1B9E77" # dark teal
7 set linetype 2 pt 7 lc rgb "#D95F02" # dark orange
8 set linetype 3 pt 11 lc rgb "#7570B3" # dark lilac
9 set linetype 4 pt 13 lc rgb "#E7298A" # dark magenta
10 set linetype 5 pt 4 lc rgb "#66A61E" # dark lime green
11 set linetype 6 pt 3 lc rgb "#E6AB02" # dark banana
12 set linetype 7 pt 5 lc rgb "#A6761D" # dark tan
13 set linetype 8 pt 2 lc rgb "#666666" # dark gray
14 set border 3 back lc rgb "#808080"
15 set tics nomirror
16 # timeseries 4 (letterbox)
17 set xlabel ''
18 set xzeroaxis
19 set datafile missing "?"
20 set key left top
21 set xrange [1974.60625:1991.14375]
22 plot \
23 '-' using 1:2 title "PRIME" w lines lw 2, \
24 '-' using 1:2 title "UNEMP" w lines lw 2

```

Figure 6.2: Plot commands editor

Here are the basic things you can do in this window. Obviously, you can edit the file you just opened. You can also send it for processing by gnuplot, by clicking the “Execute” (cogwheel) icon in the toolbar. Or you can use the “Save as” button to save a copy for editing and processing as you wish. And please note that the Help button on the toolbar (a lifebelt in Figure 6.2) gives you access to the gnuplot manual.

One relatively simple editorial job would be to set a chosen driver (or “terminal” in gnuplot parlance) and output filename. For example, to get PDF output you could insert lines like the following at the top:

```

# PDF, slightly amended (the default size is 5in x 3in)
set term pdfcairo font "Sans,6" size 5in,3.5in
set output 'mygraph1.pdf'
# or small size
set term pdfcairo font "Sans,5" size 3in,2in
set output 'mygraph2.pdf'
# or with size given in centimeters
set term pdfcairo font "Sans,6" size 6cm,4.2cm
set output 'mygraph3.pdf'

```

Or substitute `epscairo` for `pdfcairo` (and change the filenames) if you want EPS output. However, such changes may be more easily made via the Save as PDF and Save as postscript options in the plot menu.²

The real payoff to editing the plot code can be obtained if you dive into the details and employ gnuplot features that are not accessible via gretl, and/or use one of the terminal types not directly supported by gretl, such as `context` (ConTeXt), `mp` (MetaPost), `lua` (Lua) or `pslatex` (L^AT_EX picture environment with PostScript specials). The `lua` terminal with the `tikz` option is especially useful for L^AT_EX users, because it produces a `tikzpicture` environment, which offers almost unlimited customization possibilities (note that in order to use plots produced in this way you'll also need the `gnuplot-lua-tikz` L^AT_EX package).

To find out more about gnuplot visit gnuplot.sourceforge.net. This site has documentation for the current version of the program in various formats along with a large collection of demonstration plots.

Additional tips

To be written. Line widths, enhanced text. Show a “before and after” example.

6.2 Plotting graphs from scripts

When working with scripts, you may want to have a graph shown onto your display or saved into a file. In fact, if in your usual workflow you find yourself creating similar graphs over and over again, you might want to consider the option of writing a script which automates this process for you. gretl gives you two main tools for doing this: one is a command called `gnuplot`, whose main use is to create standard plot quickly. The other one is the `plot` command block, which has a more elaborate syntax but offers you more control on output.

The `gnuplot` command

The `gnuplot` command is described at length in the *Gretl Command Reference* and the online help system. Here, we just summarize its main features: basically, it consists of the `gnuplot` keyword, followed by a list of items, telling the command *what* you want plotted and a list of options, telling it *how* you want it plotted.

For example, the line

```
gnuplot y1 y2 x
```

will give you a basic XY plot of the two series `y1` and `y2` on the vertical axis versus the series `x` on the horizontal axis. In general, the arguments to the `gnuplot` command is a list of series, the last of which goes on the x-axis, while all the other ones go onto the y-axis. By default, the `gnuplot` command gives you a scatterplot. If you just have one variable on the y-axis, then gretl will also draw a the OLS interpolation, if the fit is good enough.³

Several aspects of the behavior described above can be modified. You do this by appending options to the command. Most options can be broadly grouped in three categories:

1. Plot styles: we support points (the default choice), lines, lines and points together, and impulses (vertical lines).
2. Algorithm for the fitted line: here you can choose between linear, quadratic and cubic interpolation, but also more exotic choices, such as semi-log, inverse or loess (non-parametric). Of course, you can also turn this feature off.

²A “traditional” `postscript` terminal may also be available in gnuplot, with an `eps` option. The defaults in this case are quite different from `epscairo`, and to make use of the alternative you'll have to consult the gnuplot manual.

³The technical condition for this is that the two-tailed *p*-value for the slope coefficient should be under 10%.

Listing 6.1: Plotting macroeconomic data

```

open AWM.gdt --quiet

# --- consumption and income, different styles -----

gnuplot PCR YER
gnuplot PCR YER --output=display
gnuplot PCR YER --output=display --time-series
gnuplot PCR YER --output=display --time-series --with-lines

# --- Phillips' curve, different fitted lines -----

gnuplot INFQ URX --output=display
gnuplot INFQ URX --fit=none --output=display
gnuplot INFQ URX --fit=inverse --output=display
gnuplot INFQ URX --fit=loess --output=display

```

3. Input and output: you can choose whether you want your graph on your computer screen (and possibly use the in-built graphical widget to further customize it — see above, page 37), or rather save it to a file. We support several graphical formats, among which PNG and PDF, to make it easy to incorporate your plots into text documents.

Listing 6.1 shows examples of some traditional plots in macroeconomics, using time series from the “area-wide model” dataset produced by the European Central Bank, which is shipped with gretl in the file `AWM.gdt`. PCR is aggregate private real consumption and YER is real GDP.

The first command line in the listing plots consumption against income as a kind of Keynesian consumption function. More precisely, it produces a simple scatter plot with an automatically linear fitted line. If this is executed in the gretl console the plot will be directly shown in a new window, but if this line is contained in a script then instead a file with the plot commands will be saved for later execution. The second example line changes this behavior for a script command and forces the plot to be shown directly.

The third line instead asks for a plot of the two variables as two separate curves against time on the x-axis. Each observation point is drawn separately with a certain symbol determined by gnuplot defaults. If you add the option `--with-lines` the points will be connected with a continuous line and the symbols omitted.

The second batch of examples demonstrate how the fitted line in the scatter plot can be controlled from gretl’s side. The option `--fit=none` overrides gnuplot’s default to draw a line if it deems the fit to be “good enough”. The effect of `--fit=inverse` is to consider the variable on the y-axis as a function of $1/X$ instead of X and draw the corresponding hyperbolic branch. For the workings of a Loess fit (locally-weighted polynomial regression) please refer to the documentation of the `loess` function.

For more detail, consult the *Gretl Command Reference*.

The `plot` command block

The `plot` environment is a way to pass information to Gnuplot in a more structured way, so that customization of basic plots becomes easier. It has the following characteristics:

The block starts with the `plot` keyword, followed by a required parameter: the name of a list, a single series or a matrix. This parameter specifies the data to be plotted. The starting line may be

prefixed with the `savename <- apparatus` to save a plot as an icon in the GUI program. The block ends with `end plot`.

Inside the block you have zero or more lines of these types, identified by an initial keyword:

option: specify a single option (details below)

options: specify multiple options on a single line; if more than one option is given on a line, the options should be separated by spaces.

literal: a command to be passed to gnuplot literally

printf: a printf statement whose result will be passed to gnuplot literally; this allows the use of string variables without having to resort to @-style string substitution.

The options available are basically those of the current `gnuplot` command, but with a few differences. For one thing you don't need the leading double-dash in an "option" (or "options") line. Besides that,

- You can't use the option `--matrix=whatever` with `plot`: that possibility is handled by providing the name of a matrix on the initial `plot` line.
- The `--input=filename` option is not supported: use `gnuplot` for the case where you're supplying the entire plot specification yourself.
- The several options pertaining to the presence and type of a fitted line, are replaced in `plot` by a single option `fit` which requires a parameter. Supported values for the parameter are: none, linear, quadratic, cubic, inverse, semilog and loess. Example:

```
option fit=quadratic
```

As with `gnuplot`, the default is to show a linear fit in an X-Y scatter if it's significant at the 10 percent level.

Here's a simple example, the plot specification from the "bandplot" package, which shows how to achieve the same result via the `gnuplot` command and a `plot` block, respectively—the latter occupies a few more lines but is clearer

```
gnuplot 1 2 3 4 --with-lines --matrix=plotmat \
--fit=none --output=display \
{ set linetype 3 lc rgb "#0000ff"; set title "@title"; \
  set nokey; set xlabel "@xname"; }

plot plotmat
  options with-lines fit=none
  literal set linetype 3 lc rgb "#0000ff"
  literal set nokey
  printf "set title \"%s\\\"", title
  printf "set xlabel \"%s\\\"", xname
end plot --output=display
```

Note that `--output=display` is appended to `end plot`; also note that if you give a matrix to `plot` it's assumed you want to plot all the columns. In addition, if you give a single series and the dataset is time series, it's assumed you want a time-series plot.

Listing 6.2: Plotting the log wage from the Mroz example dataset [\[Download ▼\]](#)

```
set verbose off
open mroz87.gdt --quiet

series lww = log(WW)
scalar m = mean(lww)
scalar s = sd(lww)

###
### prepare matrix with data for plot
###

# number of valid observations
scalar n = nobs(lww)
# discretize log wage
scalar k = 4
series disc_lww = round(lww*k)/k
# get frequencies
matrix f = aggregate(null, disc_lww)
# add density
phi = dnorm((f[,1] - m)/s) / (s*k)
# put columns together and add labels
plotmat = f[,2] ./ n ~ phi ~ f[,1]
strings cnames = defarray("frequency", "density", "log wage")
cnameset(plotmat, cnames)

###
### create plot
###

plot plotmat
    # move legend
    literal set key outside rmargin
    # set line style
    literal set linetype 2 dashtype 2 linewidth 2
    # set histogram color
    literal set linetype 1 lc rgb "#777777"
    # set histogram style
    literal set style fill solid 0.25 border
    # set histogram width
    printf "set boxwidth %4.2f\n", 0.5/k
    options with-lines=2 with-boxes=1
end plot --output=display
```

Example: Plotting an histogram together with a density

Listing 6.2 contains a slightly more elaborate example: here we load the Mroz example dataset and calculate the log of the individual's wage. Then, we match the histogram of a discretized version of the same variable (obtained via the `aggregate()` function) versus the theoretical density if data were Gaussian.

There are a few points to note:

- The data for the plot are passed through a matrix in which we set column names via the `cnameset` function; those names are then automatically used by the `plot` environment.
- In this example, we make extensive use of the `set` `literal` construct for refining the plot by passing instruction to `gnuplot`; the power of `gnuplot` is impossible to overstate. We encourage you to visit the “demos” version of `gnuplot`'s website (<http://gnuplot.sourceforge.net/>) and revel in amazement.
- In the `plot` environment you can use all the quantities you have in your script. This is the way we calibrate the histogram width (try setting the scalar `k` in the script to different values). Note that the `printf` command has a special meaning inside a `plot` environment.
- The script displays the plot on your screen. If you want to save it to a file instead, replace `--output=display` at the end with `--output=filename`.
- It's OK to insert comments in the `plot` environment; actually, it's a rather good idea to comment as much as possible (as always)!

The output from the script is shown in Figure 6.3.

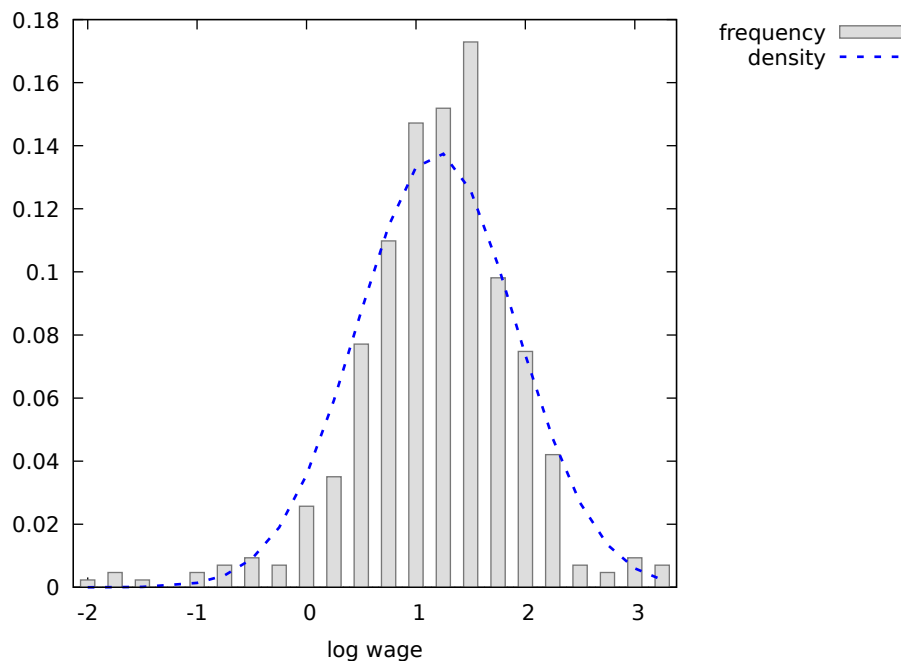


Figure 6.3: Output from listing 6.2

Example: Plotting Student's t densities

The power of the `printf` statement in a `plot` block becomes apparent when used jointly with user-defined functions, as exemplified in Listing 6.3, in which we create a plot showing the density functions of Student's t distribution for three different settings of the “degrees of freedom”

Listing 6.3: Plotting t densities for varying degrees of freedom [\[Download ▼\]](#)

```

set verbose off

function string tplot(scalar m)
    return sprintf("stud(x,%d) title \"t(%d)\", m, m)
end function

matrix dfs = {2, 4, 16}

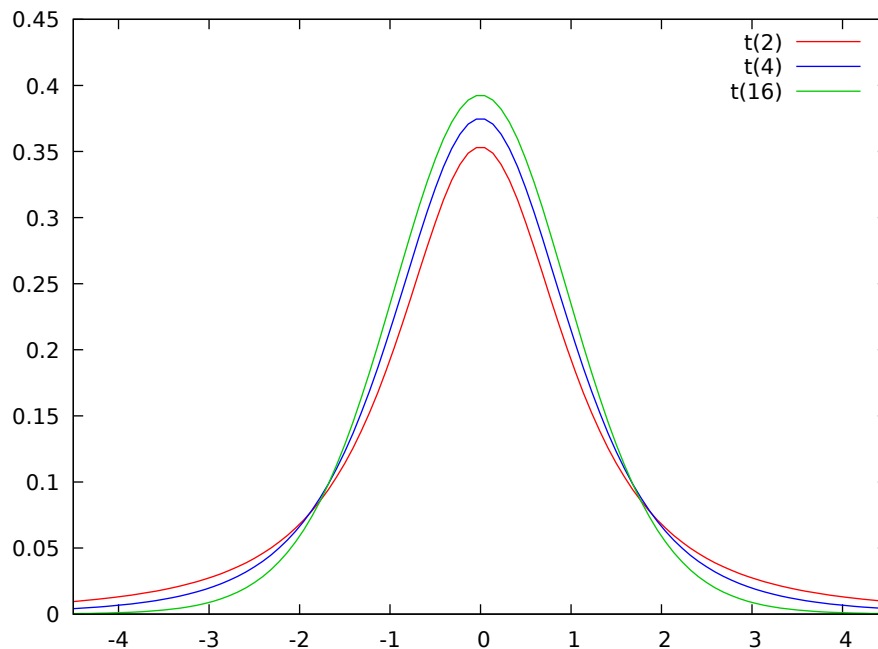
plot
    literal set xrange [-4.5:4.5]
    literal set yrange [0:0.45]
    literal Binv(p,q) = exp(lgamma(p+q)-lgamma(p)-lgamma(q))
    literal stud(x,m) = Binv(0.5*m,0.5)/sqrt(m)*(1.0+(x*x)/m)**(-0.5*(m+1.0))
    printf "plot %s, %s, %s", tplot(dfs[1]), tplot(dfs[2]), tplot(dfs[3])
end plot --output=display

```

parameter (note that plotting a t density is very easy to do from the GUI: just go to the *Tools > Distribution graphs* menu).

First we define a user function called `tplot`, which returns a string with the ingredients to pass to the gnuplot `plot` statement, as a function of a scalar parameter (the degrees of freedom in our case). Next, this function is used within the `plot` block to plot the appropriate density. Note that most of the statements to mathematically define the function to plot are outsourced to gnuplot via the `literal` command.

The output from the script is shown in Figure 6.4.

**Figure 6.4:** Output from listing 6.3

6.3 Boxplots

These plots (after Tukey and Chambers) display the distribution of a variable. Its shape depends on a few quantities, defined as follows:

x_{\min}	sample minimum
Q_1	first quartile
m	median
\bar{x}	mean
Q_3	third quartile
x_{\max}	sample maximum
$R = Q_3 - Q_1$	interquartile range

The central box encloses the middle 50 percent of the data, i.e. goes from Q_1 to Q_3 ; therefore, its height equals R . A line is drawn across the box at the median m and a “+” sign identifies the mean \bar{x} .

The length of the “whiskers” depends on the presence of outliers. The top whisker extends from the top of the box up to a maximum of 1.5 times the interquartile range, but can be shorter if the sample maximum is lower than that value; that is, it reaches $\min[x_{\max}, Q_3 + 1.5R]$. Observations larger than $Q_3 + 1.5R$, if any, are considered outliers and represented individually via dots.⁴ The bottom whisker obeys the same logic, with obvious adjustments. Figure 6.5 provides an example of all this by using the variable FAMINC from the sample dataset `mroz87`.

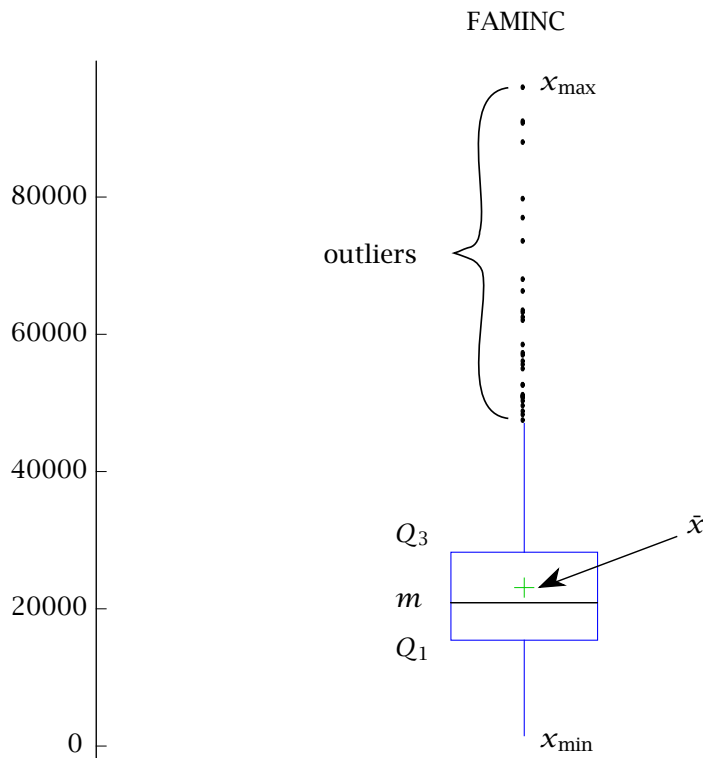


Figure 6.5: Sample boxplot

In the case of boxplots with confidence intervals, dotted lines show the limits of an approximate 90

⁴To give you an intuitive idea, if a variable is normally distributed, the chances of picking an outlier by this definition are slightly below 0.7%.

percent confidence interval for the median. This is obtained by the bootstrap method, which can take a while if the data series is very long. For details on constructing boxplots, see the entry for `boxplot` in the *Gretl Command Reference* or use the Help button that appears when you select one of the boxplot items under the menu item “View, Graph specified vars” in the main gretl window.

Factorized boxplots

A nice feature which is quite useful for data visualization is the conditional, or factorized boxplot. This type of plot allows you to examine the distribution of a variable conditional on the value of some discrete factor.

As an example, we’ll use one of the datasets supplied with gretl, that is `rac3d`, which contains an example taken from [Cameron and Trivedi \(2013\)](#) on the health conditions of 5190 people. The script below compares the unconditional (marginal) distribution of the number of illnesses in the past 2 weeks with the distribution of the same variable, conditional on age classes.

```
open rac3d.gdt
# unconditional boxplot
boxplot ILLNESS --output=display
# create a discrete variable for age class:
# 0 = below 20, 1 = between 20 and 39, etc
series age_class = floor(AGE/0.2)
# conditional boxplot
boxplot ILLNESS age_class --factorized --output=display
```

After running the code above, you should see two graphs similar to Figure 6.6. By comparing the marginal plot to the factorized one, the effect of age on the mean number of illnesses is quite evident: by joining the green crosses you get what is technically known as the conditional mean function, or regression function if you prefer.

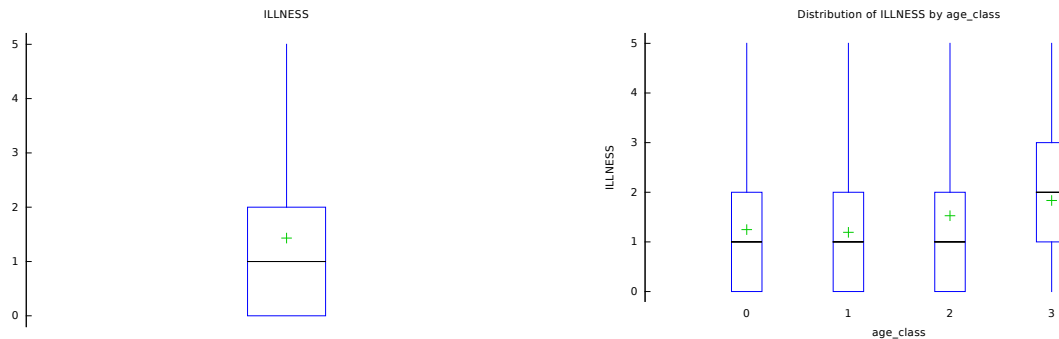


Figure 6.6: Conditional and unconditional distribution of illnesses

Chapter 7

Joining data sources

7.1 Introduction

Gretl provides two commands for adding data from file to an existing dataset in the program's workspace, namely `append` and `join`. The `append` command, which has been available for a long time, is relatively simple and is described in the *Gretl Command Reference*. Here we focus on the `join` command, which is much more flexible and sophisticated. This chapter gives an overview of the functionality of `join` along with a detailed account of its syntax and options. We provide several toy examples and discuss one real-world case at length.

First, a note on terminology: in the following we use the terms “left-hand” and “inner” to refer to the dataset that is already in memory, and the terms “right-hand” and “outer” to refer to the dataset in the file from which additional data are to be drawn.

Two main features of `join` are worth emphasizing at the outset:

- “Key” variables can be used to match specific observations (rows) in the inner and outer datasets, and this match need not be 1 to 1.
- A row filter may be applied to screen out unwanted observations in the outer dataset.

As will be explained below, these features support rather complex concatenation and manipulation of data from different sources.

A further aspect of `join` should be noted—one that makes this command particularly useful when dealing with very large data files. That is, when `gretl` executes a `join` operation it does not, in general, read into memory the entire content of the right-hand side dataset. Only those columns that are actually needed for the operation are read in full. This makes `join` faster and less demanding of computer memory than the methods available in most other software. On the other hand, `gretl`'s asymmetrical treatment of the “inner” and “outer” datasets in `join` may require some getting used to, for users of other packages.

7.2 Basic syntax

The minimal invocation of `join` is

```
join filename varname
```

where *filename* is the name of a data file and *varname* is the name of a series to be imported. Only two sorts of data file are supported at present: delimited text files (where the delimiter may be comma, space, tab or semicolon) and “native” `gretl` data files (`gdt` or `gdtb`). A series named *varname* may already be present in the left-hand dataset, but that is not required. The series to be imported may be numerical or string-valued. For most of the discussion below we assume that just a single series is imported by each `join` command, but see section 7.7 for an account of multiple imports.

The effect of the minimal version of `join` is this: `gretl` looks for a data column labeled *varname* in the specified file; if such a column is found and the number of observations on the right matches the number of observations in the current sample range on the left, then the values from the right are copied into the relevant range of observations on the left. If *varname* does not already exist

on the left, any observations outside of the current sample are set to NA; if it exists already then observations outside of the current sample are left unchanged.

The case where you want to rename a series on import is handled by the `--data` option. This option has one required argument, the name by which the series is known on the right. At this point we need to explain something about right-hand variable names (column headings).

Right-hand names

We accept on input arbitrary column heading strings, but if these strings do not qualify as valid gretl identifiers they are automatically converted, and in the context of `join` you must use the converted names. A gretl identifier must start with a letter, contain nothing but (ASCII) letters, digits and the underscore character, and must not exceed 31 characters. The rules used in name conversion are:

1. Skip any leading non-letters.
2. Until the 31-character is reached or the input is exhausted: transcribe “legal” characters; skip “illegal” characters apart from spaces; and replace one or more consecutive spaces with an underscore, unless the last character transcribed is an underscore in which case space is skipped.

In the unlikely event that this policy yields an empty string, we replace the original with `col n` , where n is replaced by the 1-based index of the column in question among those used in the `join` operation. If you are in doubt regarding the converted name of a given column, the function `fixname()` can be used as a check: it takes the original string as an argument and returns the converted name. Examples:

```
? eval fixname("valid_identifier")
valid_identifier
? eval fixname("12. Some name")
Some_name
```

Returning to the use of the `--data` option, suppose we have a column headed "12. Some name" on the right and wish to import it as `x`. After figuring how the right-hand name converts, we can do

```
join foo.csv x --data="Some_name"
```

No right-hand names?

Some data files have no column headings; they jump straight into the data (and you need to determine from accompanying documentation what the columns represent). Since gretl expects column headings, you have to take steps to get the importation right. It is generally a good idea to insert a suitable header row into the data file. However, if for some reason that's not practical, you should give the `--no-header` option, in which case gretl will name the columns on the right as `col1`, `col2` and so on. If you do not do either of these things you will likely lose the first row of data, since gretl will attempt to make variable names out of it, as described above.

7.3 Filtering

Rows from the *outer* dataset can be filtered using the `--filter` option. The required parameter for this option is a Boolean condition, that is, an expression which evaluates to non-zero (true, include the row) or zero (false, skip the row) for each of the outer rows. The filter expression may include any of the following terms: up to three “right-hand” series (under their converted names as

explained above); scalar or string variables defined “on the left”; any of the operators and functions available in `gretl` (including user-defined functions); and numeric or string constants.

Here are a few simple examples of potentially valid filter options (assuming that the specified right-hand side columns are found):

```
# 1. relationship between two right-hand variables
--filter="x15<=x17"

# 2. comparison of right-hand variable with constant
--filter="nkids>2"

# 3. comparison of string-valued right-hand variable with string constant
--filter="SEX==\"F\""

# 4. filter on valid values of a right-hand variable
--filter=!missing(income)

# 5. compound condition
--filter="x < 100 && (x > 0 || y > 0)"
```

Note that if you are comparing against a string constant (as in example 3 above) it is necessary to put the string in “escaped” double-quotes (each double-quote preceded by a backslash) so the interpreter knows that `F` is not supposed to be the name of a variable.

It is safest to enclose the whole filter expression in double quotes, however this is not strictly required unless the expression contains spaces or the equals sign.

In general, an error is flagged if a missing value is encountered in a series referenced in a filter expression, because the condition then becomes indeterminate. In example 2 above, if the `nkids` value is `NA` on any given row we are not in a position to evaluate the condition `nkids>2`. However, you can use the `missing()` function—or `ok()`, which is a shorthand for `!missing()`—if you need a filter that keys off the missing or non-missing status of a variable.

7.4 Matching with keys

Things get interesting when we come to key-matching. The purpose of this facility is perhaps best introduced by example. Suppose that (as with many survey and census-based datasets) we have a dataset that is composed of two or more related files, each having a different unit of observation; for example we have a “persons” data file and a “households” data file. Table 7.1 shows a simple, artificial case. The file `people.csv` contains a unique identifier for the individuals, `pid`. The households file, `hholds.csv`, contains the unique household identifier `hid`, which is also present in the persons file.

As a first example of `join` with keys, let’s add the household-level variable `xh` to the persons dataset:

```
open people.csv --quiet
join hholds.csv xh --ikey=hid
print --byobs
```

The basic key option is named `ikey`; this indicates “inner key”, that is, the key variable found in the left-hand or inner dataset. By default it is assumed that the right-hand dataset contains a column of the same name, though as we’ll see below that assumption can be overridden. The `join` command above says, find a series named `xh` in the right-hand dataset and add it to the left-hand one, using the values of `hid` to match rows. Looking at the data in Table 7.1 we can see how this should work. Persons 1 and 2 are both members of household 1, so they should both get values of 1 for `xh`; persons 3 and 4 are members of household 2, so that `xh = 4`; and so on. Note that the order

in which the key values occur on the right-hand side does not matter. The gretl output from the `print` command is shown in the lower panel of Table 7.1.

people.csv				hholds.csv		
pid,hid,gender,age,xp				hid,country,xh		
1,1,M,50,1				1,US,1		
2,1,F,40,2				6,IT,12		
3,2,M,30,3				3,UK,6		
4,2,F,25,2				4,IT,8		
5,3,M,40,3				2,US,4		
6,4,F,35,4				5,IT,10		
7,4,M,70,3						
8,4,F,60,3						
9,5,F,20,4						
10,6,M,40,4						
pid				hid	xh	
1				1	1	
2				1	1	
3				2	4	
4				2	4	
5				3	6	
6				4	8	
7				4	8	
8				4	8	
9				5	10	
10				6	12	

Table 7.1: Two linked CSV data files, and the effect of a `join`

Note that key variables are treated conceptually as integers. If a specified key contains fractional values these are truncated.

Two extensions of the basic key mechanism are available.

- If the outer dataset contains a relevant key variable but it goes under a different name from the inner key, you can use the `--okey` option to specify the outer key. (As with other right-hand names, this does not have to be a valid gretl identifier.) So, for example, if `hholds.csv` contained the `hid` information, but under the name `HHOLD`, the `join` command above could be modified as

```
join hholds.csv xh --ikey=hid --okey=HHOLD
```

- If a single key is not sufficient to generate the matches you want, you can specify a double key in the form of two series names separated by a comma; in this case the importation of data is restricted to those rows on which both keys match. The syntax here is, for example

```
join foo.csv x --ikey=key1,key2
```

Again, the `--okey` option may be used if the corresponding right-hand columns are named differently. The same number of keys must be given on the left and the right, but when a

double key is used and only one of the key names differs on the right, the name that is in common may be omitted (although the comma separator must be retained). For example, the second of the following lines is acceptable shorthand for the first:

```
join foo.csv x --ikey=key1,Lkey2 --okey=key1,Rkey2
join foo.csv x --ikey=key1,Lkey2 --okey=,Rkey2
```

The number of key-matches

The example shown in Table 7.1 is an instance of a 1 to 1 match: applying the matching criterion produces exactly one value of the variable `xh` corresponding to each row of the inner dataset. Three other possibilities arise:

- Some rows on the left have multiple matches on the right (“1 to n matching”).
- Some rows on the right have multiple matches on the left (“ n to 1 matching”).
- Some rows in the inner dataset have no match on the right.

The 1-to- n case is addressed in detail in the next section; here we discuss the others.

The n to 1 case is straightforward. If a particular key value (or combination of key values) occurs at each of $n > 1$ observations on the left but at a single observation on the right, then the right-hand value is entered at each of the matching slots on the left.

Treatment of the case where there’s *no* match on the right depends on whether the join operation is adding a new series to the inner dataset or modifying an existing one. When adding a new series, unmatched rows automatically get NA for the imported data. However, if join is pulling in values for a series already present on the left only matched rows will be updated. In other words we do *not* overwrite an existing value on the left with NA when there’s no match on the right.

These default policies may not produce the desired results in every case but gretl provides the means to modify the effect if need be. We will illustrate with two scenarios.

First consider adding a new series recording “number of hours worked” when the inner dataset contains individuals and the outer file contains data on jobs. If an individual does not appear in the jobs file (no match on the right) the default policy means that her hours worked will be recorded as NA. If in context you wish to set hours worked to zero rather than NA for such individuals, gretl’s `misszero()` function can be used to turn NA into 0 in the imported series.

Second, consider updating an existing series via join when the outer file is presumed to contain all available updated values, such that “no match” should be taken as an implicit NA. In that case we want the (presumably out-of-date) values on any unmatched rows to be overwritten with NA. Let the series in question be called `x` (both on the left and the right) and let the common key be called `pid`. The solution is then

```
join update.csv tmpvar --data=x --ikey=pid
x = tmpvar
```

where `tmpvar` does not already exist in the inner dataset. As a new series, `tmpvar` will get NA for all unmatched rows; we then transcribe its values into `x`. In a more complicated case one might use the `smpl` command to limit the sample range before assigning `tmpvar` to `x`, or use the conditional assignment operator `?:`.

One further point: given some missing values in an imported series you may want to know whether (a) the NAs were explicitly represented in the outer data file or (b) they arose due to “no match”. You can find this out by using a method described in the following section, namely the `count` variant of the aggregation option: this will give you a series with 0 values for all and only unmatched rows.

7.5 Aggregation

In the case of 1 to n matching of rows ($n > 1$) the user must specify an “aggregation method”; that is, a method for mapping from n rows down to one. This is handled by the `--aggr` option which requires a single argument from the following list:

<i>Code</i>	<i>Value returned</i>
<code>count</code>	count of matches
<code>avg</code>	mean of matching values
<code>sum</code>	sum of matching values
<code>min</code>	minimum of matching values
<code>max</code>	maximum of matching values
<code>seq:i</code>	the i^{th} matching value (e.g. <code>seq:2</code>)
<code>min(aux)</code>	minimum of matching values of auxiliary variable
<code>max(aux)</code>	maximum of matching values of auxiliary variable

Note that the `count` aggregation method is special, in that there is no need for a “data series” on the right; the imported series is simply a function of the specified key(s). All the other methods require that “actual data” are found on the right. Also note that when `count` is used, the value returned when no match is found is (as one might expect) zero rather than NA.

The basic use of the `seq` method is shown above: following the colon you give a positive integer representing the (1-based) position of the observation in the sequence of matched rows. Alternatively, a negative integer can be used to count down from the last match (`seq:-1` selects the last match, `seq:-2` the second-last match, and so on). If the specified sequence number is out of bounds for a given observation this method returns NA.

Referring again to the data in Table 7.1, suppose we want to import data from the persons file into a dataset established at household level. Here’s an example where we use the individual age data from `people.csv` to add the average and minimum age of household members.

```
open hholds.csv --quiet
join people.csv avgage --ikey=hid --data=age --aggr=avg
join people.csv minage --ikey=hid --data=age --aggr=min
```

Here’s a further example where we add to the household data the sum of the personal data `xp`, with the twist that we apply filters to get the sum specifically for household members under the age of 40, and for women.

```
open hholds.csv --quiet
join people.csv young_xp --ikey=hid --filter="age<40" --data=xp --aggr=sum
join people.csv female_xp --ikey=hid --filter="gender=='F'" --data=xp --aggr=sum
```

The possibility of using an auxiliary variable with the `min` and `max` modes of aggregation gives extra flexibility. For example, suppose we want for each household the income of its oldest member:

```
open hholds.csv --quiet
join people.csv oldest_xp --ikey=hid --data=xp --aggr=max(age)
```

7.6 String-valued key variables

The examples above use numerical variables (household and individual ID numbers) in the matching process. It is also possible to use string-valued variables, in which case a match means that the string values of the key variables compare equal (with case sensitivity). When using double keys,

you can mix numerical and string keys, but naturally you cannot mix a string variable on the left (via `ikey`) with a numerical one on the right (via `okey`), or vice versa.

Here's a simple example. Suppose that alongside `hholds.csv` we have a file `countries.csv` with the following content:

```
country,GDP
UK,100
US,500
IT,150
FR,180
```

The variable `country`, which is also found in `hholds.csv`, is string-valued. We can pull the GDP of the country in which the household resides into our households dataset with

```
open hholds.csv -q
join countries.csv GDP --ikey=country
```

which gives

	hid	country	GDP
1	1	1	500
2	6	2	150
3	3	3	100
4	4	2	150
5	2	1	500
6	5	2	150

7.7 Importing multiple series

The examples given so far have been limited in one respect. While several columns in the outer data file may be referenced (as keys, or in filtering or aggregation) only one column has actually provided data—and correspondingly only one series in the inner dataset has been created or modified—per invocation of `join`. However, `join` can handle the importation of several series at once. This section gives an account of the required syntax along with certain restrictions that apply to the multiple-import case.

There are two ways to specify more than one series for importation:

1. The *varname* field in the command can take the form of a space-separated list of names rather than a single name.
2. Alternatively, you can give the name of an array of strings in place of *varname*: the elements of this array should be the names of the series to import.

Here are the limitations:

1. The `--data` option, which permits the renaming of a series on import, is not available. When importing multiple series you are obliged to accept their “outer” names, fixed up as described in section 7.2.
2. While the other `join` options are available, they necessarily apply uniformly to all the series imported via a given command. This means that if you want to import several series but using different keys, filters or aggregation methods you must use a sequence of commands.

Here are a couple of examples of multiple imports.

```
# open base datafile containing keys
open PUMSdata.gdt

# join using a list of import names
join ss13pnc.csv SCHL WAGP WKHP --ikey=SERIALNO,SPORDER

# using a strings array: may be worthwhile if the array
# will be used for more than one purpose
strings S = defarray("SCHL", "WAGP", "WKHP")
join ss13pnc.csv S --ikey=SERIALNO,SPORDER
```

7.8 A real-world case

For a real use-case for `join` with cross-sectional data, we turn to the Bank of Italy's *Survey on Household Income and Wealth* (SHIW).¹ In ASCII form the 2010 survey results comprise 47 MB of data in 29 files. In this exercise we will draw on five of the SHIW files to construct a replica of the dataset used in Thomas Mroz's famous paper (Mroz, 1987) on women's labor force participation, which contains data on married women between the age of 30 and 60 along with certain characteristics of their households and husbands.

Our general strategy is as follows: we create a "core" dataset by opening the file `carcom10.csv`, which contains basic data on the individuals. After dropping unwanted individuals (all but married women), we use the resulting dataset as a base for pulling in further data via the `join` command.

The complete script to do the job is given in the Appendix to this chapter; here we walk through the script with comments interspersed. We assume that all the relevant files from the Bank of Italy survey are contained in a subdirectory called SHIW.

Starting with `carcom10.csv`, we use the `--cols` option to the `open` command to import specific series, namely NQUEST (household ID number), NORD (sequence number for individuals within each household), SEX (male = 1, female = 2), PARENT (status in household: 1 = head of household, 2 = spouse of head, etc.), STACIV (marital status: married = 1), STUDIO (educational level, coded from 1 to 8), ETA (age in years) and ACOM4C (size of town).

```
open SHIW/carcom10.csv --cols=1,2,3,4,9,10,29,41
```

We then restrict the sample to married women from 30 to 60 years of age, and additionally restrict the sample of women to those who are either heads of households or spouses of the head.

```
smp1 SEX==2 && ETA>=30 && ETA<=60 && STACIV==1 --restrict
smp1 PARENT<3 --restrict
```

For compatibility with the Mroz dataset as presented in the `gretl` data file `mroz87.gdt`, we rename the age and education variables as `WA` and `WE` respectively, we compute the CIT dummy and finally we store the reduced base dataset in `gretl` format.

```
rename ETA WA
rename STUDIO WE
series CIT = (ACOM4C > 2)

store mroz_rep.gdt
```

The next step will be to get data on working hours from the jobs file `allb1.csv`. There's a complication here. We need the total hours worked over the course of the year (for both the women

¹Details of the survey can be found at <http://www.bancaditalia.it/statistiche/indcamp/bilfait/dismicro>. The ASCII (CSV) data files for the 2010 survey are available at http://www.bancaditalia.it/statistiche/indcamp/bilfait/dismicro/annuale/ascii/ind10_ascii.zip.

and their husbands). This is not available as such, but the variables ORETOT and MESILAV give, respectively, average hours worked per week and the number of months worked in 2010, each on a per-job basis. If each person held at most one job over the year we could compute his or her annual hours as

```
HRS = ORETOT * 52 * MESILAV/12
```

However, some people had more than one job, and in this case what we want is the sum of annual hours across their jobs. We could use `join` with the `seq` aggregation method to construct this sum, but it is probably more straightforward to read the `allb1` data, compute the HRS values per job as shown above, and save the results to a temporary CSV file.

```
open SHIW/allb1.csv --cols=1,2,8,11 --quiet
series HRS = misszero(ORETOT) * 52 * misszero(MESILAV)/12
store HRS.csv NQUEST NORD HRS
```

Now we can reopen the base dataset and join the hours variable from `HRS.csv`. Note that we need a double key here: the women are uniquely identified by the combination of `NQUEST` and `NORD`. We don't need an `okey` specification since these keys go under the same names in the right-hand file. We define labor force participation, `LFP`, based on hours.

```
open mroz_rep.gdt
join HRS.csv WHRS --ikey=NQUEST,NORD --data=HRS --aggr=sum
WHRS = misszero(WHRS)
LFP = WHRS > 0
```

For reference, here's how we could have used `seq` to avoid writing a temporary file:

```
join SHIW/allb1.csv njobs --ikey=NQUEST,NORD --data=ORETOT --aggr=count
series WHRS = 0
loop i=1..max(njobs)
  join SHIW/allb1.csv htmp --ikey=NQUEST,NORD --data=ORETOT --aggr="seq:$i"
  join SHIW/allb1.csv mtmp --ikey=NQUEST,NORD --data=MESILAV --aggr="seq:$i"
  WHRS += misszero(htmp) * 52 * misszero(mtmp)/12
endloop
```

To generate the work experience variable, `AX`, we use the file `lavoro.csv`: this contains a variable named `ETALAV` which records the age at which the person first started work.

```
join SHIW/lavoro.csv ETALAV --ikey=NQUEST,NORD
series AX = misszero(WA - ETALAV)
```

We compute the woman's hourly wage, `WW`, as the ratio of total employment income to annual working hours. This requires drawing the series `YL` (payroll income) and `YM` (net self-employment income) from the persons file `rper10.csv`.

```
join SHIW/rper10.csv YL YM --ikey=NQUEST,NORD --aggr=sum
series WW = LFP ? (YL + YM)/WHRS : 0
```

The family's net disposable income is available as `Y` in the file `rfam10.csv`; we import this as `FAMINC`.

```
join SHIW/rfam10.csv FAMINC --ikey=NQUEST --data=Y
```

Data on number of children are now obtained by applying the `count` method. For the Mroz replication we want the number of children under the age of 6, and also the number aged 6 to 18.

```
join SHIW/carcom10.csv KIDS --ikey=NQUEST --aggr=count --filter="ETA<=18"
join SHIW/carcom10.csv KL6 --ikey=NQUEST --aggr=count --filter=ETA<6
series K618 = KIDS - KL6
```

We want to add data on the women's husbands, but how do we find them? To do this we create an additional inner key which we'll call `H_ID` (husband ID), by sub-sampling in turn on the observations falling into each of two classes: (a) those where the woman is recorded as head of household and (b) those where the husband has that status. In each case we want the individual ID (`NORD`) of the household member whose status is complementary to that of the woman in question. So for case (a) we subsample using `PARENT==1` (head of household) and filter the join using `PARENT==2` (spouse of head); in case (b) we do the converse. We thus construct `H_ID` piece-wise.

```
# for women who are household heads
smp1 PARENT==1 --restrict --replace
join SHIW/carcom10.csv H_ID --ikey=NQUEST --data=NORD --filter="PARENT==2"
# for women who are not household heads
smp1 PARENT==2 --restrict --replace
join SHIW/carcom10.csv H_ID --ikey=NQUEST --data=NORD --filter="PARENT==1"
smp1 full
```

Now we can use our new inner key to retrieve the husbands' data, matching `H_ID` on the left with `NORD` on the right within each household.

```
join SHIW/carcom10.csv HA --ikey=NQUEST,H_ID --okey=NQUEST,NORD --data=ETA
join SHIW/carcom10.csv HE --ikey=NQUEST,H_ID --okey=NQUEST,NORD --data=STUDIO
join HRS.csv HHRS --ikey=NQUEST,H_ID --okey=NQUEST,NORD --data=HRS --aggr=sum
HHRS = misszero(HHRS)
```

The remainder of the script is straightforward and does not require discussion here: we recode the education variables for compatibility; delete some intermediate series that are not needed any more; add informative labels; and save the final product. See the Appendix for details.

To compare the results from this dataset with those from the earlier US data used by Mroz, one can copy the input file `heckit.inp` (supplied with the `gretl` package) and substitute `mroz_rep.gdt` for `mroz87.gdt`. It turns out that the results are qualitatively very similar.

7.9 The representation of dates

Up to this point all the data we have considered have been cross-sectional. In the following sections we discuss data that have a time dimension, and before proceeding it may be useful to say something about the representation of dates. `Gretl` takes the ISO 8601 standard as its reference point but provides means of converting dates provided in other formats; it also offers a set of calendrical functions for manipulating dates (`isodate`, `isoconv`, `epochday` and others).

ISO 8601 recognizes two formats for daily dates, "extended" and "basic". In both formats dates are given as 4-digit year, 2-digit month and 2-digit day, in that order. In extended format a dash is inserted between the fields—as in 2013-10-21 or more generally YYYY-MM-DD—while in basic format the fields are run together (YYYYMMDD). Extended format is more easily parsed by human readers while basic format is more suitable for computer processing, since one can apply ordinary arithmetic to compare dates as equal, earlier or later. The standard also recognizes YYYY-MM as representing year and month, e.g. 2010-11 for November 2010,² as well as a plain four-digit number for year alone.

One problem for economists is that the "quarter" is not a period covered by ISO 8601. This could be presented by YYYY-Q (with only one digit following the dash) but in `gretl` output we in fact use a colon, as in 2013:2 for the second quarter of 2013. (For printed output of months `gretl` also uses

²The form YYYYMM is *not* recognized for year and month.

a colon, as in 2013:06. A difficulty with following ISO here is that in a statistical context a string such as 1980–10 may look more like a subtraction than a date.) Anyway, at present we are more interested in the parsing of dates on input rather than in what gretl prints. And in that context note that “excess precision” is acceptable: a month may be represented by its first day (e.g. 2005-05-01 for May, 2005), and a quarter may be represented by its first month and day (2005-07-01 for the third quarter of 2005).

Some additional points regarding dates will be taken up as they become relevant in practical cases of joining data.

7.10 Time-series data

Suppose our left-hand dataset is recognized by gretl as time series with a supported frequency (annual, quarterly, monthly, weekly, daily or hourly). This will be the case if the original data were read from a file that contained suitable time or date information, or if a time-series interpretation has been imposed using either the `setobs` command or its GUI equivalent. Then—apart, perhaps, from some very special cases—joining additional data is bound to involve matching observations by time-period. In this case, contrary to the cross-sectional case, the inner dataset has a natural ordering of which gretl is aware; hence, no “inner key” is required.

If, in addition, the file from data which are to be joined is in native gretl format and contains time-series information, keys are not needed at all. Three cases can arise: the frequency of the outer dataset may be the same, lower or higher than that of the inner dataset. In the first two cases `join` should work without any special apparatus; lower-frequency values will be repeated for each high-frequency period. In the third case, however, an aggregation method must be specified: gretl needs to know how to map higher-frequency data into the existing dataset (by averaging, summing, or whatever).

If the outer data file is *not* in native gretl format we need a means of identifying the period of each observation on the right, an outer key which we’ll call a “time key”. The `join` command provides a simple (but limited) default for extracting period information from the outer data file, plus an option that can be used if the default is not applicable, as follows.

- The default assumptions are: (1) the time key appears in the first column; (2) the heading of this column is either left blank or is one of `obs`, `date`, `year`, `period`, `observation`, or `observation_date` (on a case-insensitive comparison); and (3) the time format conforms to ISO 8601 where applicable (“extended” daily date format `YYYY-MM-DD`, monthly format `YYYY-MM`, or annual format `YYYY`).
- If dates do not appear in the first column of the outer file, or if the column heading or format is not as just described, the `--tkey` option can be used to indicate which column should be used and/or what format should be assumed.

Setting the time-key column and/or format

The `--tkey` option requires a parameter holding the name of the column in which the time key is located and/or a string specifying the format in which dates/times are written in the time-key column. This parameter should be enclosed in double-quotes. If both elements are present they should be separated by a comma; if only a format is given it should be preceded by a comma. Some examples:

```
--tkey="Period,%m/%d/%Y"
--tkey="Period"
--tkey="obsperiod"
--tkey=",%Ym%m"
```

The first of these applies if `Period` is not the first column on the right, and dates are given in the US format of month, day, year, separated by slashes. The second implies that although `Period` is not the first column, the date format is ISO 8601. The third again implies that the date format is OK; here the name is required even if `obsperiod` is the first column since this heading is not one recognized by gretl's heuristic. The last example implies that dates are in the first column (with one of the recognized headings), but are given in the non-standard format year, "m", month.

The date format string should be composed using the codes employed by the POSIX function `strptime`; Table 7.2 contains a list of the most relevant codes.³

Code	Meaning
%%	The % character.
%b	The month name according to the current locale, either abbreviated or in full.
%C	The century number (0-99).
%d	The day of month (1-31).
%D	Equivalent to %m/%d/%y. (This is the American style date, very confusing to non-Americans, especially since %d/%m/%y is widely used in Europe. The ISO 8601 standard format is %Y-%m-%d.)
%H	The hour (0-23).
%j	The day number in the year (1-366).
%m	The month number (1-12).
%n	Arbitrary whitespace.
%q	The quarter (1-4).
%w	The weekday number (0-6) with Sunday = 0.
%y	The year within century (0-99). When a century is not otherwise specified, values in the range 69-99 refer to years in the twentieth century (1969-1999); values in the range 00-68 refer to years in the twenty-first century (2000-2068).
%Y	The year, including century (for example, 1991).

Table 7.2: Date format codes

Example: daily stock prices

We show below the first few lines of a file named `IBM.csv` containing stock-price data for IBM corporation.

```
Date,Open,High,Low,Close,Volume,Adj Close
2013-08-02,195.50,195.50,193.22,195.16,3861000,195.16
2013-08-01,196.65,197.17,195.41,195.81,2856900,195.81
2013-07-31,194.49,196.91,194.49,195.04,3810000,195.04
```

Note that the data are in reverse time-series order—that won't matter to `join`, the data can appear in any order. Also note that the first column is headed `Date` and holds daily dates as ISO 8601 extended. That means we can pull the data into gretl very easily. In the following fragment we create a suitably dimensioned empty daily dataset then rely on the default behavior of `join` with time-series data to import the closing stock price.

```
nulldata 500
setobs 5 2012-01-01
join IBM.csv Close
```

³The %q code for quarter is not present in `strptime`; it is added for use with `join` since quarterly data are common in macroeconomics.

To make explicit what we're doing, we could accomplish exactly the same using the `--tkey` option:

```
join IBM.csv Close --tkey="Date,%Y-%m-%d"
```

Example: OECD quarterly data

Table 7.3 shows an excerpt from a CSV file provided by the OECD statistical site (stat.oecd.org) in response to a request for GDP at constant prices for several countries.⁴

```
Frequency,Period,Country,Value,Flags
"Quarterly","Q1-1960","France",463876.148126845,E
"Quarterly","Q1-1960","Germany",768802.119278467,E
"Quarterly","Q1-1960","Italy",414629.791450547,E
"Quarterly","Q1-1960","United Kingdom",578437.090291889,E
"Quarterly","Q2-1960","France",465618.977328614,E
"Quarterly","Q2-1960","Germany",782484.138122549,E
"Quarterly","Q2-1960","Italy",420714.910290157,E
"Quarterly","Q2-1960","United Kingdom",572853.474696578,E
"Quarterly","Q3-1960","France",469104.41925852,E
"Quarterly","Q3-1960","Germany",809532.161494483,E
"Quarterly","Q3-1960","Italy",426893.675840156,E
"Quarterly","Q3-1960","United Kingdom",581252.066618986,E
"Quarterly","Q4-1960","France",474664.327992619,E
"Quarterly","Q4-1960","Germany",817806.132384948,E
"Quarterly","Q4-1960","Italy",427221.338414114,E
...
```

Table 7.3: Example of CSV file as provided by the OECD statistical website

This is an instance of data in what we call *atomic format*, that is, a format in which each line of the outer file contains a single data-point and extracting data mainly requires filtering the appropriate lines. The outer time key is under the `Period` heading, and has the format `Q<quarter>-<year>`. Assuming that the file in Table 7.3 has the name `oecd.csv`, the following script reconstructs the time series of Gross Domestic Product for several countries:

```
nulldata 220
setobs 4 1960:1

join oecd.csv FRA --tkey="Period,Q%q-%Y" --data=Value --filter="Country==\"France\""
join oecd.csv GER --tkey="Period,Q%q-%Y" --data=Value --filter="Country==\"Germany\""
join oecd.csv ITA --tkey="Period,Q%q-%Y" --data=Value --filter="Country==\"Italy\""
join oecd.csv UK --tkey="Period,Q%q-%Y" --data=Value --filter="Country==\"United Kingdom\""
```

Note the use of the format codes `%q` for the quarter and `%Y` for the 4-digit year. A touch of elegance could have been added by storing the invariant options to `join` using the `setopt` command, as in

```
setopt join persist --tkey="Period,Q%q-%Y" --data=Value
join oecd.csv FRA --filter="Country==\"France\""
join oecd.csv GER --filter="Country==\"Germany\""
join oecd.csv ITA --filter="Country==\"Italy\""
join oecd.csv UK --filter="Country==\"United Kingdom\""
setopt join clear
```

If one were importing a large number of such series it might be worth rewriting the sequence of joins as a loop, as in

⁴Retrieved 2013-08-05. The OECD files in fact contain two leading columns with very long labels; these are irrelevant to the present example and can be omitted without altering the sample script.

```

strings countries = defarray("France", "Germany", "Italy", "United Kingdom")
strings vnames = defarray("FRA", "GER", "ITA", "UK")
setopt join persist --tkey="Period,Qq-%Y" --data=Value

loop foreach i countries
  vname = vnames[i]
  join oecd.csv @vname --filter="Country==\"$i\""
endloop
setopt join clear

```

7.11 Special handling of time columns

When dealing with straight time series data the `tkey` mechanism described above should suffice in almost all cases. In some contexts, however, time enters the picture in a more complex way; examples include panel data (see section 7.12) and so-called realtime data (see chapter 8). To handle such cases `join` provides the `--tconvert` option. This can be used to select certain columns in the right-hand data file for special treatment: strings representing dates in these columns will be converted to numerical values: 8-digit numbers on the pattern `YYYYMMDD` (ISO basic daily format). Once dates are in this form it is easy to use them in key-matching or filtering.

By default it is assumed that the strings in the selected columns are in ISO extended format, `YYYY-MM-DD`. If that is not the case you can supply a time-format string using the `--tconv-fmt` option. The format string should be written using the codes shown in Table 7.2.

Here are some examples:

```

# select one column for treatment
--tconvert=start_date

# select two columns for treatment
--tconvert="start_date,end_date"

# specify US-style daily date format
--tconv-fmt="%m/%d/%Y"

# specify quarterly date-strings (as in 2004q1)
--tconv-fmt="%Yq%q"

```

Some points to note:

- If a specified column is not selected for a substantive role in the join operation (as data to be imported, as a key, or as an auxiliary variable for use in aggregation) the column in question is not read and so no conversion is carried out.
- If a specified column contains numerical rather than string values, no conversion is carried out.
- If a string value in a selected column fails parsing using the relevant time format (user-specified or default), the converted value is NA.
- On successful conversion, the output is always in daily-date form as stated above. If you specify a monthly or quarterly time format, the converted date is the first day of the month or quarter.

7.12 Panel data

In section 7.10 we gave an example of reading quarterly GDP data for several countries from an OECD file. In that context we imported each country's data as a distinct time-series variable. Now

suppose we want the GDP data in panel format instead (stacked time series). How can we do this with `join`?

As a reminder, here's what the OECD data look like:

```
Frequency,Period,Country,Value,Flags
"Quarterly","Q1-1960","France",463876.148126845,E
"Quarterly","Q1-1960","Germany",768802.119278467,E
"Quarterly","Q1-1960","Italy",414629.791450547,E
"Quarterly","Q1-1960","United Kingdom",578437.090291889,E
"Quarterly","Q2-1960","France",465618.977328614,E
```

and so on. If we have four countries and quarterly observations running from 1960:1 to 2013:2 ($T = 214$ quarters) we might set up our panel workspace like this:

```
scalar N = 4
scalar T = 214
scalar NT = N*T
nulldata NT --preserve
setobs T 1.1 --stacked-time-series
```

The relevant outer keys are obvious: `Country` for the country and `Period` for the time period. Our task is now to construct matching keys in the inner dataset. This can be done via two panel-specific options to the `setobs` command. Let's work on the time dimension first:

```
setobs 4 1960:1 --panel-time
series quarter = $obsdate
```

This variant of `setobs` allows us to tell `gretl` that time in our panel is quarterly, starting in the first quarter of 1960. Having set that, the accessor `$obsdate` will give us a series of 8-digit dates representing the first day of each quarter—19600101, 19600401, 19600701, and so on, repeating for each country. As we explained in section 7.11, we can use the `--tconvert` option on the outer series `Period` to get exactly matching values (in this case using a format of `Q%q-%Y` for parsing the `Period` values).

Now for the country names:

```
string cstrs = sprintf("France Germany Italy \"United Kingdom\"")
setobs country cstrs --panel-groups
```

Here we write into the string `cstrs` the names of the countries, using escaped double-quotes to handle the space in "United Kingdom", then pass this string to `setobs` with the `--panel-groups` option, preceded by the identifier `country`. This asks `gretl` to construct a string-valued series named `country`, in which each name will repeat T times.

We're now ready to join. Assuming the OECD file is named `oecd.csv` we do

```
join oecd.csv GDP --data=Value \
--ikey=country,quarter --okey=Country,Period \
--tconvert=Period --tconv-fmt="Q%q-%Y"
```

Other input formats

The OECD file discussed above is in the most convenient format for `join`, with one data-point per line. But sometimes we may want to make a panel from a data file structured like this:

```
# Real GDP
Period,France,Germany,Italy,"United Kingdom"
```

```
"Q1-1960",463863,768757,414630,578437
"Q2-1960",465605,782438,420715,572853
"Q3-1960",469091,809484,426894,581252
"Q4-1960",474651,817758,427221,584779
"Q1-1961",482285,826031,442528,594684
...
```

Call this file `side_by_side.csv`. Assuming the same initial set-up as above, we can panelize the data by setting the sample to each country's time series in turn and importing the relevant column. The only point to watch here is that the string "United Kingdom", being a column heading, will become `United_Kingdom` on importing (see section 7.2) so we'll need a slightly different set of country strings.

```
strings cstrs = defarray("France", "Germany", "Italy", "United_Kingdom")
setobs country cstrs --panel-groups
loop foreach i cstrs
  smp1 country=="$i" --restrict --replace
  join side_by_side.csv GDP --data=$i \
    --ikey=quarter --okey=Period \
    --tconvert=Period --tconv-fmt="Q%q-%Y"
endloop
smp1 full
```

If our working dataset and the outer data file are dimensioned such that there are just as many time-series observations on the right as there are time slots on the left—and the observations on the right are contiguous, in chronological order, and start on the same date as the working dataset—we could dispense with the key apparatus and just use the first line of the `join` command shown above. However, in general it is safer to use keys to ensure that the data end up in correct registration.

7.13 Memo: join options

Basic syntax: `join filename varname(s) [options]`

<i>flag</i>	<i>effect</i>
<code>--data</code>	Give the name of the data column on the right, in case it differs from <i>varname</i> (7.2); single import only
<code>--filter</code>	Specify a condition for filtering data rows (7.3)
<code>--ikey</code>	Specify up to two keys for matching data rows (7.4)
<code>--okey</code>	Specify outer key name(s) in case they differ the inner ones (7.4)
<code>--aggr</code>	Select an aggregation method for 1 to <i>n</i> joins (7.5)
<code>--tkey</code>	Specify right-hand time key (7.10)
<code>--tconvert</code>	Select outer date columns for conversion to numeric form (7.11)
<code>--tconv-fmt</code>	Specify a format for use with <code>tconvert</code> (7.11)
<code>--no-header</code>	Treat the first row on the right as data (7.2)
<code>--verbose</code>	Report on progress in reading the outer data

Appendix: the full Mroz data script

```

# start with everybody; get gender, age and a few other variables
# directly while we're at it
open SHIW/carcom10.csv --cols=1,2,3,4,9,10,29,41

# subsample on married women between the ages of 30 and 60
smp1 SEX==2 && ETA>=30 && ETA<=60 && STACIV==1 --restrict
# for simplicity, restrict to heads of households and their spouses
smp1 PARENT<3 --restrict

# rename the age and education variables for compatibility; compute
# the "city" dummy and finally save the reduced base dataset
rename ETA WA
rename STUDIO WE
series CIT = (ACOM4C>2)
store mroz_rep.gdt

# make a temp file holding annual hours worked per job
open SHIW/allb1.csv --cols=1,2,8,11 --quiet
series HRS = misszero(ORETOT) * 52 * misszero(MESILAV)/12
store HRS.csv NQUEST NORD HRS

# reopen the base dataset and begin drawing assorted data in
open mroz_rep.gdt

# women's annual hours (summed across jobs)
join HRS.csv WHRS --ikey=NQUEST,NORD --data=HRS --aggr=sum
WHRS = misszero(WHRS)

# labor force participation
LFP = WHRS > 0

# work experience: ETALAV = age when started first job
join SHIW/lavoro.csv ETALAV --ikey=NQUEST,NORD
series AX = misszero(WA - ETALAV)

# women's hourly wages
join SHIW/rper10.csv YL YM --ikey=NQUEST,NORD --aggr=sum
series WW = LFP ? (YL + YM)/WHRS : 0

# family income (Y = net disposable income)
join SHIW/rfam10.csv FAMINC --ikey=NQUEST --data=Y

# get data on children using the "count" method
join SHIW/carcom10.csv KIDS --ikey=NQUEST --aggr=count --filter="ETA<=18"
join SHIW/carcom10.csv KL6 --ikey=NQUEST --aggr=count --filter="ETA<6"
series K618 = KIDS - KL6

# data on husbands: we first construct an auxiliary inner key for
# husbands, using the little trick of subsampling the inner dataset
#
# for women who are household heads
smp1 PARENT==1 --restrict --replace
join SHIW/carcom10.csv H_ID --ikey=NQUEST --data=NORD --filter="PARENT==2"
# for women who are not household heads
smp1 PARENT==2 --restrict --replace
join SHIW/carcom10.csv H_ID --ikey=NQUEST --data=NORD --filter="PARENT==1"
smp1 full

```

```

# add husbands' data via the newly-added secondary inner key
join SHIW/carcom10.csv HA --ikey=NQUEST,H_ID --okey=NQUEST,NORD --data=ETA
join SHIW/carcom10.csv HE --ikey=NQUEST,H_ID --okey=NQUEST,NORD --data=STUDIO
join HRS.csv HHRS --ikey=NQUEST,H_ID --okey=NQUEST,NORD --data=HRS --aggr=sum
HHRS = misszero(HHRS)

# final cleanup begins

# recode educational attainment as years of education
matrix eduyrs = {0, 5, 8, 11, 13, 16, 18, 21}
series WE = replace(WE, seq(1,8), eduyrs)
series HE = replace(HE, seq(1,8), eduyrs)

# cut some cruft
delete SEX STACIV KIDS YL YM PARENT H_ID ETALAV

# add some labels for the series
setinfo LFP -d "1 if woman worked in 2010"
setinfo WHRS -d "Wife's hours of work in 2010"
setinfo KL6 -d "Number of children less than 6 years old in household"
setinfo K618 -d "Number of children between ages 6 and 18 in household"
setinfo WA -d "Wife's age"
setinfo WE -d "Wife's educational attainment, in years"
setinfo WW -d "Wife's average hourly earnings, in 2010 euros"
setinfo HHRS -d "Husband's hours worked in 2010"
setinfo HA -d "Husband's age"
setinfo HE -d "Husband's educational attainment, in years"
setinfo FAMINC -d "Family income, in 2010 euros"
setinfo AX -d "Actual years of wife's previous labor market experience"
setinfo CIT -d "1 if live in large city"

# save the final product
store mroz_rep.gdt

```

Chapter 8

Realtime data

8.1 Introduction

The `join` command in `gretl` (see chapter 7) deals in a fairly straightforward manner with so-called realtime datasets. Such datasets contain information on when the observations in a time series were actually published by the relevant statistical agency and how they have been revised over time. Probably the most popular sources of such data are the “Alfred” online database at the St. Louis Fed (<http://alfred.stlouisfed.org/>) and the OECD’s StatExtracts site, <http://stats.oecd.org/>. The examples in this chapter deal with files downloaded from these sources, but should be easy to adapt to files with a slightly different format.

As already stated, `join` requires a column-oriented plain text file, where the columns may be separated by commas, tabs, spaces or semicolons. Alfred and the OECD provide the option to download realtime data in this format (tab-delimited files from Alfred, comma-delimited from the OECD). If you have a realtime dataset in a spreadsheet file you must export it to a delimited text file before using it with `join`.

Representing revision histories is more complex than just storing a standard time series, because for each observation period you have in general more than one published value over time, along with the information on when each of these values were valid or current. Sometimes this is represented in spreadsheets with two time axes, one for the observation period and another one for the publication date or “vintage”. The filled cells then form an upper triangle (or a “guillotine blade” shape, if the publication dates do not reach back far enough to complete the triangle). This format can be useful for giving a human reader an overview of realtime data, but it is not optimal for automatic processing; for that purpose “atomic” format is best.

8.2 Atomic format for realtime data

What we are calling atomic format is exactly the format used by Alfred if you choose the option “Observations by Real-Time Period”, and by the OECD if you select all editions of a series for download as plain text (CSV).¹ A file in this format contains one actual data-point per line, together with associated metadata. This is illustrated in Table 8.1, where we show the first three lines from an Alfred file and an OECD file (slightly modified).²

Consider the first data line in the Alfred file: in the `observation_date` column we find 1960-01-01, indicating that the data-point on this line, namely 112.0, is an observation or measurement (in this case, of the US index of industrial production) that refers to the period starting on January 1st 1960. The `realtime_start_date` value of 1960-02-16 tells us that this value was published on February 16th 1960, and the `realtime_end_date` value says that this vintage remained current through March 15th 1960. On the next day (as we can see from the following line) this data-point was revised slightly downward to 111.0.

Daily dates in Alfred files are given in ISO extended format, YYYY-MM-DD, but below we describe how to deal with differently formatted dates. Note that daily dates are appropriate for the last two

¹If you choose to download in Excel format from OECD you get a file in the triangular or guillotine format mentioned above.

²In the Alfred file we have used commas rather than tabs as the column delimiter; in the OECD example we have shortened the name in the `Variable` column.

Alfred: monthly US industrial production

```
observation_date,INDPRO,realtime_start_date,realtime_end_date
1960-01-01,112.0000,1960-02-16,1960-03-15
1960-01-01,111.0000,1960-03-16,1961-10-15
```

OECD: monthly UK industrial production

```
Country,Variable,Frequency,Time,Edition,Value,Flags
"United Kingdom","INDPRO","Monthly","Jan-1990","February 1999",100,
"United Kingdom","INDPRO","Monthly","Feb-1990","February 1999",99.3,
```

Table 8.1: Variant atomic formats for realtime data

columns, which jointly record the interval over which a given data vintage was current. Daily dates might, however, be considered overly precise for the first column, since the data period may well be the year, quarter or month. However, following Alfred’s practice it is acceptable to specify a daily date, indicating the first day of the period, even for non-daily data.³

Compare the first data line of the OECD example. There’s a greater amount of leading metadata, which is left implicit in the Alfred file. Here *Time* is the equivalent of Alfred’s *observation_date*, and *Edition* the equivalent of Alfred’s *realtime_start_date*. So we read that in February 1999 a value of 100 was current for the UK index of industrial production for January 1990, and from the next line we see that in the same vintage month a value of 99.3 was current for industrial production in February 1990.

Besides the different names and ordering of the columns, there are a few more substantive differences between Alfred and OECD files, most of which are irrelevant for *join* but some of which are (possibly) relevant.

The first (irrelevant) difference is the ordering of the lines. It appears (though we’re not sure how consistent this is) that in Alfred files the lines are sorted by observation date first and then by publication date—so that all revisions of a given observation are grouped together—while OECD files are sorted first by revision date (*Edition*) and then by observation date (*Time*). If we want the next revision of UK industrial production for January 1990 in the OECD file we have to scan down several lines until we find

```
"United Kingdom","INDPRO","Monthly","Jan-1990","March 1999",100,
```

This difference in format is basically irrelevant because *join* can handle the case where the lines appear in random order, although some operations can be coded more conveniently if we’re able to assume chronological ordering (either on the Alfred or the OECD pattern, it doesn’t matter).

The second (also irrelevant) difference is that the OECD seems to include periodic “*Edition*” lines even when there is no change from the previous value (as illustrated above, where the UK industrial production index for January 1990 is reported as 100 as of March 1999, the same value that we saw to be current in February 1999), while Alfred reports a new value only when it differs from what was previously current.

A third difference lies in the dating of the revisions or editions. As we have seen, Alfred gives a specific daily date while (in the UK industrial production file at any rate), the OECD just dates each edition to a month. This is not necessarily relevant for *join*, but it does raise the question of whether the OECD might date revisions to a finer granularity in some of their files, in which case one would have to be on the lookout for a different date format.

The final difference is that Alfred supplies an “end date” for each data vintage while the OECD

³Notice that this implies that in the Alfred example it is not clear without further information whether the observation period is the first quarter of 1960, the month January 1960, or the day January 1st 1960. However, we assume that this information is always available in context.

supplies only a starting date. But there is less to this difference than meets the eye: according to the Alfred webmaster, “by design, a new vintage must start immediately following (the day after) the lapse of the old vintage”—so the end date conveys no independent information.⁴

8.3 More on time-related options

Before we get properly started it is worth saying a little more about the `--tkey` and `--tconvert` options to `join` (introduced in section 7.11), as they apply in the case of realtime data.

When you're working with regular time series data `tkey` is likely to be useful while `tconvert` is unlikely to be applicable (see section 7.10). On the other hand, when you're working with panel data `tkey` is definitely not applicable but `tconvert` may well be helpful (section 7.12). When working with realtime data, however, depending on the task in hand both options may be useful. You will likely need `tkey`; you may well wish to select at least one column for `tconvert` treatment; and in fact you may want to name a given column in both contexts—that is, include the `tkey` variable among the `tconvert` columns.

Why might this make sense? Well, think of the `--tconvert` option as a “preprocessing” directive: it asks `gretl` to convert date strings to numerical values (8-digit ISO basic dates) “at source”, as they are read from the outer datafile. The `--tkey` option, on the other hand, singles out a column as the one to use for matching rows with the inner dataset. So you would want to name a column in both roles if (a) it should be used for matching periods and also (b) it is desirable to have the values from this column in numerical form, most likely for use in filtering.

As we have seen, you can supply specific formats in connection with both `tkey` and `tconvert` (in the latter case via the companion option `--tconv-fmt`) to handle the case where the date strings on the right are not ISO-friendly at source. This raises the question of how the format specifications work if a given column is named under both options. Here are the rules that `gretl` applies:

1. If a format is given with the `--tkey` option it always applies to the `tkey` column alone; and for that column it overrides any format given via the `--tconv-fmt` option.
2. If a format is given via `tconv-fmt` it is assumed to apply to all the `tconvert` columns, unless this assumption is preempted by rule 1.

8.4 Getting a certain data vintage

The most common application of realtime data is to “travel back in time” and retrieve the data that were current as of a certain date in the past. This would enable you to replicate a forecast or other statistical result that could have been produced at that date.

For example, suppose we are interested in a variable of monthly frequency named `INDPRO`, realtime data on which is stored in an Alfred file named `INDPRO.txt`, and we want to check the status quo as of June 15th 2011.

If we don't already have a suitable dataset into which to import the `INDPRO` data, our first steps will be to create an appropriately dimensioned empty dataset using the `nulldata` command and then specify its time-series character via `setobs`, as in

```
nulldata 132
setobs 12 2004:01
```

For convenience we can put the name of our realtime file into a string variable. On Windows this might look like

⁴Email received from Travis May of the Federal Reserve Bank of St. Louis, 2013-10-17. This closes off the possibility that a given vintage could lapse or expire some time before the next vintage becomes available, hence giving rise to a “hole” in an Alfred realtime file.

```
string fname = "C:/Users/yourname/Downloads/INDPRO.txt"
```

We can then import the data vintage 2011-06-15 using `join`, arbitrarily choosing the (hopefully) self-explanatory identifier `ip_asof_20110615`.

```
join @fname ip_asof_20110615 --tkey=observation_date --data=INDPRO \
--tconvert="realtime_start_date" \
--filter="realtime_start_date<=20110615" --aggr=max(realtime_start_date)
```

Here some detailed explanations of the various options are warranted:

- The `--tkey` option specifies the column which should be treated as holding the observation period identifiers to be matched against the periods in the current gretl dataset.⁵ The more general form of this option is `--tkey="colname,format"` (note the double quotes here), so if the dates do not come in standard format, we can tell gretl how to parse them by using the appropriate conversion specifiers as shown in Table 7.2. For example, here we could have written `--tkey="observation_date,%Y-%m-%d"`.
- Next, `--data=INDPRO` tells gretl that we want to retrieve the entries stored in the column named `INDPRO`.
- As explained in section 7.11 the `--tconvert` option selects certain columns in the right-hand data file for conversion from date strings to 8-digit numbers on the pattern `YYYYMMDD`. We'll need this for the next step, filtering, since the transformation to numerical values makes it possible to perform basic arithmetic on dates. Note that since date strings in Alfred files conform to gretl's default assumption it is not necessary to use the `--tconv-fmt` option here.
- The `--filter` option specification in combination with the subsequent `--aggr` aggregation treatment is the central piece of our data retrieval; notice how we use the date constant 20110615 in ISO basic form to do numerical comparisons, and how we perform the numerical `max` operation on the converted column `realtime_start_date`. It would also have been possible to predefine a scalar variable, as in

```
vintage = 20110615
```

and then use `vintage` in the `join` command instead. Here we tell `join` that we only want to extract those publications that (1) already appeared before (and including) June 15th 2011, and (2) were not yet obsoleted by a newer release.⁶

As a result, your dataset will now contain a time series named `ip_asof_20110615` with the values that a researcher would have had available on June 15th 2011. Of course, all values for the observations after June 2011 will be missing (and probably a few before that, too), because they only have become available later on.

8.5 Getting the n -th release for each observation period

For some purposes it may be useful to retrieve the n -th published value of each observation, where n is a fixed positive integer, irrespective of *when* each of these n -th releases was published. Suppose we are interested in the third release, then the relevant `join` command becomes:

```
join @fname ip_3rdpub --tkey=observation_date --data=INDPRO --aggr="seq:3"
```

⁵Strictly speaking, using `--tkey` is unnecessary in this example because we could just have relied on the default, which is to use the first column in the source file for the periods. However, being explicit is often a good idea.

⁶By implementing the second condition through the `max` aggregation on the `realtime_start_date` column alone, without using the `realtime_end_date` column, we make use of the fact that Alfred files cannot have "holes" as explained before.

Since we do not need the `realtime_start_date` information for this retrieval, we have dropped the `--tconvert` option here. Note that this formulation assumes that the source file is ordered chronologically, otherwise using the option `--aggr="seq:3"`, which retrieves the third value from each sequence of matches, could have yielded a result different from the one intended. However, this assumption holds for Alfred files and is probably rather safe in general.

The values of the variable imported as `ip_3rdpub` in this way were published at different dates, so the variable is effectively a mix of different vintages. Depending on the type of variable, this may also imply drastic jumps in the values; for example, index numbers are regularly re-based to different base periods. This problem also carries over to inflation-adjusted economic variables, where the base period of the price index changes over time. Mixing vintages in general also means mixing different scales in the output, with which you would have to deal appropriately.⁷

8.6 Getting the values at a fixed lag after the observation period

New data releases may take place on any day of the month, and as we have seen the specific day of each release is recorded in realtime files from Alfred. However, if you are working with, say, monthly or quarterly data you may sometimes want to adjust the granularity of your realtime axis to a monthly or quarterly frequency. For example, in order to analyse the data revision process for monthly industrial production you might be interested in the extent of revisions between the data available two and three months after each observation period.

This is a relatively complicated task and there is more than one way of accomplishing it. Either you have to make several passes through the outer dataset or you need a sophisticated filter, written as a `hansl` function. Either way you will want to make use of some of `gretl`'s built-in calendrical functions.

We'll assume that a suitably dimensioned workspace has been set up as described above. Given that, the key ingredients of the join are a filtering function which we'll call `rel_ok` (for "release is OK") and the join command which calls it. Here's the function:

```
function series rel_ok (const series obsdate, const series reldate, int p)
  series y_obs, m_obs, y_rel, m_rel
  # get year and month from observation date
  isoconv(obsdate, &y_obs, &m_obs)
  # get year and month from release date
  isoconv(reldate, &y_rel, &m_rel)
  # find the delta in months
  series dm = (12*y_rel + m_rel) - (12*y_obs + m_obs)
  # and implement the filter
  return dm <= p
end function
```

Note that the series arguments to `rel_ok` are marked as `const` so that they're simply shared with the function rather than being copied (since they're not being modified; see chapter 14). And here's the command:

```
scalar lag = 3 # choose your fixed lag here
join @fname ip_plus3 --data=INDPRO --tkey=observation_date \
--tconvert="observation_date,realtime_start_date" \
--filter="rel_ok(observation_date, realtime_start_date, lag)" \
--aggr=max(realtime_start_date)
```

⁷Some user-contributed functions may be available that address this issue, but it is beyond our scope here. Another even more complicated issue in the realtime context is that of "benchmark revisions" applied by statistical agencies, where the underlying definition or composition of a variable changes on some date, which goes beyond a mere rescaling. However, this type of structural change is not, in principle, a feature of realtime data alone, but applies to any time-series data.

Note that we use `--tconvert` to convert both the observation date and the realtime start date (or release date) to 8-digit numerical values. Both of these series are passed to the filter, which uses the built-in function `isoconv` to extract year and month. We can then calculate `dm`, the “delta months” since the observation date, for each release. The filter condition is that this delta should be no greater than the specified lag, p .⁸

This filter condition may be satisfied by more than one release, but only the latest of those will actually be the vintage that was current at the end of the n -th month after the observation period, so we add the option `--aggr=max(realtime_start_date)`. If instead you want to target the release at the *beginning* of the n -th month you would have to use a slightly more complicated filter function.

An illustration

Figure 8.1 shows four time series for the monthly index of US industrial production from October 2005 to June 2009: the value as of first publication plus the values current 3, 6 and 12 months out from the observation date.⁹ From visual inspection it would seem that over much of this period the Federal reserve was fairly consistently overestimating industrial production at first release and shortly thereafter, relative to the figure they arrived at with a lag of a year.

The script that produced this Figure is shown in full in Listing 8.1.

🔗 To replicate the examples in Listings 8.1 and 8.2 below you’ll need the Alfred file `INDPRO.txt`, which is available as <https://gret1.sf.net/gret1data/INDPRO.txt>.

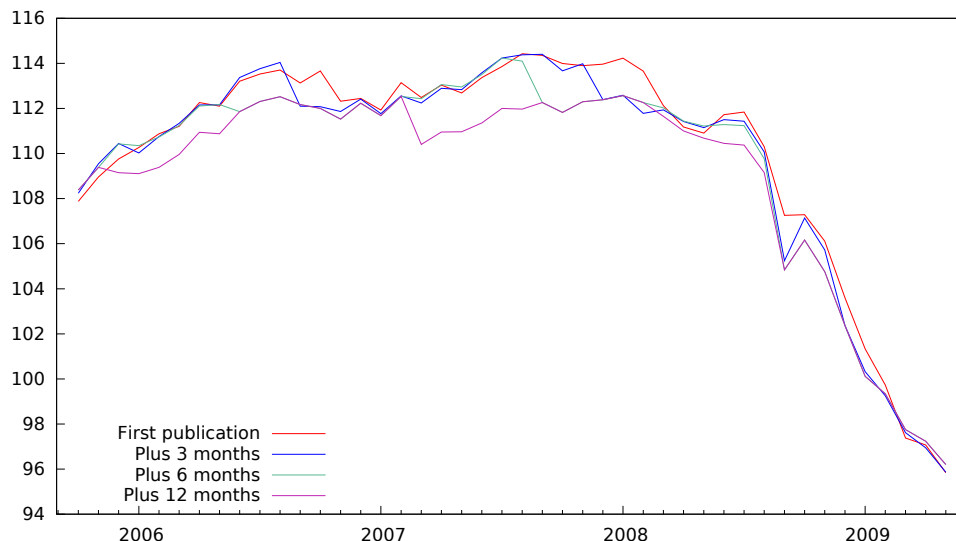


Figure 8.1: Successive revisions to US industrial production

8.7 Getting the revision history for an observation

For our final example we show how to retrieve the revision history for a given observation (again using Alfred data on US industrial production). In this exercise we are switching the time axis: the observation period is a fixed point and time is “vintage time”.

⁸The filter is written on the assumption that the lag is expressed in months; on that understanding it could be used with annual or quarterly data as well as monthly. The idea could be generalized to cover weekly or daily data without much difficulty.

⁹Why not a longer series? Because if we try to extend it in either direction we immediately run into the index re-basing problem mentioned in section 8.5, with big (staggered) leaps downward in all the series.

Listing 8.1: Retrieving successive realtime lags of US industrial production [\[Download ▼\]](#)

```

function series rel_ok (const series obsdate, const series reldate, int p)
    series y_obs, m_obs, d_obs, y_rel, m_rel, d_rel
    isoconv(obsdate, &y_obs, &m_obs, &d_obs)
    isoconv(reldate, &y_rel, &m_rel, &d_rel)
    series dm = (12*y_rel + m_rel) - (12*y_obs + m_obs)
    return dm < p || (dm == p && d_rel <= d_obs)
end function

nulldata 45
setobs 12 2005:10

string fname = "INDPRO.txt"

# initial published values
join @fname firstpub --data=INDPRO --tkey=observation_date \
--tconvert=realtime_start_date --aggr=min(realtime_start_date)

# plus 3 months
join @fname plus3 --data=INDPRO --tkey=observation_date \
--tconvert="observation_date,realtime_start_date" \
--filter="rel_ok(observation_date, realtime_start_date, 3)" \
--aggr=max(realtime_start_date)

# plus 6 months
join @fname plus6 --data=INDPRO --tkey=observation_date \
--tconvert="observation_date,realtime_start_date" \
--filter="rel_ok(observation_date, realtime_start_date, 6)" \
--aggr=max(realtime_start_date)

# plus 12 months
join @fname plus12 --data=INDPRO --tkey=observation_date \
--tconvert="observation_date,realtime_start_date" \
--filter="rel_ok(observation_date, realtime_start_date, 12)" \
--aggr=max(realtime_start_date)

setinfo firstpub --graph-name="First publication"
setinfo plus3 --graph-name="Plus 3 months"
setinfo plus6 --graph-name="Plus 6 months"
setinfo plus12 --graph-name="Plus 12 months"

# set --output=realtime.pdf for PDF
gnuplot firstpub plus3 plus6 plus12 --time --with-lines \
--output=display { set key left bottom; }

```

A suitable script is shown in Listing 8.2. We first select an observation to track (January 1970). We start the clock in the following month, when a data-point for this period was first published, and let it run to the end of the vintage history (in this file, March 2013). Our outer time key is the realtime start date and we filter on observation date; we name the imported INDPRO values as `ip_jan70`. Since it sometimes happens that more than one revision occurs in a given month we need to select an aggregation method: here we choose to take the last revision in the month.

Recall from section 8.2 that Alfred records a new revision only when the data-point in question actually changes. This means that our imported series will contain missing values for all months when no real revision took place. However, we can apply a simple autoregressive rule to fill in the blanks: each missing value equals the prior non-missing value.

Figure 8.2 displays the revision history. Over this sample period the periodic re-basing of the index overshadows amendments due to accrual of new information.

Listing 8.2: Retrieving a revision history [\[Download ▼\]](#)

```
# choose the observation to track here (YYYYMMDD)
scalar target = 19700101

nulldata 518 --preserve
setobs 12 1970:02

join INDPRO.txt ip_jan70 --data=INDPRO --tkey=realtime_start_date \
--tconvert=observation_date \
--filter="observation_date==target" --aggr=seq:-1

ip_jan70 = ok(ip_jan70) ? ip_jan70 : ip_jan70(-1)
gnuplot ip_jan70 --time --with-lines --output=display
```

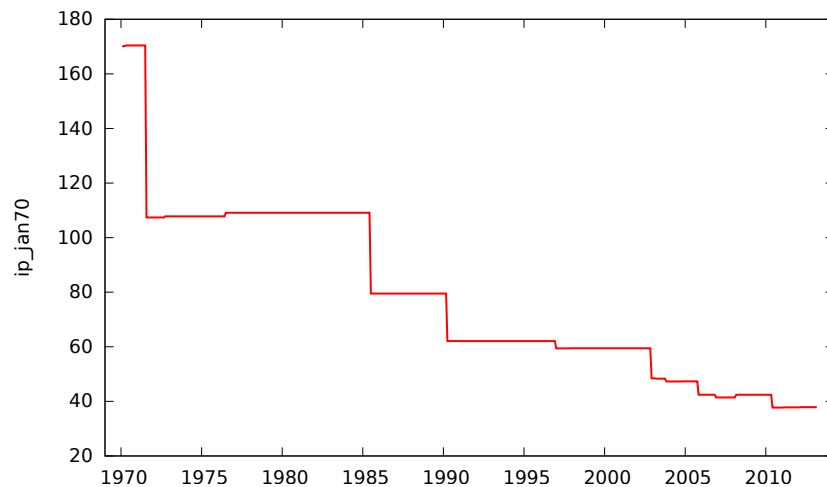


Figure 8.2: Vintages of the index of US industrial production for January 1970

Chapter 9

Temporal disaggregation

9.1 Introduction

This chapter describes and explains the facility for temporal disaggregation in gretl.¹ This is implemented by the `tdisagg` function, which supports three variants of the method of [Chow and Lin \(1971\)](#); the method of [Fernández \(1981\)](#); and two variants of the method of [Denton \(1971\)](#) as modified by [Cholette \(1984\)](#). Given the analytical similarities between them, the three Chow-Lin variants and the Fernández method will be grouped in the discussion below as “Chow-Lin methods”.

The balance of this section provides a gentle introduction to the idea of temporal disaggregation; experts may wish to skip to the next section.

Basically, temporal disaggregation is the business of taking time-series data observed at some given frequency (say, annually) and producing a counterpart series at a higher frequency (say, quarterly). The term “disaggregation” indicates the inverse operation of aggregation, and to understand temporal disaggregation it’s helpful first to understand temporal aggregation. In aggregating a high frequency series to a lower frequency there are three basic methods, the appropriate method depending on the nature of the data. Here are some illustrative examples.

- **GDP:** say we have quarterly GDP data and wish to produce an annual series. This is a *flow variable* and the annual flow will be the *sum* of the quarterly values (unless the quarterly values are annualized, in which case we would aggregate by taking their mean).
- **Industrial Production:** this takes the form of an *index* reporting the level of production over some period relative to that in a base period in which the index is by construction 100. To aggregate from (for example) monthly to quarterly we should take the *average* of the monthly values. (The sum would give a nonsense result.) The same goes for price indices, and also for ratios of stocks to flows or vice versa (inventory to sales, debt to GDP, capacity utilization).
- **Money stock:** this is typically reported as an *end-of-period* value, so in aggregating from monthly to quarterly we’d take the value from the final month of each quarter. In case a stock variable is reported as a *start-of-period* value, the aggregated version would be that of the first month of the quarter.

A central idea in temporal disaggregation is that the high frequency series must respect both the given low frequency data and the aggregation method. So for example, whatever numbers we come up with for quarterly GDP, given an annual series as starting point, our numbers must sum to the annual total. If money stock is measured at the end of the period then whatever numbers we come up with for monthly money stock, given quarterly data, the figure for the last month of the quarter must match that for the quarter as a whole. This is why temporal disaggregation is sometimes called “benchmarking”: the given low frequency data constitute a benchmark which the constructed high frequency data must match, in a well defined sense that depends on the nature of the data.

Colloquially, we might describe temporal disaggregation as “interpolation,” but strictly speaking interpolation applies only to stock variables. We have a known end-of-quarter value (say), which is also the value at the end of the last month of the quarter, and we’re trying to figure out what the

¹We are grateful to Tommaso Di Fonzo, Professor of Statistical Science at the University of Padua, for detailed and precise comments on earlier drafts. Any remaining errors are, of course, our responsibility.

value might have been at the end of months 1 and 2. We’re filling in the blanks, or interpolating. In the GDP case, however, the procedure is *distribution* rather than interpolation. We have a given annual total and we’re trying to figure out how it should be distributed over the quarters. We’re also doing distribution for variables taking the form of indices or ratios, except in this case we’re seeking plausible values whose mean equals the given low-frequency value.

While matching the low frequency benchmark is an important constraint, it obviously does not tie down the high frequency values. That is a job for either regression-based methods such as Chow-Lin or non-regression methods such as Denton. Details are provided in section 9.7.

9.2 Notation and design

Some notation first: the two main ingredients in temporal disaggregation are

- a $T \times g$ matrix \mathbf{Y} (holding the series to be disaggregated) and
- a matrix \mathbf{X} with k columns and $(s \cdot T + m)$ rows (to aid in the disaggregation).

The idea is that \mathbf{Y} contains time series data sampled at some frequency f , while each column of \mathbf{X} contains time series data at a higher frequency, sf . So for each observation Y_t we have s corresponding rows in \mathbf{X} . The object is to produce a transformation of \mathbf{Y} to frequency sf , with the help of \mathbf{X} (whose columns are typically called “related series” or “indicators” in the temporal disaggregation literature), via either distribution or interpolation depending on the nature of the data. For most of this document we will assume that $g = 1$, or in other words we are performing temporal disaggregation on a single low-frequency series, but `tdisagg` supports “batch processing” of several series and we return to this point in section 9.9.

If the m in $(s \cdot T + m)$ is greater than zero, that implies that there are some “extra” high-frequency observations available for extrapolation—see section 9.4 for details.

We need to say something more about what goes into \mathbf{X} . Under the Denton methods this must be a single series, generally known as the “preliminary series”.² For the Chow-Lin methods, \mathbf{X} can hold a combination of deterministic terms (e.g. constant, trend) and stochastic series. Naturally, suitable candidates for the role of preliminary series or indicator will be variables that are correlated with \mathbf{Y} (and in particular, might be expected to share short-run dynamics with \mathbf{Y}). However, it is possible to carry out disaggregation using deterministic terms only—in the simplest case, with \mathbf{X} containing nothing but a constant. Experts in the field tend to frown on this, with reason: in the absence of any genuine high-frequency information disaggregation just amounts to a “mechanical” smoothing. But some people may have a use for such smoothing, and it’s permitted by `tdisagg`.

We should draw attention to a design decision in `tdisagg`: we have separated the specification of indicators in \mathbf{X} from certain standard deterministic terms that might be wanted, namely, a constant, linear trend or quadratic trend. If you want a disaggregation *without* stochastic indicators, you can omit (or set to `null`) the argument corresponding to \mathbf{X} . In that case a constant (only) will be employed automatically, but for the Chow-Lin methods one can adjust the deterministic terms used via an option named `det`, described below. In other words the content of \mathbf{X} becomes implicit. See section 9.6 for more detail.

Here’s an important point to note when \mathbf{X} is given explicitly: although this matrix may contain extra observations “at the end” we assume that \mathbf{Y} and \mathbf{X} are *correctly aligned at the start*. Take for example the annual to quarterly case: if the first observation in annual \mathbf{Y} is for 1980 then the first observation in quarterly \mathbf{X} must be for the first quarter of 1980. Ensuring this is the user’s responsibility. We will have some more to say about this in the following section.

²There’s nothing to stop a user from *constructing* such a series using several primary series as input—by taking the first principal component or some other means—but that possibility is beyond our scope here.

9.3 Overview of data handling

The `tdisagg` function has three basic arguments, representing **Y**, **X** and *s* respectively (plus several options; see below). The first two arguments can be given either in matrix form as such, or as “dataset objects”—that is, a series for **Y** and a series or list of series for **X**. Or, as mentioned above, **X** can be omitted (left implicit). This gives rise to five cases; which is most convenient will depend on the user’s workflow.

1. Both **Y** and **X** are matrices. In this case, the size and periodicity of the currently open dataset (if any) are irrelevant. If **Y** has *T* rows **X** must, of course, have at least $s \cdot T$ rows; if that condition is not satisfied an “Invalid argument” error will be flagged.
2. **Y** is a series (or list) and **X** a matrix. In this case we assume that the periodicity of the currently open dataset is the *lower* one, and *T* will be taken as equal to `$nobs` (the number of observations in the current sample range). Again, **X** must have at least $s \cdot T$ rows.
3. **Y** is a matrix and **X** a series or list. We then assume that the periodicity of the currently open dataset is the *higher* one, so that `$nobs` defines $(s \cdot T + m)$. And **Y** is supposed to be at the lower frequency, so its number of rows gives *T*. We should then be able to find *m* as `$nobs` minus $s \cdot T$; if $m < 0$ an error is flagged.
4. Both **Y** and **X** are “dataset objects”. We have two sub-cases here.
 - (a) If **X** is a series, or an ordinary list of series, the periodicity of the currently open dataset is taken to be the *higher* one. The series (or list) containing **Y** should hold the appropriate entries *every s elements*. For example, if $s = 4$, Y_1 will be taken from the first observation, Y_2 from the fifth, Y_3 from the ninth, and so on. In practical terms, series of this sort are likely to be composed by repeating each element of a low-frequency variable *s* times.
 - (b) Alternatively, **X** could be a “MIDAS list”. The concept of a MIDAS list is fully explained in chapter 20 but for example, in a quarterly dataset a MIDAS list would be a list of three series, for the third, second and first month (note the ordering). In this case, the current periodicity is taken to be the *lower* one and **X** will contain one column, corresponding to the high-frequency representation of the MIDAS list.
5. **X** is omitted. If **Y** is given as a matrix it is taken to have *T* rows. Otherwise the interpretation is determined heuristically: if the **Y** series is recognized by `gretl` as composed of repeated low-frequency observations, or if a series result is requested, it is taken as having length sT , otherwise its length is taken to be *T*.

In the previous section we flagged the importance of correct alignment of **X** and **Y** at the start of the data; we’re now in a position to say a little more about this. If either **X** or **Y** are given in matrix form alignment is truly the user’s responsibility. But if they are dataset objects `gretl` can be more helpful. We automatically advance the start of the sample range to exclude any leading missing values, and retard the end of the sample ranges for **X** and **Y** to exclude trailing missing values (allowing for the possibility that **X** may extend beyond **Y**). In addition we further advance the sample start if this is required to ensure that the **X** data begin in the first high-frequency sub-period (e.g. the first quarter of a year or the first month of a quarter). But please note: when `gretl` automatically excludes leading or trailing missing values, intra-sample missing values will still provoke an error.

9.4 Extrapolation

As mentioned above, if **X** holds covariate data which extend beyond the range of the original series to be disaggregated then extrapolation is supported. But this is inherently risky, and becomes riskier the longer the horizon over which it is attempted. In `tdisagg` extrapolation is by default limited to one low-frequency period (= *s* high-frequency periods) beyond the end of the original data. The user can adjust this behavior via the `extmax` member of the `opts` bundle passed to `tdisagg`, described in the next section.

9.5 Function signature

The signature of `tdisagg` is:

```
matrix tdisagg(Y0, [X], int s, [bundle opts], [bundle results])
```

where square brackets indicate optional arguments. Note that while the return value is a matrix, if `Y0` contains a single column or series it can be assigned to a series as in

```
series ys = tdisagg(Y0, ...)
```

provided it's of the right length to match the current dataset, or the current sample range. Details on the arguments follow.

`Y0` : `Y`, as a matrix, series or list.

`X` (optional): `X` as a matrix, series or list. This should *not* contain standard deterministic terms, since they are handled separately (see `det` under `opts` below). If this matrix is omitted, then disaggregation will be performed using deterministic terms only.

`s` (int): The temporal expansion factor, for example 3 for quarterly to monthly, 4 for annual to quarterly or 12 for annual to monthly. We do not support cases such as monthly to weekly or monthly to daily, where `s` is not a fixed integer value common to all observations; otherwise, anything goes.

`opts` (bundle, optional): a bundle holding additional options. The recognized keys are (in alphabetical order):

`aggtype` (string): Specifies the type of temporal aggregation appropriate to the series in question. The value must be one of `sum` (each low-frequency value is a sum of `s` high-frequency values, the default); `avg` (each low-frequency value is the average of `s` high frequency values); or `last` or `first`, indicating respectively that each low-frequency value is the last or first of `s` high frequency values.

`det` (int): Relevant only when one of the Chow-Lin methods is selected. This is a numeric code for the deterministic terms to be included in the regressions: 0 means none; 1, constant only; 2, constant and linear trend; 3, constant and quadratic trend. The default is 1.

`extmax` (int): the maximum number of high-frequency periods over which extrapolation should be carried out, conditional on the availability of covariate data. A zero value means no extrapolation; a value of `-1` means as many periods as possible; and a positive value limits extrapolation to the specified number of periods. See section 9.4 for a statement of the default value.

`method` (string): Selects the method of disaggregation (see the listing below). Note that the Chow-Lin methods employ an autoregression coefficient, ρ , which captures the persistence of the target series at the higher frequency and is used in GLS estimation of the parameters linking `X` to `Y`.

- `chow-lin` (the default) is modeled on the original method proposed by Chow and Lin. It uses a value of ρ computed as the transformation of a maximum-likelihood estimate of the low-frequency autocorrelation coefficient.
- `chow-lin-mle` is equivalent to the method called `chow-lin-maxlog` in the `tempdisagg` package for R; ρ is estimated by iterated GLS using the loglikelihood as criterion, as recommended by [Bournay and Laroque \(1979\)](#). (The BFGS algorithm is used internally).
- `chow-lin-ssr` is equivalent to the method called `chow-lin-minrss-quilis` in `tempdisagg`; ρ is estimated by iterated GLS using the sum of squared GLS residuals as criterion (L-BFGS is used internally).

- `fernandez` is basically “Chow-Lin with $\rho = 1$ ”. It is suitable if the target series has a unit root, and is not cointegrated with the indicator series.
- `denton-pfd` is the proportional first differences variant of Denton, as modified by Cholette. See [Di Fonzo and Marini \(2012\)](#) for details.
- `denton-afd` is the additive first differences variant of Denton (again, as modified by Cholette). In contrast to the Chow-Lin methods, neither Denton procedure involves regression.

`plot` (int): If a non-zero value is given, a simple plot is displayed by way of a “sanity check” on the final series. See section 9.8 for details.

`rho` (scalar): Relevant only when one of the Chow-Lin methods is selected. If the method is `chow-lin`, then `rho` is treated as a fixed value for ρ , thus enabling the user to bypass the default estimation procedure altogether. If the method is `chow-lin-mle` or `chow-lin-ssr`, on the other hand, the supplied ρ value is used to initialize the numerical optimization algorithm.

`verbose` (int): Controls the verbosity of Chow-Lin or Fernández output. If 0 (the default) nothing is printed unless an error occurs; if 1, summary output from the relevant regression is shown; if 2, in addition output from the optimizer for the iterated GLS procedure is shown, if applicable.

`results` (bundle, optional): If present, this argument must be a previously defined bundle. Upon successful completion of any of the methods other than `denton` it contains details of the disaggregation under the following keys:

`method` : the method employed

`rho` : the value of ρ used

`lnl` : loglikelihood (maximized by the `chow-lin-mle` method)

`SSR` : sum of squared residuals (minimized by the `chow-lin-ssr` method)

`coeff` : the GLS (or OLS) coefficients

`stderr` : standard errors for the coefficients

If ρ is set to zero—either by specification of the user or because the estimate $\hat{\rho}$ turned out to be non-positive—then estimation of the coefficients is via OLS. In that case the `lnl` and `SSR` values are calculated using the OLS residuals (which will be on a different scale from the weighted residuals in GLS).

9.6 Handling of deterministic terms

It may be helpful to set out clearly, in one place, how deterministic terms are handled by `tdisagg`.

- If `X` is given explicitly: No deterministic term is added when the Denton method is used (since a single preliminary series is wanted) but a constant is added when one of the Chow-Lin methods is selected. The latter default can be overridden (i.e. the constant removed, or a trend added) by means of the `det` entry in the `options` bundle.
- If `X` is omitted: By default a constant is used for all methods. Again, for Chow-Lin this can be overridden by specifying a `det` value. If for some reason you wanted Denton with just a trend you would have to supply `X` containing a trend.

9.7 Some technical details

In this section we provide some technical details on the methods used by `tdisagg`. We will refer to the version of `Y` converted to the high frequency `sf` as the “final series”.

As regards the Cholette-modified Denton methods, for the proportional first difference variant we calculate the final series using the solution described by [Di Fonzo and Marini \(2012\)](#), specifically equation (4) on page 5, and for the additive variant we draw on [Di Fonzo \(2003\)](#), pages 3 and 5 in particular. Note that these procedures require the construction and inversion of a matrix of order $(s + 1)T$. If both s and T are large it can therefore take some time, and be quite demanding of RAM.

As regards Chow-Lin, let ρ_0 indicate the rho value passed via the options bundle (if applicable). We then take these steps:

1. If $\rho_0 > 0$ set $\rho = \rho_0$ and go to step 6 if the method is `chow-lin` or step 7 otherwise. But if $\rho_0 < 0$ set $\rho = 0$.
2. Estimate via OLS a regression of \mathbf{Y} on \mathbf{CX} ,³ where \mathbf{C} is the appropriate aggregation matrix. Let $\hat{\beta}_{\text{OLS}}$ equal the coefficients from this regression. If $\rho_0 = 0$ and the method is `chow-lin` go to step 8.
3. Calculate the (low frequency) first order autocorrelation of the OLS residuals, $\hat{\rho}_L$. If $\hat{\rho}_L \geq 10^{-6}$ go to step 4. Otherwise, if the method is `chow-lin` set $\rho = 0$ and go to step 8, else set $\rho = 0.5$ and go to step 7.
4. Refine the positive estimate of $\hat{\rho}_L$ via Maximum Likelihood estimation of the AR(1) specification as described in [Davidson and MacKinnon \(2004\)](#).
5. If $\hat{\rho}_L < 0.999$, set ρ to the high-frequency counterpart of $\hat{\rho}_L$ using the approach given in [Chow and Lin \(1971\)](#). Otherwise set $\rho = 0.999$. If the method is `chow-lin`, go to step 6, otherwise go to step 7.
6. Perform GLS with the given value of ρ , store the coefficients as $\hat{\beta}_{\text{GLS}}$ and go to step 9.
7. Perform iterated GLS starting from the prior value of ρ , adjusting ρ with the goal of either maximizing the loglikelihood (method `chow-lin-mle`) or minimizing the sum of squared GLS residuals (`chow-lin-ssr`); set $\hat{\beta}_{\text{GLS}}$ to the final coefficient estimates; and go to step 9.
8. Calculate the final series as $\mathbf{X}\hat{\beta}_{\text{OLS}} + \mathbf{C}'(\mathbf{C}\mathbf{C}')^{-1}\hat{\mathbf{u}}_{\text{OLS}}$, where $\hat{\mathbf{u}}_{\text{OLS}}$ indicates the OLS residuals, and stop.
9. Calculate the final series as $\mathbf{X}\hat{\beta}_{\text{GLS}} + \mathbf{V}\mathbf{C}'(\mathbf{C}\mathbf{V}\mathbf{C}')^{-1}\hat{\mathbf{u}}_{\text{GLS}}$, where $\hat{\mathbf{u}}_{\text{GLS}}$ indicates the GLS residuals and \mathbf{V} is the estimated high-frequency covariance matrix.

A few notes on our Chow-Lin algorithm follow.

- One might question the value of performing steps 2 to 5 when the method is one that calls for GLS iteration (`chow-lin-mle` or `chow-lin-ssr`), but our testing indicates that it can be helpful to have a reasonably good estimate of ρ in hand before embarking on these iterations.
- Conversely, one might wonder why we bother with GLS iterations if we find $\hat{\rho}_L < 10^{-6}$. But this allows for the possibility (most likely associated with small sample size) that iteration will lead to $\rho > 0$ even when the estimate based on the initial OLS residuals is zero or negative.
- Note that in all cases we are discarding an estimate of $\rho < 0$ (truncating to 0), which we take to be standard in this field. In our iterated GLS we achieve this by having the optimizer pick values x in $[-\infty, +\infty]$ which are translated to $[0, 1]$ via the logistic CDF, $\rho = 1/(1 + \exp(-x))$. To be precise, that's the case with `chow-lin-mle`. But we find that the `chow-lin-ssr` method is liable to overestimate ρ and proceed to values arbitrarily close to 1, resulting in numerical problems. We therefore bound this method to x in $[-20, +6.9]$, corresponding to ρ values between near-zero and approximately 0.999.⁴

³Strictly speaking, \mathbf{CX} uses only the first sT rows of \mathbf{X} if $m > 0$.

⁴It may be worth noting that the `tempdisagg` package for R limits both methods to a maximum ρ of 0.999. We find, however, that the ML method can “look after itself”, and does not require the fixed upper bound short of 1.0.

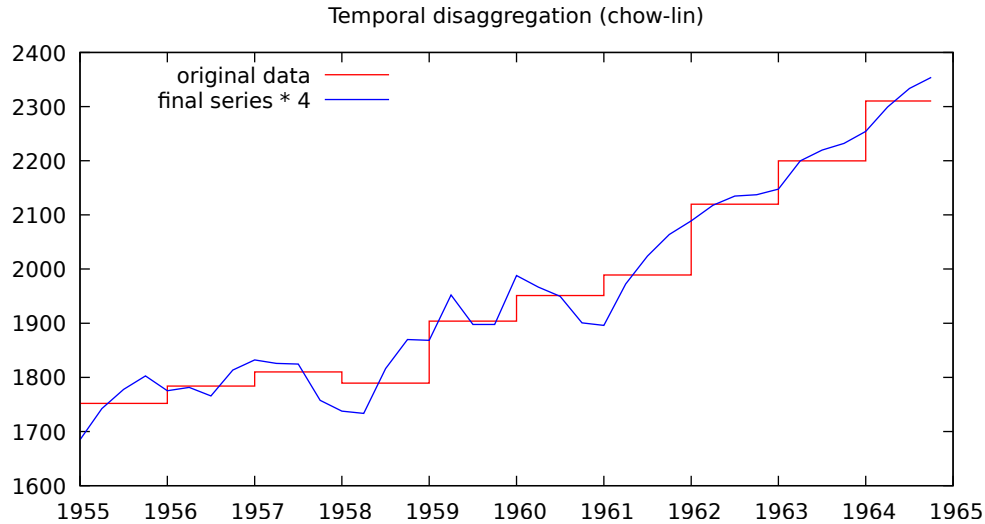


Figure 9.1: Example output from plot option, showing annual GNP (red) and quarterly final series (blue) using quarterly industrial production as indicator.

As for the Fernández method, this is quite straightforward. The place of the high-frequency covariance matrix \mathbf{V} in Chow-Lin is taken by $(\mathbf{D}'\mathbf{D})^{-1}$, where \mathbf{D} is the approximate first-differencing matrix, with 1 on the diagonal and -1 on the first sub-diagonal. For efficient computation, however, we store neither \mathbf{D} nor $\mathbf{D}'\mathbf{D}$ as such, and do not perform any explicit inversion. The special structure of $(\mathbf{D}'\mathbf{D})^{-1}$ makes it possible to produce the effect of pre-multiplication by this matrix with $O(T^2)$ floating-point operations. Estimation of ρ is not an issue since it equals 1 by assumption.

9.8 The plot option

The semantics of this option may be enriched in future but for now it's a simple boolean switch. The effect is to produce a time series plot of the final series along with the original low-frequency series, shown in “step” form. If aggregation is by sum the final series is multiplied by s for comparability with the original. If the disaggregation has been successful these two series should track closely together, with the final series showing plausible short-run dynamics. An example is shown in Figure 9.1.

If there are many observations, the two lines may appear virtually coincident. In that case one can see what's going on in more detail by exploiting the “Zoom” functionality of the plot, which is accessed via the right-click menu in the plot window.

9.9 Multiple low-frequency series

We now return to a point mentioned in section 9.2, namely, that \mathbf{Y} may be given as a $T \times g$ matrix with $g > 1$, or a list of g series. This means that a single call to `tdisagg` can be used to process several input series (“batch processing”), in which case the return value is a matrix with $(s \cdot T + m)$ rows and g columns.

There are some restrictions. First and most obviously, a single call to `tdisagg` implies a single selection of “indicators” or “related series” (\mathbf{X}) and a single selection of options (aggregation type of the data, deterministic terms, disaggregation method, and so on). So this possibility will be relevant only if you have several series that “want the same treatment.” In addition, if $g > 1$ the `plot` and `verbose` options are ignored and the `results` bundle is not filled; if you need those features you should supply a single series or vector in \mathbf{Y} .

The advantage of batch processing lies in the spreading of fixed computational cost, leading to shorter execution time. However, the relative importance of the fixed cost differs substantially according to the disaggregation method. For the Chow-Lin methods the fixed cost is relatively small and so little speed-up can be expected, but for the Denton methods it dominates, and (in our testing) you can process $g > 1$ series in little more time than it takes to process a single series.

As they say, “Your mileage may vary,” but if you have a large number of series to be disaggregated via one of the Denton methods you may well find it much faster to use the batch facility of `tdisagg`.

9.10 Examples

Listing 9.1 shows an example of usage and its output. The data are drawn from the St Louis Fed; we disaggregate quarterly GDP to monthly with the help of industrial production and payroll employment, using the default Chow-Lin method.

Several other example scripts are available from <http://gretl.sourceforge.net/tdisagg/>.

Listing 9.1: Example of tdisagg usage [\[Download ▼\]](#)

```

### Traditional Chow-Lin: y is a series with repetition
### and X is a list of series. This corresponds to case 4(a)
### as described in section 9.3 of the documentation above.
###

# ensure that no data are in place
clear
# open gretl's St Louis Fed database
open fedstl.bin
# import two monthly series
data indpro payems
# import quarterly GDP (values are repeated)
data gdpc1

# restrict sample to complete data
smp1 --no-missing

# disaggregate GDP from quarterly to monthly, using
# industrial production and payroll employment as indicators
scalar s = 3
list X = indpro payems
series gdpm = tdisagg(gdpc1, X, s, _(verbose=1, aggtype="sum"))

```

Output:

```

Aggregation type sum
GLS estimates (chow-lin) T = 294
Dependent variable: gdpc1

```

	coefficient	std. error	t-ratio	p-value	
const	312.394	263.372	1.186	0.2365	
indpro	10.9158	1.75785	6.210	1.83e-09	***
payems	0.0242860	0.00171935	14.13	7.39e-35	***

```
rho = 0.999, SSR = 51543.9, ln l = -1604.98
```

```
Generated series gdpm (ID 4)
```

Chapter 10

Special functions in `genr`

10.1 Introduction

The `genr` command provides a flexible means of defining new variables. At the same time, the somewhat paradoxical situation is that the “`genr`” keyword is almost never visible in gretl scripts. For example, it is not really recommended to write a line such as `genr b = 2.5`, because there are the following alternatives:

- `scalar b = 2.5`, which also invokes the `genr` apparatus in gretl, but provides explicit type information about the variable `b`, which is usually preferable. (gretl’s language `hansl` is statically typed, so `b` cannot switch from scalar to string or matrix, for example.)
- `b = 2.5`, leaving it to gretl to infer the admissible or most “natural” type for the new object, which would again be a scalar in this case.
- `matrix b = {2.5}`: This formulation is required if `b` is going to be expanded with additional rows or columns later on. Otherwise, gretl’s static typing would not allow `b` to be promoted from scalar to matrix, so it must be a matrix right from the start, even if it is of dimension 1×1 initially. (This definition could also be written as `matrix b = 2.5`, but the more explicit form is recommended.)

In addition to `scalar` or `matrix`, other type keywords that can be used to substitute the generic `genr` term are those enumerated in the following chapter 11. In the case of an array the concrete specification should be used, so one of `matrices`, `strings`, `lists`, `bundles`.¹

Therefore, there’s only a handful of special cases where it is really necessary to use the “`genr`” keyword:

- `genr time` — Creates a time trend variable (1,2,3,...) under the name `time`. Note that within an appropriately defined panel dataset this variable honors the panel structure and is a true time index. (In a cross-sectional dataset, the command will still work and produces the same result as `genr index` below, but of course no temporal meaning exists.)
- `genr index` — Creates an observation variable named `index`, running from 1 to the sample size.
- `genr unitdum` — In the context of panel data, creates a set of dummies for the panel groups or “units”. These are named `du_1`, `du_2`, and so forth. Actually, this particular `genr` usage is not strictly necessary, because a list of group dummies can also be obtained as:

```
series gr = $unit
list groupdums = dummify(gr, NA)
```

(The `NA` argument to the `dummify` function has the effect of not skipping any unit as the reference group, thus producing the full set of dummies.)

¹A recently added advanced datatype is an array of arrays, with the associated type specifier `arrays`.

- `genr timedum` — Again for panel data, creates a set of dummies for the time periods, named `dt_1`, `dt_2`, And again, a list-producing variant without `genr` exists, using the special accessor `$obsminor` which indexes time in the panel context and can be used as a substitute for `time` from above:

```
series tindex = $obsminor
list timedums = dummify(tindex, NA)
```

- `genr markers` — See section 4.5 for an explanation and example of this panel-related feature.

Finally, there also exists `genr dummy`, which produces a set of seasonal dummies. However, it is recommended to use the `seasonals()` function instead, which can also return centered dummies.

The rest of this chapter discusses other special function aspects.

10.2 Cumulative densities and p-values

The two functions `cdf` and `pvalue` provide complementary means of examining values from 17 probability distributions (as of July 2021), among which the most important ones: standard normal, Student's t , χ^2 , F , gamma, and binomial. The syntax of these functions is set out in the *Gretl Command Reference*; here we expand on some subtleties.

The cumulative density function or CDF for a random variable is the integral of the variable's density from its lower limit (typically either $-\infty$ or 0) to any specified value x . The p-value (at least the one-tailed, right-hand p-value as returned by the `pvalue` function) is the complementary probability, the integral from x to the upper limit of the distribution, typically $+\infty$.

In principle, therefore, there is no need for two distinct functions: given a CDF value p_0 you could easily find the corresponding p-value as $1 - p_0$ (or vice versa). In practice, with finite-precision computer arithmetic, the two functions are not redundant. This requires a little explanation. In `gretl`, as in most statistical programs, floating point numbers are represented as “doubles” — double-precision values that typically have a storage size of eight bytes or 64 bits. Since there are only so many bits available, only so many floating-point numbers can be represented: *doubles do not model the real line*. Typically doubles can represent numbers over the range (roughly) $\pm 1.7977 \times 10^{308}$, but only to about 15 digits of precision.

Suppose you're interested in the left tail of the χ^2 distribution with 50 degrees of freedom: you'd like to know the CDF value for $x = 0.9$. Take a look at the following interactive session:

```
? scalar p1 = cdf(X, 50, 0.9)
Generated scalar p1 = 8.94977e-35
? scalar p2 = pvalue(X, 50, 0.9)
Generated scalar p2 = 1
? scalar test = 1 - p2
Generated scalar test = 0
```

The `cdf` function has produced an accurate value, but the `pvalue` function gives an answer of 1, from which it is not possible to retrieve the answer to the CDF question. This may seem surprising at first, but consider: if the value of `p1` above is correct, then the correct value for `p2` is $1 - 8.94977 \times 10^{-35}$. But there's no way that value can be represented as a double: that would require over 30 digits of precision.

Of course this is an extreme example. If the x in question is not too far off into one or other tail of the distribution, the `cdf` and `pvalue` functions will in fact produce complementary answers, as shown below:

```
? scalar p1 = cdf(X, 50, 30)
Generated scalar p1 = 0.0111648
```

```
? scalar p2 = pvalue(X, 50, 30)
Generated scalar p2 = 0.988835
? scalar test = 1 - p2
Generated scalar test = 0.0111648
```

But the moral is that if you want to examine extreme values you should be careful in selecting the function you need, in the knowledge that values very close to zero can be represented as doubles while values very close to 1 cannot.

10.3 Retrieving internal variables (dollar accessors)

A very useful feature is to retrieve in a script various values calculated by `gretl` in the course of estimating models or testing hypotheses. Since they all start with a literal `$` character, they are called “dollar accessors”. The variables that can be retrieved in this way are listed in the *Gretl Command Reference* or in the built-in function help under the Help menu. The dollar accessors can be used like other `gretl` objects in script assignments or statements. Some of those accessors are actually independent of any estimation or test and describe, for example, the context of the running `gretl` program. But here we say a bit more about the special variables `$test` and `$pvalue`.

These variables hold, respectively, the value of the last test statistic calculated using an explicit testing command and the p-value for that test statistic. If no such test has been performed at the time when these variables are referenced, they will produce the missing value code. Some “explicit testing commands” that work in this way are as follows (among others): `add` (joint test for the significance of variables added to a model); `adf` (Augmented Dickey-Fuller test, see below); `arch` (test for ARCH); `chow` (Chow test for a structural break); `coeffsum` (test for the sum of specified coefficients); `coint` (Engle-Granger cointegration test); `cusum` (the Harvey-Collier *t*-statistic); `difftest` (test for a difference of two groups); `kpss` (KPSS stationarity test, no p-value available); `modtest` (see below); `meantest` (test for difference of means); `omit` (joint test for the significance of variables omitted from a model); `reset` (Ramsey’s RESET); `restrict` (general linear restriction); `runs` (runs test for randomness); and `vartest` (test for difference of variances). In most cases both a `$test` and a `$pvalue` are stored; the exception is the KPSS test, for which a p-value is not currently available.

The `modtest` command (which must follow an estimation command) offers several diagnostic tests; the particular test performed depends on the option flag provided. Please see the *Gretl Command Reference* and for example chapters 32 and 31 of this *Guide* for details.

An important point to notice about this mechanism is that the internal variables `$test` and `$pvalue` are over-written each time one of the tests listed above is performed. If you want to reference these values, you must do so at the correct point in the sequence of `gretl` commands.

Chapter 11

Gretl data types

11.1 Introduction

Gretl offers the following data types:

<code>scalar</code>	holds a single numerical value
<code>series</code>	holds n numerical values, where n is the number of observations in the current dataset
<code>matrix</code>	holds a rectangular array of numerical values, of any (two) dimensions
<code>list</code>	holds the ID numbers of a set of series
<code>string</code>	holds an array of characters
<code>bundle</code>	holds zero or more objects of various types
<code>array</code>	holds zero or more objects of a given type

The “numerical values” mentioned above are all double-precision floating point numbers.

In this chapter we give a run-down of the basic characteristics of each of these types and also explain their “life cycle” (creation, modification and destruction). The list and matrix types, whose uses are relatively complex, are discussed at greater length in chapters [15](#) and [17](#) respectively.

11.2 Series

We begin with the `series` type, which is the oldest and in a sense the most basic type in gretl. When you open a data file in the gretl GUI, what you see in the main window are the ID numbers, names (and descriptions, if available) of the series read from the file. All the series existing at any point in a gretl session are of the same length, although some may have missing values. The variables that can be added via the items under the Add menu in the main window (logs, squares and so on) are also series.

For a gretl session to contain any series, a common series length must be established. This is usually achieved by opening a data file, or importing a series from a database, in which case the length is set by the first import. But one can also use the `nulldata` command, which takes as its single argument the desired length, a positive integer.

Each series has these basic attributes: an ID number, a name, and of course n numerical values. A series may also have a description (which is shown in the main window and is also accessible via the `labels` command), a “display name” for use in graphs, a record of the compaction method used in reducing the variable’s frequency (for time-series data only) and flags marking the variable as discrete and/or as a numeric encoding of a qualitative characteristic. These attributes can be edited in the GUI by choosing Edit Attributes (either under the Variable menu or via right-click), or by means of the `setinfo` command.

In the context of most commands you are able to reference series by name or by ID number as you wish. The main exception is the definition or modification of variables via a formula; here you must use names since ID numbers would get confused with numerical constants.

Note that series ID numbers are always consecutive, and the ID number for a given series will change if you delete a lower-numbered series. In some contexts, where gretl is liable to get confused by

such changes, deletion of low-numbered series is disallowed.

Discrete series

It is possible to mark variables of the series type as *discrete*. The meaning and uses of this facility are explained in chapter 12.

String-valued series

It is generally expected that series in gretl will be “properly numeric” (on a ratio or at least an ordinal scale), or the sort of numerical indicator variables (0/1 “dummies”) that are traditional in econometrics. However, “string-valued” series are also supported—see chapter 16 for details.

11.3 Scalars

The scalar type is relatively simple: just a convenient named holder for a single numerical value. Scalars have none of the additional attributes pertaining to series, do not have ID numbers, and must be referenced by name. A common use of scalar variables is to record information made available by gretl commands for further processing, as in `scalar s2 = $sigma^2` to record the square of the standard error of the regression following an estimation command such as `ols`.

You can define and work with scalars in gretl without having any dataset in place.

In the gretl GUI, scalar variables can be inspected and their values edited via the “Icon view” (see the View menu in the main window).

11.4 Matrices

Matrices in gretl work much as in other mathematical software (e.g. MATLAB, Octave). Like scalars they have no ID numbers and must be referenced by name, and they can be used without any dataset in place. Matrix indexing is 1-based: the top-left element of matrix A is `A[1,1]`. Matrices are discussed at length in chapter 17; advanced users of gretl will want to study this chapter in detail.

Matrices have two optional attribute beyond their numerical content: they may have column and/or row names attached; these are displayed when the matrix is printed. See the `cnameset` and `rnameset` functions for details.

In the gretl GUI, matrices can be inspected, analysed and edited via the Icon view item under the View menu in the main window: each currently defined matrix is represented by an icon.

11.5 Lists

As with matrices, lists merit an explication of their own (see chapter 15). Briefly, named lists can (and should!) be used to make command scripts less verbose and repetitious, and more easily modifiable. Since lists are in fact lists of series ID numbers they can be used only when a dataset is in place.

In the gretl GUI, named lists can be inspected and edited under the Data menu in the main window, via the item Define or edit list.

11.6 Strings

String variables may be used for labeling, or for constructing commands. They are discussed in chapter 15. They must be referenced by name; they can be defined in the absence of a dataset.

Such variables can be created and modified via the command-line in the gretl console or via script; there is no means of editing them via the gretl GUI.

11.7 Bundles

A **bundle** is a container or wrapper for various sorts of objects—primarily scalars, matrices, strings, arrays and bundles. (Yes, a bundle can contain other bundles). Secondly, series and lists can be placed in bundles but this is subject to important qualifications noted below.

A bundle takes the form of a hash table or associative array: each item placed in the bundle is associated with a key which can be used to retrieve it subsequently. We begin by explaining the mechanics of bundles then offer some thoughts on what they are good for.

There are several ways of creating a bundle. Here are the first two:

- Just “declare” it, as in

```
bundle foo
```

- or define an empty bundle using the `defbundle` function without any arguments:

```
bundle foo = defbundle()
```

These formulations are basically equivalent, in that they both create an empty bundle. The difference is that the second variant may be reused—if a bundle named `foo` already exists the effect is to empty it—while the first may only be used once in a given gretl session; it is an error to attempt to declare a variable that already exists.

To create a bundle and add contents in one go, you can use the `defbundle` function with some arguments. For example:

```
bundle foo = defbundle("x", 13, "mat", I(3), "str", "some string")
```

The arguments must be given in pairs—a key followed by the object to be associated with the key—with all terms comma-separated. However, you may prefer to use one or other of the alternative idioms introduced in gretl 2021a. The first of these looks like this:

```
bundle foo = _(x = 13, mat = I(3), str = "some string")
```

It’s more streamlined than `defbundle` but not quite so flexible. You don’t have to quote the keys, but that also means that you can’t give the name of a key as a string variable; it’s always taken as a string literal. Yet more streamlined but also less flexible is this variant:

```
bundle foo = _(x, mat, str)
```

which works if and only if there are existing objects `x`, `mat` and `str` in scope and you want to add them to the bundle under keys equal to their own names.

For more on the `defbundle` function, see the *Gretl Command Reference* or the *Function Reference* under *Help* in the GUI program.

To add an object to a bundle you assign to a compound left-hand value: the name of the bundle followed by the key. Two forms of syntax are acceptable in this context. The recommended syntax (for most uses) is *bundlename.key*; that is, the name of the bundle followed by a dot, then the key. Both the bundle name and the key must be valid gretl identifiers.¹ For example, the statement

```
foo.matrix1 = m
```

¹As a reminder: 31 characters maximum, starting with a letter and composed of just letters, numbers or underscore.

adds an object called `m` (presumably a matrix) to bundle `foo` under the key `matrix1`. If you wish to make it explicit that `m` is supposed to be a matrix you can use the form

```
matrix foo.matrix1 = m
```

Alternatively, a bundle key may be given as a string enclosed in square brackets, as in

```
foo["matrix1"] = m
```

This syntax offers greater flexibility in that the key string does not have to be a valid identifier (for example it can include spaces). In addition, when using the square bracket syntax it is possible to use a string variable to define or access the key in question. For example:

```
string s = "matrix 1"
foo[s] = m # matrix is added under key "matrix 1"
```

To get an item out of a bundle, again use the name of the bundle followed by the key, as in

```
matrix bm = foo.matrix1
# or using the alternative notation
matrix bm = foo["matrix1"]
# or using a string variable
matrix bm = foo[s]
```

Note that the key identifying an object within a given bundle is necessarily unique. If you reuse an existing key in a new assignment, the effect is to replace the object which was previously stored under the given key. In this context it is not required that the type of the replacement object is the same as that of the original.

Also note that when you add an object to a bundle, what in fact happens is that the bundle acquires a *copy* of the object. The external object retains its own identity and is unaffected if the bundled object is replaced by another. Consider the following script fragment:

```
bundle foo
matrix m = I(3)
foo.mykey = m
scalar x = 20
foo.mykey = x
```

After the above commands are completed bundle `foo` does not contain a matrix under `mykey`, but the original matrix `m` is still in good health.

To delete an object from a bundle use the `delete` command, with the bundle/key combination, as in

```
delete foo.mykey
```

This destroys the object associated with `mykey` and removes the key from the hash table.

To determine whether a bundle contains an object associated with a given key, use the `inbundle()` function. This takes two arguments: the name of the bundle and the key string. The value returned by this function is an integer which codes for the type of the object (0 for no match, 1 for scalar, 2 for series, 3 for matrix, 4 for string, 5 for bundle and 6 for array). The function `typestr()` may be used to get the string corresponding to this code. For example:

```
scalar type = inbundle(foo, x)
if type == 0
```

```

    print "x: no such object"
  else
    printf "x is of type %s\n", typestr(type)
  endif

```

Besides adding, accessing, replacing and deleting individual items, the other operations that are supported for bundles are union, printing and deletion. As regards union, if bundles `b1` and `b2` are defined you can say

```
bundle b3 = b1 + b2
```

to create a new bundle that is the union of the two others. The algorithm is: create a new bundle that is a copy of `b1`, then add any items from `b2` whose keys are not already present in the new bundle. (This means that bundle union is not commutative if the bundles have one or more key strings in common.)

If `b` is a bundle and you say `print b`, you get a listing of the bundle's keys along with the types of the corresponding objects, as in

```

? print b
bundle b:
  x (scalar)
  mat (matrix)
  inside (bundle)

```

Note that in the example above the bundle `b` nests a bundle named `inside`. If you want to see what's inside nested bundles (with a single command) you can append the `--tree` option to the print command.

Series and lists as bundle members

It is possible to add both series and lists to a bundle, as in

```

open data4-10
list X = const CATHOL INCOME
bundle b
b.y = ENROLL
b.X = X
eval b.y
eval b.X

```

However, it is important to bear in mind the following limitations.

- A series, as such, is inherently a member of a dataset, and a bundle can “survive” the replacement or destruction of the dataset from which a series was added. It may then be impossible (or, even if possible, meaningless) to extract a bundled series *as a series*. However it's always possible to retrieve the values of the series in the form of a matrix (column vector).
- In gretl commands that call for series arguments you cannot give a bundled series without first extracting it. In the little example above the series `ENROLL` was added to bundle `b` under the key `y`, but `b.y` is not itself a series (member of a dataset), it's just an anonymous array of values. It therefore cannot be given as, say, the dependent variable in a call to gretl's `ols` command.
- A gretl list is just an array of ID numbers of series in a given dataset, a “macro” if you like. So as with series, there's no guarantee that a bundled list can be extracted *as a list* (though it can always be extracted as a row vector).

The points made above are illustrated in Listing 11.1. In “Case 1” we open a little dataset with just 14 cross-sectional observations and put a series into a bundle. We then open a time-series dataset with 64 observations, while preserving the bundle, and extract the bundled series. This instance is *legal*, since the stored series does not overflow the length of the new dataset (it gets written into the first 14 observations), but it’s probably not meaningful. It’s up to the user to decide if such operations make sense.

In “Case 2” a similar sequence of statements leads to an error (trapped by `catch`) because this time the stored series will not fit into the new dataset. We can nonetheless grab the data as a vector.

In “Case 3” we put a list of three series into a bundle. This does not put any actual data values into the bundle, just the ID numbers of the specified series, which happen to be 4, 5 and 6. We then switch to a dataset that contains just 4 series, so the list cannot be extracted as such (IDs 5 and 6 are out of bounds). Once again, however, we can retrieve the ID numbers in matrix form if we want.

In some cases putting a gretl list as such into a bundle may be appropriate, but in others you are better off adding the *content* of the list, in matrix form, as in

```
open data4-10
list X = const CATHOL INCOME
bundle b
matrix b.X = {X}
```

In this case we’re adding a matrix with three columns and as many rows as there are in the dataset; we have the actual data, not just a reference to the data that might “go bad”. See chapter 17 for more on this.

What are bundles good for?

Bundles are unlikely to be of interest in the context of standalone gretl scripts, but they can be very useful in the context of complex function packages where a good deal of information has to be passed around between the component functions (see [Cottrell and Lucchetti, 2016](#)). Instead of using a lengthy list of individual arguments, function *A* can bundle up the required data and pass it to functions *B* and *C*, where relevant information can be extracted via a mnemonic key.

In this context bundles should be passed in “pointer” form (see chapter 14) as illustrated in the following trivial example, where a bundle is created at one level then filled out by a separate function.

```
# modification of bundle (pointer) by user function

function void fill_out_bundle (bundle *b)
  b.mat = I(3)
  b.str = "foo"
  b.x = 32
end function

bundle my_bundle
fill_out_bundle(&my_bundle)
```

The bundle type can also be used to advantage as the *return value* from a packaged function, in cases where a package writer wants to give the user the option of accessing various results. In the gretl GUI, function packages that return a bundle are treated specially: the output window that displays the printed results acquires a menu showing the bundled items (their names and types), from which the user can save items of interest. For example, a function package that estimates a model might return a bundle containing a vector of parameter estimates, a residual series and a covariance matrix for the parameter estimates, among other possibilities.

When offering a bundle as the return value from a function it’s important to keep in mind the limitation noted above, concerning the inclusion of lists in bundles. Once again: a list is just an array of series ID numbers. Consider the following would-be function code.

Listing 11.1: Series and lists in bundles [\[Download ▼\]](#)

```
# Case 1: store and retrieve series, OK?
open data4-1
bundle b
series b.x = sqft
open data9-7 --preserve
series x = b.x
print x --byobs

# Case 2: store and retrieve series: gives an error,
# but the data can be retrieved in matrix form
open data9-7
bundle b
series b.x = QNC
open data4-1 --preserve
catch series x = b.x # wrong, won't fit!
if $error
    matrix mx = b.x
    print mx
else
    print x
endif

# Case 3: store and retrieve list: gives an error,
# but the ID numbers in the list can be retrieved
# as a row vector
open data9-7
list L = PRIME UNEMP STOCK
bundle b
list b.L = L
open data4-1 --preserve
catch list L = b.L
if $error
    matrix mL = b.L
    print mL # prints "4 5 6"
endif
```

```
function bundle bunlist (const series y)
  series y2 = y^2
  series y3 = y^3
  bundle ret
  # don't do this!
  list ret.L = y2 y3
  return ret
end function
```

If the intent is to give the caller a list containing two new series this will *not* work. Suppose that when this function is called, the caller has in place a dataset with two series (besides the built-in `const`), with ID numbers 1 and 2. Then the series `y2` and `y3` will be given IDs 3 and 4, which will be duly recorded in `ret.L`. But these series are local to the function; at caller level there will be no series answering to IDs 3 and 4, and the “list” therefore turns into the useless vector `{3,4}`. If you want to return multiple series your options are (a) return a list *directly*—in which case `gretl` adds the specified series to the caller’s dataset—or (b) turn the list into a a matrix, as in

```
list L = y2 y3
matrix Y = {L}
```

This matrix can be returned in its own right, or can be packed into a bundle if the function is to return something else besides; either way the caller can reconstitute a list using the `mat2list` function.

You might be wondering, if the direct return of a list works as mentioned above, why doesn’t a bundled list work in the same way? That’s basically because of the “encapsulation” policy: functions should not have any unexpected side effects. If a caller assigns the return value of a function that advertises a list return, it should be clear that the caller’s dataset may be modified—it’s all “above board”. If a function that advertises a bundle return value has the side effect of modifying the caller’s dataset, because the bundle happens to contain a list, that would seem to break encapsulation.

For completeness, it’s worth noting that there are cases where a function *can* successfully return a list in a bundle, without breaking encapsulation: the requirement is just that the series IDs in the list are defined at caller level. Listing 11.2 gives an example. A list argument `L` is examined and the return value is a bundle containing a list and a vector. The bundled list includes the IDs of just those series in `L` that are discrete, and the vector gives the number of distinct values for each of these series.

Adding annotations

As a refinement to support the use of bundles as a function return type, the `setnote` function can be used to add a brief explanatory note to a bundled item—such notes will then be shown in the GUI menu. This function takes three arguments: the name of a bundle, a key string, and the note. For example

```
setnote(b, "vcv", "covariance matrix")
```

After this, the object under the key `vcv` in bundle `b` will be shown as “covariance matrix” in a GUI menu.

11.8 Arrays

The `gretl` array type is intended for scripting use. Arrays have no GUI representation and they’re unlikely to acquire one.²

²However, it’s possible to save arrays “invisibly” in the context of a GUI session, by virtue of the fact that they can be packed into bundles (see below), and bundles can be saved as part of a “session”.

Listing 11.2: Returning a list in a bundle [\[Download ▼\]](#)

```

set verbose off

function bundle discrete_check (const list L)
    list dlist
    matrix nvals = {}
    bundle b
    loop i=1..nelem(L)
        b = getinfo(L[i])
        if b.discrete
            dlist += L[i]
            nvals ~= nelem(values(L[i]))
        endif
    endloop
    return _(dlist, nvals)
end function

open mroz87.gdt --quiet
list L = dataset
bundle b = discrete_check(L)
list print b.dlist

```

A gretl array is, as you might expect, a container which can hold zero or more objects of a certain type, indexed by consecutive integers starting at 1. It is one-dimensional. This type is implemented by a quite “generic” back-end. The types of object that can be put into arrays are strings, matrices, lists, bundles and arrays.³

Of gretl’s “primary” types, then, neither scalars nor series are supported by the array mechanism. There would be little point in supporting arrays of scalars as such since the matrix type already plays that role, and more flexibly. As for series, they have a special status as elements of a dataset (which is in a sense an “array of series” already) and in addition we have the list type which already functions as a sort of array for subsets of the series in a dataset.

Creating an array

An array can be brought into existence in any of three ways: bare declaration or using one of the functions `array()` or `defarray()`. In each case one of the specific type-words `strings`, `matrices`, `lists`, `bundles` or `arrays` must be used. Here are some examples:

```

# declare an empty array of strings
strings S
# make an empty array of matrices
matrices M = array(0)
# make an array with space for four bundles
bundles B = array(4)
# make an array with three specified strings
strings P = defarray("foo", "bar", "baz")

```

The “bare declaration” form and the function form with `array(0)` have the same effect of creating an empty array, but the second can be used in contexts where bare declaration is not allowed (and it can also be used to destroy the content of an existing array and reduce it to size zero).

³It was not possible to nest arrays prior to version 2019d of gretl.

The `array()` function expects a non-negative integer argument and can be used to create an array of pre-given size; in this case the elements are initialized appropriately as empty strings, empty matrices, empty lists, empty bundles or empty arrays. The `defarray()` function takes a variable number of arguments (one or more), each of which may be the name of a variable of the appropriate type or an expression which evaluates to an object of the appropriate type.

Setting and getting elements

There are two ways to set the value of an array element: you can set a particular element using the array index, or you can append an element using the `+=` operator:

```
# first case
strings S = array(3)
S[2] = "string the second"
# alternative
matrices M = array(0)
M += mnormal(T,k)
```

In the first method the index must (of course) be within bounds; that is, greater than zero and no greater than the current length of the array. When the second method is used it automatically extends the length of the array by 1.

To get hold of an element, the array index must be used:

```
# for S an array of strings
string s = S[5]
# for M an array of matrices
printf "\n%#12.5g\n", M[1]
```

Removing elements

There's a counterpart to the `+=` operator mentioned above: `-=` can be used to remove one or more elements specified by *content* from an array of strings. Note that `-=` works on all matching elements, so after the following statements

```
strings S = defarray("a", "a", "b", "a")
S -= "a"
```

`S` becomes a one-element array holding only the original third element.

More generally, a negative index can be used to remove a specified element from an array of any type, as in

```
strings S = defarray("a", "a", "b", "a")
S = S[-1]
```

where only the first element is removed. See chapter 17 for more on the semantics of negative indices.

Operations on whole arrays

Three operators are applicable to whole arrays, but only one to arrays of arbitrary type (the other two being restricted to arrays of strings). The generally available operation is appending. You can do, for example

```
# for M1 and M2 both arrays of matrices
matrices BigM = M1 + M2
# or if you wish to augment M1
M1 += M2
```

In each case the result is an array of matrices whose length is the sum of the lengths of M1 and M2—and similarly for the other supported types.

The operators specific to strings are union, via `||`, and intersection, via `&&`. Given the following code, for S1 and S2 both arrays of strings,

```
strings Su = S1 || S2
strings Si = S1 && S2
```

the array Su will contain all the strings in S1 plus any in S2 that are not in S1, while Si will contain all and only the strings that appear in both S1 and S2.

Arrays as function arguments

One can write hansl functions that take as arguments any of the array types, and it is possible to pass arrays as function arguments in “pointerized” form. In addition hansl functions may return any of the array types. Here is a trivial example for strings:

```
function void printstrings (strings *S)
  loop i=1..nelem(S)
    printf "element %d: '%s'\n", i, S[i]
  endloop
end function

function strings mkstrs (int n)
  strings S = array(n)
  loop i=1..n
    S[i] = sprintf("member %d", i)
  endloop
  return S
end function

strings Foo = mkstrs(5)
print Foo
printstrings(&Foo)
```

A couple of points are worth noting here. First, the `nelem()` function works to give the number of elements in any of the “container” types (lists, arrays, bundles, matrices). Second, if you do “print Foo” for Foo an array, you’ll see something like:

```
? print Foo
Array of strings, length 5
```

Nesting arrays

While gretl’s array structure is in itself one-dimensional you can add extra dimensions by nesting. For example, the code below creates an array holding n arrays of m bundles.

```
arrays BB = array(n)
loop i=1..n
  bundles BB[i] = array(m)
endloop
```

The syntax for setting or accessing any of the $n \times m$ bundles (or their members) is then on the following pattern:

```
BB[i][j].m = I(3)
eval BB[i][j]
eval BB[i][j].m # or eval BB[i][j]["m"]
```

where the respective array subscripts are each put into square brackets.

The elements of an array of arrays must (obviously) all be arrays, but it's not required that they have a common content-type. For example, the following code creates an array holding an array of matrices plus an array of strings.

```
arrays AA = array(2)
matrices AA[1] = array(3)
strings AA[2] = array(3)
```

Arrays and bundles

As mentioned, the `bundle` type is supported by the array mechanism. In addition, arrays (of whatever type) can be put into bundles:

```
matrices M = array(8)
# set values of M[i] here...
bundle b
b.M = M
```

The mutual “packability” of bundles and arrays means that it's possible to go quite far down the rabbit-hole... users are advised not to get carried away.

11.9 The life cycle of gretl objects

Creation

The most basic way to create a new variable of any type is by *declaration*, where one states the type followed by the name of the variable to create, as in

```
scalar x
series y
matrix A
```

and so forth. In that case the object in question is given a default initialization, as follows: a new scalar has value NA (missing); a new series is filled with NAs; a new matrix is empty (zero rows and columns); a new string is empty; a new list has no members, new bundles and new arrays are empty.

Declaration can be supplemented by a definite initialization, as in

```
scalar x = pi
series y = log(x)
matrix A = zeros(10,4)
```

The type of a new variable can be left implicit, as in

```
x = y/100
z = 3.5
```

Here the type of `x` will be determined automatically depending on the context. If `y` is a scalar, a series or a matrix `x` will inherit `y`'s type (otherwise an error will be generated, since division is applicable to these types only). The new variable `z` will “naturally” be of scalar type.

In general, however, we recommend that you state the type of a new variable explicitly. This makes the intent clearer to a reader of the script and also guards against errors that might otherwise be difficult to understand (i.e. a certain variable turns out to be of the wrong type for some subsequent calculation, but you don't notice at first because you didn't say what type you wanted). Exceptions to this rule might reasonably be granted for clear and simple cases where there's little possibility of confusion.

Modification

Typically, the values of variables of all types are modified by assignment, using the = operator with the name of the variable on the left and a suitable value or formula on the right:

```
z = normal()
x = 100 * log(y) - log(y(-1))
M = qform(a, X)
```

By a “suitable” value we mean one that is conformable for the type in question. A gretl variable acquires its type when it is first created and this cannot be changed via assignment; for example, if you have a matrix A and later want a string A, you will have to delete the matrix first.

☞ One point to watch out for in gretl scripting is type conflicts having to do with the names of series brought in from a data file. For example, in setting up a command loop (see chapter 13) it is very common to call the loop index *i*. Now a loop index is a scalar (typically incremented each time round the loop). If you open a data file that happens to contain a series named *i* you will get a type error (“Types not conformable for operation”) when you try to use *i* as a loop index.

Although the type of an existing variable cannot be changed on the fly, gretl nonetheless tries to be as “understanding” as possible. For example if *x* is an existing series and you say

```
x = 100
```

gretl will give the series a constant value of 100 rather than complaining that you are trying to assign a scalar to a series. This issue is particularly relevant for the matrix type—see chapter 17 for details.

Besides using the regular assignment operator you also have the option of using an “inflected” equals sign, as in the C programming language. This is shorthand for the case where the new value of the variable is a function of the old value. For example,

```
x += 100 # in longhand: x = x + 100
x *= 100 # in longhand: x = x * 100
```

For scalar variables you can use a more condensed shorthand for simple increment or decrement by 1, namely trailing ++ or -- respectively:

```
x = 100
x--      # x now equals 99
x++      # x now equals 100
```

In the case of objects holding more than one value—series, matrices and bundles—you can modify particular values within the object using an expression within square brackets to identify the elements to access. We have discussed this above for the bundle type and chapter 17 goes into details for matrices. As for series, there are two ways to specify particular values for modification: you can use a simple 1-based index, or if the dataset is a time series or panel (or if it has marker strings that identify the observations) you can use an appropriate observation string. Such strings are displayed by gretl when you print data with the --byobs flag. Examples:

```
x[13]      = 100 # simple index: the 13th observation
x[1995:4]  = 100 # date: quarterly time series
x[2003:08] = 100 # date: monthly time series
x["AZ"]    = 100 # the observation with marker string "AZ"
x[3:15]    = 100 # panel: the 15th observation for the 3rd unit
```

Note that with quarterly or monthly time series there is no ambiguity between a simple index number and a date, since dates always contain a colon. With annual time-series data, however, such ambiguity exists and it is resolved by the rule that a number in brackets is always read as a simple index: `x[1905]` means the nineteen-hundred and fifth observation, *not* the observation for the year 1905. You can specify a year by quotation, as in `x["1905"]`.

Destruction

Objects of the types discussed above, *with the important exception of named lists*, are all destroyed using the `delete` command: `delete objectname`.

Lists are an exception for this reason: in the context of gretl commands, a named list expands to the ID numbers of the member series, so if you say

```
delete L
```

for `L` a list, the effect is to delete all the series in `L`; the list itself is not destroyed, but ends up empty. To delete the list itself (without deleting the member series) you must invert the command and use the `list` keyword:

```
list L delete
```

Note that the `delete` command cannot be used within a `loop` construct (see chapter [13](#)).

Chapter 12

Discrete variables

When a variable can take only a finite, typically small, number of values, then it is said to be *discrete*. In gretl, variables of the series type (only) can be marked as discrete. (When we speak of “variables” below this should be understood as referring to series.) Some gretl commands act in a slightly different way when applied to discrete variables; moreover, gretl provides a few commands that only apply to discrete variables. Specifically, the `dummify` and `xtab` commands (see below) are available only for discrete variables, while the `freq` (frequency distribution) command produces different output for discrete variables.

12.1 Declaring variables as discrete

Gretl uses a simple heuristic to judge whether a given variable should be treated as discrete, but you also have the option of explicitly marking a variable as discrete, in which case the heuristic check is bypassed.

The heuristic is as follows: First, are all the values of the variable “reasonably round”, where this is taken to mean that they are all integer multiples of 0.25? If this criterion is met, we then ask whether the variable takes on a “fairly small” set of distinct values, where “fairly small” is defined as less than or equal to 8. If both conditions are satisfied, the variable is automatically considered discrete.

To mark a variable as discrete you have two options.

1. From the graphical interface, select “Variable, Edit Attributes” from the menu. A dialog box will appear and, if the variable seems suitable, you will see a tick box labeled “Treat this variable as discrete”. This dialog box can also be invoked via the context menu (right-click on a variable) or by pressing the F2 key.
2. From the command-line interface, via the `discrete` command. The command takes one or more arguments, which can be either variables or list of variables. For example:

```
list xlist = x1 x2 x3
discrete z1 xlist z2
```

This syntax makes it possible to declare as discrete many variables at once, which cannot presently be done via the graphical interface. The switch `--reverse` reverses the declaration of a variable as discrete, or in other words marks it as continuous. For example:

```
discrete foo
# now foo is discrete
discrete foo --reverse
# now foo is continuous
```

The command-line variant is more powerful, in that you can mark a variable as discrete even if it does not seem to be suitable for this treatment.

Note that marking a variable as discrete does not affect its content. It is the user’s responsibility to make sure that marking a variable as discrete is a sensible thing to do. Note that if you want to recode a continuous variable into classes, you can use gretl’s arithmetical functionality, as in the following example:

```

nulldata 100
# generate a series with mean 2 and variance 1
series x = normal() + 2
# split into 4 classes
series z = (x>0) + (x>2) + (x>4)
# now declare z as discrete
discrete z

```

Once a variable is marked as discrete, this setting is remembered when you save the data file.

12.2 Commands for discrete variables

The **dummify** command

The **dummify** command takes as argument a series x and creates dummy variables for each distinct value present in x , which must have already been declared as discrete. Example:

```

open greene22_2
discrete Z5 # mark Z5 as discrete
dummify Z5

```

The effect of the above command is to generate 5 new dummy variables, labeled DZ5_1 through DZ5_5, which correspond to the different values in Z5. Hence, the variable DZ5_4 is 1 if Z5 equals 4 and 0 otherwise. This functionality is also available through the graphical interface by selecting the menu item “Add, Dummies for selected discrete variables”.

The **dummify** command can also be used with the following syntax:

```
list dlist = dummify(x)
```

This not only creates the dummy variables, but also a named list (see section 15.1) that can be used afterwards. The following example computes summary statistics for the variable Y for each value of $Z5$:

```

open greene22_2
discrete Z5 # mark Z5 as discrete
list foo = dummify(Z5)
loop foreach i foo
  smpl $i --restrict --replace
  summary Y
endloop
smpl --full

```

Since **dummify** generates a list, it can be used directly in commands that call for a list as input, such as **ols**. For example:

```

open greene22_2
discrete Z5 # mark Z5 as discrete
ols Y 0 dummify(Z5)

```

The **freq** command

The **freq** command displays absolute and relative frequencies for a given variable. The way frequencies are counted depends on whether the variable is continuous or discrete. This command is also available via the graphical interface by selecting the “Variable, Frequency distribution” menu entry.

For discrete variables, frequencies are counted for each distinct value that the variable takes. For continuous variables, values are grouped into “bins” and then the frequencies are counted for each bin. The number of bins, by default, is computed as a function of the number of valid observations in the currently selected sample via the rule shown in Table 12.1. However, when the command is invoked through the menu item “Variable, Frequency Plot”, this default can be overridden by the user.

Observations	Bins
$8 \leq n < 16$	5
$16 \leq n < 50$	7
$50 \leq n \leq 850$	$\lceil \sqrt{n} \rceil$
$n > 850$	29

Table 12.1: Number of bins for various sample sizes

For example, the following code

```
open greene19_1
freq TUCE
discrete TUCE # mark TUCE as discrete
freq TUCE
```

yields

```
Read datafile /usr/local/share/gretl/data/greene/greene19_1.gdt
periodicity: 1, maxobs: 32,
observations range: 1-32
```

Listing 5 variables:

```
0) const    1) GPA        2) TUCE        3) PSI        4) GRADE
```

```
? freq TUCE
```

```
Frequency distribution for TUCE, obs 1-32
number of bins = 7, mean = 21.9375, sd = 3.90151
```

interval	midpt	frequency	rel.	cum.
< 13.417	12.000	1	3.12%	3.12% *
13.417 - 16.250	14.833	1	3.12%	6.25% *
16.250 - 19.083	17.667	6	18.75%	25.00% *****
19.083 - 21.917	20.500	6	18.75%	43.75% *****
21.917 - 24.750	23.333	9	28.12%	71.88% *****
24.750 - 27.583	26.167	7	21.88%	93.75% *****
>= 27.583	29.000	2	6.25%	100.00% **

```
Test for null hypothesis of normal distribution:
```

```
Chi-square(2) = 1.872 with p-value 0.39211
```

```
? discrete TUCE # mark TUCE as discrete
```

```
? freq TUCE
```

```
Frequency distribution for TUCE, obs 1-32
```

frequency	rel.	cum.
12	1	3.12% *
14	1	3.12% *
17	3	9.38% ***

19	3	9.38%	25.00%	***
20	2	6.25%	31.25%	**
21	4	12.50%	43.75%	*****
22	2	6.25%	50.00%	**
23	4	12.50%	62.50%	*****
24	3	9.38%	71.88%	***
25	4	12.50%	84.38%	*****
26	2	6.25%	90.62%	**
27	1	3.12%	93.75%	*
28	1	3.12%	96.88%	*
29	1	3.12%	100.00%	*

Test for null hypothesis of normal distribution:
Chi-square(2) = 1.872 with p-value 0.39211

As can be seen from the sample output, a Doornik-Hansen test for normality is computed automatically. This test is suppressed for discrete variables where the number of distinct values is less than 10.

This command accepts two options: `--quiet`, to avoid generation of the histogram when invoked from the command line and `--gamma`, for replacing the normality test with Locke's nonparametric test, whose null hypothesis is that the data follow a Gamma distribution.

If the distinct values of a discrete variable need to be saved, the `values()` matrix construct can be used (see chapter 17).

The `xtab` command

The `xtab` command can be invoked in either of the following ways. First,

```
xtab ylist ; xlist
```

where `ylist` and `xlist` are lists of discrete variables. This produces cross-tabulations (two-way frequencies) of each of the variables in `ylist` (by row) against each of the variables in `xlist` (by column). Or second,

```
xtab xlist
```

In the second case a full set of cross-tabulations is generated; that is, each variable in `xlist` is tabulated against each other variable in the list. In the graphical interface, this command is represented by the "Cross Tabulation" item under the View menu, which is active if at least two variables are selected.

Here is an example of use:

```
open greene22_2
discrete Z* # mark Z1-Z8 as discrete
xtab Z1 Z4 ; Z5 Z6
```

which produces

Cross-tabulation of Z1 (rows) against Z5 (columns)

	[1]	[2]	[3]	[4]	[5]	TOT.
[0]	20	91	75	93	36	315
[1]	28	73	54	97	34	286
TOTAL	48	164	129	190	70	601

Pearson chi-square test = 5.48233 (4 df, p-value = 0.241287)

Cross-tabulation of Z1 (rows) against Z6 (columns)

	[9][12][14][16][17][18][20]	TOT.
[0]	4 36 106 70 52 45 2	315
[1]	3 8 48 45 37 67 78	286
TOTAL	7 44 154 115 89 112 80	601

Pearson chi-square test = 123.177 (6 df, p-value = 3.50375e-24)

Cross-tabulation of Z4 (rows) against Z5 (columns)

	[1][2][3][4][5]	TOT.
[0]	17 60 35 45 14	171
[1]	31 104 94 145 56	430
TOTAL	48 164 129 190 70	601

Pearson chi-square test = 11.1615 (4 df, p-value = 0.0248074)

Cross-tabulation of Z4 (rows) against Z6 (columns)

	[9][12][14][16][17][18][20]	TOT.
[0]	1 8 39 47 30 32 14	171
[1]	6 36 115 68 59 80 66	430
TOTAL	7 44 154 115 89 112 80	601

Pearson chi-square test = 18.3426 (6 df, p-value = 0.0054306)

Pearson's χ^2 test for independence is automatically displayed, provided that all cells have expected frequencies under independence greater than 10^{-7} . However, a common rule of thumb states that this statistic is valid only if the expected frequency is 5 or greater for at least 80 percent of the cells. If this condition is not met a warning is printed.

Additionally, the `--row` or `--column` options can be given: in this case, the output displays row or column percentages, respectively.

If you want to cut and paste the output of `xtab` to some other program, e.g. a spreadsheet, you may want to use the `--zeros` option; this option causes cells with zero frequency to display the number 0 instead of being empty.

Chapter 13

Loop constructs

13.1 Introduction

The command `loop` opens a special mode in which `gretl` accepts a block of commands to be repeated zero or more times. This feature may be useful for, among other things, Monte Carlo simulations, bootstrapping of test statistics and iterative estimation procedures. The general form of a loop is:

```
loop control-expression [ --progressive | --verbose ]
    loop body
endloop
```

Five forms of control-expression are available, as explained in section 13.2.

Not all `gretl` commands are available within loops; the commands that are not presently accepted in this context are shown in Table 13.1.

Table 13.1: Commands not usable in loops

`function` `include` `nulldata` `quit` `run` `setmiss`

By default, the `genr` command operates quietly in the context of a loop (without printing information on the variable generated). To force the printing of feedback you may specify the `--verbose` option to `loop`.

The `--progressive` option to `loop` modifies the behavior of the commands `print` and `store`, and certain estimation commands, in a manner that may be useful with Monte Carlo analyses (see Section 13.4).

The following sections explain the various forms of the loop control expression and provide some examples of use of loops.

☞ If you are carrying out a substantial Monte Carlo analysis with many thousands of repetitions, memory capacity and processing time may be an issue. To minimize the use of computer resources, run your script using the command-line program, `gretlcli`, with output redirected to a file.

13.2 Loop control variants

Count loop

The simplest form of loop control is a direct specification of the number of times the loop should be repeated. We refer to this as a “count loop”. The number of repetitions may be a numerical constant, as in `loop 1000`, or may be read from a scalar variable, as in `loop replics`.

In the case where the loop count is given by a variable, say `replics`, in concept `replics` is an integer; if the value is not integral, it is converted to an integer by truncation. Note that `replics` is evaluated only once, when the loop is initially compiled.

While loop

A second sort of control expression takes the form of the keyword `while` followed by a Boolean expression. For example,

```
loop while essdiff > .00001
```

Execution of the commands within the loop will continue so long as (a) the specified condition evaluates as true and (b) the number of iterations does not exceed the value of the internal variable `loop_maxiter`. By default this equals 100000, but you can specify a different value (or remove the limit) via the `set` command (see the *Gretl Command Reference*).

Index loop

A third form of loop control uses an index variable, for example `i`.¹ In this case you specify starting and ending values for the index, as in `loop i=1..20`.

The index variable may be a pre-existing scalar; if this is not the case, the variable is created automatically and is destroyed on exit from the loop.

The index may be used within the loop body in either of two ways: you can access the integer value of `i` or you can use its string representation, `$i`.

The starting and ending values for the index can be given in numerical form, by reference to pre-defined scalar variables, or as expressions that evaluate to scalars. In the latter two cases the variables are evaluated once, at the start of the loop. In addition, with time series data you can give the starting and ending values in the form of dates, as in `loop i=1950:1..1999:4` for quarterly data.

This form of loop control is intended to be quick and easy, and as such it is subject to certain limitations. In particular, standard behavior is to increment the index variable by one at each iteration. So, for example, if you have

```
loop i=m..n
```

where `m` and `n` are scalar variables with values $m > n$ at the time of execution, the index will not be decremented; rather, the loop will simply be bypassed.

One modification of this behavior is supported, via the option flag `--decr` (or `-d` for short). This causes the index to be decremented by one at each iteration. For example,

```
loop i=m..n --decr
```

In this case the loop will be bypassed if $m < n$. If you need more flexible control, see the “for” form below.

The index loop is particularly useful in conjunction with the `values()` matrix function when some operation must be carried out for each value of some discrete variable (see chapter 12). Consider the following example:

```
open greene22_2
discrete Z8
v8 = values(Z8)
loop i=1..rows(v8)
  scalar xi = v8[i]
  smpl Z8==xi --restrict --replace
  printf "mean(Y | Z8 = %g) = %8.5f, sd(Y | Z8 = %g) = %g\n", \
    xi, mean(Y), xi, sd(Y)
endloop
```

¹It is common programming practice to use simple, one-character names for such variables.

In this case, we evaluate the conditional mean and standard deviation of the variable *Y* for each value of *Z8*.

Foreach loop

The fourth form of loop control also uses an index variable, in this case to index a specified set of strings. The loop is executed once for each string in the list. This can be useful for performing repetitive operations on a list of variables. Here is an example of the syntax:

```
loop foreach i peach pear plum
  print "$i"
endloop
```

This loop will execute three times, printing out “peach”, “pear” and “plum” on the respective iterations. The numerical value of the index starts at 1 and is incremented by 1 at each iteration.

If you wish to loop across a list of variables that are contiguous in the dataset, you can give the names of the first and last variables in the list, separated by “..”, rather than having to type all the names. For example, say we have 50 variables *AK*, *AL*, ..., *WY*, containing income levels for the states of the US. To run a regression of income on time for each of the states we could do:

```
genr time
loop foreach i AL..WY
  ols $i const time
endloop
```

This loop variant can also be used for looping across the elements in a *named list* (see chapter 15). For example:

```
list ylist = y1 y2 y3
loop foreach i ylist
  ols $i const x1 x2
endloop
```

Note that if you use this idiom inside a function (see chapter 14), looping across a list that has been supplied to the function as an argument, it is necessary to use the syntax *listname.\$i* to reference the list-member variables. In the context of the example above, this would mean replacing the third line with

```
ols ylist.$i const x1 x2
```

Two other cases are supported: the target of *foreach* can be a named array of strings or a bundle (see chapter 11). In the array case, *\$i* gets (naturally) the string at position *i* in the array, from 1 to the number of elements; in the bundle case it gets the key-strings of all bundle members (in no particular order). For a bundle *b*, the command “*print b*” gives a fairly terse account of the bundle’s membership; for a full account you can do:

```
loop foreach i b
  print "$i:"
  eval b["$i"]
endloop
```

For loop

The final form of loop control emulates the *for* statement in the C programming language. The syntax is *loop for*, followed by three component expressions, separated by semicolons and surrounded by parentheses. The three components are as follows:

1. Initialization: This is evaluated only once, at the start of the loop. Common example: setting a scalar control variable to some starting value.
2. Continuation condition: this is evaluated at the top of each iteration (including the first). If the expression evaluates as true (non-zero), iteration continues, otherwise it stops. Common example: an inequality expressing a bound on a control variable.
3. Modifier: an expression which modifies the value of some variable. This is evaluated prior to checking the continuation condition, on each iteration after the first. Common example: a control variable is incremented or decremented.

Here's a simple example:

```
loop for (r=0.01; r<.991; r+=.01)
```

In this example the variable `r` will take on the values 0.01, 0.02, ..., 0.99 across the 99 iterations. Note that due to the finite precision of floating point arithmetic on computers it may be necessary to use a continuation condition such as the above, `r<.991`, rather than the more “natural” `r<=.99`. (Using double-precision numbers on an x86 processor, at the point where you would expect `r` to equal 0.99 it may in fact have value 0.9900000000000001.)

Any or all of the three expressions governing a `for` loop may be omitted—the minimal form is `(; ;)`. If the continuation test is omitted it is implicitly true, so you have an infinite loop unless you arrange for some other way out, such as a `break` statement (see section 13.3 below).

If the initialization expression in a `for` loop takes the common form of setting a scalar variable to a given value, the string representation of that scalar's value is made available within the loop via the accessor `$varname`.

13.3 Special controls

Besides the control afforded by the governing expression at the top of a loop, the flow of execution can be adjusted via the keywords `break` and `continue`.

The `break` keyword terminates execution of the current loop immediately, while `continue` has the effect of skipping any subsequent statements within the loop on the current iteration; execution will proceed to the next iteration if the condition for continuation is still satisfied.

13.4 Progressive mode

If the `--progressive` option is given for a command loop, special behavior is invoked for certain commands, namely, `print`, `store` and simple estimation commands. By “simple” here we mean commands which (a) estimate a single equation (as opposed to a system of equations) and (b) do so by means of a single command statement (as opposed to a block of statements, as with `nls` and `mle`). The paradigm is `ols`; other possibilities include `tsls`, `wls`, `logit` and so on.

The special behavior is as follows.

Estimators: The results from each individual iteration of the estimator are not printed. Instead, after the loop is completed you get a printout of (a) the mean value of each estimated coefficient across all the repetitions, (b) the standard deviation of those coefficient estimates, (c) the mean value of the estimated standard error for each coefficient, and (d) the standard deviation of the estimated standard errors. Note that this is useful only if there is some random input at each step.

print: When this command is used to print the value of a variable, its value is not printed each time round the loop. Rather, when the loop is terminated you get a printout of the mean and standard deviation of the variable, across the repetitions of the loop. This mode is intended for use

with variables that have a scalar value at each iteration, for example the sum of squared residuals from a regression. Series cannot be printed in this way, and neither can matrices.

store: This command writes out the values of the specified scalars, from each time round the loop, to a specified file. Thus it keeps a complete record of their values across the iterations. For example, coefficient estimates could be saved in this way so as to permit subsequent examination of their frequency distribution. Only one such **store** can be used in a given loop.

13.5 Loop examples

Monte Carlo example

A simple example of a Monte Carlo loop in “progressive” mode is shown in Listing 13.1.

Listing 13.1: Simple Monte Carlo loop [\[Download ▼\]](#)

```

nulldata 50
set seed 547
series x = 100 * uniform()
# open a "progressive" loop, to be repeated 100 times
loop 100 --progressive
    series u = 10 * normal()
    # construct the dependent variable
    series y = 10*x + u
    # run OLS regression
    ols y const x
    # grab the coefficient estimates and R-squared
    scalar a = $coeff(const)
    scalar b = $coeff(x)
    scalar r2 = $rsq
    # arrange for printing of stats on these
    print a b r2
    # and save the coefficients to file
    store coeffs.gdt a b
endloop

```

This loop will print out summary statistics for the *a* and *b* estimates and R^2 across the 100 repetitions. After running the loop, `coeffs.gdt`, which contains the individual coefficient estimates from all the runs, can be opened in `gretl` to examine the frequency distribution of the estimates in detail.

The `nulldata` command is useful for Monte Carlo work. Instead of opening a “real” data set, `nulldata 50` (for instance) creates an artificial dataset, containing just a constant and an index variable, with 50 observations. Constructed variables can then be added. See the `set` command for information on generating repeatable pseudo-random series.

Iterated least squares

Listing 13.2 uses a “while” loop to replicate the estimation of a nonlinear consumption function of the form

$$C = \alpha + \beta Y^\gamma + \epsilon$$

as presented in [Greene \(2000\)](#), Example 11.3. This script is included in the `gretl` distribution under the name `greene11_3.inp`; you can find it in `gretl` under the menu item “File, Script files, Example scripts, Greene...”.

The option `--print-final` for the `ols` command arranges matters so that the regression results will not be printed each time round the loop, but the results from the regression on the last iteration will be printed when the loop terminates.

Listing 13.2: Nonlinear consumption function [\[Download ▼\]](#)

```
open greenell_3.gdt
# run initial OLS
ols C 0 Y
scalar essbak = $ess
scalar essdiff = 1
scalar beta = $coeff(Y)
scalar gamma = 1

# iterate OLS till the error sum of squares converges
loop while essdiff > .00001
    # form the linearized variables
    series C0 = C + gamma * beta * Y^gamma * log(Y)
    series x1 = Y^gamma
    series x2 = beta * Y^gamma * log(Y)
    # run OLS
    ols C0 0 x1 x2 --print-final --no-df-corr --vcv
    beta = $coeff[2]
    gamma = $coeff[3]
    ess = $ess
    essdiff = abs(ess - essbak)/essbak
    essbak = ess
endloop

# print parameter estimates using their "proper names"
printf "alpha = %g\n", $coeff[1]
printf "beta = %g\n", beta
printf "gamma = %g\n", gamma
```

Listing 13.3 shows how a loop can be used to estimate an ARMA model, exploiting the “outer product of the gradient” (OPG) regression discussed by [Davidson and MacKinnon \(1993\)](#).

Further examples of `loop` usage that may be of interest can be found in chapter 21.

Listing 13.3: ARMA 1, 1 [\[Download ▼\]](#)

```

# Estimation of an ARMA(1,1) model "manually", using a loop

open arma.gdt

scalar c = 0
scalar a = 0.1
scalar m = 0.1

series e = 0.0
series de_c = e
series de_a = e
series de_m = e

scalar crit = 1

loop while crit > 1.0e-9
    # one-step forecast errors
    e = y - c - a*y(-1) - m*e(-1)

    # log-likelihood
    scalar loglik = -0.5 * sum(e^2)
    print loglik

    # partials of e with respect to c, a, and m
    de_c = -1 - m * de_c(-1)
    de_a = -y(-1) -m * de_a(-1)
    de_m = -e(-1) -m * de_m(-1)

    # partials of l with respect to c, a and m
    series sc_c = -de_c * e
    series sc_a = -de_a * e
    series sc_m = -de_m * e

    # OPG regression
    ols const sc_c sc_a sc_m --print-final --no-df-corr --vcv

    # Update the parameters
    c += $coeff[1]
    a += $coeff[2]
    m += $coeff[3]

    # show progress
    printf "  constant          = %.8g (gradient %#.6g)\n", c, $coeff[1]
    printf "  ar1 coefficient = %.8g (gradient %#.6g)\n", a, $coeff[2]
    printf "  ma1 coefficient = %.8g (gradient %#.6g)\n", m, $coeff[3]

    crit = $T - $ess
    print crit
endloop

scalar se_c = $stderr[1]
scalar se_a = $stderr[2]
scalar se_m = $stderr[3]

printf "\n"
printf "constant          = %.8g (se = %#.6g, t = %.4f)\n", c, se_c, c/se_c
printf "ar1 coefficient = %.8g (se = %#.6g, t = %.4f)\n", a, se_a, a/se_a
printf "ma1 coefficient = %.8g (se = %#.6g, t = %.4f)\n", m, se_m, m/se_m

```

Chapter 14

User-defined functions

14.1 Defining a function

Gretl offers a mechanism for defining functions, which may be called via the command line, in the context of a script, or (if packaged appropriately, see section 14.5) via the program's graphical interface.

The syntax for defining a function looks like this:

```
function type funcname (parameters)
    function body
end function
```

The opening line of a function definition contains these elements, in strict order:

1. The keyword `function`.
2. *type*, which states the type of value returned by the function, if any. This must be one of `void` (if the function does not return anything), `scalar`, `series`, `matrix`, `list`, `string`, `bundle` or one of gretl's array types, `matrices`, `bundles`, `strings` (see section 11.8).
3. *funcname*, the unique identifier for the function. Function names have a maximum length of 31 characters; they must start with a letter and can contain only letters, numerals and the underscore character. You will get an error if you try to define a function having the same name as an existing gretl command.
4. The function's *parameters*, in the form of a comma-separated list enclosed in parentheses. This may be run into the function name, or separated by white space as shown. In case the function takes no arguments (unusual, but acceptable) this should be indicated by placing the keyword `void` between the parameter-list parentheses.

Function parameters can be of any of the types shown below.¹

Type	Description
<code>bool</code>	scalar variable acting as a Boolean switch
<code>int</code>	scalar variable acting as an integer
<code>scalar</code>	scalar variable
<code>series</code>	data series
<code>list</code>	named list of series
<code>matrix</code>	matrix or vector
<code>string</code>	string variable or string literal
<code>bundle</code>	all-purpose container (see section 11.7)
<code>matrices</code>	array of matrices (see section 11.8)
<code>bundles</code>	array of bundles
<code>strings</code>	array of strings

¹An additional parameter type is available for GUI use, namely `obs`; this is equivalent to `int` except for the way it is represented in the graphical interface for calling a function.

Each element in the listing of parameters must include two terms: a type specifier, and the name by which the parameter shall be known within the function. An example follows:

```
function scalar myfunc (series y, list xvars, bool verbose)
```

Each of the type-specifiers, with the exception of `list` and `string`, may be modified by prepending an asterisk to the associated parameter name, as in

```
function scalar myfunc (series *y, scalar *b)
```

The meaning of this modification is explained below (see section 14.4); it is related to the use of pointer arguments in the C programming language.

Function parameters: optional refinements

Besides the required elements mentioned above, the specification of a function parameter may include some additional fields, as follows:

- The `const` modifier.
- For `scalar` or `int` parameters: minimum, maximum and/or default values; or for `bool` parameters, just a default value. And in addition for `scalar` parameters, a step size.
- For optional arguments other than `scalar`, `int` and `bool`, the special default value `null`.
- For all parameters, a descriptive string.
- For `int` parameters with minimum and maximum values specified, a set of strings to associate with the allowed numerical values (that is, value labels).

The first three of these options may be useful in many contexts; the last two may be helpful if a function is to be packaged for use in the `gretl` GUI (but probably not otherwise). We now expand on each of the options.

- The `const` modifier: must be given as a prefix to the basic parameter specification, as in

```
const matrix M
```

This constitutes a promise that the corresponding argument will not be modified within the function; `gretl` will flag an error if the function attempts to modify the argument.

- Minimum, maximum and default values for `scalar` or `int` types: These values should directly follow the name of the parameter, enclosed in square brackets and with the individual elements separated by colons. For example, suppose we have an integer parameter `order` for which we wish to specify a minimum of 1, a maximum of 12, and a default of 4. We can write

```
int order[1:12:4]
```

If you wish to omit any of the three specifiers, leave the corresponding field empty. For example `[1: :4]` would specify a minimum of 1 and a default of 4 while leaving the maximum unlimited. However, as a special case, it is acceptable to give just one value, with no colons, in which case the value is interpreted as a default. So for example

```
int k[0]
```

designates a default value of 0 for the parameter `k`, with no minimum or maximum specified. If you wished to specify a minimum of zero with no maximum or default you would have to write

```
int k[0::]
```

For a parameter of type `bool` (whose values are just zero or non-zero), you can specify a default of 1 (true) or 0 (false), as in

```
bool verbose[0]
```

- **Descriptive string:** This will show up as an aid to the user if the function is packaged (see section 14.5 below) and called via gretl's graphical interface. The string should be enclosed in double quotes and separated from the preceding elements of the parameter specification with a space, as in

```
series y "dependent variable"
```

- **Value labels:** These may be used only with `int` parameters for which minimum and maximum values have been specified (so that there is a fixed number of admissible values) and the number of labels must match the number of values. They will show up in the graphical interface in the form of a drop-down list, making the function writer's intent clearer when an integer argument represents a categorical selection. A set of value labels must be enclosed in braces, and the individual labels must be enclosed in double quotes and separated by commas or spaces. For example:

```
int case[1:3:1] {"Fixed effects", "Between model", "Random effects"}
```

- **Step size:** This is only supported only for real-valued scalar parameters. It is relevant only in the graphical interface, and must be combined with specification of minimum, maximum and default values. The effect is that the argument selector takes the form of a “spin button”: clicking on the up- or down-buttons in the selector changes the value by the specified step. Otherwise the selector for such a parameter simply appears as an entry box into which a number should be typed. For example, the following could be used to stipulate that a scalar argument should have a minimum of 1, a maximum of 10, a default of 4 and a step size of 0.1:

```
scalar x[1:10:4:0.1]
```

If two or more of the trailing optional fields are given in a parameter specification, they must be given in the order shown above: min/max/default, description, value labels. Note that there is no facility for “escaping” characters within descriptive strings or value labels; these may contain spaces but they cannot contain the double-quote character.

Here is an example of a well-formed function specification using all the elements mentioned above:

```
function matrix myfunc (series y "dependent variable",
                        list X "regressors",
                        int p[0::1] "lag order",
                        int c[1:2:1] "criterion" {"AIC", "BIC"},
                        bool quiet[0])
```

One advantage of specifying default values for parameters, where applicable, is that in script or command-line mode users may omit trailing arguments that have defaults. For example, `myfunc` above could be invoked with just two arguments, corresponding to `y` and `X`; implicitly `p = 1`, `c = 1` and `quiet` is false.

Functions taking no parameters

You may define a function that has no parameters (these are called “routines” in some programming languages). In this case, use the keyword `void` in place of the listing of parameters:

```
function matrix myfunc2 (void)
```

The function body

The *function body* is composed of gretl commands, or calls to user-defined functions (that is, function calls may be nested). A function may call itself (that is, functions may be recursive). While the function body may contain function calls, it may not contain function definitions. That is, you cannot define a function inside another function. For further details, see section [14.4](#).

14.2 Calling a function

A user function is called by typing its name followed by zero or more arguments enclosed in parentheses. If there are two or more arguments they must be separated by commas.

There are automatic checks in place to ensure that the number of arguments given in a function call matches the number of parameters, and that the types of the given arguments match the types specified in the definition of the function. An error is flagged if either of these conditions is violated. One qualification: allowance is made for omitting arguments at the end of the list, provided that default values are specified in the function definition. To be precise, the check is that the number of arguments is at least equal to the number of *required* parameters, and is no greater than the total number of parameters.

In general, an argument to a function may be given either as the name of a pre-existing variable or as an expression which evaluates to a variable of the appropriate type.

The following trivial example illustrates a function call that correctly matches the corresponding function definition.

```
# function definition
function scalar ols_ess (series y, list xvars)
  ols y 0 xvars --quiet
  printf "ESS = %g\n", $ess
  return $ess
end function

# main script
open data4-1
list xlist = 2 3 4
# function call (the return value is ignored here)
ols_ess(price, xlist)
```

The function call gives two arguments: the first is a data series specified by name and the second is a named list of regressors. Note that while the function offers the Error Sum of Squares as a return value, it is ignored by the caller in this instance. (As a side note here, if you want a function to calculate some value having to do with a regression, but are not interested in the full results of the regression, you may wish to use the `--quiet` flag with the estimation command as shown above.)

A second example shows how to write a function call that assigns a return value to a variable in the caller:

```
# function definition
function series get_uhat (series y, list xvars)
  ols y 0 xvars --quiet
  return $uhat
end function

# main script
open data4-1
list xlist = 2 3 4
# function call
series resid = get_uhat(price, xlist)
```

14.3 Deleting a function

If you have defined a function and subsequently wish to clear it out of memory, you can do so using the keywords `delete` or `clear`, as in

```
function myfunc delete
function get_uhat clear
```

Note, however, that if `myfunc` is already a defined function, providing a new definition automatically overwrites the previous one, so it should rarely be necessary to delete functions explicitly.

14.4 Function programming details

Variables versus pointers

Most arguments to functions can be passed in two ways: “as they are”, or via pointers (the exception is the list type, which cannot be passed as a pointer). First consider the following rather artificial example:

```
function series triple1 (series x)
    return 3*x
end function

function void triple2 (series *x)
    x *= 3
end function

nulldata 10
series y = normal()
series y3 = triple1(y)
print y3
triple2(&y)
print y
```

These two functions produce essentially the same result—the two `print` statements in the caller will show the same values—but in quite different ways. The first explicitly returns a modified version of its input (which must be a plain series): after the call to `triple1`, `y` is unaltered; it would have been altered only if the return value were assigned back to `y` rather than `y3`. The second function modifies its input (given as a pointer to a series) in place without actually *returning* anything.

It’s worth noting that `triple2` as it stands would *not* be considered idiomatic as a `gretl` function (although it’s formally OK). The point here is just to illustrate the distinction between passing an argument in the default way and in pointer form.

Why make this distinction? There are two main reasons for doing so: modularity and performance.

By modularity we mean the insulation of a function from the rest of the script which calls it. One of the many benefits of this approach is that your functions are easily reusable in other contexts. To achieve modularity, *variables created within a function are local to that function, and are destroyed when the function exits*, unless they are made available as return values and these values are “picked up” or assigned by the caller. In addition, functions do not have access to variables in “outer scope” (that is, variables that exist in the script from which the function is called) except insofar as these are explicitly passed to the function as arguments.

By default, when a variable is passed to a function as an argument, what the function actually “gets” is a *copy* of the outer variable, which means that the value of the outer variable is not modified by anything that goes on inside the function. This means that you can pass arguments to a function

without worrying about possible side effects; at the same time the function writer can use argument variables as workspace without fear of disruptive effects at the level of the caller.

The use of pointers, however, allows a function and its caller to cooperate such that an outer variable *can* be modified by the function. In effect, this allows a function to “return” more than one value (although only one variable can be returned directly—see below). To indicate that a particular object is to be passed as a pointer, the parameter in question is marked with a prefix of `*` in the function definition, and the corresponding argument is marked with the complementary prefix `&` in the caller. For example,

```
function series get_uhat_and_ess(series y, list xvars, scalar *ess)
  ols y 0 xvars --quiet
  ess = $ess
  series uh = $uhat
  return uh
end function

open data4-1
list xlist = 2 3 4
scalar SSR
series resid = get_uhat_and_ess(price, xlist, &SSR)
```

In the above, we may say that the function is given the *address* of the scalar variable `SSR`, and it assigns a value to that variable (under the local name `ess`). (For anyone used to programming in C: note that it is not necessary, or even possible, to “dereference” the variable in question within the function using the `*` operator. Unadorned use of the name of the variable is sufficient to access the variable in outer scope.)

An “address” parameter of this sort can be used as a means of offering optional information to the caller. (That is, the corresponding argument is not strictly needed, but will be used if present). In that case the parameter should be given a default value of `null` and the the function should test to see if the caller supplied a corresponding argument or not, using the built-in function `exists()`. For example, here is the simple function shown above, modified to make the filling out of the `ess` value optional.

```
function series get_uhat_and_ess(series y, list xvars, scalar *ess[null])
  ols y 0 xvars --quiet
  if exists(ess)
    ess = $ess
  endif
  return $uhat
end function
```

If the caller does not care to get the `ess` value, it can use `null` in place of a real argument:

```
series resid = get_uhat_and_ess(price, xlist, null)
```

Alternatively, trailing function arguments that have default values may be omitted, so the following would also be a valid call:

```
series resid = get_uhat_and_ess(price, xlist)
```

One limitation on the use of pointer-type arguments should be noted: you cannot supply a given variable as a pointer argument more than once in any given function call. For example, suppose we have a function that takes two matrix-pointer arguments,

```
function scalar pointfunc (matrix *a, matrix *b)
```


And suppose we have two matrices, `x` and `y`, at the caller level. The call

```
pointfunc(&x, &y)
```

is OK, but the call

```
pointfunc(&x, &x) # will not work
```

will generate an error. That's because the situation inside the function would become too confusing, with the same object present under two different names.

Const parameters

Pointer-type arguments may also be useful for optimizing performance. Even if a variable is not modified inside the function, it may be a good idea to pass it as a pointer if it occupies a lot of memory. Otherwise, the time `gretl` spends transcribing the value of the variable to the local copy may be non-negligible compared to the time the function spends doing the job it was written for.

Listing 14.1 takes this to the extreme. We define two functions which return the number of rows of a matrix (a pretty fast operation). The first gets a matrix as argument while the second gets a pointer to a matrix. The functions are evaluated 500 times on a matrix with 2000 rows and 2000 columns; on a typical system floating-point numbers take 8 bytes of memory, so the total size of the matrix is roughly 32 megabytes.

Running the code in example 14.1 will produce output similar to the following (the actual numbers of course depend on the machine you're using):

```
Elapsed time:
without pointers (copy) = 2.47197 seconds,
with pointers (no copy) = 0.00378627 seconds
```

If a pointer argument is used for this sort of purpose—and the object to which the pointer points is not modified (is treated as read-only) by the function—one can signal this to the user by adding the `const` qualifier, as shown for function `rowcount2` in Listing 14.1. When a pointer argument is qualified in this way, any attempt to modify the object within the function will generate an error.

However, combining the `const` flag with the pointer mechanism is technically redundant for the following reason: if you mark a matrix argument as `const` then `gretl` will in fact pass it in pointer mode internally (since it can't be modified within the function there's no downside to simply making it available to the function rather than copying it). So in the example above we could revise the signature of the second function as

```
function scalar rowcount2a (const matrix X)
```

and call it with `r = rowcount2a(X)`, for the same speed-up relative to `rowcount1`.

From the caller's point of view the second option—using the `const` modifier *without* pointer notation—is preferable, as it allows the caller to pass an object created “on the fly”. Suppose the caller has two matrices, `A` and `B`, in scope, and wishes to pass their vertical concatenation as an argument. The following call would work fine:

```
r = rowcount2a(A|B)
```

To use `rowcount2`, on the other hand, the caller would have to create a named variable first (since you cannot give the “address” of an anonymous object such as `A|B`):

```
matrix AB = A|B
r = rowcount2(&AB)
```

Listing 14.1: Performance comparison: values versus pointer [\[Download ▼\]](#)

```
function scalar rowcount1 (matrix X)
    return rows(X)
end function

function scalar rowcount2 (const matrix *X)
    return rows(X)
end function

set verbose off
X = zeros(2000,2000)
scalar r

set stopwatch
loop 500
    r = rowcount1(X)
endloop
e1 = $stopwatch

set stopwatch
loop 500
    r = rowcount2(&X)
endloop
e2 = $stopwatch

printf "Elapsed time:\n\
without pointers (copy) = %g seconds,\n \
with pointers (no copy) = %g seconds\n", e1, e2
```

This requires an extra line of code, and leaves AB occupying memory after the call.

We have illustrated using a matrix parameter, but the `const` modifier may be used with the same effect—namely, the argument is passed directly, without being copied, but is protected against modification within the function—for all the types that support the pointer apparatus.

List arguments

The use of a named list as an argument to a function gives a means of supplying a function with a set of variables whose number is unknown when the function is written—for example, sets of regressors or instruments. Within the function, the list can be passed on to commands such as `ols`.

A list argument can also be “unpacked” using a `foreach` loop construct, but this requires some care. For example, suppose you have a list X and want to calculate the standard deviation of each variable in the list. You can do:

```
loop foreach i X
    scalar sd_$i = sd(X.$i)
endloop
```

Please note: a special piece of syntax is needed in this context. If we wanted to perform the above task on a list in a regular script (not inside a function), we could do

```
loop foreach i X
    scalar sd_$i = sd($i)
endloop
```

where `$i` gets the name of the variable at position *i* in the list, and `sd($i)` gets its standard deviation. But inside a function, working on a list supplied as an argument, if we want to reference an individual variable in the list we must use the syntax *listname.varname*. Hence in the example above we write `sd(X.$i)`.

This is necessary to avoid possible collisions between the name-space of the function and the name-space of the caller script. For example, suppose we have a function that takes a list argument, and that defines a local variable called `y`. Now suppose that this function is passed a list containing a variable named `y`. If the two name-spaces were not separated either we’d get an error, or the external variable `y` would be silently over-written by the local one. It is important, therefore, that list-argument variables should not be “visible” by name within functions. To “get hold of” such variables you need to use the form of identification just mentioned: the name of the list, followed by a dot, followed by the name of the variable.

Constancy of list arguments When a named list of variables is passed to a function, the function is actually provided with a copy of the list. The function may modify this copy (for instance, adding or removing members), but the original list at the level of the caller is not modified.

Optional list arguments If a list argument to a function is optional, this should be indicated by appending a default value of `null`, as in

```
function scalar myfunc (scalar y, list X[null])
```

In that case, if the caller gives `null` as the list argument (or simply omits the last argument) the named list X inside the function will be empty. This possibility can be detected using the `nelem()` function, which returns 0 for an empty list.

String arguments

String arguments can be used, for example, to provide flexibility in the naming of variables created within a function. In the following example the function `mavg` returns a list containing two moving averages constructed from an input series, with the names of the newly created variables governed by the string argument.

```
function list mavg (series y, string vname)
  list retlist = deflist()
  string newname = sprintf("%s_2", vname)
  retlist += genseries(newname, (y+y(-1)) / 2)
  newname = sprintf("%s_4", vname)
  retlist += genseries(newname, (y+y(-1)+y(-2)+y(-3)) / 4)
  return retlist
end function

open data9-9
list malist = mavg(nocars, "nocars")
print malist --byobs
```

The last line of the script will print two variables named `nocars_2` and `nocars_4`. For details on the handling of named strings, see [chapter 15](#).

If a string argument is considered optional, it may be given a `null` default value, as in

```
function scalar foo (series y, string vname[null])
```

Retrieving the names of arguments

The variables given as arguments to a function are known inside the function by the names of the corresponding parameters. For example, within the function whose signature is

```
function void somefun (series y)
```

we have the series known as `y`. It may be useful, however, to be able to determine the names of the variables provided as arguments. This can be done using the function `argname`, which takes the name of a function parameter as its single argument and returns a string. Here is a simple illustration:

```
function void namefun (series y)
  printf "the series given as 'y' was named %s\n", argname(y)
end function

open data9-7
namefun(QNC)
```

This produces the output

```
the series given as 'y' was named QNC
```

Please note that this will not always work: the arguments given to functions may be anonymous variables, created on the fly, as in `somefun(log(QNC))` or `somefun(CPI/100)`. In that case the `argname` function returns an empty string. Function writers who wish to make use of this facility should check the return from `argname` using the `strlen()` function: if this returns 0, no name was found.

Return values

Functions can return nothing (just printing a result, perhaps), or they can return a single variable. The return value, if any, is specified via a statement within the function body beginning with the keyword `return`, followed by either the name of a variable (which must be of the type announced on the first line of the function definition) or an expression which produces a value of the correct type.

Having a function return a list, bundle or array (see Chapter 11) is a way of permitting the “return” of more than one variable. For example, you can define several series inside a function and package them as a list; in this case they are not destroyed when the function exits. Here is a simple example, which also illustrates the possibility of setting the descriptive labels for variables generated in a function.

```
function list make_cubes (list xlist)
  list cubes = deflist()
  loop foreach i xlist
    series $i3 = (xlist.$i)^3
    setinfo $i3 -d "cube of $i"
    list cubes += $i3
  endloop
  return cubes
end function

open data4-1
list xlist = price sqft
list cubelist = make_cubes(xlist)
print xlist cubelist --byobs
labels
```

For details about the case of returning a bundle, see Section 11.7, in particular the sub-sections titled “Series and lists as bundle members” and “What are bundles good for?”.

A `return` statement causes the function to return (exit) at the point where it appears within the body of the function. A function may also exit when (a) the end of the function code is reached (in the case of a function with no return value), (b) a gretl error occurs, or (c) a `funcerr` statement is reached.

The `funcerr` keyword—which may be followed by a string enclosed in double quotes, or the name of a string variable, or nothing—causes a function to exit with an error flagged. If a string is provided (either literally or via a variable), this is printed on exit, otherwise a generic error message is printed. This mechanism enables the author of a function to pre-empt an ordinary execution error and/or offer a more specific and helpful error message. For example,

```
if nelem(xlist) == 0
  funcerr "xlist must not be empty"
endif
```

A function may contain more than one `return` statement, as in

```
function scalar multi (bool s)
  if s
    return 1000
  else
    return 10
  endif
end function
```

However, it is recommended programming practice to have a single return point from a function unless this is very inconvenient. The simple example above would be better written as

```
function scalar multi (bool s)
  return s ? 1000 : 10
end function
```

Overloading

You may have noticed that several built-in functions in gretl are “overloaded”—that is, a given argument slot may accept more than one type of argument, and the return value may depend on the type of the argument in question. For instance, the argument `x` for the `pdf()` function may be a scalar, series or matrix and the return type will match that choice on the caller’s part.

Since gretl-2021b this possibility also exists for user-defined functions. The meta-type `numeric` can be used in place of a specific type to accept a scalar, series or matrix argument, and similarly the return-type of a function can be marked as `numeric`.

As a function writer you can choose to be more restrictive than the default (which allows scalar, series or matrix for any `numeric` argument). For instance, if you write a function in which two arguments, `x` and `y`, are specified as `numeric` you might decide to disallow the case where `x` is a matrix and `y` a series, or vice versa, as too complicated. You can use the `typeof()` function to determine what types of arguments were supplied, and the `funcerr` command or `errorif()` function to reject an unsupported combination.

If your function is going to return a certain specific type (say, `matrix`) regardless of the type of the input, then the return value should be labeled accordingly: use `numeric` for the return only if it’s truly unknown in advance.

Listing 14.2 offers an (admittedly artificial) example: its `numeric` inputs can be scalars, series or column vectors but they must be of a single type.

Naturally, if your overloaded function is intended for public use you should state clearly in its documentation what is supported and what is not.

Error checking

When gretl first reads and “compiles” a function definition there is minimal error-checking: the only checks are that the function name is acceptable, and, so far as the body is concerned, that you are not trying to define a function inside a function (see Section 14.1). Otherwise, if the function body contains invalid commands this will become apparent only when the function is called and its commands are executed.

Debugging

The usual mechanism whereby gretl echoes commands and reports on the creation of new variables is by default suppressed when a function is being executed. If you want more verbose output from a particular function you can use either or both of the following commands within the function:

```
set echo on
set messages on
```

Alternatively, you can achieve this effect for all functions via the command `set debug 1`. Usually when you set the value of a state variable using the `set` command, the effect applies only to the current level of function execution. For instance, if you do `set messages on` within function `f1`, which in turn calls function `f2`, then messages will be printed for `f1` but not `f2`. The debug variable, however, acts globally; all functions become verbose regardless of their level.

Further, you can do `set debug 2`: in addition to command echo and the printing of messages, this is equivalent to setting `max_verbose` (which produces verbose output from the BFGS maximizer) at all levels of function execution.

Listing 14.2: Example of overloaded function [\[Download ▼\]](#)

```
function numeric x_plus_b_y (numeric x, scalar b, numeric y)
  errorif(typeof(x) != typeof(y), "x and y must be of the same type")
  if typeof(x) <= 2 # scalar or series
    return x + b*y
  elif rows(x) == rows(y) && cols(x) == 1 && cols(y) == 1
    return x + b*y
  else
    funcerr "x and y should be column vectors"
  endif
end function

set seed 12345

# call 1: x and y are scalars
eval x_plus_b_y(10, 3, 2)

# call 2: x and y are vectors
matrix x = mnormal(10, 1)
matrix y = mnormal(10, 1)
eval x_plus_b_y(x, 2, y)

open data4-1
# call 3: x and y are series
series bb = x_plus_b_y(bedrms, 0.5, baths)
print bb --byobs
```

14.5 Function packages

At various points above we have alluded to function packages, and the use of these via the gretl GUI. This topic is covered in depth by the *Gretl Function Package Guide*. If you're running gretl you can find this under the Help menu. Alternatively you may download it from

<https://sourceforge.net/projects/gretl/files/manual/>

Chapter 15

Named lists and strings

15.1 Named lists

Many gretl commands take one or more lists of series as arguments. To make this easier to handle in the context of command scripts, and in particular within user-defined functions, gretl offers the possibility of *named lists*.

Creating and modifying named lists

A named list is created using the keyword `list`, followed by the name of the list, an equals sign, and an expression that forms a list. The most basic sort of expression that works in this context is a space-separated list of variables, given either by name or by ID number. For example,

```
list xlist = 1 2 3 4
list reglist = income price
```

Note that the variables in question must be of the series type.

Two abbreviations are available in defining lists:

- You can use the wildcard character, “*”, to create a list of variables by name. For example, `dum*` can be used to indicate all variables whose names begin with `dum`.
- You can use two dots to indicate a range of variables. For example `income..price` indicates the set of variables whose ID numbers are greater than or equal to that of `income` and less than or equal to that of `price`.

In addition there are two special forms:

- If you use the keyword `null` on the right-hand side, you get an empty list.
- If you use the keyword `dataset` on the right, you get a list containing all the series in the current dataset (except the pre-defined `const`).

The name of the list must start with a letter, and must be composed entirely of letters, numbers or the underscore character. The maximum length of the name is 31 characters; list names cannot contain spaces.

Once a named list has been created, it will be “remembered” for the duration of the gretl session (unless you delete it), and can be used in the context of any gretl command where a list of variables is expected. One simple example is the specification of a list of regressors:

```
list xlist = x1 x2 x3 x4
ols y 0 xlist
```

To get rid of a list, you use the following syntax:

```
list xlist delete
```

Be careful: `delete xlist` will delete the series contained in the list, so it implies data loss (which may not be what you want). On the other hand, `list xlist delete` will simply “undefine” the `xlist` identifier; the series themselves will not be affected.

Similarly, to print the names of the members of a list you have to invert the usual print command, as in

```
list xlist print
```

If you just say `print xlist` the list will be expanded and the values of all the member series will be printed.

Lists can be modified in various ways. To *redefine* an existing list altogether, use the same syntax as for creating a list. For example

```
list xlist = 1 2 3
xlist = 4 5 6
```

After the second assignment, `xlist` contains just variables 4, 5 and 6.

To *append* or *prepend* variables to an existing list, we can make use of the fact that a named list stands in for a “longhand” list. For example, we can do

```
list xlist = xlist 5 6 7
xlist = 9 10 xlist 11 12
```

Another option for appending a term (or a list) to an existing list is to use `+=`, as in

```
xlist += cpi
```

To drop a variable from a list, use `-=`:

```
xlist -= cpi
```

In most contexts where lists are used in `gretl`, it is expected that they do not contain any duplicated elements. If you form a new list by simple concatenation, as in `list L3 = L1 L2` (where `L1` and `L2` are existing lists), it’s possible that the result may contain duplicates. To guard against this you can form a new list as the union of two existing ones:

```
list L3 = L1 || L2
```

The result is a list that contains all the members of `L1`, plus any members of `L2` that are not already in `L1`.

In the same vein, you can construct a new list as the intersection of two existing ones:

```
list L3 = L1 && L2
```

Here `L3` contains all the elements that are present in both `L1` and `L2`.

You can also subtract one list from another:

```
list L3 = L1 - L2
```

The result contains all the elements of `L1` that are not present in `L2`.

Indexing into a defined list is also possible, as if it were a vector:

```
list L2 = L1[1:4]
```

This leaves `L2` with the first four members of `L1`. Notice that the ordering of list members is path-dependent.

Lists and matrices

There are two ways one can think of lists and matrices being interchangeable: either you think of a list as a collection of references to series, or you may consider the rectangle of data given by the series that the list contains.

In the former case, a list may be translated into (or created from) a one-dimensional matrix, that is a vector. Therefore, the matrix in question must be interpretable as a vector containing ID numbers of data series. It may be either a row or a column vector, and each of its elements must have an integer part that is no greater than the number of variables in the data set. For example:

```
matrix m = {1,2,3,4}
list L = m
```

The above is OK provided the data set contains at least 4 variables. Conversely, the command

```
matrix m = L
```

will create a row vector with the ID numbers of the series referenced by L.

The latter case occurs when the matrix is assumed to contain valid data. To create a matrix from the list, simply assign to a matrix the list name surrounded by curly brackets, as in

```
matrix m = { L }
```

Note the difference with the above: without the curly brackets, matrix `m` would have been just a vector. Also note that any row corresponding to one or more missing entries will be dropped, unless the `skip_missing` set variable is set to on.

For the reverse operation, `gretl` provides the `mat2list` function, which takes a matrix (say, `X`) as argument and creates new series as well as a list containing them. The row dimension of `X` must equal either the length of the current dataset or the number of observations in the current sample range.

The naming of the series in the returned list proceeds as follows. First, if the optional prefix argument is supplied, the series created from column *i* of `X` is named by appending *i* to the given string. Otherwise, if `X` has column names set these names are used. Finally, if neither of the above conditions is satisfied, the names are `column1`, `column2` and so on.

For example,

```
matrix X = mnormal($nobs, 8)
list L = mat2list(X, "xnorm")
```

will add to the dataset eight full-length series named `xnorm1`, `xnorm2` and so on.

Querying a list

You can determine the number of variables or elements in a list using the function `nelem()`.

```
list xlist = 1 2 3
n1 = nelem(xlist)
```

The (scalar) variable `n1` will be assigned a value of 3 since `xlist` contains 3 members.

You can determine whether a given series is a member of a specified list using the function `inlist()`, as in

```
scalar k = inlist(L, y)
```

where `L` is a list and `y` a series. The series may be specified by name or ID number. The return value is the (1-based) position of the series in the list, or zero if the series is not present in the list.

Generating lists of transformed variables

Given a named list of series, you are able to generate lists of transformations of these series using the functions `log`, `lags`, `diff`, `ldiff`, `sdiff` or `dummi`. For example

```
list xlist = x1 x2 x3
list lxlist = log(xlist)
list difflist = diff(xlist)
```

When generating a list of *lags* in this way, you specify the maximum lag order inside the parentheses, before the list name and separated by a comma. For example

```
list xlist = x1 x2 x3
list laglist = lags(2, xlist)
```

or

```
scalar order = 4
list laglist = lags(order, xlist)
```

These commands will populate `laglist` with the specified number of lags of the variables in `xlist`. You can give the name of a single series in place of a list as the second argument to `lags`: this is equivalent to giving a list with just one member.

The `dummi` function creates a set of dummy variables coding for all but one of the distinct values taken on by the original variable, which should be discrete. (The smallest value is taken as the omitted category.) Like `lags`, this function returns a list even if the input is a single series.

Another useful operation you can perform with lists is creating *interaction* variables. Suppose you have a discrete variable x_i , taking values from 1 to n and a variable z_i , which could be continuous or discrete. In many cases, you want to “split” z_i into a set of n variables via the rule

$$z_i^{(j)} = \begin{cases} z_i & \text{when } x_i = j \\ 0 & \text{otherwise;} \end{cases}$$

in practice, you create dummies for the x_i variable first and then you multiply them all by z_i ; these are commonly called the *interactions* between x_i and z_i . In `gretl` you can do

```
list H = D ^ Z
```

where `D` is a list of discrete series (or a single discrete series), `Z` is a list (or a single series)¹; all the interactions will be created and listed together under the name `H`.

An example is provided in Listing 15.1.

Generating series from lists

There are various ways of retrieving or generating individual series from a named list. The most basic method is indexing into the list. For example,

```
series x3 = Xlist[3]
```

will retrieve the third element of the list `Xlist` under the name `x3` (or will generate an error if `Xlist` has less than three members).

¹This construct does *not* work if neither `D` nor `Z` are of the list type. However, a simple workaround is to turn `D` into a one-element list in this case, by writing `deflist(D) ^ Z`.

Listing 15.1: Usage of interaction lists [\[Download ▼\]](#)

Input:

```
open mroz87.gdt --quiet

# the coding below makes it so that
# KIDS = 0 -> no kids
# KIDS = 1 -> young kids only
# KIDS = 2 -> young or older kids

series KIDS = (KL6 > 0) + ((KL6 > 0) || (K618 > 0))

list D = CIT KIDS # interaction discrete variables
list X = WE WA    # variables to "split"
list INTER = D ^ X

smp1 1 6

print D X INTER -o
```

Output (selected portions):

	CIT	KIDS	WE	WA	WE_CIT_0
1	0	2	12	32	12
2	1	1	12	30	0
3	0	2	12	35	12
4	0	1	12	34	12
5	1	2	14	31	0
6	1	0	12	54	0

	WE_CIT_1	WA_CIT_0	WA_CIT_1	WE_KIDS_0	WE_KIDS_1
1	0	32	0	0	0
2	12	0	30	0	12
3	0	35	0	0	0
4	0	34	0	0	12
5	14	0	31	0	0
6	12	0	54	12	0

	WE_KIDS_2	WA_KIDS_0	WA_KIDS_1	WA_KIDS_2
1	12	0	0	32
2	0	0	30	0
3	12	0	0	35
4	0	0	34	0
5	14	0	0	31
6	0	54	0	0

In addition gretl offers several functions that apply to a list and return a series. In most cases, these functions also apply to single series and behave as natural extensions when applied to lists, but this is not always the case.

For recognizing and handling missing values, gretl offers several functions (see the *Gretl Command Reference* for details). In this context, it is worth remarking that the `ok()` function can be used

	YpcFR	YpcGE	YpcIT	NFR	NGE	NIT
1997	114.9	124.6	119.3	59830.635	82034.771	56890.372
1998	115.3	122.7	120.0	60046.709	82047.195	56906.744
1999	115.0	122.4	117.8	60348.255	82100.243	56916.317
2000	115.6	118.8	117.2	60750.876	82211.508	56942.108
2001	116.0	116.9	118.1	61181.560	82349.925	56977.217
2002	116.3	115.5	112.2	61615.562	82488.495	57157.406
2003	112.1	116.9	111.0	62041.798	82534.176	57604.658
2004	110.3	116.6	106.9	62444.707	82516.260	58175.310
2005	112.4	115.1	105.1	62818.185	82469.422	58607.043
2006	111.9	114.2	103.3	63195.457	82376.451	58941.499

Table 15.1: GDP per capita and population in 3 European countries (Source: Eurostat)

with a list argument. For example,

```
list xlist = x1 x2 x3
series xok = ok(xlist)
```

After these commands, the series `xok` will have value 1 for observations where none of `x1`, `x2`, or `x3` has a missing value, and value 0 for any observations where this condition is not met.

The functions `max`, `min`, `mean`, `sd`, `sum` and `var` behave “horizontally” rather than “vertically” when their argument is a list. For instance, the following commands

```
list Xlist = x1 x2 x3
series m = mean(Xlist)
```

produce a series `m` whose i -th element is the average of $x_{1,i}$, $x_{2,i}$ and $x_{3,i}$; missing values, if any, are implicitly discarded.

In addition, `gretl` provides three functions for weighted operations: `wmean`, `wsd` and `wvar`. Consider as an illustration Table 15.1: the first three columns are GDP per capita for France, Germany and Italy; columns 4 to 6 contain the population for each country. If we want to compute an aggregate indicator of per capita GDP, all we have to do is

```
list Ypc = YpcFR YpcGE YpcIT
list N = NFR NGE NIT
y = wmean(Ypc, N)
```

so for example

$$y_{1996} = \frac{114.9 \times 59830.635 + 124.6 \times 82034.771 + 119.3 \times 56890.372}{59830.635 + 82034.771 + 56890.372} = 120.163$$

See the *Gretl Command Reference* for more details.

15.2 Named strings

For some purposes it may be useful to save a string (that is, a sequence of characters) as a named variable that can be reused.

Some examples of the definition of a string variable are shown below.

```
string s1 = "some stuff I want to save"
string s2 = getenv("HOME")
string s3 = s1 + 11
```

The first field after the type-name `string` is the name under which the string should be saved, then comes an equals sign, then comes a specification of the string to be saved. This may take any of the following forms:

- a string literal (enclosed in double quotes); or
- the name of an existing string variable; or
- a function that returns a string (see below); or
- any of the above followed by `+` and an integer offset.

The role of the integer offset is to use a substring of the preceding element, starting at the given character offset. An empty string is returned if the offset is greater than the length of the string in question.

To add to the end of an existing string you can use the operator `~=`, as in

```
string s1 = "some stuff I want to "
string s1 ~= "save"
```

or you can use the `~` operator to join two or more strings, as in

```
string s1 = "sweet"
string s2 = "Home, " ~ s1 ~ " home."
```

Note that when you define a string variable using a string literal, only a single “escape” sequence is recognized: if a backslash is immediately followed by a double-quote character this is interpreted as an embedded quote. Otherwise all characters are treated literally. If you wish to use backslash-escapes to denote newlines, tabs and so on, use the `sprintf` function instead (see the `printf` command for an account of the escape-characters). This function can also be used to produce a string variable whose definition involves the values of other variables, as in

```
scalar x = 8
foo = sprintf("var%d", x) # produces "var8"
```

String variables and string substitution

String variables can be used in two ways in scripting: the name of the variable can be typed “as is”, or it may be preceded by the “at” sign, `@`. In the first variant the named string is treated as a variable in its own right, while the second calls for “string substitution”. The context determines which of these variants is appropriate.

In the following contexts the names of string variables should be given in plain form (without the “at” sign):

- When such a variable appears among the arguments to the `printf` command or `sprintf` function.
- When such a variable is given as the argument to a function.
- On the right-hand side of a `string` assignment.

Here is an illustration of the use of a named string argument with `printf`:

```
? string vstr = "variance"
Generated string vstr
? printf "vstr: %12s\n", vstr
vstr:      variance
```

String substitution can be used in contexts where a string variable is not acceptable as such. If `gretl` encounters the symbol `@` followed directly by the name of a string variable, this notation is treated as a “macro”: the value of the variable is substituted literally into the command line before the regular parsing of the command is carried out.

One common use of string substitution is when you want to construct and use the name of a series programmatically. For example, suppose you want to create 10 random normal series named `norm1` to `norm10`. This can be accomplished as follows.

```
string sname
loop i=1..10
  sname = sprintf("norm%d", i)
  series @sname = normal()
endloop
```

Note that plain `sname` could not be used in the second line within the loop: the effect would be to attempt to overwrite the string variable named `sname` with a series of the same name. What we want is for the current *value* of `sname` to be dumped directly into the command that defines a series, and the “`@`” notation achieves that.

Another typical use of string substitution is when you want the options used with a particular command to vary depending on some condition. For example,

```
function void use_optstr (series y, list xlist, int verbose)
  string optstr = verbose ? "" : "--simple-print"
  ols y xlist @optstr
end function

open data4-1
list X = const sqft
use_optstr(price, X, 1)
use_optstr(price, X, 0)
```

When printing the value of a string variable using the `print` command, the plain variable name should generally be used, as in

```
string s = "Just testing"
print s
```

The following variant is equivalent, though clumsy.

```
string s = "Just testing"
print "@s"
```

But note that this next variant does something quite different.

```
string s = "Just testing"
print @s
```

After string substitution, the `print` command reads

```
print Just testing
```

which attempts to print the values of two variables, `Just` and `testing`.

Built-in strings

Apart from any strings that the user may define, some string variables are defined by gretl itself. These may be useful for people writing functions that include shell commands. The built-in strings are as shown in Table 15.2.

<code>gretldir</code>	the gretl installation directory
<code>workdir</code>	user's current gretl working directory
<code>dotdir</code>	the directory gretl uses for temporary files
<code>gnuplot</code>	path to, or name of, the <code>gnuplot</code> executable
<code>tramo</code>	path to, or name of, the <code>tramo</code> executable
<code>x12a</code>	path to, or name of, the <code>x-12-arma</code> executable
<code>tramodir</code>	tramo data directory
<code>x12adir</code>	<code>x-12-arma</code> data directory

Table 15.2: Built-in string variables

To access these as ordinary string variables, prepend a dollar sign (as in `$dotdir`); to use them in string-substitution mode, prepend the at-sign (`@dotdir`).

Reading strings from the environment

It is possible to read into gretl's named strings, values that are defined in the external environment. To do this you use the function `getenv`, which takes the name of an environment variable as its argument. For example:

```
? string user = getenv("USER")
Generated string user
? string home = getenv("HOME")
Generated string home
? printf "%s's home directory is %s\n", user, home
cottrell's home directory is /home/cottrell
```

To check whether you got a non-empty value from a given call to `getenv`, you can use the function `strlen`, which retrieves the length of the string, as in

```
? string temp = getenv("TEMP")
Generated string temp
? scalar x = strlen(temp)
Generated scalar x = 0
```

Capturing strings via the shell

If shell commands are enabled in gretl, you can capture the output from such commands using the syntax

```
string stringname = $(shellcommand)
```

That is, you enclose a shell command in parentheses, preceded by a dollar sign.

Reading from a file into a string

You can read the content of a file into a string variable using the syntax

```
string stringname = readfile(filename)
```

The *filename* field may be given as a string variable. For example

```
? fname = sprintf("%s/QNC.rts", $x12adir)
Generated string fname
? string foo = readfile(fname)
Generated string foo
```

More string functions

Gretl offers several functions for creating or manipulating strings. You can find these listed and explained in the *Function Reference* under the category Strings.

Chapter 16

String-valued series

16.1 Introduction

By a string-valued series we mean a series whose primary values are strings (though internally such series comprise an integer coding plus a “dictionary” mapping from the integer values to strings). This chapter explains how to create such series and describes the operations that are supported for them.

16.2 Creating a string-valued series

This can be done in three ways:

- by reading such a series from a suitable source file;
- by taking a suitable numerical series within gretl and adding string values using the `stringify()` function; and
- by direct assignment to a series from an array of strings.

In each case string values will be preserved when such a series is saved in a gretl-native data file.

Reading string-valued series

The primary “suitable source” for string-valued series is a delimited text data file (but see section 16.5 below). Here’s a little example. The following is the content of a file named `gc.csv`:

```
city,year
"Bilbao",2009
"Toruń",2011
"Oklahoma City",2013
"Berlin",2015
"Athens",2017
"Naples",2019
```

A script to read this file and its output are shown in Listing 16.1, from which we can see a few things.

- By default the `print` command shows us the string values of the series `city`, and it handles non-ASCII characters provided they’re in UTF-8 (but it doesn’t handle longer strings very elegantly).
- The `--numeric` option to `print` exposes the integer codes for a string-valued series.
- The syntax `seriesname[obs]` yields a string when a series is string-valued.

If you want to access the numeric code for a particular string-valued observation you can get it by “casting” the series in question to a vector (by wrapping the identifier in curly brackets). So, for example,

Listing 16.1: Working with a string-valued series

Input:

```
open gc.csv --quiet
print --byobs
print city --byobs --numeric
printf "The third gretl conference took place in %s.\n", city[3]
```

Output:

```
? print --byobs
```

	city	year
1	Bilbao	2009
2	Toruń	2011
3	Oklahoma C..	2013
4	Berlin	2015
5	Athens	2017
6	Naples	2019

```
? print city --byobs --numeric
```

	city
1	1
2	2
3	3
4	4
5	5
6	6

The third gretl conference took place in Oklahoma City.

```
printf "The code for '%s' is %d.\n", city[3], {city}[3]
```

gives

The code for 'Oklahoma City' is 3.

The numeric codes for string-valued series are always assigned thus: reading the data file row by row, the first string value is assigned 1, the next *distinct* string value is assigned 2, and so on.

Assigning string values to a numeric series

This is done via the `stringify()` function, which takes two arguments, the name of a series and an array of strings. For this to work two conditions must be met:

1. The series must have only integer values and the smallest value must be 1 or greater.
2. The array of strings must have at least n distinct members, where n is the largest value found in the series.

The logic of these conditions is that we're looking to create a mapping as described above, from a 1-based sequence of integers to a set of strings. However, we're allowing for the possibility that the series in question is an incomplete sample from an associated population. Suppose we have a series that goes 2, 3, 5, 9, 10. This is taken to be a sample from a population that has at least 10 discrete values, 1, 2, ..., 10, and so requires at least 10 value-strings.

Here's (a simplified version of) an example that one of the authors has had cause to use: deriving US-style "letter grades" from a series containing percentage scores for students. Call the percentage series x , and say we want to create a series with values A for $x \geq 90$, B for $80 \leq x < 90$, and so on down to F for $x < 60$. Then we can do:

```
series grade = 1 # F, the least value
grade += x >= 60 # D
grade += x >= 70 # C
grade += x >= 80 # B
grade += x >= 90 # A
stringify(grade, strsplit("F D C B A"))
```

The way the `grade` series is constructed is not the most compact, but it's nice and explicit, and easy to amend if one wants to adjust the threshold values. Note the use of `strsplit()` to create an on-the-fly array of strings from a string literal; this is convenient when the array contains a moderate number of elements with no embedded spaces. An alternative way to get the same result is to define the array of strings via the `defarray()` function, as in

```
stringify(grade, defarray("F","D","C","B","A"))
```

The inverse operation of `stringify()` is performed by the `strvals()` function: this retrieves the array of distinct string values from a series (or returns an empty array if the series is not string-valued).

Assigning from an array of strings

Given an array of strings whose length matches the full length of the current dataset you can assign directly to a series result, provided these conditions are satisfied: the dataset is not sub-sampled, and if the assignment is to a pre-existing series it is not already string-valued.

Here's a trivial example:

```

nulldata 6
strings S = defarray("a", "b", "c", "b", "a", "d")
series sx = S
print sx --byobs

```

Here's a second example where we create a string-valued series using the “observation markers” from the current dataset, after grabbing them as an array via the `markers` command:

```

open data4-10
markers --to-array=S
series state = S
print state --byobs

```

And here's a third example where we construct the array of strings by reading from a text file:

```

nulldata 8
series sv = strsplit(readfile("ABCD.txt"))
print sv --byobs

```

This will work fine if the content of `ABCD.txt` is something like

```
A B C D D C B A
```

(containing 8 space-separated values, with or without line breaks). If the strings in question contain embedded spaces you would have to make use of the optional second argument to `strsplit`.

16.3 Permitted operations

One question that arises with string-valued series is, what exactly are you allowed to do with them? The optimal policy may be debatable, but here we set out the current state of things.

Setting values per observation

You can set particular values in a string-valued series either by string or numeric code. For example, suppose (in relation to the example in section 16.2) that for some reason student number 31 with a percentage score of 88 nonetheless merits an A grade. We could do

```
grade[31] = "A"
```

or, if we're confident about the mapping,

```
grade[31] = 5
```

Or to raise the student's grade by one letter:

```
grade[31] += 1
```

What you're *not* allowed to do here is make a numerical adjustment that would put the value out of bounds in relation to the set of string values. For example, if we tried `grade[31] = 6` we'd get an error.

On the other hand, you *can* implicitly extend the set of string values. This wouldn't make sense for the letter grades example but it might for, say, city names. Returning to the example in section 16.2 suppose we try

```
dataset addobs 1
year[7] = 2023
city[7] = "Gdańsk"
```

This will work: we're implicitly adding another member to the string table for `city`; the associated numeric code will be the next available integer.¹

Logical product of two string-valued series

The operator \wedge can be used to produce what we might call the logical product of two string-valued series, as in

```
series sv3 = sv1 ^ sv2
```

The result is another string-valued series with value $s_i.s_j$ at observations where `sv1` has value s_i and `sv2` has value s_j . For example, if at a given observation `sv1` has value "A" and `sv2` has value "X", then `sv3` will have value "A.X". The set of strings attached to the resulting series will include all such string combinations even if they are not all represented in the given sample.

Assignment to a string-valued series

In an assignment statement where the left-hand side (LHS) term is an existing string-valued series two general conditions must be met. First, the right-hand side (RHS) term must be a series (either numeric or string-valued) and second, the assignment operator must be plain "="; inflected operators such as `+=` and `*=` are not supported.

When the RHS series is numeric, all its values must be either integers between 1 and the number of strings attached to the LHS series, or NA. This is required to preserve the integrity of the LHS. When the RHS series is itself string-valued there are two cases to consider: there's no sample restriction in place, or there is such a restriction. In the unrestricted case the LHS series is in effect destroyed and replaced by a clone of the RHS. Otherwise string values on the RHS are written into the LHS only within the current sample range. If an RHS string is already present on the left its numerical code is adjusted if necessary to match the LHS string table; if it is not present on the left it is appended to the LHS string table.

Missing values

We support one exception to the general rule, never break the mapping between strings and numeric codes for string-valued series: you can mark particular observations as missing. This is done in the usual way, e.g.,

```
grade[31] = NA
```

Note, however, that on importing a string series from a delimited text file any non-blank strings (including "NA") will be interpreted as valid values; any missing values in such a file should therefore be represented by blank cells.

Copying a string-valued series

If you make a copy of a string-valued series, as in

```
series foo = city
```

the string values are *not* copied over: you get a purely numerical series holding the codes of the original series. But if you want a full copy with the string values that can easily be arranged:

¹So please be careful: one may inadvertently add a new string value by mistyping a string that's already present.

```
series citycopy = city
stringify(citycopy, strvals(city))
```

String-valued series in other contexts

String-valued series can be used on the right-hand side of assignment statements at will, and in that context their numerical values are taken. For example,

```
series y = sqrt(city)
```

will elicit no complaint and generate a numerical series 1, 1.41421, It's up to the user to judge whether this sort of thing makes any sense.

Similarly, it's up to the user to decide if it makes sense to use a string-valued series “as is” in a regression model, whether as regressand or regressor—again, the numerical values of the series are taken. Often this will not make sense, but sometimes it may: the numerical values may by design form an ordinal, or even a cardinal, scale (as in the “grade” example in section 16.2).

More likely, one would want to use `dummify` on a string-valued series before using it in statistical modeling. In that context gretl's series labels are suitably informative. For example, suppose we have a series `race` with numerical values 1, 2 and 3 and associated strings “White”, “Black” and “Other”. Then the `hansl` code

```
list D = dummify(race)
labels
```

will show these labels:

```
Drace_2: dummy for race = 'Black'
Drace_3: dummy for race = 'Other'
```

Given a series such as `race` you can use its string values in a sample restriction, as in

```
smp1 race == "Black" --restrict
```

(although `race == 2` would also be acceptable).

Accessing string values

We have mentioned above two ways of accessing string values from a given series: via the syntax

```
seriesname[obs]
```

to obtain a single such value; and via the `strvals()` function to obtain an array holding all its distinct values. Here we note a third option: direct assignment from a string-valued series to an array of strings, as in

```
strings S = sv
```

where `sv` is a suitable series. In this case you get an array holding *all* the `sv` strings for observations in the current sample range, not just the distinct values as with `strvals`.

16.4 String-valued series and functions

We first offer a few words on built-in functions that can be applied to string-valued series. The five functions `substr`, `strsub`, `regsub`, `tolower` and `toupper` all perform transformations on

strings—respectively, extraction of a substring, replacement of a substring, replacement via regular expression, conversion to all lower-case and to all upper-case (see the *Gretl Command Reference* for details). These functions work on single strings, arrays of strings and also string-valued series. Note that when applied to a string-valued series these functions may reduce the number of distinct strings attached to the series. For example, some string values that are originally distinct may “collapse” into identity when converted to all lower-case. This possibility is handled by adjustment of the integer codes as needed.

A special case is presented by the built-in `strvsort` function: this does not return a modified string-valued series but rather modifies such a series in place. It puts the string values into alphabetical order and recalculates the integer codes so as to preserve the original association between observation number and string. If, for example, the first observation had a string value of “X”, coded as 1, it will still have value “X” but its code will reflect the position of “X” in the alphabetized ordering. This can be particularly useful if a dataset comprises several series having the same string values, but occurring in various orders. The effect of running `strvsort` on such series will be to impose a common numerical encoding.

User-defined `hansl` functions can also deal with string-valued series. If you supply such a series as an argument to a `hansl` function its string values will be accessible within the function. One can test whether a given series `arg` is string-valued as follows:

```
if nelem(strvals(arg)) > 0
  # yes
else
  # no
endif
```

It’s also possible, since `gretl` version 2023c, to put something like the code that generated the `grade` series in section 16.2 into a function, and return the stringified series, as in the following (where we assume that `x` contains percentage scores):

```
function series letter_grade (series x)
  series grade
  # define grade based on x and stringify it, as shown above
  return grade
end function
```

An alternative means of achieving the same effect—and the only means available prior to `gretl` 2023c—is to to define `grade` as a series at the level of the caller and pass it in “pointer” form to `letter_grade()`, as in

```
function void letter_grade (series x, series *grade)
  # define grade based on x and stringify it
end function

# caller
...
series grade
letter_grade(x, &grade)
```

As you’ll see from the account above, we don’t offer any very fancy facilities for string-valued series. We’ll read them from suitable sources and we’ll create them natively via `stringify`—and we’ll try to ensure that they retain their integrity—but we don’t, for example, take the specification of a string-valued series as a regressor as an implicit request to include the dummification of its distinct values.

16.5 Other import formats

In section 16.2 we illustrated the reading of string-valued series with reference to a delimited text data file. Gretl can also handle several other sources of string-valued data, including the spreadsheet formats `xls`, `xlsx`, `gnumeric` and `ods` and (to a degree) the formats of Stata, SAS and SPSS.

Stata files

Stata supports two relevant sorts of variables: (1) those that are of “string type” and (2) variables of one or other numeric type that have “value labels” defined. Neither of these is exactly equivalent to what we call a “string-valued series” in gretl.

Stata variables of string type have no numeric representation; their values are literally strings, and that’s all. Stata’s numeric variables with value labels do not have to be integer-valued and their least value does not have to be 1; however, you can’t define a label for a value that is not an integer. Thus in Stata you can have a series that comprises both integer and non-integer values, but only the integer values can be labeled.²

This means that on import to gretl we can readily handle variables of string type from Stata’s `dta` files. We give them a 1-based numeric encoding; this is arbitrary but does not conflict with any information in the `dta` file. On the other hand, in general we’re not able to handle Stata’s numeric variables with value labels; currently we report the value labels to the user but do not attempt to store them in the gretl dataset. We could check such variables and import them as string-valued series if they satisfy the criteria stated in section 16.2 but we don’t at present.

SAS and SPSS files

Gretl is able to read and preserve string values associated with variables from SAS “export” (`xpt`) files, and also from SPSS `sav` files. Such variables seem to be on the same pattern as Stata variables of string type.

²Verified in Stata 12.

Chapter 17

Matrix manipulation

Together with the other two basic types of data (series and scalars), gretl offers a quite comprehensive array of matrix methods. This chapter illustrates the peculiarities of matrix syntax and discusses briefly some of the more advanced matrix functions. For a full listing of matrix functions and a comprehensive account of their syntax, please refer to the *Gretl Command Reference*.

In this chapter we're concerned with real matrices; most of the points made here also apply to complex matrices but see the following chapter for additional specifics on the complex case.

17.1 Creating matrices

Matrices can be created using any of these methods:

1. By direct specification of the scalar values that compose the matrix—either in numerical form, or by reference to pre-existing scalar variables, or using computed values.
2. By providing a list of data series.
3. By providing a *named list* of series.
4. Via a suitable expression that references existing matrices and/or scalars, or via some special functions.

To specify a matrix *directly in terms of scalars*, the syntax is, for example:

```
matrix A = {1, 2, 3 ; 4, 5, 6}
```

The matrix is defined by rows; the elements on each row are separated by commas and the rows are separated by semi-colons. The whole expression must be wrapped in braces. Spaces within the braces are not significant. The above expression defines a 2×3 matrix. Each element should be a numerical value, the name of a scalar variable, or an expression that evaluates to a scalar. Directly after the closing brace you can append a single quote (') to obtain the transpose.

To specify a matrix *in terms of data series* the syntax is, for example,

```
matrix A = {x1, x2, x3}
```

where the names of the series are separated by commas. Besides names of existing series, you can use expressions that yield a series result. For example, given a series *x* you could do

```
matrix A = {x, x^2}
```

Each series occupies a column (and there can only be one series per column). The semicolon cannot be used as a row separator in this case: if you want the series arranged in rows, append the transpose symbol. The range of data values included in the matrix depends on the current setting of the sample range.

Instead of giving an explicit list of series, you may instead provide the *name of a saved list* (see Chapter 15), as in

```
list xlist = x1 x2 x3
matrix A = {xlist}
```

When you provide a named list, the data series are by default placed in columns, as is natural in an econometric context: if you want them in rows, append the transpose symbol.

As a special case of constructing a matrix from a list of series, you can say

```
matrix A = {dataset}
```

This builds a matrix using all the series in the current dataset, apart from the constant (series 0). When this dummy list is used, it must be the sole element in the matrix definition {...}. You can, however, create a matrix that includes the constant along with all other series using horizontal concatenation (see below), as in

```
matrix A = {const}~{dataset}
```

By default, when you build a matrix from series that include missing values any observations (rows) that contain NAs are skipped. This behavior can be modified via the command `set skip_missing off`. In that case missing values are represented in the matrix as NaN (“Not a Number”). Note that as per the IEEE standard, arithmetic operations involving one or more NaNs always produce a NaN result. Alternatively, you can take greater control over the observations (data rows) that are included in the matrix using the “set” variable `matrix_mask`, as in

```
set matrix_mask msk
```

where `msk` is the name of a series. Subsequent commands that form matrices from series or lists will include only observations for which `msk` has non-zero (and non-missing) values. You can remove this mask via the command `set matrix_mask null`.

☞ Names of matrices must satisfy the same requirements as names of gretl variables in general: the name can be no longer than 31 characters, must start with a letter, and must be composed of nothing but letters, numbers and the underscore character.

17.2 Empty matrices

The syntax

```
matrix A = {}
```

creates an empty matrix—a matrix with zero rows and zero columns.

The main purpose of this construct is to allow the user to define a starting point for subsequent concatenation operations. For instance, if `X` is an already defined matrix of any size, the commands

```
matrix A = {}
matrix B = A ~ X
```

produce a matrix `B` that is identical to `X`.

From an algebraic point of view, one can make sense of the idea of an empty matrix in terms of vector spaces: if a matrix is an ordered set of vectors, then `A={}` is the empty set. As a consequence, operations involving addition and multiplications don’t have any clear meaning (arguably, they have none at all), but operations involving the cardinality of this set (that is, the dimension of the space spanned by `A`) are meaningful.

Legal function calls with an empty matrix argument are listed in Table 17.1; other matrix functions generate an error if given an empty argument. In line with the above interpretation, the functions

<i>Function</i>	<i>Return value</i>	<i>Function</i>	<i>Return value</i>
<code>A', transp(A)</code>	<code>A</code>	<code>rows(A)</code>	<code>0</code>
<code>cols(A)</code>	<code>0</code>	<code>rank(A)</code>	<code>0</code>
<code>det(A)</code>	<code>NA</code>	<code>ldet(A)</code>	<code>NA</code>
<code>tr(A)</code>	<code>NA</code>	<code>onenorm(A)</code>	<code>NA</code>
<code>infnorm(A)</code>	<code>NA</code>	<code>rcond(A)</code>	<code>NA</code>
<code>diag(A)</code>	<code>{}</code>	<code>vec(A)</code>	<code>{}</code>
<code>vech(A)</code>	<code>{}</code>	<code>unvech(A)</code>	<code>{}</code>

Table 17.1: Valid functions on an empty matrix, `A`

`I`, `ones`, `zeros`, `mnormal` and `muniform` return an empty matrix when or more of the arguments is 0, as well as the function `nullspace` when its argument is of full column rank.

While the 0×0 matrix produced by `{}` is the most common sort of empty matrix, matrices with one zero and one positive dimension are also supported. For example, the call

```
matrix A = zeros(3,0)
```

produces a 3×0 matrix, as does

```
matrix A = zeros(3,1)
A = A[,-1] # delete column 1 (see below)
```

The handling of such matrices by `gretl` is very similar to that in `Matlab`.

17.3 Selecting submatrices

You can select submatrices of a given matrix using the syntax

```
A[rows,cols]
```

where *rows* can take any of these forms:

- | | |
|--------------------------------------|----------------------------------|
| 1. empty | selects all rows |
| 2. a single integer | selects the single specified row |
| 3. two integers separated by a colon | selects a range of rows |
| 4. the name of a matrix | selects the specified rows |

With regard to option 2, the integer value can be given numerically, as the name of an existing scalar variable, or as an expression that evaluates to a scalar. With option 4, the index matrix given in the *rows* field must be either $p \times 1$ or $1 \times p$, and should contain integer values in the range 1 to n , where n is the number of rows in the matrix from which the selection is to be made.

The *cols* specification works in the same way, *mutatis mutandis*. Here are some examples.

```
matrix B = A[1,]
matrix B = A[2:3,3:5]
matrix B = A[2,2]
matrix idx = {1, 2, 6}
matrix B = A[idx,]
```

The first example selects row 1 from matrix `A`; the second selects a 2×3 submatrix; the third selects a scalar; and the fourth selects rows 1, 2, and 6 from matrix `A`.

If the matrix in question is $n \times 1$ or $1 \times m$, it is OK to give just one index specifier and omit the comma. For example, `A[2]` selects the second element of `A` if `A` is a vector. Otherwise the comma is mandatory.

In addition there are some predefined index specifications, represented by the keywords `diag`, `lower`, `upper`, `real`, `imag` and `end`. With the exception of `end`, these keywords imply specific row *and* column selections, and therefore cannot be combined with any additional, comma-separated term.

- The `diag` specification selects the principal diagonal of a matrix.
- `lower` and `upper` select, respectively, the elements of a matrix below and those above the principal diagonal.
- `real` and `imag` are specific to complex matrices and are described in chapter 18.
- `end` selects the last element in a given row or column. It can be employed in arithmetical expressions, so for example `end-1` accesses the second-last element in a row or column.

Submatrix selections can be used on either the right-hand side of a matrix-generating formula or the left. Here is an example of use of a selection on the right, to extract a 2×2 submatrix `B` from a 3×3 matrix `A`, then the lower triangle of `A`:

```
matrix A = {1, 2, 3; 4, 5, 6; 7, 8, 9}
matrix B = A[1:2,2:3]
matrix C = A[lower]
```

And here are examples of selection on the left. The second line below writes a 2×2 identity matrix into the bottom right corner of the 3×3 matrix `A`. The fourth line replaces the diagonal of `A` with 1s.

```
matrix A = {1, 2, 3; 4, 5, 6; 7, 8, 9}
matrix A[2:3,2:3] = I(2)
matrix d = {1, 1, 1}
matrix A[diag] = d
```

When the `lower` and `upper` selections are used on the right, they yield a vector holding the elements in their scope. The ordering of the elements is column-major in both cases, as illustrated below for the 4×4 case.

<i>d</i>	1	2	4
1	<i>d</i>	3	5
2	4	<i>d</i>	6
3	5	6	<i>d</i>

This means that `lower` and `upper` do not produce the same result for symmetric matrices bigger than 3×3 , which may seem unfortunate, but it gives the user a degree of flexibility in respect of the ordering of the elements. Suppose you have a non-symmetric matrix `M` and you'd like to extract the infradiagonal elements in row-major order: `(M')[upper]` will do the job.

When `lower` and `upper` are used on the left, the replacement must be either (a) a vector of length equal to the number of elements in the selection or (b) a scalar value. In case (a) the elements of the target matrix are filled in column-major order; in case (b) they are all set using the scalar.

One possible use of these tools is taking (say) a lower triangular matrix and rendering it symmetric by copying the elements from beneath the diagonal to above. The way to get this right (assuming you have a lower triangular matrix `L`) is

```
L[upper] = (L')[upper] # note: not L[upper] = L[lower]
```

17.4 Deleting rows or columns

A variant of submatrix notation is available for convenience in dropping specified rows and/or columns from a matrix, namely giving negative values for the indices. Here is a simple example,

```
matrix A = {1, 2, 3; 4, 5, 6; 7, 8, 9}
matrix B = A[-2,-3]
```

which creates B as a 2×2 matrix which drops row 2 and column 3 from A. Negative indices can also be given in the form of an index vector:

```
matrix rdrop = {-1,-3,-5}
matrix B = A[rdrop,]
```

In this case B is formed by dropping rows 1, 3 and 5 from A (which must have at least 5 rows), but retaining the column dimension of A.

There are two limitations on the use of negative indices. First, the `from:to` range syntax described in the previous section is not available, but you can use the `seq` function to achieve an equivalent effect, as in

```
matrix A = muniform(1, 10)
matrix B = A[,-seq(3,7)]
```

where B drops columns 3 to 7 from A. Second, use of negative indices is valid only on the right-hand side of a matrix calculation; there is no “negative index” equivalent of assignment to a submatrix, as in

```
A[1:3,] = ones(3, cols(A))
```

17.5 Matrix operators

The following binary operators are available for matrices:

+	addition
-	subtraction
*	ordinary matrix multiplication
'	pre-multiplication by transpose
\	matrix “left division” (see below)
/	matrix “right division” (see below)
~	column-wise concatenation
	row-wise concatenation
**	Kronecker product
==	test for equality
!=	test for inequality

In addition, the following operators (“dot” operators) apply on an element-by-element basis:

```
.+ .- .* ./ .^ . = .> .< .>= .<= .!=
```

Here are explanations of the less obvious cases.

For matrix addition and subtraction, in general the two matrices have to be of the same dimensions but an exception to this rule is granted if one of the operands is a 1×1 matrix or scalar. The scalar

is implicitly promoted to the status of a matrix of the correct dimensions, all of whose elements are equal to the given scalar value. For example, if A is an $m \times n$ matrix and k a scalar, then the commands

```
matrix C = A + k
matrix D = A - k
```

both produce $m \times n$ matrices, with elements $c_{ij} = a_{ij} + k$ and $d_{ij} = a_{ij} - k$ respectively.

By “pre-multiplication by transpose” we mean, for example, that

```
matrix C = X'Y
```

produces the product of X -transpose and Y . In effect, the expression $X'Y$ is shorthand for $X'*Y$, which is also valid syntax. In the special case $X = Y$, however, the two are not exactly equivalent. The former expression uses a specialized algorithm with two advantages: it is more efficient computationally, and ensures that the result is free of machine precision artifacts that may render it numerically non-symmetric. This, however, is unlikely to be an issue unless your X matrix is rather large (at least several hundreds rows/columns).

In matrix “left division”, the statement

```
matrix X = A \ B
```

is interpreted as a request to find the matrix X that solves $AX = B$, so A and B must have the same number of rows. If A is a square matrix, this is in principle equivalent to $A^{-1}B$, which fails if A is singular; the numerical method employed here is the LU decomposition. If A is a $T \times k$ matrix with $T > k$, then X is the least-squares solution, $X = (A'A)^{-1}A'B$, which fails if $A'A$ is singular; the numerical method is the QR decomposition. Otherwise, the operation fails.

For matrix “right division”, as in $X = A / B$, X is the matrix that solves $XB = A$, so A and B must have the same number of columns. If B is non-singular this is in principle equivalent to AB^{-1} , otherwise X is the least-squares solution.

In “dot” operations a binary operation is applied element by element; the result of this operation is obvious if the matrices are of the same size. However, there are several other cases where such operators may be applied. For example, if we write

```
matrix C = A .- B
```

then the result C depends on the dimensions of A and B . Let A be an $m \times n$ matrix and let B be $p \times q$; the result is as follows:

<i>Case</i>	<i>Result</i>
Dimensions match ($m = p$ and $n = q$)	$c_{ij} = a_{ij} - b_{ij}$
A is a column vector; rows match ($m = p$; $n = 1$)	$c_{ij} = a_i - b_{ij}$
B is a column vector; rows match ($m = p$; $q = 1$)	$c_{ij} = a_{ij} - b_i$
A is a row vector; columns match ($m = 1$; $n = q$)	$c_{ij} = a_j - b_{ij}$
B is a row vector; columns match ($m = p$; $q = 1$)	$c_{ij} = a_{ij} - b_j$
A is a column vector; B is a row vector ($n = 1$; $p = 1$)	$c_{ij} = a_i - b_j$
A is a row vector; B is a column vector ($m = 1$; $q = 1$)	$c_{ij} = a_j - b_i$
A is a scalar ($m = 1$ and $n = 1$)	$c_{ij} = a - b_{ij}$
B is a scalar ($p = 1$ and $q = 1$)	$c_{ij} = a_{ij} - b$

If none of the above conditions are satisfied the result is undefined and an error is flagged.

Note that this convention makes it unnecessary, in most cases, to use diagonal matrices to perform transformations by means of ordinary matrix multiplication: if $Y = XV$, where V is diagonal, it is computationally much more convenient to obtain Y via the instruction

```
matrix Y = X .* v
```

where v is a row vector containing the diagonal of V .

Concatenation

In *column-wise concatenation* of an $m \times n$ matrix A and an $m \times p$ matrix B , the result is an $m \times (n+p)$ matrix. That is,

```
matrix C = A ~ B
```

produces $C = \begin{bmatrix} A & B \end{bmatrix}$.

Row-wise concatenation of an $m \times n$ matrix A and an $p \times n$ matrix B produces an $(m+p) \times n$ matrix. That is,

```
matrix C = A | B
```

produces $C = \begin{bmatrix} A \\ B \end{bmatrix}$.

In general the two matrix operands must be conformable, as indicated above. But as a special case for convenience, a scalar or 1×1 matrix can be concatenated with a matrix of any size; the single value is automatically repeated, if necessary, to form a row or column vector of length conformable with the matrix in question. So for example

```
matrix A = {1, 2, 3}
matrix B = A | 1
```

produces $B = \begin{bmatrix} 1 & 2 & 3 \\ 1 & 1 & 1 \end{bmatrix}$.

17.6 Matrix-scalar operators

For matrix A and scalar k , the operators shown in Table 17.2 are available. (Addition and subtraction were discussed in section 17.5 but we include them in the table for completeness.) In addition, for square A and scalar x , $B = A^x$ produces a matrix B which is A raised to the power x , but only if either of two conditions are satisfied. First, if x is a non-negative integer then Golub and Van Loan's "Binary Powering" Algorithm 11.2.2 is used—see [Golub and Van Loan \(1996\)](#)—and A can then be a generic square matrix. Second, if A is positive semidefinite the power is computed via its eigen-decomposition and x can be a real number, subject to the constraint that x can be negative only if A is invertible.

17.7 Matrix functions

Most of the functions available for scalars and series also apply to matrices on an element-by-element basis. This is the case for `log`, `exp`, `sqrt`, `sin` and many others. For example, if a matrix A is already defined, then

```
matrix B = sqrt(A)
```

<i>Expression</i>	<i>Effect</i>
matrix B = A * k	$b_{ij} = ka_{ij}$
matrix B = A / k	$b_{ij} = a_{ij}/k$
matrix B = k / A	$b_{ij} = k/a_{ij}$
matrix B = A + k	$b_{ij} = a_{ij} + k$
matrix B = A - k	$b_{ij} = a_{ij} - k$
matrix B = k - A	$b_{ij} = k - a_{ij}$
matrix B = A % k	$b_{ij} = a_{ij} \text{ modulo } k$

Table 17.2: Matrix-scalar operators

generates a matrix such that $b_{ij} = \sqrt{a_{ij}}$. All such functions require a single matrix as argument, or an expression which evaluates to a single matrix.¹

In this section, we review some aspects of functions that apply specifically to matrices. A full account of each function is available in the *Gretl Command Reference*.

Matrix manipulation

bin2dec	cnameset	cols	dec2bin	diag	diagcat
halton	I	lower	mlag	mnormal	mrndgen
mreverse	mshape	msortby	msplitby	uniform	ones
rnameset	rows	selifc	selifr	seq	trimr
unvech	upper	vec	vech	zeros	

Matrix algebra

cholesky	cnumber	commute	conv2d	det	eigen
eigengen	eigensym	eigsolve	fft	ffti	ginv
hdprod	infnorm	inv	invpd	ldet	lsolve
mexp	mlog	nullspace	onenorm	psdroot	qform
qrdecomp	rank	rcond	svd	toepsolv	tr
transp					

Statistics/transformations

aggregate	bkw	corr	corresp	cov	ecdf
fcstats	ghk	gini	imaxc	imaxr	iminc
iminr	kpsscrit	max	maxc	maxr	mcorr
mcov	mcovg	meanc	meanr	min	minc
minr	mols	mpols	mrls	mxtab	normtest
npcorr	princomp	prodc	prodr	quadtable	quantile
ranking	resample	sdv	sphericorrsst		sumc
sumr	uniq	values			

Numerical methods

BFGSmax	BFGSmax	fdjac	fzero	GSSmax	NMmax
NRmax	numhess	simann			

Table 17.3: Matrix functions by category

¹Note that to find the “matrix square root” you need the `cholesky` function (see below). And since the `exp` function computes the exponential element by element, it does *not* return the matrix exponential unless the matrix is diagonal. To get the matrix exponential, use `mexp`.

Matrix reshaping

In addition to the methods discussed in sections 17.1 and 17.3, a matrix can also be created by re-arranging the elements of a pre-existing matrix. This is accomplished via the `mshape` function. It takes three arguments: the input matrix, A , and the rows and columns of the target matrix, r and c respectively. Elements are read from A and written to the target in column-major order. If A contains fewer elements than $n = r \times c$, they are repeated cyclically; if A has more elements, only the first n are used.

For example:

```
matrix a = mnormal(2,3)
a
matrix b = mshape(a,3,1)
b
matrix b = mshape(a,5,2)
b
```

produces

```
? a
a
      1.2323      0.99714      -0.39078
      0.54363      0.43928      -0.48467

? matrix b = mshape(a,3,1)
Generated matrix b
? b
b
      1.2323
      0.54363
      0.99714

? matrix b = mshape(a,5,2)
Replaced matrix b
? b
b
      1.2323      -0.48467
      0.54363      1.2323
      0.99714      0.54363
      0.43928      0.99714
      -0.39078      0.43928
```

Multiple returns and the `null` keyword

The functions listed below take one or more matrices as arguments and compute one or more matrices.

<code>eigensym</code>	Eigen-analysis of symmetric matrix
<code>eigen</code>	Eigen-analysis of general matrix
<code>mo1s</code>	Matrix OLS
<code>qrdecomp</code>	QR decomposition
<code>svd</code>	Singular value decomposition (SVD)

The “main” result of the function is always returned as the result proper. Auxiliary returns, if wanted, are retrieved using pre-existing matrices, passed to the function in “pointer” form (Section 14.4). If such values are not needed, the pointer may be substituted with the keyword `null`.

The syntax for `qrdecomp` and `eigensym` is of the form

```
matrix B = func(A, &C)
```

The first argument, *A*, represents the input data, that is, the matrix whose decomposition or analysis is required. The second argument must be either the name of an existing matrix preceded by `&` (to indicate the “address” of the matrix in question), in which case an auxiliary result is written to that matrix, or the keyword `null`, in which case the auxiliary result is not produced.

In case a non-null second argument is given, the specified matrix will be over-written with the auxiliary result. (It is not required that the existing matrix be of the right dimensions to receive the result.)

The function `eigensym` computes the eigenvalues, and optionally the right eigenvectors, of a symmetric $n \times n$ matrix. The eigenvalues are returned directly in a column vector of length n ; if the eigenvectors are required, they are returned in an $n \times n$ matrix. For example:

```
matrix V = {}
matrix E = eigensym(M, &V)
matrix E = eigensym(M, null)
```

In the first case *E* holds the eigenvalues of *M* and *V* holds the eigenvectors. In the second, *E* holds the eigenvalues but the eigenvectors are not computed.

The function `eigen` computes the eigenvalues, and optionally the right and/or left eigenvectors, of a general $n \times n$ matrix. Following the input matrix argument there are two slots for matrix-addresses, the first to retrieve the right eigenvectors and the second for the left. Calls to this function should therefore conform to one of the following patterns.

```
# get the eigenvalues only
matrix E = eigen(M)

# get the right eigenvectors as well
matrix V = {}
matrix E = eigen(M, &V)

# get both sets of eigenvectors
matrix V = {}
matrix W = {}
matrix E = eigen(M, &V, &W)

# get the left eigenvectors but not the right
matrix W = {}
matrix E = eigen(M, null, &W)
```

The eigenvalues are returned directly in a complex n -vector. If the eigenvectors are wanted they are returned in a $n \times n$ complex matrix.

The `qrdecomp` function computes the QR decomposition of an $m \times n$ matrix *A*: $A = QR$, where *Q* is an $m \times n$ orthogonal matrix and *R* is an $n \times n$ upper triangular matrix. The matrix *Q* is returned directly, while *R* can be retrieved via the second argument. Here are two examples:

```
matrix R
matrix Q = qrdecomp(M, &R)
matrix Q = qrdecomp(M, null)
```

In the first example, the triangular R is saved as R ; in the second, R is discarded. The first line above shows an example of a “simple declaration” of a matrix: R is declared to be a matrix but is not given any explicit value. The result is that it is automatically initialized as an empty matrix (see Section 17.2).

The syntax for `svd` is

```
matrix B = func(A, &C, &D)
```

The function `svd` computes all or part of the singular value decomposition of the real $m \times n$ matrix A . Let $k = \min(m, n)$. The decomposition is

$$A = U\Sigma V'$$

where U is an $m \times k$ orthogonal matrix, Σ is an $k \times k$ diagonal matrix, and V is an $k \times n$ orthogonal matrix.² The diagonal elements of Σ are the singular values of A ; they are real and non-negative, and are returned in descending order. The first k columns of U and V are the left and right singular vectors of A .

The `svd` function returns the singular values, in a vector of length k . The left and/or right singular vectors may be obtained by supplying non-null values for the second and/or third arguments respectively. For example:

```
matrix s = svd(A, &U, &V)
matrix s = svd(A, null, null)
matrix s = svd(A, null, &V)
```

In the first case both sets of singular vectors are obtained, in the second case only the singular values are obtained; and in the third, the right singular vectors are obtained but U is not computed. *Please note:* when the third argument is non-null, it is actually V' that is provided. To reconstitute the original matrix from its SVD, one can do:

```
matrix s = svd(A, &U, &V)
matrix B = (U.*s)*V
```

Finally, the syntax for `ols` is

```
matrix B = ols(Y, X, &U)
```

This function returns the OLS estimates obtained by regressing the $T \times n$ matrix Y on the $T \times k$ matrix X , that is, a $k \times n$ matrix holding $(X'X)^{-1}X'Y$. The Cholesky decomposition is used. The matrix U , if not null, is used to store the residuals.

Reading and writing matrices from/to text files

The two functions `mread` and `mwri te` can be used for basic matrix input/output. This can be useful to enable `gretl` to exchange data with other programs.

The `mread` function accepts one string parameter: the name of the (plain text) file from which the matrix is to be read. The file in question may start with any number of comment lines, defined as lines that start with the hash mark, “#”; such lines are ignored. Beyond that, the content must conform to the following rules:

1. The first non-comment line must contain two integers, separated by a space or a tab, indicating the number of rows and columns, respectively.

²This is not the only definition of the SVD: some writers define U as $m \times m$, Σ as $m \times n$ (with k non-zero diagonal elements) and V as $n \times n$.

2. The columns must be separated by spaces or tab characters.
3. The decimal separator must be the dot “.” character.

Should an error occur (such as the file being badly formatted or inaccessible), an empty matrix (see section 17.2) is returned.

The complementary function `mwrite` produces text files formatted as described above. The column separator is the tab character, so import into spreadsheets should be straightforward. Usage is illustrated in Listing 17.1. Matrices stored via the `mwrite` command can be easily read by other programs; the following table summarizes the appropriate commands for reading a matrix `A` from a file called `a.mat` in some widely-used programs.³ Note that the Python example requires that the `numpy` module is loaded.

Program	Sample code
GAUSS	<code>tmp[] = load a.mat; A = reshape(tmp[3:rows(tmp)],tmp[1],tmp[2]);</code>
Octave	<code>fd = fopen("a.mat"); [r,c] = fscanf(fd, "%d %d", "C"); A = reshape(fscanf(fd, "%g", r*c),c,r)'; fclose(fd);</code>
Ox	<code>decl A = loadmat("a.mat");</code>
R	<code>A <- as.matrix(read.table("a.mat", skip=1))</code>
Python	<code>A = numpy.loadtxt('a.mat', skiprows=1)</code>
Julia	<code>A = readdlm("a.mat", skipstart=1)</code>

Optionally, the `mwrite` and `mread` functions can use gzip compression: this is invoked if the name of the matrix file has the suffix “.gz.” In this case the elements of the matrix are written in a single column. Note, however, that compression should not be applied when writing matrices for reading by third-party software unless you are sure that the software can handle compressed data.

17.8 Matrix accessors

In addition to the matrix functions discussed above, various “accessor” strings allow you to create copies of internal matrices associated with models previously estimated. These are set out in Table 17.4.

Many of the accessors in Table 17.4 behave somewhat differently depending on the sort of model that is referenced, as follows:

- Single-equation models: `$sigma` gets a scalar (the standard error of the regression); `$coeff` and `$stderr` get column vectors; `$uhat` and `$yhat` get series.
- System estimators: `$sigma` gets the cross-equation residual covariance matrix; `$uhat` and `$yhat` get matrices with one column per equation. The format of `$coeff` and `$stderr` depends on the nature of the system: for VARs and VECMs (where the matrix of regressors is the same for all equations) these return matrices with one column per equation, but for other system estimators they return a big column vector.
- VARs and VECMs: `$vcv` is not available, but $X'X^{-1}$ (where X is the common matrix of regressors) is available as `$txinv`, such that for VARs and VECMs (without restrictions on α) a `vcv` equivalent can be easily and efficiently constructed as `$sigma ** $txinv`.

³Matlab users may find the Octave example helpful, since the two programs are mostly compatible with one another.

Listing 17.1: Matrix input/output via text files [\[Download ▼\]](#)

```

nulldata 64
scalar n = 3
string f1 = "a.csv"
string f2 = "b.csv"

matrix a = mnormal(n,n)
matrix b = inv(a)

err = mwrite(a, f1)

if err != 0
    fprintf "Failed to write %s\n", f1
else
    err = mwrite(b, f2)
endif

if err != 0
    fprintf "Failed to write %s\n", f2
else
    c = mread(f1)
    d = mread(f2)
    a = c*d
    printf "The following matrix should be an identity matrix\n"
    print a
endif

```

<code>\$coeff</code>	matrix of estimated coefficients
<code>\$compan</code>	companion matrix (after VAR or VECM estimation)
<code>\$jalpha</code>	matrix α (loadings) from Johansen's procedure
<code>\$jbeta</code>	matrix β (cointegration vectors) from Johansen's procedure
<code>\$jvbeta</code>	covariance matrix for the unrestricted elements of β from Johansen's procedure
<code>\$rho</code>	autoregressive coefficients for error process
<code>\$sigma</code>	residual covariance matrix
<code>\$stderr</code>	matrix of estimated standard errors
<code>\$uhat</code>	matrix of residuals
<code>\$vcv</code>	covariance matrix of parameter estimates
<code>\$vma</code>	VMA matrices in stacked form (see section 32.2)
<code>\$yhat</code>	matrix of fitted values

Table 17.4: Matrix accessors for model data

If the accessors are given without any prefix, they retrieve results from the last model estimated, if any. Alternatively, they may be prefixed with the name of a saved model plus a period (`.`), in which case they retrieve results from the specified model. Here are some examples:

```
matrix u = $uhat
matrix b = m1.$coeff
matrix v2 = m1.$vcv[1:2,1:2]
```

The first command grabs the residuals from the last model; the second grabs the coefficient vector from model `m1`; and the third (which uses the mechanism of submatrix selection described above) grabs a portion of the covariance matrix from model `m1`.

If the model in question a VAR or VECM (only) `$compan` and `$vma` return the companion matrix and the VMA matrices in stacked form, respectively (see section 32.2 for details). After a vector error correction model is estimated via Johansen's procedure, the matrices `$jalpha` and `$jbeta` are also available. These have a number of columns equal to the chosen cointegration rank; therefore, the product

```
matrix Pi = $jalpha * $jbeta'
```

returns the reduced-rank estimate of $A(1)$. Since β is automatically identified via the Phillips normalization (see section 33.5), its unrestricted elements do have a proper covariance matrix, which can be retrieved through the `$jvbeta` accessor.

17.9 Namespace issues

Matrices share a common namespace with data series and scalar variables. In other words, no two objects of any of these types can have the same name. It is an error to attempt to change the type of an existing variable, for example:

```
scalar x = 3
matrix x = ones(2,2) # wrong!
```

It is possible, however, to delete or rename an existing variable then reuse the name for a variable of a different type:

```
scalar x = 3
delete x
matrix x = ones(2,2) # OK
```

17.10 Creating a data series from a matrix

Section 17.1 above describes how to create a matrix from a data series or set of series. You may sometimes wish to go in the opposite direction, that is, to copy values from a matrix into a regular data series. The syntax for this operation is

```
series sname = mspec
```

where *sname* is the name of the series to create and *mspec* is the name of the matrix to copy from, possibly followed by a matrix selection expression. Here are two examples.

```
series s = x
series u1 = U[,1]
```

It is assumed that `x` and `U` are pre-existing matrices. In the second example the series `u1` is formed from the first column of the matrix `U`.

For this operation to work, the matrix (or matrix selection) must be a vector with length equal to either the full length of the current dataset, n , or the length of the current sample range, n' . If $n' < n$ then only n' elements are drawn from the matrix; if the matrix or selection comprises n elements, the n' values starting at element t_1 are used, where t_1 represents the starting observation of the sample range. Any values in the series that are not assigned from the matrix are set to the missing code.

17.11 Matrices and lists

To facilitate the manipulation of named lists of series (see Chapter 15), it is possible to convert between matrices and lists. In section 17.1 above we mentioned the facility for creating a matrix from a list of variables, as in

```
matrix M = { listname }
```

That formulation, with the name of the list enclosed in braces, builds a matrix whose columns hold the series referenced in the list. What we are now describing is a different matter: if we say

```
matrix M = listname
```

(without the braces), we get a row vector whose elements are the ID numbers of the series in the list. This special case of matrix generation cannot be embedded in a compound expression. The syntax must be as shown above, namely simple assignment of a list to a matrix.

To go in the other direction, you can include a matrix on the right-hand side of an expression that defines a list, as in

```
list X1 = M
```

where M is a matrix. The matrix must be suitable for conversion; that is, it must be a row or column vector containing non-negative integer values, none of which exceeds the highest ID number of a series in the current dataset.

Listing 17.2 illustrates the use of this sort of conversion to “normalize” a list, moving the constant (variable 0) to first position.

17.12 Deleting a matrix

To delete a matrix, just write

```
delete M
```

where M is the name of the matrix to be deleted.

17.13 Printing a matrix

To print a matrix, the easiest way is to give the name of the matrix in question on a line by itself, which is equivalent to using the `print` command:

```
matrix M = mnormal(100,2)
M
print M
```

You can get finer control on the formatting of output by using the `printf` command, as illustrated in the interactive session below:

Listing 17.2: Manipulating a list [\[Download ▼\]](#)

```

function void normalize_list (matrix *x)
  # If the matrix (representing a list) contains var 0,
  # but not in first position, move it to first position
  if (x[1] != 0)
    scalar k = cols(x)
    loop for (i=2; i<=k; i++)
      if (x[i] == 0)
        x[i] = x[1]
        x[1] = 0
        break
      endif
    endloop
  endif
end function

open data9-7
list X1 = 2 3 0 4
matrix x = X1
normalize_list(&x)
list X1 = x
list X1 print

```

```

? matrix Id = I(2)
matrix Id = I(2)
Generated matrix Id
? print Id
print Id
Id (2 x 2)

1  0
0  1

? printf "%10.3f", Id
1.000    0.000
0.000    1.000

```

For presentation purposes you may wish to give titles to the columns of a matrix. For this you can use the function `cnameset`. The first argument to this function is a matrix and the second can take any of three forms: a string that contains as many space-separated substrings as the matrix has columns; an array of strings (see Section 11.8) of the right length; or a named list of series, whose names will be used as headings. For example,

```

? matrix M = mnormal(3,3)
? cnameset(M, "foo bar baz")
? print M
M (3 x 3)

      foo      bar      baz
1.7102 -0.76072 0.089406
-0.99780 -1.9003 -0.25123
-0.91762 -0.39237 -1.6114

```

Row names may be added via the function `rnameset`, which works in the same way.

17.14 Example: OLS using matrices

Listing 17.3 shows how matrix methods can be used to replicate gretl's built-in OLS functionality.

Listing 17.3: OLS via matrix methods [\[Download ▼\]](#)

```
open data4-1
matrix X = { const, sqft }
matrix y = { price }
matrix b = invpd(X'X) * X'y
print "estimated coefficient vector"
b
matrix u = y - X*b
scalar SSR = u'u
scalar s2 = SSR / (rows(X) - rows(b))
matrix V = s2 * inv(X'X)
V
matrix se = sqrt(diag(V))
print "estimated standard errors"
se
# compare with built-in function
ols price const sqft --vcv
```

Chapter 18

Complex matrices

18.1 Introduction

Native support for complex matrices was added to gretl in version 2019d.¹ Not all of hansl's matrix functions accept complex input, but we have enabled a sizable subset of these functions which should suffice for most econometric purposes.

Complex numbers are not used in most areas of econometrics, but there are a few notable exceptions: among these, complex numbers allow for an elegant treatment of univariate spectral analysis of time series, and become indispensable if you consider multivariate spectral analysis—see for example [Shumway and Stoffer \(2017\)](#). A more recent example is the numerical solution of linear models with rational expectations, which are widely used in modern macroeconomics, for which the complex Schur factorization has become the tool of choice ([Klein, 2000](#)).

A first point to note is that complex values are treated as a special case of the `hansl matrix` type; there's no `complex` type as such. Complex scalars fall under the `matrix` type as 1×1 matrices; the `hansl scalar` type is only for real values (as is the `series` type). A 1×1 complex matrix should do any work you might require of a complex scalar.

Before we proceed to the details of complex matrices in gretl, here's a brief reminder of the relevant concepts and notation. Complex numbers are pairs of the form $a + b i$ where a and b are real numbers and i is defined as the square root of -1 : a is the real part and b the imaginary part. One can specify a complex number either via a and b or in "polar" form. The latter pertains to the complex plane, which has the real component on the horizontal axis and the imaginary component on the vertical. The polar representation of a complex number is composed of the length r of the ray from the origin to the point in question and the angle θ subtended between the positive real axis and this ray, measured counter-clockwise in radians. In polar form the complex number $z = a + b i$ can be written as

$$z = |z| (\cos \theta + i \sin \theta) = |z| e^{i\theta}$$

where $|z| = r = \sqrt{a^2 + b^2}$ and $\theta = \tan^{-1}(b/a)$. The quantity $|z|$ is known as the modulus of z , and θ as its complex "argument" (or sometimes "phase"). The notation \bar{z} is used for the complex conjugate of z : if $z = a + b i$, then $\bar{z} = a - b i$.

18.2 Creating a complex matrix

The standard constructor for complex matrices is the `complex()` function. This takes two arguments, giving the real and imaginary parts respectively, and sticks them together, as in

```
C = complex(A, B)
```

Four cases are supported, as follows.

- A and B are both $m \times n$ real matrices. Then C is an $m \times n$ complex matrix such that $c_{kj} = a_{kj} + b_{kj} i$.
- A and B are both scalars: C is a 1×1 complex matrix such that $c = a + b i$.

¹Prior to that release gretl offered improvised support for some complex functionality; see section [18.7](#) for details.

- A is an $m \times n$ real matrix and B is a scalar: C is an $m \times n$ matrix such that $c_{kj} = a_{kj} + b i$.
- A is a scalar and B is an $m \times n$ real matrix: C is an $m \times n$ matrix such that $c_{kj} = a + b_{kj} i$.

In addition, complex matrices may naturally arise as the result of certain computations.

With both real and complex matrices in circulation, one may wish to determine whether a particular matrix is complex. The function `iscomplex()` can tell you. Passed an identifier, it returns non-zero if it names a complex matrix, 0 if it names a real matrix, or NA otherwise. The non-zero return value is either 1 or 2, with the following interpretation:

- 1 indicates that the matrix is “nominally complex” (each element is represented as having a real part and an imaginary part) but all imaginary parts are zero.
- 2 indicates that at least one element has a non-zero imaginary part.

The following code snippet illustrates the point.

```
matrix z1 = complex(1,0)
scalar a = iscomplex(z1)
matrix z2 = complex(1,1)
scalar b = iscomplex(z2)
printf "a = %d, b = %d\n", a, b
```

The code above gives

```
a = 1, b = 2
```

18.3 Indexation

Indexation of complex matrices works as with real matrices, on the understanding that each element of a complex matrix is a complex pair. So for example `C[i,j]` gets you the complex pair at row *i*, column *j* of C, in the form of a 1×1 complex matrix.

If you wish to access just the real or imaginary part of a given element, or range of elements, you can use the functions `Re()` or `Im()`, as in

```
scalar rij = Re(C[i,j])
```

which gets you the real part of c_{ij} .

In addition the dummy selectors `real` and `imag` can be used to assign to just the real or imaginary component of a complex matrix. Here are two examples:

```
# replace the real part of C with random normals
C[real] = mnormal(rows(C), cols(C))

# set the imaginary part of C to all zeros
C[imag] = 0
```

The replacement must be either a real matrix of the same dimensions as the target, or a scalar.

Further, the `real` and `imag` selectors may be combined with regular selectors to access specific portions of a complex matrix for either reading or writing. Examples:

```
# retrieve the real part of a submatrix of C
matrix R = C[1:2,1:2][real]

# set the imaginary part of C[3,3] to y
C[3,3][imag] = y
```

18.4 Operators

Most of the operators available for working with real matrices are also available for complex ones; this includes the “dot-operators” which work element-wise or by “broadcasting” vectors. Moreover, mixed operands are accepted, as in $D = C + A$ where C is complex and A real; the result, D , will be complex. In such cases the real operand is treated as a complex matrix with an all-zero imaginary part.

The operators *not* defined for complex values are:

- Those that include the inequality tests “>” or “<”, since complex values as such cannot be compared as greater or lesser (though they can be compared as equal or not equal).
- The (real) modulus operator (percent sign), as in $x \% y$ which gives the remainder on division of x by y .

As for real matrices, the transposition operator “'” is available in both unary form, as in $B = A'$, and binary form, as in $C = A'B$ (transpose-multiply). But note that for complex A this means the conjugate transpose, A^H . If you need the non-conjugated transpose you can use `transp()`.

You may wish to note: although none of gretl’s explicit regression functions (or commands) accept complex input you can calculate parameter estimates for a least-squares regression of complex Y ($T \times 1$) on complex X ($T \times k$) via $B = X \setminus Y$.

18.5 Functions

To give an idea of what works, and what doesn’t, for complex matrices, we’ll walk through the `hansl` function-space using the categories employed in gretl’s online “Function reference” (under the Help menu in the GUI program).

Linear algebra

The functions that accept complex arguments are: `cholesky`, `det`, `ldet`, `eigen`, `eigensym` (for Hermitian matrices), `fft`, `ffti`, `inv`, `ginv`, `hdprod`, `mexp`, `mlog`, `qrdecomp`, `rank`, `svd`, `tr`, and `transp`. Note, however, that `mexp` and `mlog` require that the input matrix be diagonalizable, and `cholesky` requires a positive definite Hermitian matrix.

In addition there are the complex-only functions `ctrans`, which gives the conjugate transpose,² and `schur` for the Schur factorization.

Matrix building

Given what was said in section 18.2 above, several of the functions in this category should be thought of as applying to the real or imaginary part of a complex matrix (for example, `ones` and `mnormal`), and are of course usable in that way. However, some of these functions can be applied to complex matrices as such, namely, `diag`, `diagcat`, `lower`, `upper`, `vec`, `vech` and `unvech`.

Please note: when `unvech` is applied to a suitable real vector it produces a symmetric matrix, but when applied to a complex vector it produces a Hermitian matrix.

The only functions *not* available for complex matrices are `cnameset` and `rnameset`. That is, you cannot name the columns or rows of such matrices (although this restriction could probably be lifted without great difficulty).

²The `transp` function gives the straight (non-conjugated) transpose of a complex matrix.

Matrix shaping

The functions that accept complex input are: `cols`, `rows`, `mreverse`, `mshape`, `selifc`, `selifr` and `trimr`.

The functions `msortby`, `sort` and `dsort` are excluded for the reason mentioned in section 18.4.

Statistical

Supported for complex input: `meanc`, `meanr`, `sumc`, `sumr`, `prodc` and `prodr`. And that's all.

Mathematical

In the matrix context, these are functions that are applied element by element. For complex input the following are supported: `log`, `exp` and `sqrt`, plus all of the trigonometric functions with the exception of `atan2`.

In addition there are the complex-only functions `cmod` (complex modulus, also accessible via `abs`), `carg` (complex argument), `conj` (complex conjugate), `Re` (real part) and `Im` (imaginary part). Note that $\text{carg}(z) = \text{atan2}(y, x)$ for $z = x + yi$. Listing 18.1 illustrates usage of `cmod` and `carg`.

Transformations

In this category only two functions can be applied to complex matrices, namely `cum` and `diff`.

18.6 File input/output

Complex matrices are stored and retrieved correctly in the XML serialization used for gretl session files (*.gretl).

The functions `mwrite` and `mread` work in two modes: binary mode if the filename ends with “.bin” and text mode otherwise. Both modes handle complex matrices correctly if both the writing and the reading are to be done by gretl, but for exchange of data with “foreign” programs text mode will *not* work for complex matrices as a whole. The options are:

- In text mode, use `mwrite` and `mread` on the two parts of a complex matrix separately, and reassemble the matrix in the target program.
- Use binary mode (on the whole matrix), if this is supported for the given foreign program.

At present binary mode transfer of complex matrices is supported for octave, python and julia. Listing 18.2 shows some examples: we export a complex matrix to each of these programs in turn; calculate its inverse in the foreign program; then verify that the result as imported back into gretl is the same as that calculated in gretl.

18.7 Backward (in)compatibility

Prior to version 2019d gretl did not provide native support for complex matrices. It did, however, offer an improvised representation of such matrices for certain restricted purposes, taking the form of an expanded regular gretl matrix with real values and imaginary parts in odd- and even-numbered columns, respectively. The functions `fft`, `eigegen` and `polroots` returned matrices in this special form, and the functions `cmult` and `cdiv` operated on such matrices.

As of version 2022b, `fft` and `polroots` have been redefined to work with “proper” complex matrices as described above. The other affected functions are deprecated and will be removed or redefined in a subsequent release. If you have any hansl code using the legacy representation the following brief porting guide may be helpful.

Listing 18.1: Variant representations of complex numbers. We picked 8 points on the unit circle in the complex plane, so their modulus is constant and equal to 1. The Polar matrix below shows that the complex argument is expressed in radians; multiplying by $180/\pi$ gives degrees. The chk matrix verifies that we can retrieve the original representation of the complex values from the polar form in either of the two ways mentioned at the start of the chapter: $z = |z| (\cos \theta + i \sin \theta)$ or $z = |z| e^{i\theta}$. [\[Download ▼\]](#)

```
# complex values in a + b*i form
scalar rp5 = sqrt(0.5)
matrix A = {1, rp5, 0, -rp5, -1, -rp5, 0, rp5}'
matrix B = {0, rp5, 1, rp5, 0, -rp5, -1, -rp5}'
matrix Z = complex(A, B)

# calculate modulus and argument
matrix zmod = cmod(Z)
matrix theta = carg(Z)
matrix Polar = zmod ~ theta ~ (theta * 180/$pi)
cnameset(Polar, "modulus radians degrees")
printf "%12.4f\n", Polar

# reconstitute the original Z matrix in two ways
matrix Z1 = zmod .* complex(cos(theta), sin(theta))
matrix Z2 = zmod .* exp(complex(0, theta))
matrix chk = Z ~ Z1 ~ Z2
print chk
```

Printing of Polar and chk

modulus	radians	degrees
1.0000	0.0000	0.0000
1.0000	0.7854	45.0000
1.0000	1.5708	90.0000
1.0000	2.3562	135.0000
1.0000	3.1416	180.0000
1.0000	-2.3562	-135.0000
1.0000	-1.5708	-90.0000
1.0000	-0.7854	-45.0000

1.00000 + 0.00000i	1.00000 + 0.00000i	1.00000 + 0.00000i
0.70711 + 0.70711i	0.70711 + 0.70711i	0.70711 + 0.70711i
0.00000 + 1.00000i	0.00000 + 1.00000i	0.00000 + 1.00000i
-0.70711 + 0.70711i	-0.70711 + 0.70711i	-0.70711 + 0.70711i
-1.00000 + 0.00000i	-1.00000 + 0.00000i	-1.00000 + 0.00000i
-0.70711 - 0.70711i	-0.70711 - 0.70711i	-0.70711 - 0.70711i
0.00000 - 1.00000i	0.00000 - 1.00000i	0.00000 - 1.00000i
0.70711 - 0.70711i	0.70711 - 0.70711i	0.70711 - 0.70711i

Listing 18.2: Exporting and importing complex matrices [\[Download ▼\]](#)

```
set seed 34756
matrix C = complex(mnormal(3,3), mnormal(3,3))
D = inv(C)

mwrite(C, "C.bin", 1)

foreign language=octave
    C = gretl_loadmat('C.bin');
    gretl_export(inv(C), 'oct_D.bin');
end foreign

oct_D = mread("oct_D.bin", 1)
eval D - oct_D

foreign language=python
    import numpy as np
    C = gretl_loadmat('C.bin')
    gretl_export(np.linalg.inv(C), 'py_D.bin')
end foreign

py_D = mread("py_D.bin", 1)
eval D - py_D

foreign language=julia
    C = gretl_loadmat("C.bin")
    gretl_export(inv(C), "jl_D.bin")
end foreign

jl_D = mread("jl_D.bin", 1)
eval D - jl_D
```

Porting old complex code

`cmult` and `cdiv`: These functions performed element-wise multiplication and division of complex column vectors in the old two-column form. The statements

```
# old element-wise operations
c1 = cmult(a1, b1)
d1 = cdiv(a1, b1)
```

can be updated as

```
# new element-wise operations
c2 = a2 .* b2
d2 = a2 ./ b2
```

(where `a2` and `b2` are new-style complex vectors or matrices). The following statements

```
c3 = a2 * b2
d3 = a2 / b2
```

are also valid but have different effects, the first performing standard (rather than element-wise) multiplication of matrices (complex or real) and the second performing “right division”, equivalent to `a2 * inv(b2)`. Note that while the return value from `cmult` and `cdiv` could be either a real vector or a (two column) complex vector, the new-style operations yield a nominally complex result if at least one of the operands is complex, even if the result has an all-zero imaginary part.

A piece of code that appears in some contexts (such as calculation of a periodogram) is as follows: given a complex vector, `v`, compute a vector `w` holding the squared moduli of the elements of `v`. The old-style code to accomplish this was

```
# legacy: v has two columns
w = sumr(v.^2)
```

and the new replacement is

```
# current: v has a single complex column
w = abs(v).^2
```

where `abs` gives the complex modulus.

eigen: Most uses of this legacy function simply retrieve the eigenvalues of a general (that is, not symmetric) matrix, and do not exploit the option of retrieving eigenvectors. In that context it is straightforward to substitute a call to the new function `eigen`. The only point to note is that `eigen` returns a new-style complex vector; if you have need to convert this to the legacy representation you can use the `cswitch` function, which is documented in the *Gretl Command Reference*. In brief, the following code gives you the legacy equivalent of a new-style complex vector `v`: `newvec`.

```
if v[imag] == 0
    oldv = v[real]
else
    oldv = cswitch(v, 2)
endif
```

polroots: This function now returns a new-style complex vector. As with `eigen`, you can use `cswitch` to convert the vector if necessary.

Chapter 19

Calendar dates

19.1 Introduction

Any software that aims to handle dates and times must have a good built-in calendar. Gretl offers several functions to handle date and time information, which are documented in the *Gretl Command Reference*. To facilitate their effective use this chapter lists the various possibilities for storing dates and times and discusses ways of converting between variant representations. Our main focus in this chapter is dates as such (year, month and day) but we add some discussion of time-of-day where relevant. A final section addresses the somewhat arcane issue of handling historical dates on the Julian calendar.

First of all it may be useful to distinguish two contexts:

- You have a time-series dataset in place, or a panel dataset with a well-defined time dimension.
- You have no such dataset in place, or perhaps no dataset at all.

While you can work with dates in the second case, in the first case you have extra resources.

You probably know that if you open a dataset that is in fact time series but gretl has not immediately recognized that fact, you can rectify matters by use of the `setobs` command, or via the menu item `/Data/Dataset structure` in the gretl GUI. You may also know that with a panel dataset you can impose a definite dating and frequency in its time dimension (if appropriate)—again, via the `setobs` command but with the `--panel-time` option.

In what follows we state if a relevant function or accessor requires a time-series dataset or well-defined panel-data time; otherwise you can assume it does not carry such a requirement.

19.2 Date and time representations

In gretl there is more than one way to encode a date such as “May 26th, 1993”. Some are more intuitive, some less obvious from a human viewpoint but easier to handle for an algorithm. The basic representations we discuss here are:

1. the three-numbers approach
2. date as string
3. the ISO 8601 standard
4. the epoch day
5. Unix time (seconds)

We first explain what these representations are, then explain how to convert between them.

The three-numbers approach

Since a date (without regard to intra-day detail) basically consists of three numbers, it can obviously be encoded in precisely that way. For example the date “May 26th, 1993” can be stored as

```
scalar y = 1993
scalar m = 5
scalar d = 26
```

Gretl's multiple-element objects can be used to extend this approach, for example by using a 3-element vector for year, month and day, or a 3-column matrix for storing as many dates as desired. If you wish to store dates as series in your dataset this approach would lead you to use three series, possibly grouping them into a list, as in

```
nulldata 60
setobs 7 2020-01-01
series y = $obsmajor
series m = $obsminor
series d = $obsmicro
list DATE = y m d
```

This example above will generate daily dates for January and February 2020. Note that use of the `$obsm*` accessors requires a time-series dataset, and `$obsmicro` in particular requires daily data. See Section 19.5 for details.

Some CSV files represent dates in this sort of broken-down format, with various conventions on the ordering of the three components.

Date as string

To a human being, this may seem the most natural choice. The string “26/6/1953” is pretty much unambiguous. But using such a format for machine processing can be problematic due to differing conventions regarding the separators between day, month and year, as well as the order in which the three pieces of information are arranged. For example, “2/6/1953” is *not* unambiguous: it will “naturally” be read differently by Europeans and Americans. This can be a problem with CSV files found “in the wild”, containing arbitrarily formatted dates. Therefore gretl provides fairly comprehensive functionality for converting dates of this sort into more manageable formats.

The ISO 8601 standard

Among other things, the ISO 8601 standard provides two representations for a daily date: the “basic” representation, which uses an 8-digit integer, and the “extended” representation, which uses a 10-character string.

In the basic version the first four digits represent the year, the middle two the month and the rightmost two the day, so that for example 20170219 indicates February 19th, 2017. The extended representation is similar except that the date is a string in which the items are separated by hyphens, so the same date would be represented as “2017-02-19”.

In several contexts ISO 8601 dates are privileged by gretl: the ISO format as taken as the default and you need to supply an additional function argument or take extra steps if the representation is non-standard.

Using series and/or matrices to store ISO 8601 basic dates is perfectly straightforward.

Epoch days

In gretl an “epoch day” is an unsigned 32-bit integer which represents a date as the number of days since January 1, 1 AD (that is, the first day of the Common Era), on the proleptic Gregorian calendar.¹ For example, 1993-05-26 corresponds to 727709.²

¹The term “proleptic,” as applied to a calendar, indicates that it is extrapolated backwards or forwards relative to its period of actual historical use.

²This representation derives from the astronomers’ “Julian day” which is also a count of days since a benchmark, namely January 1, 4713 BC, at which time certain astronomical cycles were aligned.

This is the convention used by the GLib library, on which gretl depends for much of its calendrical calculation. Since an epoch day is an unsigned integer, neither GLib nor gretl supports dates “BC”, or prior to the Common Era.

This representation has several advantages. Like ISO 8601 basic, it lends itself naturally to storing dates as series. Compared to ISO 8601, it has the disadvantage of not being readily understandable by humans, but to compensate for that it makes it very easy to determine the length of a range of dates. ISO basic dates can be used for comparison (which of two dates, on a given calendar, refers to a later day?) but with epoch days one can carry out fully-fledged “dates arithmetic.” Epoch days are always consecutive by construction, but 8-digit basic dates are consecutive only within a given month.³ For more on arithmetic with epoch days see Section 19.4.

Unix seconds

In this representation—the cornerstone of date and time handling on Unix-like systems—time is the number of seconds since midnight at the start of 1970 according to Coordinated Universal Time (UTC).⁴ This format is therefore ideal for storing fine-grained information, including time of day as well as date.

This representation is not transparent to humans (for example, the number 123456789 corresponds to the start of Thursday, 29 Nov 1973) but again it lends itself naturally to calculation. Since Unix seconds are hard-wired to UTC a given value will correspond to different times, and possibly different dates, if evaluated in different time zones; we expand on this point below.

19.3 Converting between representations

To support conversion between different representations, gretl provides several dedicated functions, although in some cases conversion can be carried out by using general-purpose functions. Figure 19.1 displays a summary: solid lines represent dedicated functions, while dashed lines indicate that no special function is needed. Numerical formats are depicted as boxes and string formats as ovals. For a full description of the functions referenced in the figure, see the *Gretl Command Reference*. In the rest of this section we discuss several cases of conversion with the help of examples.

Strings and three-number dates

As indicated in Figure 19.1, converting between date strings and the three-number representation does not require date-specific functions. The two “generic” functions that can be used for this purpose are `printf` and `sscanf`. Here’s how: suppose you encode a date via the three scalars `d=30`, `m=10` and `y=1983`. You can use `printf` to turn it into a date string rather easily, as in

```
eu_s = printf("%d/%m/%y", d, m, y)
us_s = printf("%m/%d/%y", m, d, y)
```

where the two strings follow the European and US conventions, respectively.

The reverse operation, using the `sscanf` function, is a little trickier (see the *Gretl Command Reference* for a full illustration). The string `s="1983-10-30"` can be broken down into three scalars as

```
scalar d m y
n = sscanf(s, "%d-%d-%d", y, m, d)
```

³In fact, they advance by 101 minus the number of days in the previous month at the start of each month other than January, and by 8870 at the start of each year.

⁴UTC is, to a first approximation, the time such that the Sun is at its highest point at noon over the prime meridian, the line of 0° longitude, which as a matter of historical contingency runs through Greenwich, England.

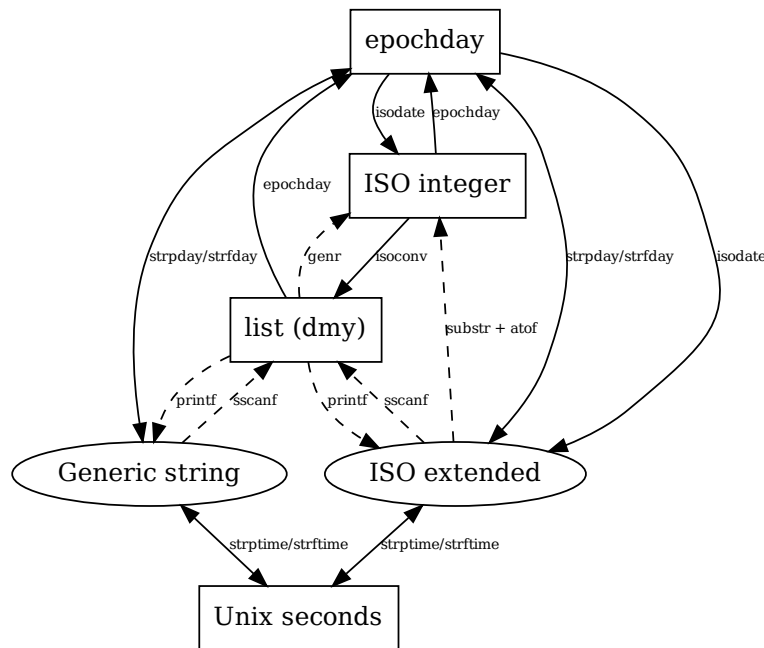


Figure 19.1: Conversions between different date formats

Note that in this case “%d” in the format specification does not mean “day”, but rather “decimal integer”, which is why there are three instances. Alternatively, one could have used a 3-element vector, as in

```
matrix date = zeros(1,3)
n = sscanf(s, "%d-%d-%d", &date[1], &date[2], &date[3])
```

Decomposing a series of “basic” dates

To generate from a series of dates in ISO 8601 basic format distinct series holding year, month and day, the function `isoconv` can be used. This function should be passed the original series followed by “pointers to” the series to be filled out. For example, if we have a series named `dates` in the prescribed format we might do

```
series y, m, d
isoconv(dates, &y, &m, &d)
```

This is mostly just a convenience function: provided the `dates` input is valid on the (possibly proleptic) Gregorian calendar it is equivalent to:

```
series y = floor(dates/10000)
series m = floor((dates-10000*y)/100)
series d = dates - 10000*y - 100*m
```

However, there is some “value added”: `isoconv` checks the validity of the `dates` input. If the implied year, month and day for any `dates` observation do not correspond to a valid date, then all the derived series will have value NA at that observation.

The inverse operation is trivial:

```
series dates = 10000 * y + 100 * m + d
```

The use of series here means that such operations require that a dataset is in place, but although they would most naturally occur in the context of a time-series dataset they could equally well occur with an undated dataset, since an ISO 8601 basic value is just a numeric value (with some restrictions) and such values do not have to appear in chronological order.

String/numeric conversions: dedicated functions

The primary means of converting between string and scalar numeric representations of dates and times is provided by two pairs of functions, `strptime/strftime` and `strpday/strfdday`. The first of each pair takes string input and outputs a numeric value, and the second performs the inverse operation, as shown in Table 19.1. With the first pair, the numeric value is Unix seconds; with the second it's an epoch day. Numeric values are always relative to UTC, and string values are (by default, at least) always relative to local time.

<i>function</i>	<i>input</i>	<i>output</i>
<code>strptime</code>	date/time string + format	Unix seconds
<code>strftime</code>	Unix seconds + format	date/time string
<code>strpday</code>	date string + format	epoch day
<code>strfdday</code>	epoch day + format	date string

Table 19.1: String \longleftrightarrow numeric date/time conversions

Before moving on, let's be clear on what we mean by "local time". Generically, this is time according to the local time zone (with or without a "Daylight saving" or "Summer" adjustment depending on the time of year). In a computing context we have to be more specific: the "local" time zone is whatever is set as such via the operating system (and possibly adjusted via an environment variable) on the host computer. It will usually be the same as the geographically local zone but there's nothing to stop a user making a different setting.

Dates as string-valued series

It often happens that CSV files contain date information stored as strings. Take for example a file containing earthquake data like the following:⁵

Date	Time	Latitude	Longitude	Magnitude
"01/02/1965"	"13:44:18"	19.246	145.616	6.0
"01/04/1965"	"11:29:49"	1.863	127.352	5.8
"01/05/1965"	"18:05:58"	-20.579	-173.972	6.2
"01/08/1965"	"18:49:43"	-59.076	-23.557	5.8
"01/09/1965"	"13:32:50"	11.938	126.427	5.8
"01/10/1965"	"13:36:32"	-13.405	166.629	6.7
"01/12/1965"	"13:32:25"	27.357	87.867	5.9
"01/15/1965"	"23:17:42"	-13.309	166.212	6.0

Suppose we want to convert the Date column to epoch days. Note that the date format follows the American convention month/day/year. The simplest way to accomplish the task is shown in Listing 19.1, where we assume that the data file is named `earthquakes.csv`. Note that the `--all-cols` option is wanted here, so that `gretl` treats Dates as a string-valued series rather than just a source of time-series information. For good measure we show how to add an ISO 8601 date series.

⁵See <https://www.kaggle.com/datasets/usgs/earthquake-database> for the dataset of which this is an extract.

Listing 19.1: Converting a string-valued date series to epoch day

```
open earthquakes.csv --all-cols
series eday = strpday(Date, "%m/%d/%Y")
series isodates = strfday(eday, "%Y-%m-%d")
print Date eday isodates -o
```

Output:

	Date	eday	isodates
1	01/02/1965	717338	1965-01-02
2	01/04/1965	717340	1965-01-04
3	01/05/1965	717341	1965-01-05
4	01/08/1965	717344	1965-01-08
5	01/09/1965	717345	1965-01-09
6	01/10/1965	717346	1965-01-10
7	01/12/1965	717348	1965-01-12
8	01/15/1965	717351	1965-01-15

Alternatively, one might like to convert the Date and Time columns jointly to Unix seconds. This can be done by sticking the two strings together at each observation and calling `strptime` with a suitable format, as follows:

```
series usecs # Unix seconds
loop i=1..$nobs
  usecs[i] = strptime(Date[i] ~ Time[i], "%m/%d/%Y%H:%M:%S")
endloop
```

Unix seconds and time zones

At 8:46 in the morning of September 11, 2001, an airliner crashed into the North Tower of the World Trade Center in New York. Relative to what time zone is that statement correct? Eastern Daylight Time (EDT), of course. Unless we have special reason to do otherwise we report the time of an event relative to the time zone in which it occurred; and if we do otherwise we need to state the metric we're using (for example, one might say that this event occurred at 2001-09-11 12:46 UTC).

Now consider the following script:

```
date = "2001-09-11 08:46"
format = "%Y-%m-%d %H:%M"
usecs = strptime(date, format)
check = strftime(usecs, format)
printf "Unix time %d\n", usecs
printf "original: %s\n", date
printf "recovered: %s\n", check
```

Run this script in any time zone you like and the last line of output will read

```
recovered: 2001-09-11 08:46
```

The `usecs` value will differ by time zone—for example it'll be 1000212360 under Eastern Daylight Time but 1000194360 under Central European Time—but this difference “cancels out” in recovering the original time via `strftime`.

So far, so good. But suppose I write a script in which I store the date as Unix seconds, with my laptop's clock set to EDT:


```
usecs = 1000212360
date = strftime(usecs, "%Y-%m-%d %H:%M")
print date
```

Running this script under EDT will again print out “2001-09-11 08:46”, but if I take my laptop to Italy in June, set its clock to the local time, and rerun the script, I’ll get

```
2001-09-11 14:46
```

Is that a problem? Well, 14:46 is indeed the time in Italy when it’s 08:46 in New York (with both zones in their Summer variants); it’s a problem only if you want to preserve the locality of the original time. To do that you need to give time-zone information to both `strptime` and `strftime`. This is illustrated in Listing 19.2.

Listing 19.2: Date/time invariance with respect to current time zone

```
string date = "2001-09-11 08:46 -0400"
string format = "%Y-%m-%d %H:%M %Z"
usecs = strptime(date, format)
printf "Unix time %d\n", usecs
```

In the code above we specify the time zone in `date` using `-0400`, meaning 4 hours behind UTC, which is correct when Daylight Saving time is in force in the Eastern US. And we match this with the “%Z” specifier in `format`. As a result, regardless of the time zone in which the code is run the Unix time value will be 1000212360. Then we come to unpacking that value:

```
date = strftime(1000212360, "%Y-%m-%d %H:%M %Z", -4*3600)
print date
```

Here we use the third, optional argument to `strftime` to supply the offset in seconds of EDT relative to UTC. Having told `strptime` the time zone, why do we need this? Well, remember that Unix time is just a scalar value, always relative to UTC: it cannot store time-zone information. Anyway, the result is that this code will print 2001-09-11 08:46 -0400 regardless of where and when it is executed.

Some additional comments are in order. First, spaces matter in parsing the `strptime` arguments: they must match between the date and format strings. In the example above we inserted spaces before `-0400` and `%Z`. We could have omitted both spaces, but not just one of them. Second, the C standard does not require that `strptime` and `strftime` know anything about time zones; the extensions used in this example are supported by GLib functionality.

19.4 Epoch day arithmetic

Given the way epoch days are defined, they provide a useful tool for checking whether daily data are complete. Suppose we have what purport to be 7-day daily data with a starting date of 2015-01-01 and an ending date of 2016-12-31. How many observations should there be?

```
ed1 = epochday(2015,1,1)
ed2 = epochday(2016,12,31)
n = ed2 - ed1 + 1
```

We find that there should be $n = 731$ observations; if there are fewer there’s something missing. If the data are supposed to be on a 5-day week (skipping Saturday and Sunday) or 6-day week (skipping Sunday alone) the calculation is more complicated; in this case we can use the `dayspan` function, providing as arguments the epoch-day values for the first and last dates and the number of days per week:

```
ed1 = epochday(2015,1,1)
ed2 = epochday(2016,12,30)
n = dayspan(ed1, ed2, 5)
```

We discover that there were $n = 522$ weekdays in this period.

The `dayspan` function can also be helpful if you wish to construct a suitably sized “empty” daily dataset prior to importing data from a third-party database (for example, stock prices from Yahoo). Say the data to be imported are on a 5-day week and you want the range to be from 2000-01-03 (the first weekday in 2000) to 2020-12-30 (a Wednesday). Here’s how one could initialize a suitable “host” dataset:

```
ed1 = epochday(2000,1,3)
ed2 = epochday(2020,12,30)
n = dayspan(ed1, ed2, 5)
nulldata n
setobs 5 2000-01-03
```

Another use of arithmetic using epoch days is constructing a sequence of dates of non-standard frequency. Suppose you want a biweekly series including alternate Saturdays in 2023. Here’s a solution:

```
nulldata 26
setobs 1 1 --special-time-series
series eday
eday[1] = epochday(20230107) # the first Saturday
loop i=2..$nobs
    eday[i] = eday[i-1] + 14
endloop
series dates = strfday(eday, "%Y-%m-%d")
```

19.5 Other accessors and functions

Accessors

Gretl offers various accessors for generating dates. One is `$now`, which returns the current date/time as a 2-element vector. The first element is Unix seconds and the second an epoch day (see Section 19.2). This is always available regardless of the presence or absence of a dataset.

When a time-series dataset is open, up to four accessors are available to retrieve observation dates as numeric series. First there is `$obsdate`, which returns ISO 8601 basic dates. If the frequency is annual, quarterly or monthly these dates represent the first day of the period in question; if the frequency is hourly this accessor is not available. Then there’s a set of up to three accessors, `$obsmajor`, `$obsminor` and `$obsmicro`. The availability and interpretation of these values depends on the character of the dataset, as shown in Table 19.2. For reference, the “constructor” column shows the argument that should be supplied to the `setobs` command to impose each frequency on a dataset, assuming it starts on January 1, 1990.

The hourly frequency is not fully supported by gretl’s calendrical apparatus. But an epoch day value can be used to set the starting day for an hourly time series, as exemplified in Table 19.2 (726468 for 1990-01-01). One could then construct a string-valued hourly date/time series in this way:

```
series day = strptime(isodate($obsmajor))
series usecs = day + 3600 * ($obsminor - 1) # Unix seconds
series tstrs = strftime(usecs, "%Y-%m-%d %H:%M")
```

When a panel dataset is open and its time dimension is specified (see Section 19.1 and the documentation for the `setobs` command), `$obsdate` works as described for time-series datasets. But

frequency	description	constructor	\$obsmajor	\$obsminor	\$obsmicro
1	annual	1 1990	year	-	-
4	quarterly	4 1990:1	year	quarter	-
12	monthly	12 1990:01	year	month	-
5, 6, 7	daily	<i>n</i> 1990-01-01	year	month	day
52	weekly	52 1990-01-01	year	month	day
24	hourly	24 726468:01	day	hour	-

Table 19.2: Calendrical frequencies and accessors

`$obsmajor` and `$obsminor` do not refer to the time dimension; rather they give the 1-based indices of the individuals and time periods, respectively. And `$obsmicro` is not available.

Miscellaneous functions

Besides conversion, several other calendrical functions are available:

monthlen given month and year, returns the length of the month in days (optionally ignoring weekends).

weekday given a date as year, month and day (or ISO 8601 basic), returns a number from 0 (Sunday) to 6 (Saturday) corresponding to day of the week.

juldate given an epoch day, returns the corresponding date on the Julian calendar (see Section 19.6 below).

dayspan given two epoch days, calculates their distance, optionally taking weekends into account.

easterday given the year, returns the date of Easter on the Gregorian calendar.

isoweek given a date as year, month and day, returns the progressive number of the week within that year as per the ISO 8601 specification.

19.6 Working with pre-Gregorian dates

Working with dates is fairly straightforward in the current era, with the Gregorian calendar used universally for the dating of socioeconomic observations. It is not so straightforward, however, when dealing with historical data recorded prior to the adoption of the Gregorian calendar in place of the Julian, an event which first occurred in the principal Catholic countries in 1582 but which took place at different dates in different countries over a span of several centuries.

Gretl, like most data-oriented software, uses the Gregorian calendar by default for all dates, thereby ensuring that dates are all consecutive (the latter being a requirement of the ISO 8601 standard for dates and times).

As readers probably know, the Julian calendar adds a leap day (February 29) on each year that is divisible by 4 with no remainder. But this over-compensates for the fact that a 365-day year is too short to keep the calendar synchronized with the seasons. The Gregorian calendar introduced a more complex rule which maintains better synchronization, namely, each year divisible by 4 with no remainder is a leap year *unless* it's a centurial year (e.g. 1900) in which case it's a leap year only if it is divisible by 400 with no remainder. So the years 1600 and 2000 were leap years on both calendars, but 1700, 1800, and 1900 were leap years only on the Julian calendar. While the average length of a Julian year is 365.25 days, the Gregorian average is 365.2425 days.

The fact that the Julian calendar inserts leap days more frequently means that the Julian date progressively (although very slowly) falls behind the Gregorian date. For example, February 18

2017 (Gregorian) is February 5 2017 on the Julian calendar. On adoption of the Gregorian calendar it was therefore necessary to skip several days. In England, where the transition occurred in 1752, Wednesday September 2 was directly followed by Thursday September 14.

In comparing calendars one wants to refer to a given day in terms that are not specific to either calendar—but how to define a “given day”? This is accomplished by a count of days following some definite temporal benchmark. As described in Section 19.2, `gretl` uses days since the start of 1 AD, which we call epoch days.

In this section we address the problem of constructing within `gretl` a calendar which agrees with the actual historical calendar prior to the switch to Gregorian dating. Most people will have no use for this, but researchers working with archival data may find it helpful: it would be tricky and error-prone to enter on the Gregorian calendar data whose dates are given on the Julian at source.

In order to represent Julian dates, `Gretl` uses two basic tools: one is the `juldate` function, which converts a Gregorian epoch day into an ISO8601-like integer and the convention that for some functions, a negative value where a year is expected acts as a “Julian calendar flag”.

So, for example, the following code fragment,

```
edg = epochday(1700,1,1)
edj = epochday(-1700,1,1)
```

produces `edg = 620548` and `edj = 620558`, indicating that the two calendars differed by 10 days at the point in time known as January 1, 1700, on the proleptic Gregorian calendar.

Taken together with the `isodate` and `juldate` functions (which each take an epoch day argument and return an ISO 8601 basic date on, respectively, the Gregorian and Julian calendars), `epochday` can be used to convert between the two calendars. For example, what was the date in England (still on the Julian calendar) on the day known to Italians as June 26, 1740 (Italy having been on the Gregorian calendar since October 1582)?

```
ed = epochday(1740,6,26)
english_date = juldate(ed)
printf "%d\n", english_date
```

We find that the English date was 17400615, the 15th of June. Working in the other direction, what Italian date corresponded to the 5th of November, 1740, in England?

```
ed = epochday(-1740,11,5)
italian_date = isodate(ed)
printf "%d\n", italian_date
```

Answer: 17401116; Guy Fawkes night in 1740 occurred on November 16 from the Italian point of view.

We’ll now consider the trickiest case, namely a calendar which includes the day on which the Julian to Gregorian switch occurred. If we can handle this, it should be relatively simple to handle a purely Julian calendar. Our illustration will be England in 1752 (a similar analysis could be done for Spain in 1582 or Greece in 1923). A solution is presented in Listing 19.3.

The first step is to find the epoch day corresponding to the Julian date 1752-01-01 (which turns out to be 639551). Then we can create a series of epoch days, from which we get both Julian and Gregorian dates for 355 days starting on epoch day 639551. Note, 355 days because this was a short year: it was a leap year, but 11 days were skipped in September in making the transition to the Gregorian calendar. We can then construct a series, `hcal`, which switches calendar at the right historical point.

Notice that although the series `hcal` contains the correct historical calendar (in “basic” form), the observation labels (in the first column of the output) are still just index numbers. It may be preferable to have historical dates in that role. To achieve this we can decompose the `hcal` series into

Listing 19.3: Historical calendar for Britain in 1752 [\[Download ▼\]](#)

```
# 1752 was a short year on the British calendar!
nulldata 355
# give a negative year to indicate Julian date
ed0 = epochday(-1752,1,1)
# consistent series of epoch day values
series ed = ed0 + index - 1
# Julian dates as YYYYMMDD
series jdate = juldate(ed)
# Gregorian dates as YYYYMMDD
series gdate = isodate(ed)
# Historical: cut-over in September
series hcal = ed > epochday(-1752,9,2) ? gdate : jdate
# And let's take a look
print ed jdate gdate hcal -o
```

Partial output:

	ed	jdate	gdate	hcal
1	639551	17520101	17520112	17520101
2	639552	17520102	17520113	17520102
...				
245	639795	17520901	17520912	17520901
246	639796	17520902	17520913	17520902
247	639797	17520903	17520914	17520914
248	639798	17520904	17520915	17520915
...				
355	639905	17521220	17521231	17521231

year, month and day, then use the `genr` markers apparatus (see chapter 4). Here's additional code to do this job and show the result.

```
series y, m, d
isoconv(hcal, &y, &m, &d)
genr markers = "%04d-%02d-%02d", y, m, d
print ed jdate gdate hcal -o
```

Year numbering

A further complication in dealing with archival data is that the year number has not always been advanced on January 1; for example in Britain prior to 1752, March 25 was taken as the start of the new year. On `gretl`'s calendar (whether Julian or Gregorian) the year number *always* advances on January 1, but it's possible to construct observation markers following the old scheme. This is illustrated for the year 1751 (as we would now call it) in Listing 19.4.

Listing 19.4: Historical calendar for England in 1751 [\[Download ▼\]](#)

```
nulldata 365 # a common year
ed0 = epochday(-1751,1,1)
ed1 = epochday(-1751,3,25)
series ed = ed0 + index - 1
series jdate = juldate(ed)
series y, m, d
isoconv(jdate, &y, &m, &d)
y = ed < ed1 ? y-1 : y
genr markers = "%04d-%02d-%02d", y, m, d
print index -o
```

Partial output:

1750-01-01	1
1750-01-02	2
1750-01-03	3
...	
1750-03-23	82
1750-03-24	83
1751-03-25	84
1751-03-26	85
...	
1751-12-31	365

Day of week and length of month

Two of the functions described in Section 19.5, that by default operate on the Gregorian calendar, can be induced to work on the Julian by the trick mentioned above, namely giving the negative of the year. These are `weekday` (which takes arguments year, month and day) and `monthlen` (which takes arguments month, year and days per week). Thus for example

```
eval weekday(-1700,2,29)
```

gives 4, indicating that Julian February 29, 1700 was a Thursday. And

```
eval monthlen(2,-1900,5)
```

gives 21, indicating that there were 21 weekdays in Julian February 1900.

Chapter 20

Mixed-frequency data

20.1 Basics

In some cases one may want to handle data that are observed at different frequencies, a facility known as “MIDAS” (Mixed Data Sampling). A common pairing includes GDP, usually available quarterly, and industrial production, often available monthly. The most common context when this feature is required is specification and estimation of MIDAS models (see Chapter 41), but other cases are possible.

A gretl dataset formally handles only a single data frequency, but we have adopted a straightforward means of representing nested frequencies: a higher frequency series x_H is represented by a set of m series, each holding the value of x_H in a sub-period of the “base” (lower-frequency) period (where m is the ratio of the higher frequency to the lower).

This is most easily understood by means of an example. Suppose our base frequency is quarterly and we wish to include a monthly series in the analysis. Then a relevant fragment of the gretl dataset might look as shown in Table 20.1. Here, `gdpc96` is a quarterly series while `indpro` is monthly, so $m = 12/4 = 3$ and the per-month values of `indpro` are identified by the suffix `_mn`, $n = 3, 2, 1$.

	gdpc96	indpro_m3	indpro_m2	indpro_m1
1947:1	1934.47	14.3650	14.2811	14.1973
1947:2	1932.28	14.3091	14.3091	14.2532
1947:3	1930.31	14.4209	14.3091	14.2253
1947:4	1960.70	14.8121	14.7562	14.5606
1948:1	1989.54	14.7563	14.9240	14.8960
1948:2	2021.85	15.2313	15.0357	14.7842

Table 20.1: A slice of MIDAS data

To recover the actual monthly time series for `indpro` one must read the three relevant series right-to-left by row. At first glance this may seem perverse, but in fact it is the most convenient setup for MIDAS analysis. In such models, the high-frequency variables are represented by lists of lags, and of course in econometrics it is standard to give the most recent lag first (x_{t-1}, x_{t-2}, \dots).

One can construct such a dataset manually from “raw” sources using `hansl`’s matrix-handling methods or the `join` command (see Section 20.6 for illustrations), but we have added native support for the common cases shown below.

<i>base frequency</i>	<i>higher frequency</i>
annual	quarterly or monthly
quarterly	monthly or daily
monthly	daily

The examples below mostly pertain to the case of quarterly plus monthly data. Section 20.6 has details on handling of daily data.

A mixed-frequency dataset can be created in either of two ways: by selective importation of series from a database, or by creating two datasets of different frequencies then merging them.

Importation from a database

Here's a simple example, in which we draw from the `fedstl` (St Louis Fed) database which is supplied in the gretl distribution:

```
clear
open fedstl.bin
data gdpc96
data indpro --compact=spread
store gdp_indpro.gdt
```

Since `gdpc96` is a quarterly series, its importation via the `data` command establishes a quarterly dataset. Then the MIDAS work is done by the option `--compact=spread` for the second invocation of `data`. This “spreads” the series `indpro`—which is monthly at source—into three quarterly series, exactly as shown in Table 20.1.

Merging two datasets

In this case we consider an Excel file provided by Eric Ghysels in his MIDAS Matlab Toolbox,¹ namely `mydata.xlsx`. This contains quarterly real GDP in Sheet1 and monthly non-farm payroll employment in Sheet2. A hansl script to build a MIDAS-style file named `gdp_payroll_midas.gdt` is shown in Listing 20.1.

Listing 20.1: Building a gretl MIDAS dataset via merger

```
# sheet 2 contains monthly employment data
open MIDASv2.2/mydata.xlsx --sheet=2
rename VALUE payems
dataset compact 4 spread
# limit to the sample range of the GDP data
smp1 1947:1 2011:2
setinfo payems_m3 --description="Non-farm payroll employment, month 3 of quarter"
setinfo payems_m2 --description="Non-farm payroll employment, month 2 of quarter"
setinfo payems_m1 --description="Non-farm payroll employment, month 1 of quarter"
store payroll_midas.gdt

# sheet 1 contains quarterly GDP data
open MIDASv2.2/mydata.xlsx --sheet=1
rename VALUE qgdp
setinfo qgdp --description="Real quarterly US GDP"
append payroll_midas.gdt
store gdp_payroll_midas.gdt
```

Note that both series are simply named `VALUE` in the source file, so we use gretl's `rename` command to set distinct and meaningful names. The heavy lifting is done here by the line

```
dataset compact 4 spread
```

¹See <http://eghyse1s.web.unc.edu/> for links.

which tells gretl to compact an entire dataset (in this case, as it happens, just containing one series) to quarterly frequency using the “spread” method. Once this is done, it is straightforward to append the compacted data to the quarterly GDP dataset.

We will put an extended version of this dataset (supplied with gretl, and named `gdp_midas.gdt`) to use in subsequent sections.

20.2 The notion of a “MIDAS list”

In the following two sections we’ll describe functions that (rather easily) do the right thing if you wish to create lists of lags or first differences of high-frequency series. However, we should first be clear about the correct domain for such functions, since they could produce the most diabolical mash-up of your data if applied to the wrong sort of list argument—for instance, a regular list containing distinct series, all observed at the “base frequency” of the dataset.

So let us define a **MIDAS list**: this is a list of m series holding per-period values of a *single* high-frequency series, arranged in the order of most recent first, as illustrated above. Given the dataset shown in Table 20.1, an example of a correctly formulated MIDAS list would be

```
list INDPRO = indpro_m3 indpro_m2 indpro_m1
```

Or, since the monthly observations are already in the required order, we could define the list by means of a “wildcard”:

```
list INDPRO = indpro_m*
```

Having created such a list, one can use the `setinfo` command to tell gretl that it’s a *bona fide* MIDAS list:

```
setinfo INDPRO --midas
```

This will spare you some warnings that gretl would otherwise emit when you call some of the functions described below. This step should not be necessary, however, if the series in question are the product of a compact operation with the `spread` parameter.

Inspecting high-frequency data

The layout of high-frequency data shown in Table 20.1 is convenient for running regressions, but not very convenient for inspecting and checking such data. We therefore provide some methods for displaying MIDAS data at their “natural” frequency. Figure 20.1 shows the gretl main window with the `gdp_midas` dataset loaded, along with the menu that pops up if you right-click with the `payems` series highlighted. The items “Display values” and “Time series plot” show the data on their original monthly calendar, while the “Display components” item shows the three component series on a quarterly calendar, as in Table 20.1.

These methods are also available via the command line. For example, the commands

```
list PAYEMS = payems_*
print PAYEMS --byobs --midas
hfplot PAYEMS --with-lines --output=display
```

produce a monthly printout of the payroll employment data, followed by a monthly time-series plot. (See section 20.5 for more on `hfplot`.)

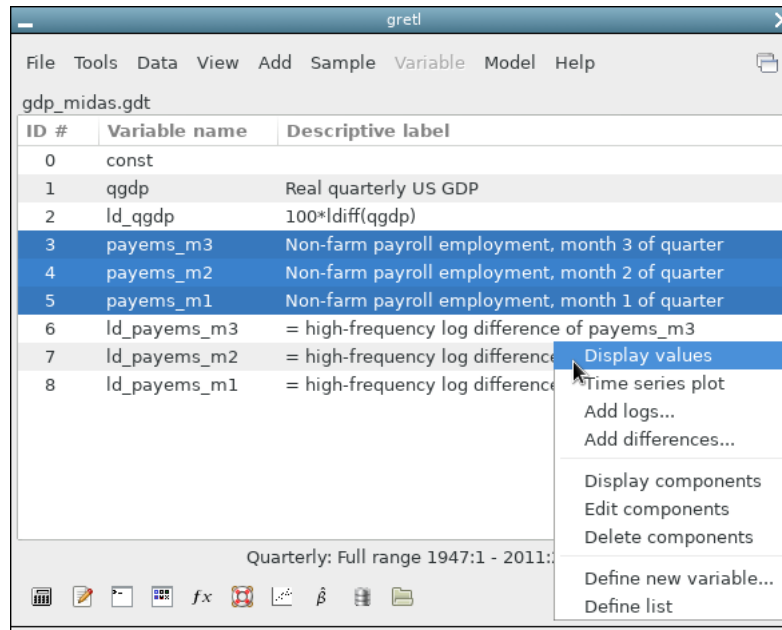


Figure 20.1: MIDAS data menu

20.3 High-frequency lag lists

A basic requirement of MIDAS is the creation of lists of high-frequency lags for use on the right-hand side of a regression specification. This is possible, but not very convenient, using the gretl's `lags` function; it is made easier by a dedicated variant of that function described below.

For illustration we'll consider an example presented in Ghysels' Matlab implementation of MIDAS: this uses 9 monthly lags of payroll employment, starting at lag 3, in a model for quarterly GDP. The estimation period for this model starts in 1985Q1. At this observation, the stipulation that we start at lag 3 means that the first (most recent) lag is employment for October 1984,² and the 9-lag window means that we need to include monthly lags back to February 1984. Let the per-month employment series be called `x_m3`, `x_m2` and `x_m1`, and let (quarterly) lags be represented by `(-1)`, `(-2)` and so on. Then the terms we want are (reading left-to-right by row):

			<code>x_m1(-1)</code>
<code>x_m3(-2)</code>	<code>x_m2(-2)</code>	<code>x_m1(-2)</code>	
<code>x_m3(-3)</code>	<code>x_m2(-3)</code>	<code>x_m1(-3)</code>	
<code>x_m3(-4)</code>	<code>x_m2(-4)</code>		

We could construct such a list in gretl using the following standard syntax. (Note that the third argument of 1 to `lags` below tells gretl that we want the terms ordered "by lag" rather than "by variable"; this is required to respect the order of the terms shown above.)

```
list X = x_m*
# create lags for 4 quarters, "by lag"
list XL = lags(4,X,1)
# convert the list to a matrix
matrix tmp = XL
# trim off the first two elements, and the last
tmp = tmp[3:11]
```

²That is what Ghysels means, but see the sub-section on "Leads and nowcasting" below for a possible ambiguity in this regard.

```
# and convert back to a list
XL = tmp
```

However, the following specialized syntax is more convenient:

```
list X = x_m*
setinfo X --midas
# create high-frequency lags 3 to 11
list XL = hflags(3, 11, X)
```

In the case of `hflags` the length of the list given as the third argument defines the “compaction ratio” ($m = 3$ in this example); we can (in fact, must) specify the lags we want in high-frequency terms; and ordering of the generated series by lag is automatic.

Word to the wise: do not use `hflags` on anything other than a **MIDAS list** as defined in section 20.2, unless perhaps you have some special project in mind and really know what you are doing.

Leads and nowcasting

Before leaving the topic of lags, it is worth commenting on the question of leads and so-called “nowcasting”—that is, prediction of the current value of a lower-frequency variable before its measurement becomes available.

In a regular dataset where all series are of the same frequency, lag 1 means the observation from the previous period, lag 0 is equivalent to the current observation, and lag -1 (or lead 1) is the observation for the next period into the relative future.

When considering high-frequency lags in the MIDAS context, however, there is no uniquely determined high-frequency sub-period which is temporally coincident with a given low-frequency period. The placement of high-frequency lag 0 therefore has to be a matter of convention. Unfortunately, there are two incompatible conventions in currently available MIDAS software, as follows.

- High-frequency lag 0 corresponds to the *first* sub-period within the current low-frequency period. This is what we find in Eric Ghysels’ MIDAS Matlab Toolbox; it’s also clearly stated and explained in [Armesto *et al.* \(2010\)](#).
- High-frequency lag 0 corresponds to the *last* sub-period in the current low-frequency period. This convention is employed in the `midasr` package for R.³

Consider, for example, the quarterly/monthly case. In Matlab, high-frequency (HF) lag 0 is the first month of the current quarter, HF lag 1 is the last month of the prior quarter, and so on. In `midasr`, however, HF lag 0 is the last month of the current quarter, HF lag 1 the middle month of the quarter, and HF lag 3 is the first one to take you “back in time” relative to the start of the current quarter, namely to the last month of the prior quarter.

In `gretl` we have chosen to employ the first of these conventions. So lag 1 points to the most recent sub-period in the previous base-frequency period, lag 0 points to the first sub-period in the current period, and lag -1 to the second sub-period within the current period. Continuing with the quarterly/monthly case, monthly observations for lags 0 and -1 are likely to become available before a measurement for the quarterly variable is published (possibly also a monthly value for lag -2). The first “truly future” lead does not occur until lag -3 .

The `hflags` function supports negative lags. Suppose one wanted to use 9 lags of a high-frequency variable, $-1, 0, 1, \dots, 7$, for nowcasting. Given a suitable MIDAS list, `X`, the following would do the job:

```
list XLnow = hflags(-1, 7, X)
```

³See <http://cran.r-project.org/web/packages/midasr/>, and for documentation <https://github.com/mpiktas/midasr-user-guide/raw/master/midasr-user-guide.pdf>.

This means that one could generate a forecast for the current low-frequency period (which is not yet completed and for which no observation is available) using data from two sub-periods into the low-frequency period (e.g. the first two months of the quarter).

20.4 High-frequency first differences

When working with non-stationary data one may wish to take first differences, and in the MIDAS context that probably means high-frequency differences of the high-frequency data. Note that the ordinary gretl functions `diff` and `ldiff` will *not* do what is wanted for series such as `indpro`, as shown in Table 20.1: these functions will give per-month *quarterly* differences of the data (month 3 of the current quarter minus month 3 of the previous quarter, and so on).

To get the desired result one could create the differences before compacting the high-frequency data but this may not be convenient, and it's not compatible with the method of constructing a MIDAS dataset shown in section 20.1. The alternative is to employ the specialized differencing function `hfdiff`. This takes one required argument, a **MIDAS list** as defined in section 20.2. A second, optional argument is a scalar multiplier (with default value 1.0); this permits scaling the output series by a constant. There's also an `hflldiff` function for creating high-frequency log differences; this has the same syntax as `hfdiff`.

So for example, the following creates a list of high-frequency percentage changes (100 times log-difference) then a list of high-frequency lags of the changes.

```
list X = indpro_*
setinfo X --midas
list dX = hflldiff(X, 100)
list dXL = hflags(3, 11, dX)
```

If you only need the series in the list `dXL`, however, you can nest these two function calls:

```
list dXL = hflags(3, 11, hflldiff(X, 100))
```

20.5 MIDAS-related plots

In the context of MIDAS analysis one may wish to produce time-series plots which show high- and low-frequency data in correct registration (as in Figures 1 and 2 in [Armesto *et al.*, 2010](#)). This can be done using the `hfplot` command, which has the following syntax:

```
hfplot midas-list [; lflist ] options
```

The required argument is a MIDAS list, as defined above. Optionally, one or more lower-frequency series (*lflist*) can be added to the plot following a semicolon. Supported options are `--with-lines`, `--time-series` and `--output`. These have the same effects as with the gretl's `gnuplot` command.

An example based on Figure 1 in [Armesto *et al.* \(2010\)](#) is shown in Listing 20.2 and Figure 20.2.

20.6 Alternative MIDAS data methods

Importation via a column vector

Listing 20.3 illustrates how one can construct via `hansl` a MIDAS list from a matrix (column vector) holding data of a higher frequency than the given dataset. In practice one would probably read high frequency data from file using the `mread` function, but here we just construct an artificial sequential vector.

Note the check in the `high_freq_list` function: we determine the current sample size, `T`, and insist that the input matrix is suitably dimensioned, with a single column of length equal to `T` times the compaction factor (here 3, for monthly to quarterly).

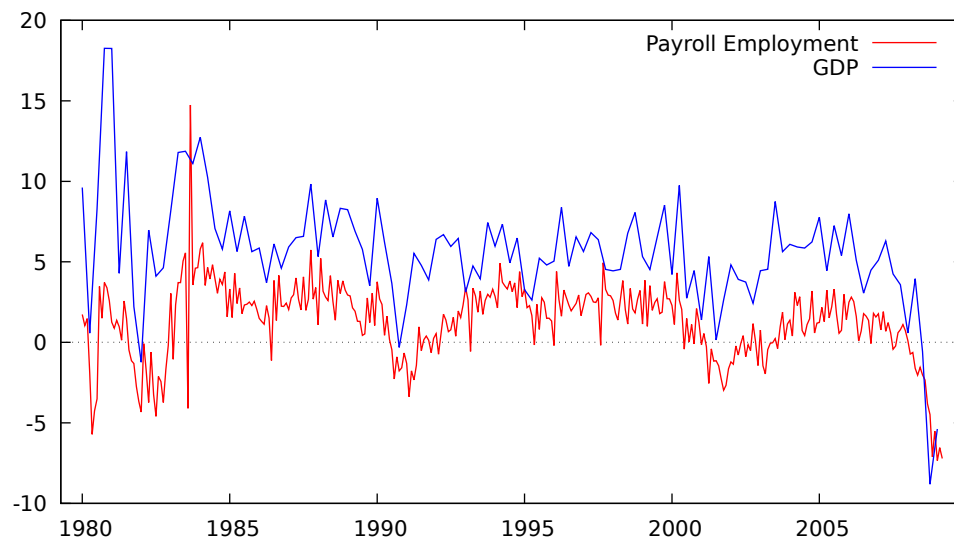
Listing 20.2: Replication of a plot from Armesto et al [\[Download ▼\]](#)

```
open gdp_midas.gdt

# form and label the dependent variable
series dy = log(qgdp/qgdp(-1))*400
setinfo dy --graph-name="GDP"

# form list of annualized HF differences
list X = payems*
list dX = hfldiff(X, 1200)
setinfo dX --graph-name="Payroll Employment"

smp1 1980:1 2009:1
hfplot dX ; dy --with-lines --time-series --output=display
```

**Figure 20.2:** Quarterly GDP and monthly Payroll Employment, annualized percentage changes

Listing 20.3: Create a midas list from a matrix [\[Download ▼\]](#)

```

function list high_freq_list (const matrix x, int compfac, string vname)
    list ret = deflist()
    scalar T = $nobs
    if rows(x) != compfac*T || cols(x) != 1
        funcerr "Invalid x matrix"
    endif
    matrix m = mreverse(mshape(x, compfac, T))'
    loop i=1..compfac
        scalar k = compfac + 1 - i
        ret += genseries(sprintf("%s%d", vname, k), m[,i])
    endloop
    setinfo ret --midas
    return ret
end function

# construct a little "quarterly" dataset
nulldata 12
setobs 4 1980:1

# generate "monthly" data, 1,2,...,36
matrix x = seq(1,3*$nobs)'
print x
# turn into midas list
list H = high_freq_list(x, 3, "test_m")
print H --byobs

```

The final command in the script should produce

	test_m3	test_m2	test_m1
1980:1	3	2	1
1980:2	6	5	4
1980:3	9	8	7
...			

This functionality is available in the built-in function `hflist`, which has the same signature as the `hansl` prototype above.

Importation via `join`

The `join` command provides a general and flexible framework for importing data from external files (see chapter 7).

In order to handle multiple-frequency data, it supports the “spreading” of high-frequency series to a MIDAS list in a single operation. This requires use of the `--aggr` option with parameter `spread`. There are two acceptable forms of usage, illustrated below. Note that `AWM` is a quarterly dataset while `hamilton` is monthly. First case:

```
open AWM.gdt
join hamilton.gdt PC6IT --aggr=spread
```

and second case:

```
open AWM.gdt
join hamilton.gdt PCI --data=PC6IT --aggr=spread
```

In the first case MIDAS series `PC6IT_m3`, `PC6IT_m2` and `PC6IT_m1` are added to the working dataset. In the second case “`PCI`” is used as the base name for the imports, giving `PCI_m3`, `PCI_m2` and `PCI_m1` as the names of the per-month series.

Note that only one high-frequency series can be imported in a given `join` invocation with the option `--aggr=spread`, which already implies the writing of multiple series in the lower frequency dataset.

An important point to note is that the `--aggr=spread` mechanism (where we map from one higher-frequency series to a set of lower-frequency ones) relies on finding a known, reliable time-series structure in the “outer” data file. Native `gretl` time-series data files will have such a structure, and also well-formed `gretl`-friendly CSV files, but not arbitrary comma-separated files. So if you have difficulty importing data MIDAS-style from a given CSV file using `--aggr=spread` you might want to drop back to a more agnostic, piece-wise approach (agnostic in the sense of assuming less about `gretl`’s ability to detect any time-series structure that might be present). Here’s an example:

```
open hamilton.gdt
# create month-of-quarter series for filtering
series mofq = ($obsminor - 1) % 3 + 1
# write example CSV file: the first column holds, e.g. "1973M01"
store test.csv PC6IT mofq
open AWM.gdt -q
# import monthly components one at a time, using a filter
join test.csv PCI_m3 --data=PC6IT --tkey=",%YM%m" --filter="mofq==3"
join test.csv PCI_m2 --data=PC6IT --tkey=",%YM%m" --filter="mofq==2"
join test.csv PCI_m1 --data=PC6IT --tkey=",%YM%m" --filter="mofq==1"
list PCI = PCI_*
setinfo PCI --midas
print PCI_m* --byobs
```


The example is artificial in that a time-series CSV file of suitable frequency written by gretl itself should work without special treatment. But you may have to add “helper” columns (such as the `mofq` series above) to a third-party CSV file to enable a piece-wise MIDAS join via filtering.

Daily data

Daily data (commonly financial-market data) are often used in practical applications of the MIDAS methodology. It’s therefore important that gretl support use of such data, but there are special issues arising from the fact that the number of days in a month, quarter or year is not a constant.

It seems to us that it’s necessary to stipulate a fixed, conventional number of days per lower-frequency period (that is, in practice, per month or quarter, since for the moment we’re ignoring the week as a basic temporal unit and we’re not yet attempting to support the combination of annual and daily data). But matters are further complicated by the fact that daily data come in (at least) three sorts: 5 days per week (as in financial-market data), 6-day (some commercial data which skip Sunday) and 7-day.

That said, we currently support—via `compact=spread`, as described in section 20.1—the following conversions:

- Daily to monthly: If the daily data are 5-days per week, we impose 22 days per month. This is the median, and also the mode, of weekdays per month, although some months have as few as 20 weekdays and some have 23. If the daily data are 6-day we impose 26 days per month, and in the 7-day case, 30 days per month.
- Daily to quarterly: In this case the stipulated days per quarter are simply 3 times the days-per-month values specified above.

So, given a daily dataset, you can say

```
dataset compact 12 spread
```

to convert MIDAS-wise to monthly (or substitute 4 for 12 for a quarterly target). And this is supposed to work whether the number of days per week is 5, 6 or 7.

That leaves the question of how we handle cases where the actual number of days in the calendar month or quarter falls short of, or exceeds, the stipulated number. We’ll talk this through with reference to the conversion of 5-day daily data to monthly; all other cases are essentially the same, *mutatis mutandis*.⁴

We start at “day 1,” namely the first relevant daily date within the calendar period (so the first weekday, with 5-day data). From that point on we fill up to 22 slots with relevant daily observations (including, not skipping, NAs due to holidays or whatever). If at the end we have daily observations left over, we ignore them. If we’re short we fill the empty slots with the arithmetic mean of the valid, used observations;⁵ and we fill in any missing values in the same way.

This means that lags 1 to 22 of 5-day daily data in a monthly dataset are always observations from days within the prior month (or in some cases “padding” that substitutes for such observations); lag 23 takes you back to the most recent day in the month before that.

Clearly, we *could* get a good deal fancier in our handling of daily data: for example, letting the user determine the number of days per month or quarter, and/or offering more elaborate means of filling in missing and non-existent daily values. It’s not clear that this would be worthwhile, but it’s open to discussion.

A little daily-to-monthly example is shown in Listing 20.4 and Figure 20.3. The example exercises the `hfpplot` command (see section 20.5).

⁴Or should be! We’re not ready to guarantee that just yet.

⁵This is the procedure followed in some example programs in the MIDAS Matlab Toolbox.

Listing 20.4: Monthly plus daily data [\[Download ▼\]](#)

```
# open a daily dataset
open djclose.gdt

# spread the data to monthly
dataset compact 12 spread
list DJ = djc*

# import an actual monthly series
open fedstl.bin
data indpro

# high-frequency plot (set --output=daily.pdf for PDF)
hfplot DJ ; indpro --with-lines --output=display \
{set key top left;}
```

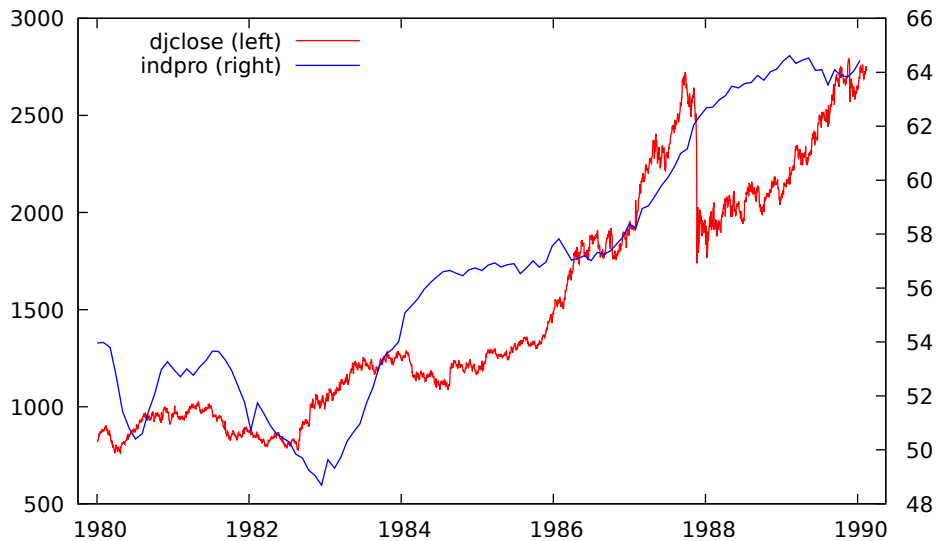


Figure 20.3: Monthly industrial production and daily Dow Jones close

Chapter 21

Cheat sheet

This chapter explains how to perform some common—and some not so common—tasks in gretl's scripting language, hansl. Some but not all of the techniques listed here are also available through the graphical interface. Although the graphical interface may be more intuitive and less intimidating at first, we encourage users to take advantage of the power of gretl's scripting language as soon as they feel comfortable with the program.

21.1 Dataset handling

“Weird” periodicities

Problem: You have data sampled each 3 minutes from 9am onwards; you'll probably want to specify the hour as 20 periods.

Solution:

```
setobs 20 9:1 --special
```

Comment: Now functions like `sdiff()` (“seasonal” difference) or estimation methods like seasonal ARIMA will work as expected.

Generating a panel dataset of given dimensions

Problem: You want to generate via `nulldata` a panel dataset and specify in advance the number of units and the time length of your series via two scalar variables.

Solution:

```
scalar n_units = 100
scalar T = 12
scalar NT = T * n_units

nulldata NT --preserve
setobs T 1:1 --stacked-time-series
```

Comment: The essential ingredient that we use here is the `--preserve` option: it protects existing scalars (and matrices, for that matter) from being trashed by `nulldata`, thus making it possible to use the scalar *T* in the `setobs` command.

Help, my data are backwards!

Problem: Gretl expects time series data to be in chronological order (most recent observation last), but you have imported third-party data that are in reverse order (most recent first).

Solution:

```
setobs 1 1 --cross-section
series sortkey = -obs
dataset sortby sortkey
setobs 1 1950 --time-series
```

Comment: The first line is required only if the data currently have a time series interpretation: it removes that interpretation, because (for fairly obvious reasons) the `dataset sortby` operation is not allowed for time series data. The following two lines reverse the data, using the negative of the built-in index variable `obs`. The last line is just illustrative: it establishes the data as annual time series, starting in 1950.

If you have a dataset that is mostly the right way round, but a particular variable is wrong, you can reverse that variable as follows:

```
x = sortby(-obs, x)
```

Dropping missing observations selectively

Problem: You have a dataset with many variables and want to restrict the sample to those observations for which there are no missing observations for the variables `x1`, `x2` and `x3`.

Solution:

```
list X = x1 x2 x3
smp1 --no-missing X
```

Comment: You can save the file via a `store` command to preserve a subsampled version of the dataset. Alternative solutions based on the `ok` function, such as

```
list X = x1 x2 x3
series sel = ok(X)
smp1 sel --restrict
```

are perhaps less obvious, but more flexible. Pick your poison.

“By” operations

Problem: You have a discrete variable `d` and you want to run some commands (for example, estimate a model) by splitting the sample according to the values of `d`.

Solution:

```
matrix vd = values(d)
m = rows(vd)
loop i=1..m
  scalar sel = vd[i]
  smp1 d==sel --restrict --replace
  ols y const x
endloop
smp1 --full
```

Comment: The main ingredient here is a loop. You can have `gretl` perform as many instructions as you want for each value of `d`, as long as they are allowed inside a loop. Note, however, that if all you want is descriptive statistics, the `summary` command does have a `--by` option.

Adding a time series to a panel

Problem: You have a panel dataset (comprising observations of n individuals in each of T periods) and you want to add a variable which is available in straight time-series form. For example, you want to add annual CPI data to a panel in order to deflate nominal income figures.

In `gretl` a panel is represented in stacked time-series format, so in effect the task is to create a new variable which holds n stacked copies of the original time series. Let's say the panel comprises 500 individuals observed in the years 1990, 1995 and 2000 ($n = 500$, $T = 3$), and we have these CPI data in the ASCII file `cpi.txt`:

```
date cpi
1990 130.658
1995 152.383
2000 172.192
```

What we need is for the CPI variable in the panel to repeat these three values 500 times.

Solution: Simple! With the panel dataset open in gretl,

```
append cpi.txt
```

Comment: If the length of the time series is the same as the length of the time dimension in the panel (3 in this example), gretl will perform the stacking automatically. Rather than using the `append` command you could use the “Append data” item under the File menu in the GUI program.

If the length of your time series does not exactly match the T dimension of your panel dataset, `append` will not work but you can use the `join` command, which is able to pick just the observations with matching time periods. On selecting “Append data” in the GUI you are given a choice between plain “append” and “join” modes, and if you choose the latter you get a dialog window allowing you to specify the key(s) for the join operation. For native gretl data files you can use built-in series that identify the time periods, such as `$obsmajor`, for your outer key to match the dates. In the example above, if the CPI data were in gretl format `$obsmajor` would give you the year of the observations.

Time averaging of panel datasets

Problem: You have a panel dataset (comprising observations of n individuals in each of T periods) and you want to lower the time frequency by averaging. This is commonly done in empirical growth economics, where annual data are turned into 3- or 4- or 5-year averages (see for example [Islam, 1995](#)).

Solution: In a panel dataset, gretl functions that deal with time are aware of the panel structure, so they will automatically “do the right thing”. Therefore, all you have to do is use the `movavg()` function for computing moving averages and then just drop the years you don’t need. An example with the Grunfeld dataset follows:

```
open grunfeld

# how many periods (here: years) to average
ave = 4

# a dummy for endpoints of each time block
# (using the modulo operator)
series endpoint = ($time % ave == 0)

list X = invest value kstock # time-varying variables

# compute averages
loop foreach i X
    series $i = movavg($i, ave)
endloop

# drop extra observations
smpl endpoint --dummy --permanent

# restore panel structure
setobs firm year --panel-vars
print firm year X -o
```

Running the above script produces (among other output):

```
? print firm year X -o
      firm      year      invest      value      kstock

1:1      1      1938      344.425      3979.875      105.375
1:2      1      1942      438.000      4188.100      242.375
1:3      1      1946      574.100      4543.700      283.225
1:4      1      1950      574.025      3559.250      950.750
1:5      1      1954      1109.550      5398.300      1660.450
2:1      2      1938      324.350      1911.925      120.650
2:2      2      1942      377.600      2177.325      281.750
2:3      2      1946      332.200      1929.225      231.825
2:4      2      1950      434.725      1691.725      320.150
2:5      2      1954      583.500      2148.925      519.900
...
9:1      9      1938      25.390      290.675      179.250
9:2      9      1942      30.000      281.875      228.250
9:3      9      1946      51.858      364.250      293.500
9:4      9      1950      42.717      285.150      359.500
9:5      9      1954      59.480      446.300      429.000
10:1     10     1938      2.180      74.943      4.585
10:2     10     1942      1.960      76.713      4.135
10:3     10     1946      1.427      64.863      3.382
10:4     10     1950      4.275      68.315      6.352
10:5     10     1954      5.580      69.772      11.253
```

Turning observation-marker strings into a series

Problem: Here's one that might turn up in the context of the `join` command (see chapter 7). The current dataset contains a string-valued series that you'd like to use as a key for matching observations, perhaps the two-letter codes for the names of US states. The file from which you wish to add data contains that same information, but *not* in the form of a string-valued series, rather it exists in the form of “observation markers”. Such markers cannot be used as a key directly, but is there a way to parlay them into a string-valued series? Why, of course there is!

Solution: We'll illustrate with the Ramanathan data file `data4-10.gdt`, which contains private school enrollment data and covariates for the 50 US states plus Washington, D.C. ($n = 51$).

```
open data4-10.gdt
markers --to-array="state_codes"
genr index
stringify(index, state_codes)
store joindata.gdt
```

Comment: The `markers` command saves the observation markers to an array of strings. The command `genr index` creates a series that goes 1, 2, 3, ..., and we attach the state codes to this series via `stringify()`. After saving the result we have a datafile that contains a series, `index`, that can be matched with whatever series holds the state code strings in the target dataset.

Suppose the relevant string-valued key series in the target dataset is called `state`. We might prefer to avoid the need to specify a distinct “outer” key (again see chapter 7). In that case, in place of

```
genr index
stringify(index, state_codes)
```

we could do

```
genr index
series state = index
stringify(state, state_codes)
```

and the two datafiles will contain a comparable string-valued `state` series.

21.2 Creating/modifying variables

Generating a dummy variable for a specific observation

Problem: Generate $d_t = 0$ for all observations but one, for which $d_t = 1$.

Solution:

```
series d = (t=="1984:2")
```

Comment: The internal variable `t` is used to refer to observations in string form, so if you have a cross-section sample you may just use `d = (t=="123")`. If the dataset has observation labels you can use the corresponding label, in which case it's more idiomatic to use `obs` rather than `t`. For example, if you open the dataset `mrw.gdt`, supplied with `gretl` among the examples, a dummy variable for Italy could be generated via

```
series DIta = (obs=="Italy")
```

Note that this method does not require scripting. You can use the GUI menu item “Add/Define new variable” for the same purpose, with the same syntax.

Generating a discrete variable out of a set of dummies

Problem: The `dummi fy` function (also available as a command) generates a set of mutually exclusive dummies from a discrete variable. The reverse functionality, however, seems to be absent.

Solution:

```
series x = lincomb(D, seq(1, nelem(D)))
```

Comment: Suppose you have a list `D` of mutually exclusive dummies, that is a full set of 0/1 variables coding for the value of some characteristic, such that the sum of the values of the elements of `D` is 1 at each observation. This is, by the way, exactly what the `dummi fy` command produces. The reverse job of `dummi fy` can be performed neatly by using the `lincomb` function.

The code above multiplies the first dummy variable in the list `D` by 1, the second one by 2, and so on. Hence, the return value is a series whose value is i if and only if the i -th member of `D` has value 1.

If you want your coding to start from 0 instead of 1, you'll have to modify the code snippet above into

```
series x = lincomb(D, seq(0, nelem(D)-1))
```

Easter

Problem: I have a 7-day daily dataset. How do I create an “Easter” dummy?

Solution: We have the `easterday()` function, which returns the month and day of Easter (in the form of a single scalar that must be unpacked) given the year. The following example script uses this function and a few string magic tricks. It assumes a 7-day dataset that spans at least 2011 to 2016.

```
series Easter = 0
loop y=2011..2016
  a = easterday(y)
```

```

m = floor(a)
d = round(100*(a-m))
ed_str = sprintf("%04d-%02d-%02d", y, m, d)
Easter["@ed_str"] = 1
endloop

```

Comment: The `round()` function is necessary for the “day” component because otherwise floating-point problems may ensue. Try the year 2015, for example.

Recoding a variable

Problem: You want to perform a 1-to-1 recode on a variable. For example, consider tennis points: you may have a variable x holding values 1 to 3 and you want to recode it to 15, 30, 40.

Solution 1:

```

series x = replace(x, 1, 15)
series x = replace(x, 2, 30)
series x = replace(x, 3, 40)

```

Solution 2:

```

matrix tennis = {15, 30, 40}
series x = replace(x, seq(1,3), tennis)

```

Comment: There are many equivalent ways to achieve the same effect, but for simple cases such as this, the `replace` function is simple and transparent. If you don’t mind using matrices, scripts using `replace` can also be remarkably compact. Note that `replace` also performs n -to-1 (“surjective”) replacements, such as

```

series x = replace{z, {2, 3, 5, 11, 22, 33}, 1)

```

which would turn all entries equal to 2, 3, 5, 11, 22 or 33 to 1 and leave the other ones unchanged.

Generating a “subset of values” dummy

Problem: You have a dataset which contains a fine-grained coding for some qualitative variable and you want to “collapse” this to a relatively small set of dummy variables. Examples: you have place of work by US state and you want a small set of regional dummies; or you have detailed occupational codes from a census dataset and you want a manageable number of occupational category dummies.

Let’s call the source series `src` and one of the target dummies `D1`. And let’s say that the values of `src` to be grouped under `D1` are 2, 13, 14 and 25. We’ll consider three possible solutions:

“Longhand” solution:

```

series D1 = src==2 || src==13 || src==14 || src==25

```

Comment: The above works fine if the number of distinct values in the source to be condensed into each dummy variable is fairly small, but it becomes cumbersome if a single dummy must comprise dozens of source values.

Condensed solution:

```

matrix sel = {2,13,14,25}
series D1 = contains(src, sel)

```


Comment: The subset of values to be grouped together can be written out as a matrix relatively compactly.

Of course, whichever procedure you use, you have to repeat it for each of the dummy series you want to create.

Proper solution:

The best solution, in terms of both computational efficiency and code clarity, would be using a “conversion table” and the `replace` function, to produce a series on which the `dummi fy` command can be used. For example, suppose we want to convert from a series called `fips` holding FIPS codes¹ for the 50 US states plus the District of Columbia to a series holding codes for the four standard US regions. We could create a 2×51 matrix—call it `srmmap`—with the 51 FIPS codes on the first row and the corresponding region codes on the second, and then do

```
series region = replace(fips, srmmap[1,], srmmap[2,])
dummify region
```

Comment: With this approach all the subset dummies are created in one go, using the naming pattern `Dregion_1` and so on. The minor price to pay is that the relatively large conversion table `srmmap` has to be constructed first.

Generating an ARMA(1,1)

Problem: Generate $y_t = 0.9y_{t-1} + \varepsilon_t - 0.5\varepsilon_{t-1}$, with $\varepsilon_t \sim NIID(0, 1)$.

Recommended solution:

```
alpha = 0.9
theta = -0.5
series y = filter(normal(), {1, theta}, alpha)
```

“Bread and butter” solution:

```
alpha = 0.9
theta = -0.5
series e = normal()
series y = 0
series y = alpha * y(-1) + e + theta * e(-1)
```

Comment: The `filter` function is specifically designed for this purpose so in most cases you’ll want to take advantage of its speed and flexibility. That said, in some cases you may want to generate the series in a manner which is more transparent (maybe for teaching purposes).

In the second solution, the statement `series y = 0` is necessary because the next statement evaluates `y` recursively, so `y[1]` must be set. Note that you must use the keyword `series` here instead of writing `genr y = 0` or simply `y = 0`, to ensure that `y` is a series and not a scalar.

Recoding a variable by classes

Problem: You want to recode a variable by classes. For example, you have the age of a sample of individuals (x_i) and you need to compute age classes (y_i) as

$$\begin{aligned} y_i &= 1 & \text{for } x_i < 18 \\ y_i &= 2 & \text{for } 18 \leq x_i < 65 \\ y_i &= 3 & \text{for } x_i \geq 65 \end{aligned}$$

Solution:

¹FIPS is the Federal Information Processing Standard: it assigns numeric codes from 1 to 56 to the US states and outlying areas.

```
series y = 1 + (x >= 18) + (x >= 65)
```

Comment: True and false expressions are evaluated as 1 and 0 respectively, so they can be manipulated algebraically as any other number. The same result could also be achieved by using the conditional assignment operator (see below), but in most cases it would probably lead to more convoluted constructs.

Conditional assignment

Problem: Generate y_t via the following rule:

$$y_t = \begin{cases} x_t & \text{for } d_t > a \\ z_t & \text{for } d_t \leq a \end{cases}$$

Solution:

```
series y = (d > a) ? x : z
```

Comment: There are several alternatives to the one presented above. One is a brute force solution using loops. Another one, more efficient but still suboptimal, would be

```
series y = (d>a)*x + (d<=a)*z
```

However, the ternary conditional assignment operator is not only the most efficient way to accomplish what we want, it is also remarkably transparent to read when one gets used to it. Some readers may find it helpful to note that the conditional assignment operator works exactly the same way as the =IF() function in spreadsheets.

Generating a time index for panel datasets

Comment: gretl has a \$unit as well as a \$time accessor. These special constructs as well as variants such as genr time are aware of whether a dataset is a panel.

Sanitizing a list of regressors

Problem: I noticed that built-in commands like ols automatically drop collinear variables and put the constant first. How can I achieve the same result for an estimator I'm writing?

Solution: No worry. The function below does just that

```
function list sanitize(list X)
  list R = X - const
  if nelem(R) < nelem(X)
    R = const R
  endif
  return dropcoll(R)
end function
```

so for example the code below

```
nulldata 20
x = normal()
y = normal()
z = x + y # collinear
list A = x y const z
list B = sanitize(A)

list print A
list print B
```

returns

```
? list print A
x y const z
? list print B
const x y
```

Aside: it has been brought to our attention that some mischievous programs out there put the constant *last*, instead of first, like God intended. We are not amused by this utter disrespect of econometric tradition, but if you want to pursue the way of evil, it is rather simple to adapt the script above to that effect.

Generating the “hat” values after an OLS regression

Problem: I’ve just run an OLS regression, and now I need the so-called the leverage values (also known as the “hat” values). I know you can access residuals and fitted values through “dollar” accessors, but nothing like that seems to be available for “hat” values.

Solution: “Hat” values are can be thought of as the diagonal of the projection matrix P_X , or more explicitly as

$$h_i = \mathbf{x}_i' (X'X)^{-1} \mathbf{x}_i$$

where X is the matrix of regressors and \mathbf{x}_i' is its i -th row.

The reader is invited to study the code below, which offers four different solutions to the problem:

```
open data4-1.gdt --quiet
list X = const sqft bedrms baths
ols price X

# method 1
leverage --save --quiet
series h1 = lever

# these are necessary for what comes next
matrix mX = {X}
matrix iXX = invpd(mX'mX)

# method 2
series h2 = diag(qform(mX, iXX))
# method 3
series h3 = sumr(mX .* (mX*iXX))
# method 4
series h4 = NA
loop i=1..$nobs
    matrix x = mX[i,]'
    h4[i] = x'iXX*x
endloop

# verify
print h1 h2 h3 h4 --byobs
```

Comment: Solution 1 is the preferable one: it relies on the built-in `leverage` command, which computes the requested series quite efficiently, taking care of missing values, possible restrictions to the sample, etc.

However, three more are shown for didactical purposes, mainly to show the user how to manipulate matrices. Solution 2 first constructs the P_X matrix explicitly, via the `qform` function, and then takes its diagonal; this is definitely *not* recommended (despite its compactness), since you generate a

much bigger matrix than you actually need and waste a lot of memory and CPU cycles in the process. It doesn't matter very much in the present case, since the sample size is very small, but with a big dataset this could be a very bad idea.

Solution 3 is more clever, and relies on the fact that, if you define $Z = X \cdot (X'X)^{-1}$, then h_i could also be written as

$$h_i = \mathbf{x}_i' \mathbf{z}_i = \sum_{k=1}^k x_{ik} z_{ik}$$

which is in turn equivalent to the sum of the elements of the i -th row of $X \odot Z$, where \odot is the element-by-element product. In this case, your clever usage of matrix algebra would produce a solution computationally much superior to solution 2.

Solution 4 is the most old-fashioned one, and employs an indexed loop. While this wastes practically no memory and employs no more CPU cycles in algebraic operations than strictly necessary, it imposes a much greater burden on the `hansl` interpreter, since handling a loop is conceptually more complex than a single operation. In practice, you'll find that for any realistically-sized problem, solution 4 is much slower than solution 3.

Moving functions for time series

Problem: `gretl` provides native functions for moving averages, but I need a to compute a different statistic on a sliding data window. Is there a way to do this without using loops?

Solution: One of the nice things of the `list` data type is that, if you define a list, then several functions that would normally apply "vertically" to elements of a series apply "horizontally" across the list. So for example, the following piece of code

```
open bjg.gdt
order = 12
list L = lg || lags(order-1, lg)
smp1 +order ;
series movmin = min(L)
series movmax = max(L)
series movmed = median(L)
smp1 full
```

computes the moving minimum, maximum and median of the `lg` series. Plotting the four series would produce something similar to figure [21.1](#).

Generating data with a prescribed correlation structure

Problem: I'd like to generate a bunch of normal random variates whose covariance matrix is exactly equal to a given matrix Σ . How can I do this in `gretl`?

Solution: The Cholesky decomposition is your friend. If you want to generate data with a given *population* covariance matrix, then all you have to do is post-multiply your pseudo-random data by the Cholesky factor (transposed) of the matrix you want. For example:

```
set seed 123
S = {2,1;1,1}
T = 1000
X = mnormal(T, rows(S))
X = X * cholesky(S)'
eval mcov(X)
```

should give you

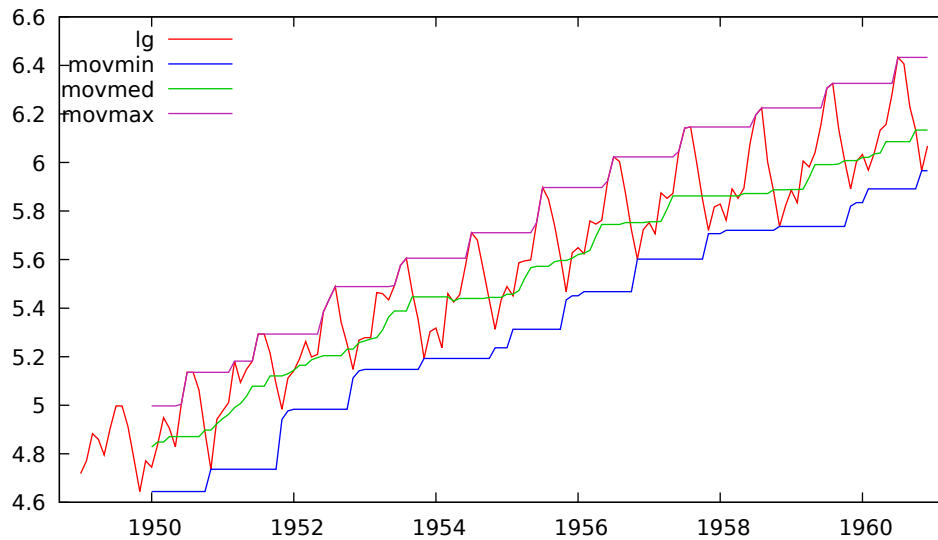


Figure 21.1: "Moving" functions

```
? eval mcov(X)
      2.0016      1.0157
      1.0157      1.0306
```

If, instead, you want your simulated data to have a given *sample* covariance matrix, you have to apply the same technique twice: one for standardizing the data, another one for giving it the covariance structure you want. Example:

```
S = {2,1;1,1}
T = 1000
X = mnormal(T, rows(S))
X = X * (cholesky(S)/cholesky(mcov(X)))'
eval mcov(X)
```

gives you

```
? eval mcov(X)
      2      1
      1      1
```

as required.

21.3 Neat tricks

Interaction dummies

Problem: You want to estimate the model $y_i = \mathbf{x}_i\beta_1 + \mathbf{z}_i\beta_2 + d_i\beta_3 + (d_i \cdot \mathbf{z}_i)\beta_4 + \varepsilon_t$, where d_i is a dummy variable while \mathbf{x}_i and \mathbf{z}_i are vectors of explanatory variables.

Solution: Gretl provides the \wedge operator to make this operation easy, which essentially boils down to creating a new list with $d \wedge z$ and adding that to the regressors. See section 15.1 for details (especially Listing 15.1). This method avoids an explicit loop construct in which products of the series would be formed.

Realized volatility

Problem: Given data by the minute, you want to compute the “realized volatility” for the hour as $RV_t = \frac{1}{60} \sum_{\tau=1}^{60} y_{t;\tau}^2$. Imagine your sample starts at time 1:1.

Solution:

```

nulldata 720
setobs 60 1:1 --time-series # 60 minutes per hour

# artificial data by the minute
series x = normal()

# calculate variance using the 60 obs within each hour
matrix v = aggregate(x, $obsmajor, var) # $obsmajor means hour here

# go from minute data to lower hourly periodicity
dataset compact 1
series rv = v[,end] # final column of v holds the variance results

```

Comment: Here we require that the dataset by the minute is explicitly defined with the special time-series periodicity of 60, so that it can be compacted to hourly data by using the `dataset compact 1` command. If needed, the dataset’s new periodicity can be re-set to 24 afterwards with the `setobs` command, which is the usual property of hourly data.

Looping over two paired lists

Problem: Suppose you have two lists with the same number of elements, and you want to apply some command to corresponding elements over a loop. For example you want to regress each element of one list on the corresponding element of the other.

Solution:

```

list Y = y1 y2 y3
list X = x1 x2 x3
loop i=1..nelem(Y)
  ols Y[i] 0 X[i]
endloop

```

Convolution / polynomial multiplication

Problem: How do I multiply polynomials? There’s no dedicated function to do that, and yet it’s a fairly basic mathematical task.

Solution: Never fear! We have the `conv2d` function, which is a tool for a more general problem, but includes polynomial multiplication as a special case..

Suppose you want to multiply two finite-order polynomials $P(x) = \sum_{i=0}^m p_i x^i$ and $Q(x) = \sum_{i=0}^n q_i x^i$. What you want is the sequence of coefficients of the polynomial

$$R(x) = P(x) \cdot Q(x) = \sum_{k=0}^{m+n} r_k x^k$$

where

$$r_k = \sum_{i=0}^k p_i q_{k-i}$$

is the *convolution* of the p_i and q_i coefficients. The same operation can be performed via the FFT, but in most cases using `conv2d` is quicker and more natural.

As an example, we'll use the same one we used in Section 30.5: consider the multiplication of two polynomials:

$$\begin{aligned} P(x) &= 1 + 0.5x \\ Q(x) &= 1 + 0.3x - 0.8x^2 \\ R(x) = P(x) \cdot Q(x) &= 1 + 0.8x - 0.65x^2 - 0.4x^3 \end{aligned}$$

The following code snippet performs all the necessary calculations:

```
p = {1; 0.5}
q = {1; 0.3; -0.8}
r = conv2d(p, q)
print r
```

Running the above produces

```
r (4 x 1)

  1
 0.8
-0.65
-0.4
```

which is indeed the desired result. Note that the same computation could also be performed via the `filter` function, at the price of slightly more elaborate syntax.

Comparing two lists

Problem: How can I tell if two lists contain the same variables (not necessarily in the same order)?

Solution: In many respects, lists are like sets, so it makes sense to use the so-called “symmetric difference” operator, which is defined as

$$A \triangle B = (A \setminus B) \cup (B \setminus A)$$

where in this context backslash represents the relative complement operator, which gives the elements of set A than are not in set B :

$$A \setminus B = \{x \in A : x \notin B\}$$

So we first check if there are any series in A but not in B , then we perform the reverse check. If the union of the two results is an empty set, then the lists must contain the same variables. The `hansl` syntax for this would be something like

```
scalar NotTheSame = nElem((A-B) || (B-A)) > 0
```

Reordering list elements

Problem: Is there a way to reorder list elements?

Solution: You can use the fact that a list can be cast into a vector of integers and then manipulated via ordinary matrix syntax. So, for example, if you wanted to “flip” a list you may just use the `mreverse` function. For example:

```
open AWM.gdt --quiet
list X = 3 6 9 12
matrix tmp = X
list revX = mreverse(tmp')

list X print
list revX print
```

will produce

```
? list X print
D1 D872 EEN_DIS GCD
? list revX print
GCD EEN_DIS D872 D1
```

Plotting an asymmetric confidence interval

Problem: “I like the look of the `--band` option to the `gnuplot` and `plot` commands, but it’s set up for plotting a symmetric interval and I want to show an asymmetric one.”

Solution: Any interval is by construction symmetrical about its mean at each observation. So you just need to perform a little tweak. Say you want to plot a series `x` along with a band defined by the two series `top` and `bot`. Here we go:

```
# create series for mid-point and deviation
series mid = (top + bot)/2
series dev = top - mid
gnuplot x --band=mid,dev --time-series --with-lines --output=display
```

Cross-validation

Problem: “I’d like to compute the so-called *leave-one-out cross-validation criterion* for my regression. Is there a command in `gretl`?”

If you have a sample with n observations, the “leave-one-out” cross-validation criterion can be mechanically computed by running n regressions in which one observation at a time is omitted and all the other ones are used to forecast its value. The sum of the n squared forecast errors is the statistic we want. Fortunately, there is no need to do so. It is possible to prove that the same statistic can be computed as

$$CV = \sum_{i=1}^n [\hat{u}_i / (1 - h_i)]^2,$$

where h_i is the i -th element of the “hat” matrix (see section 21.2) from a regression on the whole sample.

This method is natively provided by `gretl` as a side benefit to the `leverage` command, that stores the CV criterion into the `$test` accessor. The following script shows the equivalence of the two approaches:

```
set verbose off
open data4-1.gdt
list X = const sqft bedrms baths

# compute the CV criterion the silly way

scalar CV = 0
matrix mX = {X}
loop i = 1 .. $nobs
  xi = mX[i,]
  yi = price[i]
  smpl obs != i --restrict
  ols price X --quiet
  smpl full
  scalar fe = yi - xi * $coeff
  CV += fe^2
endloop
```



```
printf "CV = %g\n", CV

# the smart way

ols price X --quiet
leverage --quiet
printf "CV = %g\n", $test
```

Is my matrix result broken?

Problem: Most of the matrix manipulation functions available in gretl flag an error if something goes wrong, but there's no guarantee that every matrix computation will return an entirely finite matrix, containing no infinities or NaNs. So how do I tell if I've got a fully valid matrix?

Solution: The `sum` function applied to a matrix `m` returns the sum of all of its elements or NA if any elements are non-finite. So “`eval sum(m)`” can be used as a check—or more explicitly,

```
if !ok(sum(m))
    print "m is broken"
endif
```

Also note that the call “`ok(m)`” returns a matrix with the same dimensions as `m`, with elements 1 for finite values and 0 for infinities or NaNs.

Part II

Econometric methods

Chapter 22

Robust covariance matrix estimation

22.1 Introduction

Consider (once again) the linear regression model

$$y = X\beta + u \quad (22.1)$$

where y and u are T -vectors, X is a $T \times k$ matrix of regressors, and β is a k -vector of parameters. As is well known, the estimator of β given by Ordinary Least Squares (OLS) is

$$\hat{\beta} = (X'X)^{-1}X'y \quad (22.2)$$

If the condition $E(u|X) = 0$ is satisfied, this is an unbiased estimator; under somewhat weaker conditions the estimator is biased but consistent. It is straightforward to show that when the OLS estimator is unbiased (that is, when $E(\hat{\beta} - \beta) = 0$), its variance is

$$\text{Var}(\hat{\beta}) = E\left((\hat{\beta} - \beta)(\hat{\beta} - \beta)'\right) = (X'X)^{-1}X'\Omega X(X'X)^{-1} \quad (22.3)$$

where $\Omega = E(uu')$ is the covariance matrix of the error terms.

Under the assumption that the error terms are independently and identically distributed (iid) we can write $\Omega = \sigma^2 I$, where σ^2 is the (common) variance of the errors (and the covariances are zero). In that case (22.3) simplifies to the “classical” formula,

$$\text{Var}(\hat{\beta}) = \sigma^2 (X'X)^{-1} \quad (22.4)$$

If the iid assumption is not satisfied, two things follow. First, it is possible in principle to construct a more efficient estimator than OLS—for instance some sort of Feasible Generalized Least Squares (FGLS). Second, the simple “classical” formula for the variance of the least squares estimator is no longer correct, and hence the conventional OLS standard errors—which are just the square roots of the diagonal elements of the matrix defined by (22.4)—do not provide valid means of statistical inference.

In the recent history of econometrics there are broadly two approaches to the problem of non-iid errors. The “traditional” approach is to use an FGLS estimator. For example, if the departure from the iid condition takes the form of time-series dependence, and if one believes that this could be modeled as a case of first-order autocorrelation, one might employ an AR(1) estimation method such as Cochrane–Orcutt, Hildreth–Lu, or Prais–Winsten. If the problem is that the error variance is non-constant across observations, one might estimate the variance as a function of the independent variables and then perform weighted least squares, using as weights the reciprocals of the estimated variances.

While these methods are still in use, an alternative approach has found increasing favor: that is, use OLS but compute standard errors (or more generally, covariance matrices) that are robust with respect to deviations from the iid assumption. This is typically combined with an emphasis on using large datasets—large enough that the researcher can place some reliance on the (asymptotic) consistency property of OLS. This approach has been enabled by the availability of cheap computing power. The computation of robust standard errors and the handling of very large datasets were daunting tasks at one time, but now they are unproblematic. The other point favoring the newer methodology is that while FGLS offers an efficiency advantage in principle, it often involves making

additional statistical assumptions which may or may not be justified, which may not be easy to test rigorously, and which may threaten the consistency of the estimator—for example, the “common factor restriction” that is implied by traditional FGLS “corrections” for autocorrelated errors.

James Stock and Mark Watson’s *Introduction to Econometrics* illustrates this approach at the level of undergraduate instruction: many of the datasets they use comprise thousands or tens of thousands of observations; FGLS is downplayed; and robust standard errors are reported as a matter of course. In fact, the discussion of the classical standard errors (labeled “homoskedasticity-only”) is confined to an Appendix.

Against this background it may be useful to set out and discuss all the various options offered by gretl in respect of robust covariance matrix estimation. The first point to notice is that gretl produces “classical” standard errors by default (in all cases apart from GMM estimation). In script mode you can get robust standard errors by appending the `--robust` flag to estimation commands. In the GUI program the model specification dialog usually contains a “Robust standard errors” check box, along with a “configure” button that is activated when the box is checked. The configure button takes you to a configuration dialog (which can also be reached from the main menu bar: Tools → Preferences → General → HCCME). There you can select from a set of possible robust estimation variants, and can also choose to make robust estimation the default.

The specifics of the available options depend on the nature of the data under consideration—cross-sectional, time series or panel—and also to some extent the choice of estimator. (Although we introduced robust standard errors in the context of OLS above, they may be used in conjunction with other estimators too.) The following three sections of this chapter deal with matters that are specific to the three sorts of data just mentioned. Note that additional details regarding covariance matrix estimation in the context of GMM are given in chapter 27.

We close this introduction with a brief statement of what “robust standard errors” can and cannot achieve. They can provide for asymptotically valid statistical inference in models that are basically correctly specified, but in which the errors are not iid. The “asymptotic” part means that they may be of little use in small samples. The “correct specification” part means that they are not a magic bullet: if the error term is correlated with the regressors, so that the parameter estimates themselves are biased and inconsistent, robust standard errors will not save the day.

22.2 Cross-sectional data and the HCCME

With cross-sectional data, the most likely departure from iid errors is heteroskedasticity (non-constant variance).¹ In some cases one may be able to arrive at a judgment regarding the likely form of the heteroskedasticity, and hence to apply a specific correction. The more common case, however, is where the heteroskedasticity is of unknown form. We seek an estimator of the covariance matrix of the parameter estimates that retains its validity, at least asymptotically, in face of unspecified heteroskedasticity. It is not obvious *a priori* that this should be possible, but White (1980) showed that

$$\widehat{\text{Var}}_h(\hat{\beta}) = (X'X)^{-1}X'\hat{\Omega}X(X'X)^{-1} \quad (22.5)$$

does the trick. (As usual in statistics we need to say “under certain conditions”, but the conditions are not very restrictive.) $\hat{\Omega}$ is in this context a diagonal matrix, whose non-zero elements may be estimated using squared OLS residuals. White referred to (22.5) as a heteroskedasticity-consistent covariance matrix estimator (HCCME).

Davidson and MacKinnon (2004, chapter 5) offer a useful discussion of several variants on White’s HCCME theme. They refer to the original variant of (22.5)—in which the diagonal elements of $\hat{\Omega}$ are estimated directly by the squared OLS residuals, \hat{u}_t^2 —as HC₀. (The associated standard errors are often called “White’s standard errors”.) The various refinements of White’s proposal share a common point of departure, namely the idea that the squared OLS residuals are likely to be “too

¹In some specialized contexts spatial autocorrelation may be an issue. Gretl does not have any built-in methods to handle this and we will not discuss it here.

small” on average. This point is quite intuitive. The OLS parameter estimates, $\hat{\beta}$, satisfy by design the criterion that the sum of squared residuals,

$$\sum \hat{u}_t^2 = \sum (y_t - X_t \hat{\beta})^2$$

is minimized for given X and y . Suppose that $\hat{\beta} \neq \beta$. This is almost certain to be the case: even if OLS is not biased it would be a miracle if the $\hat{\beta}$ calculated from any finite sample were exactly equal to β . But in that case the sum of squares of the true, unobserved *errors*, $\sum u_t^2 = \sum (y_t - X_t \beta)^2$ is bound to be greater than $\sum \hat{u}_t^2$. The elaborated variants on HC₀ take this point on board as follows:

- HC₁: Applies a degrees-of-freedom correction, multiplying the HC₀ matrix by $T/(T - k)$.
- HC₂: Instead of using \hat{u}_t^2 for the diagonal elements of $\hat{\Omega}$, uses $\hat{u}_t^2/(1 - h_t)$, where $h_t = X_t(X'X)^{-1}X'_t$, the t^{th} diagonal element of the projection matrix P_X , which has the property that $P_X \cdot y = \hat{y}$. The relevance of h_t is that if the variance of all the u_t is σ^2 , the expectation of \hat{u}_t^2 is $\sigma^2(1 - h_t)$, or in other words, the ratio $\hat{u}_t^2/(1 - h_t)$ has expectation σ^2 . As Davidson and MacKinnon show, $0 \leq h_t < 1$ for all t , so this adjustment cannot reduce the the diagonal elements of $\hat{\Omega}$ and in general revises them upward.
- HC₃: Uses $\hat{u}_t^2/(1 - h_t)^2$. The additional factor of $(1 - h_t)$ in the denominator, relative to HC₂, may be justified on the grounds that observations with large variances tend to exert a lot of influence on the OLS estimates, so that the corresponding residuals tend to be underestimated. See Davidson and MacKinnon for a fuller explanation.
- HC_{3a}: Implements the jackknife approach from [MacKinnon and White \(1985\)](#). (HC₃ is a close approximation of this.)

The relative merits of these variants have been explored by means of both simulations and theoretical analysis. Unfortunately there is not a clear consensus on which is “best”. Davidson and MacKinnon argue that the original HC₀ is likely to perform worse than the others and in *gretl* the default is HC₁. If you want comparability with other software that reports “White’s standard errors” you can choose HC₀.

If you wish to use a version other than HC₁ you can arrange for this in either of two ways. In script or console mode you can do, for example,

```
set hc_version 2
```

and the version you specify will be applied in the current *gretl* session. In the GUI program you can go to the HCCME configuration dialog, as noted above, and choose any of these variants to be the default: a choice made in this way persists across *gretl* sessions.

22.3 Time series data and HAC covariance matrices

Heteroskedasticity may be an issue with time series data too but it is unlikely to be the only, or even the primary, concern.

One form of heteroskedasticity is common in macroeconomic time series but is fairly easily dealt with. That is, in the case of strongly trending series such as Gross Domestic Product, aggregate consumption, aggregate investment, and so on, higher levels of the variable in question are likely to be associated with higher variability in absolute terms. The obvious “fix”, employed in many macroeconometric studies, is to use the logs of such series rather than the raw levels. Provided the *proportional* variability of such series remains roughly constant over time the log transformation is effective.

Other forms of heteroskedasticity may resist the log transformation, but may demand a special treatment distinct from the calculation of robust standard errors. We have in mind here *autoregressive conditional* heteroskedasticity, for example in the behavior of asset prices, where large

disturbances to the market may usher in periods of increased volatility. Such phenomena call for specific estimation strategies, such as GARCH (see chapter 31).

Despite the points made above, some residual degree of heteroskedasticity may be present in time series data: the key point is that in most cases it is likely to be combined with serial correlation (autocorrelation), hence demanding a special treatment. In White's approach, $\hat{\Omega}$, the estimated covariance matrix of the u_t , remains conveniently diagonal: the variances, $E(u_t^2)$, may differ by t but the covariances, $E(u_t u_s)$ for $s \neq t$, are all zero. Autocorrelation in time series data means that at least some of the off-diagonal elements of $\hat{\Omega}$ should be non-zero. This introduces a substantial complication and requires another piece of terminology: estimates of the covariance matrix that are asymptotically valid in face of both heteroskedasticity and autocorrelation of the error process are termed HAC (heteroskedasticity- and autocorrelation-consistent).

The issue of HAC estimation is treated in more technical terms in chapter 27. Here we try to convey some of the intuition at a more basic level. We begin with a general comment: residual autocorrelation is not so much a property of the data as a symptom of an inadequate model. Data may be persistent though time, and if we fit a model that does not take this aspect into account properly we end up with a model with autocorrelated disturbances. Conversely, it is often possible to mitigate or even eliminate the problem of autocorrelation by including relevant lagged variables in a time series model, or in other words, by specifying the dynamics of the model more fully. HAC estimation should not be seen as the first resort in dealing with an autocorrelated error process.

That said, the “obvious” extension of White's HCCME to the case of autocorrelated errors would seem to be this: estimate the off-diagonal elements of $\hat{\Omega}$ (that is, the autocovariances, $E(u_t u_s)$) using, once again, the appropriate OLS residuals: $\hat{\omega}_{ts} = \hat{u}_t \hat{u}_s$. This is basically right, but demands an important amendment. We seek a *consistent* estimator, one that converges towards the true Ω as the sample size tends towards infinity. This can't work if we allow unbounded serial dependence. A larger sample will enable us to estimate more of the true ω_{ts} elements (that is, for t and s more widely separated in time) but will not contribute ever-increasing information regarding the maximally separated ω_{ts} pairs since the maximal separation itself grows with the sample size. To ensure consistency we have to confine our attention to processes exhibiting temporally limited dependence. In other words we cut off the computation of the $\hat{\omega}_{ts}$ values at some maximum value of $p = t - s$, where p is treated as an increasing function of the sample size, T , although it cannot increase in proportion to T .

The simplest variant of this idea is to truncate the computation at some finite lag order p , where p grows as, say, $T^{1/4}$. The trouble with this is that the resulting $\hat{\Omega}$ may not be a positive definite matrix. In practical terms, we may end up with negative estimated variances. One solution to this problem is offered by The Newey–West estimator (Newey and West, 1987), which assigns declining weights to the sample autocovariances as the temporal separation increases.

To understand this point it is helpful to look more closely at the covariance matrix given in (22.5), namely,

$$(X'X)^{-1}(X'\hat{\Omega}X)(X'X)^{-1}$$

This is known as a “sandwich” estimator. The bread, which appears on both sides, is $(X'X)^{-1}$. This $k \times k$ matrix is also the key ingredient in the computation of the classical covariance matrix. The filling in the sandwich is

$$\begin{array}{ccccc} \hat{\Sigma} & = & X' & \hat{\Omega} & X \\ (k \times k) & & (k \times T) & (T \times T) & (T \times k) \end{array}$$

It can be proven that under mild regularity conditions $T^{-1}\hat{\Sigma}$ is a consistent estimator of the long-run covariance matrix of the random k -vector $x_t \cdot u_t$.

From a computational point of view it is neither necessary nor desirable to store the (potentially very large) $T \times T$ matrix $\hat{\Omega}$ as such. Rather, one computes the sandwich filling by summation as a weighted sum:

$$\hat{\Sigma} = \hat{\Gamma}(0) + \sum_{j=1}^p w_j (\hat{\Gamma}(j) + \hat{\Gamma}'(j))$$

where w_j is the weight given to lag $j > 0$ and the $k \times k$ matrix $\hat{\Gamma}(j)$, for $j \geq 0$, is given by

$$\hat{\Gamma}(j) = \sum_{t=j+1}^T \hat{u}_t \hat{u}_{t-j}' X_t' X_{t-j};$$

that is, the sample autocovariance matrix of $x_t \cdot u_t$ at lag j , apart from a scaling factor T .

This leaves two questions. How exactly do we determine the maximum lag length or “bandwidth”, p , of the HAC estimator? And how exactly are the weights w_j to be determined? We will return to the (difficult) question of the bandwidth shortly. As regards the weights, gretl offers three variants. The default is the Bartlett kernel, as used by Newey and West. This sets

$$w_j = \begin{cases} 1 - \frac{j}{p+1} & j \leq p \\ 0 & j > p \end{cases}$$

so the weights decline linearly as j increases. The other two options are the Parzen kernel and the Quadratic Spectral (QS) kernel. For the Parzen kernel,

$$w_j = \begin{cases} 1 - 6a_j^2 + 6a_j^3 & 0 \leq a_j \leq 0.5 \\ 2(1 - a_j)^3 & 0.5 < a_j \leq 1 \\ 0 & a_j > 1 \end{cases}$$

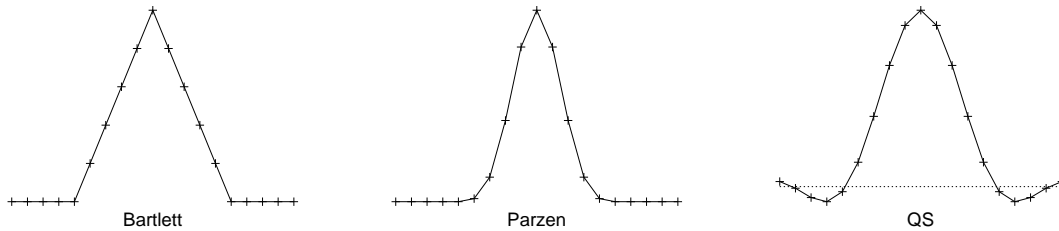
where $a_j = j/(p+1)$, and for the QS kernel,

$$w_j = \frac{25}{12\pi^2 d_j^2} \left(\frac{\sin m_j}{m_j} - \cos m_j \right)$$

where $d_j = j/p$ and $m_j = 6\pi d_j/5$.

Figure 22.1 shows the weights generated by these kernels, for $p = 4$ and $j = 1$ to 9.

Figure 22.1: Three HAC kernels



In gretl you select the kernel using the `set` command with the `hac_kernel` parameter:

```
set hac_kernel parzen
set hac_kernel qs
set hac_kernel bartlett
```

Selecting the HAC bandwidth

The asymptotic theory developed by Newey, West and others tells us in general terms how the HAC bandwidth, p , should grow with the sample size, T —that is, p should grow in proportion to some fractional power of T . Unfortunately this is of little help to the applied econometrician, working with a given dataset of fixed size. Various rules of thumb have been suggested and gretl implements two such. The default is $p = 0.75T^{1/3}$, as recommended by [Stock and Watson \(2003\)](#). An alternative is $p = 4(T/100)^{2/9}$, as in [Wooldridge \(2002b\)](#). In each case one takes the integer part of the result. These variants are labeled `nw1` and `nw2` respectively, in the context of the `set` command with the `hac_lag` parameter. That is, you can switch to the version given by Wooldridge with

```
set hac_lag nw2
```

As shown in Table 22.1 the choice between nw1 and nw2 does not make a great deal of difference.

T	p (nw1)	p (nw2)
50	2	3
100	3	4
150	3	4
200	4	4
300	5	5
400	5	5

Table 22.1: HAC bandwidth: two rules of thumb

You also have the option of specifying a fixed numerical value for p , as in

```
set hac_lag 6
```

In addition you can set a distinct bandwidth for use with the Quadratic Spectral kernel (since this need not be an integer). For example,

```
set qs_bandwidth 3.5
```

Prewhitening and data-based bandwidth selection

An alternative approach is to deal with residual autocorrelation by attacking the problem from two sides. The intuition behind the technique known as *VAR prewhitening* (Andrews and Monahan, 1992) can be illustrated by a simple example. Let x_t be a sequence of first-order autocorrelated random variables

$$x_t = \rho x_{t-1} + u_t$$

The long-run variance of x_t can be shown to be

$$V_{LR}(x_t) = \frac{V_{LR}(u_t)}{(1 - \rho)^2}$$

In most cases u_t is likely to be less autocorrelated than x_t , so a smaller bandwidth should suffice. Estimation of $V_{LR}(x_t)$ can therefore proceed in three steps: (1) estimate ρ ; (2) obtain a HAC estimate of $\hat{u}_t = x_t - \hat{\rho}x_{t-1}$; and (3) divide the result by $(1 - \rho)^2$.

The application of the above concept to our problem implies estimating a finite-order Vector Autoregression (VAR) on the vector variables $\xi_t = X_t \hat{u}_t$. In general the VAR can be of any order, but in most cases 1 is sufficient; the aim is not to build a watertight model for ξ_t , but just to “mop up” a substantial part of the autocorrelation. Hence, the following VAR is estimated

$$\xi_t = A\xi_{t-1} + \varepsilon_t$$

Then an estimate of the matrix $X'\Omega X$ can be recovered via

$$(I - \hat{A})^{-1} \hat{\Sigma}_\varepsilon (I - \hat{A}')^{-1}$$

where $\hat{\Sigma}_\varepsilon$ is any HAC estimator, applied to the VAR residuals.

You can ask for prewhitening in gretl using

```
set hac_prewhitened on
```


There is at present no mechanism for specifying an order other than 1 for the initial VAR.

A further refinement is available in this context, namely data-based bandwidth selection. It makes intuitive sense that the HAC bandwidth should not simply be based on the size of the sample, but should somehow take into account the time-series properties of the data (and also the kernel chosen). A nonparametric method for doing this was proposed by [Newey and West \(1994\)](#); a good concise account of the method is given in [Hall \(2005\)](#). This option can be invoked in gretl via

```
set hac_lag nw3
```

This option is the default when prewhitening is selected, but you can override it by giving a specific numerical value for `hac_lag`.

Even the Newey–West data-based method does not fully pin down the bandwidth for any particular sample. The first step involves calculating a series of residual covariances. The length of this series is given as a function of the sample size, but only up to a scalar multiple—for example, it is given as $O(T^{2/9})$ for the Bartlett kernel. Gretl uses an implied multiple of 1.

Newey–West with missing values

If the estimation sample for a time-series model includes incomplete observations—where the value of the dependent variable or one more regressors is missing—the Newey–West procedure must be either modified or abandoned, since some ingredients of the $\hat{\Sigma}$ matrix defined above will be absent. Two modified methods have been discussed in the literature. [Parzen \(1963\)](#) proposed what he called Amplitude Modulation (AM), which involves setting the values of the residual and each of the regressors to zero for the incomplete observations (and then proceeding as usual). [Datta and Du \(2012\)](#) propose the so-called Equal Spacing (ES) method: calculate as if the incomplete observations did not exist, and the complete observations therefore form an equally-spaced series. Somewhat suprisingly, it can be shown that both of these methods have appropriate asymptotic properties; see [Rho and Vogelsang \(2018\)](#) for further elaboration.

In gretl you can select a preferred method via one or other of these commands:

```
set hac_missvals es # ES, Datta and Du
set hac_missvals am # AM, Parzen
set hac_missvals off
```

The ES method is the default. The `off` option means that gretl will refuse to produce HAC standard errors when the sample includes incomplete observations: use this if you have qualms about the modified methods.

VARs: a special case

A well-specified vector autoregression (VAR) will generally include enough lags of the dependent variables to obviate the problem of residual autocorrelation, in which case HAC estimation is redundant—although there may still be a need to correct for heteroskedasticity. For that reason plain HCCME, and not HAC, is the default when the `--robust` flag is given in the context of the `var` command. However, if for some reason you need HAC you can force the issue by giving the option `--robust-hac`.

Long-run variance

Let us expand a little on the subject of the long-run variance that was mentioned above and the associated tools offered by gretl for scripting. (You may also want to check out the reference for the `lrcovar` function for the multivariate case.) As is well known, the variance of the average of T random variables x_1, x_2, \dots, x_T with equal variance σ^2 equals σ^2/T if the data are uncorrelated. In this case, the sample variance of x_t over the sample size provides a consistent estimator.

If, however, there is serial correlation among the x_t s, the variance of $\bar{X} = T^{-1} \sum_{t=1}^T x_t$ must be estimated differently. One of the most widely used statistics for this purpose is a nonparametric kernel estimator with the Bartlett kernel defined as

$$\hat{\omega}^2(k) = T^{-1} \sum_{t=k}^{T-k} \left[\sum_{i=-k}^k w_i (x_t - \bar{X})(x_{t-i} - \bar{X}) \right], \quad (22.6)$$

where the integer k is known as the window size and the w_i terms are the so-called *Bartlett weights*, defined as $w_i = 1 - \frac{|i|}{k+1}$. It can be shown that, for k large enough, $\hat{\omega}^2(k)/T$ yields a consistent estimator of the variance of \bar{X} .

gretl implements this estimator by means of the function `lrvar()`. This function takes one required argument, namely the series whose long-run variance is to be estimated, followed by two optional arguments. The first of these can be used to supply a value for k ; if it is omitted or negative, the popular choice $T^{1/3}$ is used. The second allows specification of an assumed value for the population mean of X , which then replaces \bar{X} in the variance calculation. Usage is illustrated below.

```
# automatic window size; use xbar for mean
lrs2 = lrvar(x)
# set a window size of 12
lrs2 = lrvar(x, 12)
# set window size and impose assumed mean of zero
lrs2 = lrvar(x, 12, 0)
# impose mean zero, automatic window size
lrs2 = lrvar(x, -1, 0)
```

22.4 Special issues with panel data

Since panel data have both a time-series and a cross-sectional dimension one might expect that, in general, robust estimation of the covariance matrix would require handling both heteroskedasticity and autocorrelation (the HAC approach). In addition, some special features of panel data require attention.

- The variance of the error term may differ across the cross-sectional units.
- The covariance of the errors across the units may be non-zero in each time period.
- If the “between” variation is not swept out, the errors may exhibit autocorrelation, not in the usual time-series sense but in the sense that the mean value of the error term may differ across units. This is relevant when estimation is by pooled OLS.

Gretl currently offers three panel-specific covariance matrix estimators in response to the `--robust` option. These are available for models estimated via fixed effects, random effects, pooled OLS, and pooled two-stage least squares. The default robust estimator is that suggested by [Arellano \(2003\)](#), which is HAC provided the panel is of the “large n , small T ” variety (that is, many units are observed in relatively few periods). The Arellano estimator involves clustering by the cross-sectional unit:

$$\hat{\Sigma}_A = (X'X)^{-1} \left(\sum_{i=1}^n X_i' \hat{u}_i \hat{u}_i' X_i \right) (X'X)^{-1}$$

where X is the matrix of regressors (with the group means subtracted in the case of fixed effects, or quasi-demeaned in the case of random effects) \hat{u}_i denotes the vector of residuals for unit i , and n is the number of such units. [Cameron and Trivedi \(2005\)](#) make a strong case for using this estimator; they note that the ordinary White HCCME can produce misleadingly small standard errors in the panel context because it fails to take autocorrelation into account.² In addition [Stock and Watson \(2008\)](#) show that the White HCCME is inconsistent in the fixed-effects panel context for fixed $T > 2$.

²See also [Cameron and Miller \(2015\)](#) for a discussion of the Arellano-type estimator in the context of the random effects model.

In cases where autocorrelation is not an issue the estimator proposed by [Beck and Katz \(1995\)](#) and discussed by [Greene \(2003, chapter 13\)](#) may be appropriate. This estimator, which takes into account contemporaneous correlation across the units and heteroskedasticity by unit, is

$$\hat{\Sigma}_{BK} = (X'X)^{-1} \left(\sum_{i=1}^n \sum_{j=1}^n \hat{\sigma}_{ij} X_i' X_j \right) (X'X)^{-1}$$

The covariances $\hat{\sigma}_{ij}$ are estimated via

$$\hat{\sigma}_{ij} = \frac{\hat{u}_i' \hat{u}_j}{T_i}$$

where T_i is the length of the time series for unit i . Beck and Katz call the associated standard errors “Panel-Corrected Standard Errors” (PCSE). This estimator can be invoked in `gretl` via the command

```
set panel_robust pcse
```

The Arellano default can be re-established via

```
set panel_robust arellano
```

The third panel-specific option is the spatial correlation consistent (SCC) estimator developed by [Driscoll and Kraay \(1998\)](#). This addresses cross-sectional dependence of the disturbances as well as heteroskedasticity and autocorrelation. Serial correlation is handled in the manner of Newey–West and, unlike the Arellano estimator, consistency is not limited to the “small T ” case. The command to select SCC is

```
set panel_robust scc
```

An additional “set” variable is relevant when using this estimator, namely `hac_lag`, which governs the bandwidth of the kernel employed in the Newey–West component as described in section 22.3 above. But note that in the SCC context only the Bartlett kernel is supported, and neither prewhitening nor data-based bandwidth selection are available. So the applicable `hac_lag` variants are just `nw1`, `nw2` or a user-specified maximum (integer) lag. To replicate results from the `xtscc` command for Stata ([Hoechle, 2007](#)) the `nw2` variant should be selected.

Note that regardless of the `panel_robust` setting, the robust estimator is not used unless the `--robust` flag is given with the estimation command (or the “Robust” box is checked in the graphical interface). For some further remarks on the panel case, the following section.

22.5 The cluster-robust estimator

We begin by describing the cluster-robust variance estimator in general terms. Specific points pertaining to panel data follow in the final subsection.

This estimator is appropriate when the observations naturally fall into groups or clusters, and the error term exhibits dependency within the clusters and/or heteroskedasticity across clusters. Such clusters may be binary (e.g. employed versus unemployed workers), categorical with several values (e.g. products grouped by manufacturer) or ordinal (e.g. individuals with low, middle or high education levels).

For linear regression models estimated via least squares the cluster estimator is defined as

$$\hat{\Sigma}_C = (X'X)^{-1} \left(\sum_{j=1}^m X_j' \hat{u}_j \hat{u}_j' X_j \right) (X'X)^{-1}$$

where m denotes the number of clusters, and X_j and \hat{u}_j denote, respectively, the matrix of regressors and the vector of residuals that fall within cluster j . As noted above, the Arellano variance estimator for panel data models is a special case of this, where the clustering is by panel unit.

For models estimated by the method of Maximum Likelihood (in which case the standard variance estimator is the inverse of the negative Hessian, H), the cluster estimator is

$$\hat{\Sigma}_C = H^{-1} \left(\sum_{j=1}^m G_j' G_j \right) H^{-1}$$

where G_j is the sum of the “score” (that is, the derivative of the loglikelihood with respect to the parameter estimates) across the observations falling within cluster j .

It is common to apply a degrees of freedom adjustment to these estimators (otherwise the variance may appear misleadingly small in comparison with other estimators if the number of clusters is small). In the least squares case the factor is $(m/(m-1)) \times (n-1)/(n-k)$, where n is the total number of observations and k is the number of parameters estimated; in the case of ML estimation the factor is just $m/(m-1)$.

Availability and syntax

Cluster-robust estimation is invoked via the `--cluster` option, which is available for models estimated via OLS and TSLS, and also for most ML estimators other than those specialized for time-series data; so binary logit and probit, ordered logit and probit, multinomial logit, Tobit, interval regression, biprobit, count models and duration models are all supported. In addition this option is available for generic maximum likelihood estimation as provided by the `mle` command (see chapter 26 for more details).

The `--cluster` option has a required parameter, the name of a series that defines the clusters, as in

```
ols y 0 x1 x2 --cluster=cvar
```

The specified series must (a) be defined (not missing) at all observations used in estimating the model and (b) take on at least two distinct values over the estimation range. The clusters are defined as sets of observations having a common value for the series in question. It is generally expected that the number of clusters is substantially less than the total number of observations.

Panel data specifics

In the case of panel data, two additional features are supported. First, two comma-separated cluster variables can be given with the `--cluster` option, for two-way clustering. Second, the special terms `$unit` and `$time` can be used in place of names of existing series to specify, respectively, clustering by cross-sectional unit and by time period. So for example, the command

```
panel ... --cluster=$unit,$time
```

invokes two-way clustering that allows for dependence of the error term both within unit and within period. The special terms can be used individually, in combination as shown above, or in combination with other suitable series.

☞ You can use named series that identify unit and time rather than the `$`-terms, but the latter are a good deal more efficient since they key directly into the panel structure of the dataset. Given an arbitrary named series more work is needed to determine which observations fall within which clusters.

A plausible case for clustering by a named series arises if the dataset contains a series that identifies a set of groups into which the panel units fall—for example, the panel units are individuals but you know which individuals are members of which household, or the panel units are counties but you know in which state each county is located. Then you may wish to cluster at the more aggregated level, as in

```

panel ... --cluster=household
# OR
panel ... --cluster=state

```

In these cases, of course, the parameter to `--cluster` must be the name of a series that does the job, providing a unique identifier for each of the groups.

The method for two-way clustering is that described by [Cameron *et al.* \(2011\)](#); that is, the variance estimator is

$$\hat{\Sigma}_{C2} = \Sigma_1 + \Sigma_2 - \Sigma_{1,2}$$

where Σ_1 and Σ_2 are the variance estimators produced using the two cluster variables taken individually and $\Sigma_{1,2}$ is the estimator obtained from their combination. In case $\hat{\Sigma}_{C2}$ is not positive semi-definite we calculate its eigen decomposition, set any negative eigenvalues to zero, and recreate the matrix.

Note that if a cluster variable C1 is nested within a more highly aggregated one, C2, then two-way clustering is not called for since it amounts to clustering on C2 alone. To continue the example from above, if the panel units are counties and the assignment of counties to states is time-invariant, the command

```

panel ... --cluster=$unit,state # not recommended!

```

is just a round-about way of asking for clustering by state.

The precise magnitude of standard errors produced in case of cluster-robust estimation depends on whether a degrees of freedom adjustment is applied, and if so on how exactly the adjustment is calculated—a matter which is somewhat debatable. The default procedure in `gretl` is that of [Cameron *et al.* \(2011\)](#). That is, we apply an adjustment factor equal to

$$\frac{m}{m-1} \times \frac{n-1}{n-k}$$

where m is the number of clusters, n is the total number of observations, and k is the number of parameters estimated. Results then agree with Stata's `xtreg` command and also the `cgmreg` command made available by Colin Cameron.³ To produce clustered standard errors in agreement with the popular contributed Stata command `xtivreg2` it is necessary to suppress this adjustment: append the `--no-df-corr` option to the `panel` command.

³As of 2023-10-12 this is available via <https://cameron.econ.ucdavis.edu/research/cgmreg.ado>.

Chapter 23

Panel data

A panel dataset is one in which each of $N > 1$ units (sometimes called “individuals” or “groups”) is observed over time. In a balanced panel there are $T > 1$ observations on each unit; more generally the number of observations may differ by unit. In the following we index units by i and time by t . To allow for imbalance in a panel we use the notation T_i to refer to the number of observations for unit or individual i .

23.1 Estimation of panel models

Pooled Ordinary Least Squares

The simplest estimator for panel data is pooled OLS. In most cases this is unlikely to be adequate, but it provides a baseline for comparison with more complex estimators.

If you estimate a model on panel data using OLS an additional test item becomes available. In the GUI model window this is the item “panel specification” under the Tests menu; the script counterpart is the `panspec` command.

To take advantage of this test, you should specify a model without any dummy variables representing cross-sectional units. The test compares pooled OLS against the principal alternatives, the fixed effects and random effects models. These alternatives are explained in the following section.

The fixed and random effects models

In the graphical interface these options are found under the menu item “Model/Panel/Fixed and random effects”. In the command-line interface one uses the `panel` command, with or without the `--random-effects` option. (The `--fixed-effects` option is also allowed but not strictly necessary, being the default.)

This section explains the nature of these models and comments on their estimation via `gretl`.

The pooled OLS specification may be written as

$$y_{it} = X_{it}\beta + u_{it} \quad (23.1)$$

where y_{it} is the observation on the dependent variable for cross-sectional unit i in period t , X_{it} is a $1 \times k$ vector of independent variables observed for unit i in period t , β is a $k \times 1$ vector of parameters, and u_{it} is an error or disturbance term specific to unit i in period t .

The fixed and random effects models have in common that they decompose the unitary pooled error term, u_{it} . For the *fixed effects* model we write $u_{it} = \alpha_i + \varepsilon_{it}$, yielding

$$y_{it} = X_{it}\beta + \alpha_i + \varepsilon_{it} \quad (23.2)$$

That is, we decompose u_{it} into a unit-specific and time-invariant component, α_i , and an observation-specific error, ε_{it} .¹ The α_i s are then treated as fixed parameters (in effect, unit-specific y -intercepts), which are to be estimated. This can be done by including a dummy variable for each cross-sectional

¹It is possible to break a third component out of u_{it} , namely w_t , a shock that is time-specific but common to all the units in a given period. In the interest of simplicity we do not pursue that option here.

unit (and suppressing the global constant). This is sometimes called the Least Squares Dummy Variables (LSDV) method. Alternatively, one can subtract the group mean from each of variables and estimate a model without a constant. In the latter case the dependent variable may be written as

$$\tilde{y}_{it} = y_{it} - \bar{y}_i$$

The “group mean”, \bar{y}_i , is defined as

$$\bar{y}_i = \frac{1}{T_i} \sum_{t=1}^{T_i} y_{it}$$

where T_i is the number of observations for unit i . An exactly analogous formulation applies to the independent variables. Given parameter estimates, $\hat{\beta}$, obtained using such de-meaned data we can recover estimates of the α_i s using

$$\hat{\alpha}_i = \frac{1}{T_i} \sum_{t=1}^{T_i} (y_{it} - X_{it}\hat{\beta})$$

These two methods (LSDV, and using de-meaned data) are numerically equivalent. gretl takes the approach of de-meaning the data. If you have a small number of cross-sectional units, a large number of time-series observations per unit, and a large number of regressors, it is more economical in terms of computer memory to use LSDV. If need be you can easily implement this manually. For example,

```
genr unitdum
ols y x du_*
```

(See Chapter 10 for details on `unitdum`).

The $\hat{\alpha}_i$ estimates are not printed as part of the standard model output in gretl (there may be a large number of these, and typically they are not of much inherent interest). However you can retrieve them after estimation of the fixed effects model if you wish. In the graphical interface, go to the “Save” menu in the model window and select “per-unit constants”. In command-line mode, you can do `series newname = $ahat`, where *newname* is the name you want to give the series.

For the *random effects* model we write $u_{it} = v_i + \varepsilon_{it}$, so the model becomes

$$y_{it} = X_{it}\beta + v_i + \varepsilon_{it} \quad (23.3)$$

In contrast to the fixed effects model, the v_i s are not treated as fixed parameters, but as random drawings from a given probability distribution.

The celebrated Gauss-Markov theorem, according to which OLS is the best linear unbiased estimator (BLUE), depends on the assumption that the error term is independently and identically distributed (IID). In the panel context, the IID assumption means that $E(u_{it}^2)$, in relation to equation 23.1, equals a constant, σ_u^2 , for all i and t , while the covariance $E(u_{is}u_{it})$ equals zero for all $s \neq t$ and the covariance $E(u_{jt}u_{it})$ equals zero for all $j \neq i$.

If these assumptions are not met—and they are unlikely to be met in the context of panel data—OLS is not the most efficient estimator. Greater efficiency may be gained using generalized least squares (GLS), taking into account the covariance structure of the error term.

Consider observations on a given unit i at two different times s and t . From the hypotheses above it can be worked out that $\text{Var}(u_{is}) = \text{Var}(u_{it}) = \sigma_v^2 + \sigma_\varepsilon^2$, while the covariance between u_{is} and u_{it} is given by $E(u_{is}u_{it}) = \sigma_v^2$.

In matrix notation, we may group all the T_i observations for unit i into the vector \mathbf{y}_i and write it as

$$\mathbf{y}_i = \mathbf{X}_i\beta + \mathbf{u}_i \quad (23.4)$$

The vector \mathbf{u}_i , which includes all the disturbances for individual i , has a variance-covariance matrix given by

$$\text{Var}(\mathbf{u}_i) = \Sigma_i = \sigma_\varepsilon^2 I + \sigma_v^2 J \quad (23.5)$$

where J is a square matrix with all elements equal to 1. It can be shown that the matrix

$$K_i = I - \frac{\theta_i}{T_i} J,$$

where $\theta_i = 1 - \sqrt{\sigma_\varepsilon^2 / (\sigma_\varepsilon^2 + T_i \sigma_v^2)}$, has the property

$$K_i \Sigma K_i' = \sigma_\varepsilon^2 I$$

It follows that the transformed system

$$K_i \mathbf{y}_i = K_i \mathbf{X}_i \beta + K_i \mathbf{u}_i \quad (23.6)$$

satisfies the Gauss-Markov conditions, and OLS estimation of (23.6) provides efficient inference. But since

$$K_i \mathbf{y}_i = \mathbf{y}_i - \theta_i \bar{\mathbf{y}}_i$$

GLS estimation is equivalent to OLS using “quasi-demeaned” variables; that is, variables from which we subtract a fraction θ of their average.² Notice that for $\sigma_\varepsilon^2 \rightarrow 0$, $\theta \rightarrow 1$, while for $\sigma_v^2 \rightarrow 0$, $\theta \rightarrow 0$. This means that if all the variance is attributable to the individual effects, then the fixed effects estimator is optimal; if, on the other hand, individual effects are negligible, then pooled OLS turns out, unsurprisingly, to be the optimal estimator.

To implement the GLS approach we need to calculate θ , which in turn requires estimates of the two variances σ_ε^2 and σ_v^2 . (These are often referred to as the “within” and “between” variances respectively, since the former refers to variation within each cross-sectional unit and the latter to variation between the units). Several means of estimating these magnitudes have been suggested in the literature (see Baltagi, 1995); by default gretl uses the method of Swamy and Arora (1972): σ_ε^2 is estimated by the residual variance from the fixed effects model, and σ_v^2 is estimated indirectly with the help of the “between” regression which uses the group means of all the relevant variables: is,

$$\bar{\mathbf{y}}_i = \bar{\mathbf{X}}_i \beta + e_i$$

The residual variance from this regression, s_e^2 , can be shown to estimate the sum $\sigma_v^2 + \sigma_\varepsilon^2/T$. An estimate of σ_v^2 can therefore be obtained by subtracting $1/T$ times the estimate of σ_ε^2 from s_e^2 :

$$\hat{\sigma}_v^2 = s_e^2 - \hat{\sigma}_\varepsilon^2/T \quad (23.7)$$

Alternatively, if the `--nerlove` option is given, gretl uses the method suggested by Nerlove (1971). In this case σ_v^2 is estimated as the sample variance of the fixed effects, $\hat{\alpha}_i$,

$$\hat{\sigma}_v^2 = \frac{1}{N-1} \sum_{i=1}^n (\hat{\alpha}_i - \bar{\hat{\alpha}})^2 \quad (23.8)$$

where N is the number of individuals and $\bar{\hat{\alpha}}$ is the mean of the estimated fixed effects.

Swamy and Arora’s equation (23.7) involves T , hence assuming a balanced panel. When the number of time series observations, T_i , differs across individuals some sort of adjustment is needed. By default gretl follows Stata by using the harmonic mean of the T_i s in place of T . It may be argued, however, that a more substantial adjustment is called for in the unbalanced case. Baltagi and Chang (1994) recommend a variant of Swamy–Arora which involves T_i -weighted estimation of the between regression, on the basis that units with more observations will be more informative about the variance of interest. In gretl one can switch to the Baltagi–Chang variant by giving the `--unbalanced`

²In a balanced panel, the value of θ is common to all individuals, otherwise it differs depending on the value of T_i .

option with the `panel` command. But the gain in efficiency from doing so may well be slim; for a discussion of this point and related matters see [Cottrell \(2017\)](#). Unbalancedness also affects the [Nerlove \(1971\)](#) estimator, but the econometric literature offers no guidance on the details. Gretl uses the weighted average of the fixed effects as a natural extension of the original method. Again, see [Cottrell \(2017\)](#) for further details.

Choice of estimator

Which panel method should one use, fixed effects or random effects?

One way of answering this question is in relation to the nature of the data set. If the panel comprises observations on a fixed and relatively small set of units of interest (say, the member states of the European Union), there is a presumption in favor of fixed effects. If it comprises observations on a large number of randomly selected individuals (as in many epidemiological and other longitudinal studies), there is a presumption in favor of random effects.

Besides this general heuristic, however, various statistical issues must be taken into account.

1. Some panel data sets contain variables whose values are specific to the cross-sectional unit but which do not vary over time. If you want to include such variables in the model, the fixed effects option is simply not available. When the fixed effects approach is implemented using dummy variables, the problem is that the time-invariant variables are perfectly collinear with the per-unit dummies. When using the approach of subtracting the group means, the issue is that after de-meaning these variables are nothing but zeros.
2. A somewhat analogous issue arises with the random effects estimator. As mentioned above, the default Swamy–Arora method relies on the group-means regression to obtain a measure of the between variance. Suppose we have observations on n units or individuals and there are k independent variables of interest. If $k > n$, this regression cannot be run—since we have only n effective observations—and hence Swamy–Arora estimates cannot be obtained. In this case, however, it is possible to use Nerlove’s method instead.

If both fixed effects and random effects are feasible for a given specification and dataset, the choice between these estimators may be expressed in terms of the two econometric *desiderata*, efficiency and consistency.

From a purely statistical viewpoint, we could say that there is a tradeoff between robustness and efficiency. In the fixed effects approach, we do not make any hypotheses on the “group effects” (that is, the time-invariant differences in mean between the groups) beyond the fact that they exist—and that can be tested; see below. As a consequence, once these effects are swept out by taking deviations from the group means, the remaining parameters can be estimated.

On the other hand, the random effects approach attempts to model the group effects as drawings from a probability distribution instead of removing them. This requires that individual effects are representable as a legitimate part of the disturbance term, that is, zero-mean random variables, uncorrelated with the regressors.

As a consequence, the fixed-effects estimator “always works”, but at the cost of not being able to estimate the effect of time-invariant regressors. The richer hypothesis set of the random-effects estimator ensures that parameters for time-invariant regressors can be estimated, and that estimation of the parameters for time-varying regressors is carried out more efficiently. These advantages, though, are tied to the validity of the additional hypotheses. If, for example, there is reason to think that individual effects may be correlated with some of the explanatory variables, then the random-effects estimator would be inconsistent, while fixed-effects estimates would still be valid. The Hausman test is built on this principle (see below): if the fixed- and random-effects estimates agree, to within the usual statistical margin of error, there is no reason to think the additional hypotheses invalid, and as a consequence, no reason *not* to use the more efficient RE estimator.

Testing panel models

If you estimate a fixed effects or random effects model in the graphical interface, you may notice that the number of items available under the “Tests” menu in the model window is relatively limited. Panel models carry certain complications that make it difficult to implement all of the tests one expects to see for models estimated on straight time-series or cross-sectional data.

Nonetheless, various panel-specific tests are printed along with the parameter estimates as a matter of course, as follows.

When you estimate a model using *fixed effects*, you automatically get an *F*-test for the null hypothesis that the cross-sectional units all have a common intercept. That is to say that all the α_i s are equal, in which case the pooled model (23.1), with a column of 1s included in the X matrix, is adequate.

When you estimate using *random effects* (RE), the Breusch–Pagan and Hausman tests are presented automatically. To save their results in the context of a script one would copy the `$model.bp_test` or `$model.hausman_test` bundles which are nested inside the `$model` bundle. Both of these inner bundles contain the elements `test`, `dfn` (degrees of freedom), and `pvalue`.

The Breusch–Pagan test is the counterpart to the *F*-test mentioned above. The null hypothesis is that the variance of v_i in equation (23.3) equals zero; if this hypothesis is not rejected, then again we conclude that the simple pooled model is adequate. If the panel is unbalanced the method from Baltagi and Li (1990) is used to perform the Breusch–Pagan test for individual effects.

The Hausman test probes the consistency of the GLS estimates. The null hypothesis is that these estimates are consistent—that is, that the requirement of orthogonality of the v_i and the X_i is satisfied. The test is based on a measure, H , of the “distance” between the fixed-effects and random-effects estimates, constructed such that under the null it follows the χ^2 distribution with degrees of freedom equal to the number of time-varying regressors in the matrix X . If the value of H is “large” this suggests that the random effects estimator is not consistent and the fixed-effects model is preferable.

There are two ways of calculating H , the matrix-difference method and the regression method. The procedure for the matrix-difference method is this:

- Collect the fixed-effects estimates in a vector $\tilde{\beta}$ and the corresponding random-effects estimates in $\hat{\beta}$, then form the difference vector $(\tilde{\beta} - \hat{\beta})$.
- Form the covariance matrix of the difference vector as $\text{Var}(\tilde{\beta} - \hat{\beta}) = \text{Var}(\tilde{\beta}) - \text{Var}(\hat{\beta}) = \Psi$, where $\text{Var}(\tilde{\beta})$ and $\text{Var}(\hat{\beta})$ are estimated by the sample variance matrices of the fixed- and random-effects models respectively.³
- Compute $H = (\tilde{\beta} - \hat{\beta})' \Psi^{-1} (\tilde{\beta} - \hat{\beta})$.

Given the relative efficiencies of $\tilde{\beta}$ and $\hat{\beta}$, the matrix Ψ “should be” positive definite, in which case H is positive, but in finite samples this is not guaranteed and of course a negative χ^2 value is not admissible.

The regression method avoids this potential problem. The procedure is to estimate, via OLS, an augmented regression in which the dependent variable is quasi-demeaned y and the regressors include both quasi-demeaned X (as in the RE specification) and the de-meaned variants of all the time-varying variables (i.e. the fixed-effects regressors). The Hausman null then implies that the coefficients on the latter subset of regressors should be statistically indistinguishable from zero.

If the RE specification employs the default covariance-matrix estimator (assuming IID errors), H can be obtained as follows:

³Hausman (1978) showed that the covariance of the difference takes this simple form when $\hat{\beta}$ is an efficient estimator and $\tilde{\beta}$ is inefficient.

- Treat the random-effects model as the restricted model, and record its sum of squared residuals as SSR_r .
- Estimate the augmented (unrestricted) regression and record its sum of squared residuals as SSR_u .
- Compute $H = n (SSR_r - SSR_u) / SSR_u$, where n is the total number of observations used.

Alternatively, if the `--robust` option is selected for RE estimation, H is calculated as a Wald test based on a robust estimate of the covariance matrix of the augmented regression. Either way, H cannot be negative.

By default `gretl` computes the Hausman test via the regression method, but it uses the matrix-difference method if you pass the option `--matrix-diff` to the `panel` command.

Serial correlation

A simple test for first-order autocorrelation of the error term, namely the Durbin-Watson (DW) statistic, is printed as part of the output for pooled OLS as well as fixed-effects and random-effects estimation. Let us define “serial correlation proper” as serial correlation strictly in the time dimension of a panel dataset. When based on the residuals from fixed-effects estimation, the DW statistic is a test for serial correlation proper.⁴ The DW value shown in the case of random-effects estimation is based on the fixed-effects residuals. When DW is based on pooled OLS residuals it tests for serial correlation proper only on the assumption of a common intercept. Put differently, in this case it tests a joint null hypothesis: absence of fixed effects plus absence of (first order) serial correlation proper. In the presence of missing observations the DW statistic is calculated as described in [Baltagi and Wu \(1999\)](#) (their expression for d_1 under equation (16) on page 819).

When it is computed, the DW statistic can be retrieved via the accessor `$dw` after estimation. In addition, an approximate P -value for the null of no serial correlation ($\rho = 0$) against the alternative of $\rho > 0$ may be available via the accessor `$dwpval`. This is based on the analysis in [Bhargava et al. \(1982\)](#); strictly speaking it is the marginal significance level of DW considered as a d_L value (the value below which the test rejects, as opposed to d_U , the value above which the test fails to reject). In the panel case, however, d_L and d_U are quite close, particularly when N (the number of individual units) is large. At present `gretl` does not attempt to compute such P -values when the number of observations differs across individuals.

Robust standard errors

For most estimators, `gretl` offers the option of computing an estimate of the covariance matrix that is robust with respect to heteroskedasticity and/or autocorrelation (and hence also robust standard errors). In the case of panel data, robust covariance matrix estimators are available for the pooled, fixed effects and random effects models. See section [22.4](#) for details.

The constant in the fixed effects model

Users are sometimes puzzled by the constant or intercept reported by `gretl` on estimation of the fixed effects model: how can a constant remain when the group means have been subtracted from the data? The method of calculation of this term is a matter of convention, but the `gretl` authors decided to follow the convention employed by `Stata`; this involves adding the global mean back into the variables from which the group means have been removed.⁵ If you prefer to interpret the fixed effects model as “OLS plus unit dummies throughout”, it can be proven the this approach is equivalent to using centered unit dummies instead of plain 0/1 dummies.

⁴The generalization of the Durbin-Watson statistic from the straight time-series context to panel data is due to [Bhargava et al. \(1982\)](#).

⁵See [Gould \(2013\)](#) for an extended explanation.

The method that gretl uses internally is exemplified in Listing 23.1. The coefficients in the second OLS estimation, including the intercept, agree with those in the initial fixed effects model, though the standard errors differ due to a degrees of freedom correction in the fixed-effects covariance matrix. (Note that the `pmean` function returns the group mean of a series.) The third estimator—which produces quite a lot of output—instead uses the `stdize` function to create the centered dummies. It thereby shows the equivalence of the internally-used method to “OLS plus centered dummies”. (Note that in this case the standard errors agree with the initial estimates.)

Listing 23.1: Calculating the intercept in the fixed effects model [\[Download ▼\]](#)

```
open abdata.gdt

list X = w k ys          # list of explanatory variables

### built-in method
panel n const X --fixed-effects

### recentering "by hand"
depvar = n - pmean(n) + mean(n) # redefine the dependent variable
list indepvars = const
loop foreach i X
    # redefine the explanatory variables
    x_$i = $i - pmean($i) + mean($i)
    indepvars += x_$i
endloop
ols depvar indepvars      # perform estimation

### using centered dummies
list C = dummify(unit)    # create the unit dummies
smpl n X --no-missing     # adjust to perform centering correctly
list D = stdize(C, -1)    # center the unit dummies
ols n const X D          # perform estimation
```

R-squared in the fixed effects model

There is no uniquely “correct” way of calculating R^2 in the context of the fixed-effects model. It may be argued that a measure of the squared correlation between the dependent variable and the prediction yielded by the model is a desirable descriptive statistic to have, but which model and which (variant of the) dependent variable are we talking about?

Fixed-effects models can be thought of in two equally defensible ways. From one perspective they provide a nice, clean way of sweeping out individual effects by using the fact that in the linear model a sufficient statistic is easy to compute. Alternatively, they provide a clever way to estimate the “important” parameters of a model in which you want to include (for whatever reason) a full set of individual dummies. If you take the second of these perspectives, your dependent variable is unmodified y and your model includes the unit dummies; the appropriate R^2 measure is then the squared correlation between y and the \hat{y} computed using both the measured individual effects and the effects of the explicitly named regressors. This is reported by gretl as the “LSDV R-squared”. If you take the first point of view, on the other hand, your dependent variable is really $y_{it} - \bar{y}_i$ and your model just includes the β terms, the coefficients of deviations of the x variables from their per-unit means. In this case, the relevant measure of R^2 is the so-called “within” R^2 ; this variant is printed by gretl for fixed-effects model in place of the adjusted R^2 (it being unclear in this case what exactly the “adjustment” should amount to anyway).

Residuals in the fixed and random effect models

After estimation of most kinds of models in gretl, you can retrieve a series containing the residuals using the \$uhat accessor. This is true of the fixed and random effects models, but the exact meaning of gretl's \$uhat in these cases requires a little explanation.

Consider first the fixed effects model:

$$y_{it} = X_{it}\beta + \alpha_i + \varepsilon_{it}$$

In this model gretl takes the “fitted value” (\$yhat) to be $\hat{\alpha}_i + X_{it}\hat{\beta}$, and the residual (\$uhat) to be y_{it} minus this fitted value. This makes sense because the fixed effects (the α_i terms) are taken as parameters to be estimated. However, it can be argued that the fixed effects are not really “explanatory” and if one defines the residual as the observed y_{it} value minus its “explained” component one might prefer to see just $y_{it} - X_{it}\hat{\beta}$. You can get this after fixed-effects estimation as follows:

```
series ue_fe = $uhat + $ahat - $coeff[1]
```

where \$ahat gives the unit-specific intercept (as it would be calculated if one included all N unit dummies and omitted a common y -intercept), and \$coeff[1] gives the “global” y -intercept.⁶

Now consider the random-effects model:

$$y_{it} = X_{it}\beta + v_i + \varepsilon_{it}$$

In this case gretl considers the error term to be $v_i + \varepsilon_{it}$ (since v_i is conceived as a random drawing) and the \$uhat series is an estimate of this, namely

$$y_{it} - X_{it}\hat{\beta}$$

What if you want an estimate of just v_i (or just ε_{it}) in this case? This poses a signal-extraction problem: given the composite residual, how to recover an estimate of its components? The solution is to ascribe to the individual effect, \hat{v}_i , a suitable fraction of the mean residual per individual, $\hat{u}_i = \sum_{t=1}^{T_i} \hat{u}_{it}$. The “suitable fraction” is the proportion of the variance of the variance of \hat{u}_i that is due to v_i , namely

$$\frac{\sigma_v^2}{\sigma_v^2 + \sigma_\varepsilon^2/T_i} = 1 - (1 - \theta_i)^2$$

After random effects estimation in gretl you can access a series containing the \hat{v}_i s under the name \$ahat. This series can be calculated by hand as follows:

```
# case 1: balanced panel
scalar theta = $["theta"]
series vhat = (1 - (1 - theta)^2) * pmean($uhat)

# case 2: unbalanced, Ti varies by individual
scalar s2v = $["s2v"]
scalar s2e = $["s2e"]
series frac = s2v / (s2v + s2e/pnobs($uhat))
series ahat = frac * pmean($uhat)
```

If an estimate of ε_{it} is wanted, it can then be obtained by subtraction from \$uhat.

⁶For anyone used to Stata, gretl's fixed-effects \$uhat corresponds to what you get from Stata's “predict, e” after xtreg, while the second variant corresponds to Stata's “predict, ue”.

23.2 Autoregressive panel models

Special problems arise when a lag of the dependent variable is included among the regressors in a panel model. Consider a dynamic variant of the pooled model (eq. 23.1):

$$y_{it} = X_{it}\beta + \rho y_{it-1} + u_{it} \quad (23.9)$$

First, if the error u_{it} includes a group effect, v_i , then y_{it-1} is bound to be correlated with the error, since the value of v_i affects y_i at all t . That means that OLS applied to (23.9) will be inconsistent as well as inefficient. The fixed-effects model sweeps out the group effects and so overcomes this particular problem, but a subtler issue remains, which applies to both fixed and random effects estimation. Consider the de-meaned representation of fixed effects, as applied to the dynamic model,

$$\tilde{y}_{it} = \tilde{X}_{it}\beta + \rho \tilde{y}_{i,t-1} + \varepsilon_{it}$$

where $\tilde{y}_{it} = y_{it} - \bar{y}_i$ and $\varepsilon_{it} = u_{it} - \bar{u}_i$ (or $u_{it} - \alpha_i$, using the notation of equation 23.2). The trouble is that $\tilde{y}_{i,t-1}$ will be correlated with ε_{it} via the group mean, \bar{y}_i . The disturbance ε_{it} influences y_{it} directly, which influences \bar{y}_i , which, by construction, affects the value of \tilde{y}_{it} for all t . The same issue arises in relation to the quasi-demeaning used for random effects. Estimators which ignore this correlation will be consistent only as $T \rightarrow \infty$ (in which case the marginal effect of ε_{it} on the group mean of y tends to vanish).

One strategy for handling this problem, and producing consistent estimates of β and ρ , was proposed by Anderson and Hsiao (1981). Instead of de-meaning the data, they suggest taking the first difference of (23.9), an alternative tactic for sweeping out the group effects:

$$\Delta y_{it} = \Delta X_{it}\beta + \rho \Delta y_{i,t-1} + \eta_{it} \quad (23.10)$$

where $\eta_{it} = \Delta u_{it} = \Delta(v_i + \varepsilon_{it}) = \varepsilon_{it} - \varepsilon_{i,t-1}$. We're not in the clear yet, given the structure of the error η_{it} : the disturbance $\varepsilon_{i,t-1}$ is an influence on both η_{it} and $\Delta y_{i,t-1} = y_{it} - y_{i,t-1}$. The next step is then to find an instrument for the “contaminated” $\Delta y_{i,t-1}$. Anderson and Hsiao suggest using either $y_{i,t-2}$ or $\Delta y_{i,t-2}$, both of which will be uncorrelated with η_{it} provided that the underlying errors, ε_{it} , are not themselves serially correlated.

The Anderson-Hsiao estimator is not provided as a built-in function in gretl, since gretl's sensible handling of lags and differences for panel data makes it a simple application of regression with instrumental variables—see Listing 23.2, which is based on a study of country growth rates by Nerlove (1999).⁷

Although the Anderson-Hsiao estimator is consistent, it is not most efficient: it does not make the fullest use of the available instruments for $\Delta y_{i,t-1}$, nor does it take into account the differenced structure of the error η_{it} . It is improved upon by the methods of Arellano and Bond (1991) and Blundell and Bond (1998). These methods are taken up in the next chapter.

⁷Also see Clint Cummins' benchmarks page, <http://www.stanford.edu/~clint/bench/>.

Listing 23.2: The Anderson-Hsiao estimator for a dynamic panel model [\[Download ▼\]](#)

```
# Penn World Table data as used by Nerlove
open penngrow.gdt

# Fixed effects (for comparison)
panel Y 0 Y(-1) X

# Random effects (for comparison)
panel Y 0 Y(-1) X --random-effects

# take differences of all variables
diff Y X

# Anderson-Hsiao, using Y(-2) as instrument
tsls d_Y d_Y(-1) d_X ; 0 d_X Y(-2)

# Anderson-Hsiao, using d_Y(-2) as instrument
tsls d_Y d_Y(-1) d_X ; 0 d_X d_Y(-2)
```

Chapter 24

Dynamic panel models

The command for estimating dynamic panel models in gretl is `dpanel`. This command supports both the “difference” estimator ([Arellano and Bond, 1991](#)) and the “system” estimator ([Blundell and Bond, 1998](#)), which has become the method of choice in the applied literature.

24.1 Introduction

Notation

A dynamic linear panel data model can be represented as follows (in notation based on [Arellano \(2003\)](#)):

$$y_{it} = \alpha y_{i,t-1} + \beta' x_{it} + \eta_i + v_{it} \quad (24.1)$$

where $i = 1, 2, \dots, N$ indexes the cross-section units and t indexes time.

The main idea behind the difference estimator is to sweep out the individual effect via differencing. First-differencing eq. (24.1) yields

$$\Delta y_{it} = \alpha \Delta y_{i,t-1} + \beta' \Delta x_{it} + \Delta v_{it} = y' W_{it} + \Delta v_{it}, \quad (24.2)$$

in obvious notation. The error term of (24.2) is, by construction, autocorrelated and also correlated with the lagged dependent variable, so an estimator that takes both issues into account is needed. The endogeneity issue is solved by noting that all values of $y_{i,t-k}$ with $k > 1$ can be used as instruments for $\Delta y_{i,t-1}$: unobserved values of $y_{i,t-k}$ (whether missing or pre-sample) can safely be substituted with 0. In the language of GMM, this amounts to using the relation

$$E(\Delta v_{it} \cdot y_{i,t-k}) = 0, \quad k > 1 \quad (24.3)$$

as an orthogonality condition.

Autocorrelation is dealt with by noting that if v_{it} is white noise, the covariance matrix of the vector whose typical element is Δv_{it} is proportional to a matrix H that has 2 on the main diagonal, -1 on the first subdiagonals and 0 elsewhere. One-step GMM estimation of equation (24.2) amounts to computing

$$\hat{y} = \left[\left(\sum_i W_i' Z_i \right) A_N \left(\sum_i Z_i' W_i \right) \right]^{-1} \left(\sum_i W_i' Z_i \right) A_N \left(\sum_i Z_i' \Delta y_i \right) \quad (24.4)$$

where

$$\begin{aligned} \Delta y_i &= \begin{bmatrix} \Delta y_{i3} & \cdots & \Delta y_{iT} \end{bmatrix}' \\ W_i &= \begin{bmatrix} \Delta y_{i2} & \cdots & \Delta y_{i,T-1} \\ \Delta x_{i3} & \cdots & \Delta x_{iT} \end{bmatrix}' \\ Z_i &= \begin{bmatrix} y_{i1} & 0 & 0 & \cdots & 0 & \Delta x_{i3} \\ 0 & y_{i1} & y_{i2} & \cdots & 0 & \Delta x_{i4} \\ & & \vdots & & & \\ 0 & 0 & 0 & \cdots & y_{i,T-2} & \Delta x_{iT} \end{bmatrix} \end{aligned}$$

and

$$\mathbf{A}_N = \left(\sum_i \mathbf{Z}_i' H \mathbf{Z}_i \right)^{-1}$$

Once the 1-step estimator is computed, the sample covariance matrix of the estimated residuals can be used instead of H to obtain 2-step estimates, which are not only consistent but asymptotically efficient. (In principle the process may be iterated, but nobody seems to be interested.) Standard GMM theory applies, except for one point: [Windmeijer \(2005\)](#) has computed finite-sample corrections to the asymptotic covariance matrix of the parameters, which are nowadays almost universally used.

The difference estimator is consistent, but has been shown to have poor properties in finite samples when α is near one. People these days prefer the so-called “system” estimator, which complements the differenced data (with lagged levels used as instruments) with data in levels (using lagged differences as instruments). The system estimator relies on an extra orthogonality condition which has to do with the earliest value of the dependent variable $y_{i,1}$. The interested reader is referred to [Blundell and Bond \(1998, pp. 124–125\)](#) for details, but here it suffices to say that this condition is satisfied in mean-stationary models and brings an improvement in efficiency that may be substantial in many cases.

The set of orthogonality conditions exploited in the system approach is not very much larger than with the difference estimator since most of the possible orthogonality conditions associated with the equations in levels are redundant, given those already used for the equations in differences.

The key equations of the system estimator can be written as

$$\hat{y} = \left[\left(\sum_i \tilde{\mathbf{W}}_i' \tilde{\mathbf{Z}}_i \right) \mathbf{A}_N \left(\sum_i \tilde{\mathbf{Z}}_i' \tilde{\mathbf{W}}_i \right) \right]^{-1} \left(\sum_i \tilde{\mathbf{W}}_i' \tilde{\mathbf{Z}}_i \right) \mathbf{A}_N \left(\sum_i \tilde{\mathbf{Z}}_i' \Delta \tilde{\mathbf{y}}_i \right) \quad (24.5)$$

where

$$\begin{aligned} \Delta \tilde{\mathbf{y}}_i &= \begin{bmatrix} \Delta y_{i3} & \cdots & \Delta y_{iT} & y_{i3} & \cdots & y_{iT} \end{bmatrix}' \\ \tilde{\mathbf{W}}_i &= \begin{bmatrix} \Delta y_{i2} & \cdots & \Delta y_{i,T-1} & y_{i2} & \cdots & y_{i,T-1} \\ \Delta x_{i3} & \cdots & \Delta x_{iT} & x_{i3} & \cdots & x_{iT} \end{bmatrix}' \\ \tilde{\mathbf{Z}}_i &= \begin{bmatrix} y_{i1} & 0 & 0 & \cdots & 0 & 0 & \cdots & 0 & \Delta x_{i3} \\ 0 & y_{i1} & y_{i2} & \cdots & 0 & 0 & \cdots & 0 & \Delta x_{i4} \\ & & \vdots & & & & & & \\ 0 & 0 & 0 & \cdots & y_{i,T-2} & 0 & \cdots & 0 & \Delta x_{iT} \\ & & \vdots & & & & & & \\ 0 & 0 & 0 & \cdots & 0 & \Delta y_{i2} & \cdots & 0 & x_{i3} \\ & & \vdots & & & & & & \\ 0 & 0 & 0 & \cdots & 0 & 0 & \cdots & \Delta y_{i,T-1} & x_{iT} \end{bmatrix} \end{aligned}$$

and

$$\mathbf{A}_N = \left(\sum_i \tilde{\mathbf{Z}}_i' H^* \tilde{\mathbf{Z}}_i \right)^{-1}$$

In this case choosing a precise form for the matrix H^* for the first step is no trivial matter. Its north-west block should be as similar as possible to the covariance matrix of the vector Δv_{it} , so

the same choice as the “difference” estimator is appropriate. Ideally, the south-east block should be proportional to the covariance matrix of the vector $\mathbf{u}\eta_i + \mathbf{v}$, that is $\sigma_v^2 I + \sigma_\eta^2 \mathbf{u}\mathbf{u}'$; but since σ_η^2 is unknown and any positive definite matrix renders the estimator consistent, people just use I . The off-diagonal blocks should, in principle, contain the covariances between Δv_{is} and v_{it} , which would be an identity matrix if v_{it} is white noise. However, since the south-east block is typically given a conventional value anyway, the benefit in making this choice is not obvious. Some packages use I ; others use a zero matrix. Asymptotically, it should not matter, but on real datasets the difference between the resulting estimates can be noticeable.

Rank deficiency

Both the difference estimator (24.4) and the system estimator (24.5) depend for their existence on the invertibility of \mathbf{A}_N . This matrix may turn out to be singular for several reasons. However, this does not mean that the estimator is not computable. In some cases, adjustments are possible such that the estimator does exist, but the user should be aware that in such cases not all software packages use the same strategy and replication of results may prove difficult or even impossible.

A first reason why \mathbf{A}_N may be singular is unavailability of instruments, chiefly because of missing observations. This case is easy to handle. If a particular row of $\tilde{\mathbf{Z}}_i$ is zero for all units, the corresponding orthogonality condition (or the corresponding instrument if you prefer) is automatically dropped; the overidentification rank is then adjusted for testing purposes.

Even if no instruments are zero, however, \mathbf{A}_N could be rank deficient. A trivial case occurs if there are collinear instruments, but a less trivial case may arise when T (the total number of time periods available) is not much smaller than N (the number of units), as, for example, in some macro datasets where the units are countries. The total number of potentially usable orthogonality conditions is $O(T^2)$, which may well exceed N in some cases. Since \mathbf{A}_N is the sum of N matrices which have, at most, rank $2T - 3$ it could well happen that the sum is singular.

In all these cases, `dpanel` substitutes the pseudo-inverse of \mathbf{A}_N (Moore–Penrose) for its regular inverse. Our choice is shared by some software packages, but not all, so replication may be hard.

Covariance matrix and standard errors

By default the standard errors shown for 1-step estimation are robust, based on the heteroskedasticity-consistent variance estimator

$$\widehat{\text{Var}}(\hat{\mathbf{y}}) = \mathbf{M}^{-1} \left(\sum_i \mathbf{W}_i' \mathbf{Z}_i \right) \mathbf{A}_N \hat{\mathbf{V}}_N \mathbf{A}_N \left(\sum_i \mathbf{Z}_i' \mathbf{W}_i \right) \mathbf{M}^{-1}$$

where $\mathbf{M} = (\sum_i \mathbf{W}_i' \mathbf{Z}_i) \mathbf{A}_N (\sum_i \mathbf{Z}_i' \mathbf{W}_i)$ and $\hat{\mathbf{V}}_N = N^{-1} \sum_i \mathbf{Z}_i' \hat{\mathbf{u}}_i \hat{\mathbf{u}}_i' \mathbf{Z}_i$, with $\hat{\mathbf{u}}_i$ the vector of residuals in differences for individual i . In addition, as noted above, the variance estimator for 2-step estimation employs the finite-sample correction of [Windmeijer \(2005\)](#).

When the `--asymptotic` option is passed to `dpanel`, however, the 1-step variance estimator is simply $\hat{\sigma}_u^2 \mathbf{M}^{-1}$, which is not heteroskedasticity-consistent, and the Windmeijer correction is not applied for 2-step estimation. Use of this option is not recommended unless you wish to replicate prior results that did not report robust standard errors. In particular, tests based on the asymptotic 2-step variance estimator are known to over-reject quite substantially (standard errors too small).

Treatment of missing values

Textbooks seldom bother with missing values, but in some cases their treatment may be far from obvious. This is especially true if missing values are interspersed between valid observations. For example, consider the plain difference estimator with one lag, so

$$y_t = \alpha y_{t-1} + \eta + \epsilon_t$$

where the i index is omitted for clarity. Suppose you have an individual with $t = 1 \dots 5$, for which y_3 is missing. It may seem that the data for this individual are unusable, because differencing y_t would produce something like

t	1	2	3	4	5
y_t	*	*	o	*	*
Δy_t	o	*	o	o	*

where $*$ = nonmissing and o = missing. Estimation seems to be unfeasible, since there are no periods in which Δy_t and Δy_{t-1} are both observable.

However, we can use a k -difference operator and get

$$\Delta_k y_t = \alpha \Delta_k y_{t-1} + \Delta_k \epsilon_t$$

where $\Delta_k = 1 - L^k$ and past levels of y_t are valid instruments. In this example, we can choose $k = 3$ and use y_1 as an instrument, so this unit is in fact usable.

Not all software packages seem to be aware of this possibility, so replicating published results may prove tricky if your dataset contains individuals with gaps between valid observations.

24.2 Usage

One feature of `dpanel`'s syntax is that you get default values for several choices you may wish to make, so that in a "standard" situation the command is very concise. The simplest case of the model (24.1) is a plain AR(1) process:

$$y_{i,t} = \alpha y_{i,t-1} + \eta_i + v_{it}. \quad (24.6)$$

If you give the command

```
dpanel 1 ; y
```

Gretl assumes that you want to estimate (24.6) via the difference estimator (24.4), using as many orthogonality conditions as possible. The scalar 1 between `dpanel` and the semicolon indicates that only one lag of y is included as an explanatory variable; using 2 would give an AR(2) model. The syntax that `gretl` uses for the non-seasonal AR and MA lags in an ARMA model is also supported in this context. For example, if you want the first and third lags of y (but not the second) included as explanatory variables you can say

```
dpanel {1 3} ; y
```

or you can use a pre-defined matrix for this purpose:

```
matrix ylags = {1, 3}
dpanel ylags ; y
```

To use a single lag of y other than the first you need to employ this mechanism:

```
dpanel {3} ; y # only lag 3 is included
dpanel 3 ; y   # compare: lags 1, 2 and 3 are used
```

To use the system estimator instead, you add the `--system` option, as in

```
dpanel 1 ; y --system
```

The level orthogonality conditions and the corresponding instrument are appended automatically (see eq. 24.5).

Regressors

If additional regressors are to be included, they should be listed after the dependent variable in the same way as other gretl estimation commands, such as `ols`. For the difference orthogonality relations, `dpanel` takes care of transforming the regressors in parallel with the dependent variable.

One case of potential ambiguity is when an intercept is specified but the difference-only estimator is selected, as in

```
dpanel 1 ; y const
```

In this case the default `dpanel` behavior, which agrees with David Roodman's `xtabond2` for Stata (Roodman, 2009a), is to drop the constant (since differencing reduces it to nothing but zeros). However, for compatibility with the DPD package for Ox, you can give the option `--dpdstyle`, in which case the constant is retained (equivalent to including a linear trend in equation 24.1). A similar point applies to the period-specific dummy variables which can be added in `dpanel` via the `--time-dummies` option: in the differences-only case these dummies are entered in differenced form by default, but when the `--dpdstyle` switch is applied they are entered in levels.

The standard gretl syntax applies if you want to use lagged explanatory variables, so for example the command

```
dpanel 1 ; y const x(0 to -1) --system
```

would result in estimation of the model

$$y_{it} = \alpha y_{i,t-1} + \beta_0 + \beta_1 x_{it} + \beta_2 x_{i,t-1} + \eta_i + v_{it}.$$

Instruments

The default rules for instruments are:

- lags of the dependent variable are instrumented using all available orthogonality conditions; and
- additional regressors are considered exogenous, so they are used as their own instruments.

If a different policy is wanted, the instruments should be specified in an additional list, separated from the regressors list by a semicolon. The syntax closely mirrors that of the `tsls` command, but in this context it is necessary to distinguish between “regular” instruments and what are often called “GMM-style” instruments (that is, instruments that are handled in the same block-diagonal manner as lags of the dependent variable, as described above).

“Regular” instruments are transformed in the same way as regressors, and the contemporaneous value of the transformed variable is used to form an orthogonality condition. Since regressors are treated as exogenous by default, it follows that these two commands estimate the same model:

```
dpanel 1 ; y z
dpanel 1 ; y z ; z
```

The instrument specification in the second case simply confirms what is implicit in the first: that `z` is exogenous. Note, though, that if you have some additional variable `z2` which you want to add as a regular instrument, it then becomes necessary to include `z` in the instrument list if it is to be treated as exogenous:

```
dpanel 1 ; y z ; z2 # z is now implicitly endogenous
dpanel 1 ; y z ; z z2 # z is treated as exogenous
```

The specification of “GMM-style” instruments is handled by the special constructs `GMM()` and `GMMlevel()`. The first of these relates to instruments for the equations in differences, and the second to the equations in levels. The syntax for `GMM()` is

```
GMM(name, minlag, maxlag[,collapse])
```

where *name* is replaced by the name of a series (or the name of a list of series), and *minlag* and *maxlag* are replaced by the minimum and maximum lags to be used as instruments. The same goes for `GMMlevel()`.

One common use of `GMM()` is to limit the number of lagged levels of the dependent variable used as instruments for the equations in differences. It’s well known that although exploiting all possible orthogonality conditions yields maximal asymptotic efficiency, in finite samples it may be preferable to use a smaller subset—see [Roodman \(2009b\)](#), [Okui \(2009\)](#). For example, the specification

```
dpanel 1 ; y ; GMM(y, 2, 4)
```

ensures that no lags of y_t earlier than $t - 4$ will be used as instruments.

A second means of limiting the number of instruments is to “collapse” the sets of block-diagonal instruments shown following equations 24.4 and 24.5. Instead of having a distinct instrument per observation per lag, this is reduced to a distinct instrument per lag, as shown in Figure 24.1.

$$\begin{array}{c}
 \text{GMM()} \\
 \left[\begin{array}{cccccc} y_{i1} & 0 & 0 & 0 & 0 & 0 & \cdots \\ 0 & y_{i1} & y_{i2} & 0 & 0 & 0 & \cdots \\ 0 & 0 & 0 & y_{i1} & y_{i2} & y_{i3} & \cdots \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \ddots \end{array} \right] \Rightarrow \left[\begin{array}{cccc} y_{i1} & 0 & 0 & \cdots \\ y_{i1} & y_{i2} & 0 & \cdots \\ y_{i1} & y_{i2} & y_{i3} & \cdots \\ \vdots & \vdots & \vdots & \ddots \end{array} \right] \\
 \text{GMMlevel()} \\
 \left[\begin{array}{cccc} \Delta y_{i2} & 0 & 0 & \cdots \\ 0 & \Delta y_{i3} & 0 & \cdots \\ 0 & 0 & \Delta y_{i4} & \cdots \\ \vdots & \vdots & \vdots & \ddots \end{array} \right] \Rightarrow \left[\begin{array}{c} \Delta y_{i2} \\ \Delta y_{i3} \\ \Delta y_{i4} \\ \vdots \end{array} \right]
 \end{array}$$

Figure 24.1: Collapsing block-diagonal instruments

This treatment of instruments can be selected per `GMM` or `GMMlevel` case—by appending the `collapse` flag following the *maxlag* value—or it can be set “globally” by use of the `--collapse` option to the `dpanel` command. To our knowledge Roodman’s `xtabond2` was the first software to offer this useful facility.

A further use of `GMM()` is to exploit more fully the potential orthogonality conditions afforded by an exogenous regressor, or a related variable that does not appear as a regressor. For example, in

```
dpanel 1 ; y x ; GMM(z, 2, 6)
```

the variable *x* is considered an endogenous regressor, and up to 5 lags of *z* are used as instruments. Note that in the following script fragment

```
dpanel 1 ; y z
dpanel 1 ; y z ; GMM(z,0,0)
```

the two estimation commands should not be expected to give the same result, as the sets of orthogonality relationships are subtly different. In the latter case, you have $T - 2$ separate orthogonality relationships pertaining to z_{it} , none of which has any implication for the other ones; in the former case, you only have one. In terms of the Z_i matrix, the first form adds a single row to the bottom of the instruments matrix, while the second form adds a diagonal block with $T - 2$ columns; that is,

$$\begin{bmatrix} z_{i3} & z_{i4} & \cdots & z_{it} \end{bmatrix}$$

versus

$$\begin{bmatrix} z_{i3} & 0 & \cdots & 0 \\ 0 & z_{i4} & \cdots & 0 \\ & \ddots & \ddots & \\ 0 & 0 & \cdots & z_{it} \end{bmatrix}$$

24.3 Replication of DPD results

In this section we show how to replicate the results of some of the pioneering work with dynamic panel-data estimators by Arellano, Bond and Blundell. As the DPD manual (Doornik, Arellano and Bond, 2006) explains, it is difficult to replicate the original published results exactly, for two main reasons: not all of the data used in those studies are publicly available; and some of the choices made in the original software implementation of the estimators have been superseded. Here, therefore, our focus is on replicating the results obtained using the current DPD package and reported in the DPD manual.

The examples are based on the program files `abest1.ox`, `abest3.ox` and `bbest1.ox`. These are included in the DPD package, along with the Arellano-Bond database files `abdata.bn7` and `abdata.in7`.¹ The Arellano-Bond data are also provided with `gretl`, in the file `abdata.gdt`. In the following we do not show the output from DPD or `gretl`; it is somewhat voluminous, and is easily generated by the user. As of this writing the results from Ox/DPD and `gretl` are identical in all relevant respects for all of the examples shown.²

An Ox/DPD program to generate the results of interest takes the general form shown in Listing 24.1. In the examples below we take this template for granted and show just the model-specific code.

In the examples below we take this template for granted and show just the model-specific code.

Example 1

The following Ox/DPD code—drawn from `abest1.ox`—replicates column (b) of Table 4 in Arellano and Bond (1991), an instance of the differences-only or GMM-DIF estimator. The dependent variable is the log of employment, n ; the regressors include two lags of the dependent variable, current and lagged values of the log real-product wage, w , the current value of the log of gross capital, k , and current and lagged values of the log of industry output, ys . In addition the specification includes a constant and five year dummies; unlike the stochastic regressors, these deterministic terms are not differenced. In this specification the regressors w , k and ys are treated as exogenous and serve as their own instruments. In DPD syntax this requires entering these variables twice, on the `X_VAR` and `I_VAR` lines. The GMM-type (block-diagonal) instruments in this example are the second and subsequent lags of the level of n . Both 1-step and 2-step estimates are computed.

```
dpd.SetOptions(FALSE); // don't use robust standard errors
dpd.Select(DPD::Y_VAR, {"n", 0, 2});
dpd.Select(DPD::X_VAR, {"w", 0, 1, "k", 0, 0, "ys", 0, 1});
dpd.Select(DPD::I_VAR, {"w", 0, 1, "k", 0, 0, "ys", 0, 1});
```

¹See <http://www.doornik.com/download.html>.

²To be specific, this was last tested using Ox Console version 9.10, version 1.28 of the DPD package, and `gretl` built from git as of 2024-02-12, all on Linux.

Listing 24.1: Template for Ox/DPD program

```

#include <oxstd.h>
#import <packages/DPD/dpd>

main()
{
    decl dpd = new DPD();

    dpd.Load("abdata.in7");
    dpd.SetYear("YEAR");

    // model-specific code goes here

    delete dpd;
}

dpd.Gmm("n", 2, 99);
dpd.SetDummies(DPD::D_CONSTANT + DPD::D_TIME);

print("\n\n***** Arellano & Bond (1991), Table 4 (b)");
dpd.SetMethod(DPD::M_1STEP);
dpd.Estimate();
dpd.SetMethod(DPD::M_2STEP);
dpd.Estimate();

```

Here is gretl code to do the same job:

```

open abdata.gdt
list X = w w(-1) k ys ys(-1)
dpanel 2 ; n X const --time-dummies --asy --dpdstyle
dpanel 2 ; n X const --time-dummies --asy --two-step --dpdstyle

```

Note that in gretl the switch to suppress robust standard errors is `--asymptotic`, here abbreviated to `--asy`.³ The `--dpdstyle` flag specifies that the constant and dummies should not be differenced, in the context of a GMM-DIF model. With gretl's `dpanel` command it is not necessary to specify the exogenous regressors as their own instruments since this is the default; similarly, the use of the second and all longer lags of the dependent variable as GMM-type instruments is the default and need not be stated explicitly.

Example 2

The DPD file `abest3.ox` contains a variant of the above that differs with regard to the choice of instruments: the variables `w` and `k` are now treated as predetermined, and are instrumented GMM-style using the second and third lags of their levels. This approximates column (c) of Table 4 in [Arellano and Bond \(1991\)](#). We have modified the code in `abest3.ox` slightly to allow the use of robust (Windmeijer-corrected) standard errors, which are the default in both DPD and gretl with 2-step estimation:

```

dpd.Select(DPD::Y_VAR, {"n", 0, 2});
dpd.Select(DPD::X_VAR, {"w", 0, 1, "k", 0, 0, "ys", 0, 1});

```

³Option flags in gretl can always be truncated, down to the minimal unique abbreviation.

```

dpd.Select(DPD::I_VAR, {"ys", 0, 1});
dpd.SetDummies(DPD::D_CONSTANT + DPD::D_TIME);

dpd.Gmm("n", 2, 99);
dpd.Gmm("w", 2, 3);
dpd.Gmm("k", 2, 3);

print("\n***** Arellano & Bond (1991), Table 4 (c)\n");
print("      (but using different instruments!!)\n");
dpd.SetMethod(DPD::M_2STEP);
dpd.Estimate();

```

The gretl code is as follows:

```

open abdata.gdt
list X = w w(-1) k ys ys(-1)
list Ivars = ys ys(-1)
dpanel 2 ; n X const ; GMM(w,2,3) GMM(k,2,3) Ivars --time --two-step --dpd

```

Note that since we are now calling for an instrument set other than the default (following the second semicolon), it is necessary to include the `Ivars` specification for the variable `ys`. However, it is not necessary to specify `GMM(n,2,99)` since this remains the default treatment of the dependent variable.

Example 3

Our third example replicates the DPD output from `bbest1.ox`: this uses the same dataset as the previous examples but the model specifications are based on [Blundell and Bond \(1998\)](#), and involve comparison of the GMM-DIF and GMM-SYS (“system”) estimators. The basic specification is slightly simplified in that the variable `ys` is not used and only one lag of the dependent variable appears as a regressor. The Ox/DPD code is:

```

dpd.Select(DPD::Y_VAR, {"n", 0, 1});
dpd.Select(DPD::X_VAR, {"w", 0, 1, "k", 0, 1});
dpd.SetDummies(DPD::D_CONSTANT + DPD::D_TIME);

print("\n\n***** Blundell & Bond (1998), Table 4: 1976-86 GMM-DIF");
dpd.Gmm("n", 2, 99);
dpd.Gmm("w", 2, 99);
dpd.Gmm("k", 2, 99);
dpd.SetMethod(DPD::M_2STEP);
dpd.Estimate();

print("\n\n***** Blundell & Bond (1998), Table 4: 1976-86 GMM-SYS");
dpd.GmmLevel("n", 1, 1);
dpd.GmmLevel("w", 1, 1);
dpd.GmmLevel("k", 1, 1);
dpd.SetMethod(DPD::M_2STEP);
dpd.Estimate();

```

Here is the corresponding gretl code:

```

open abdata.gdt
list X = w w(-1) k k(-1)
list Z = w k

# Blundell & Bond (1998), Table 4: 1976-86 GMM-DIF

```



```
dpanel 1 ; n X const ; GMM(Z,2,99) --time --two-step --dpd

# Blundell & Bond (1998), Table 4: 1976-86 GMM-SYS
dpanel 1 ; n X const ; GMM(Z,2,99) GMMlevel(Z,1,1) \
--time --two-step --dpd --system
```

Note the use of the `--system` option flag to specify GMM-SYS, including the default treatment of the dependent variable, which corresponds to `GMMlevel(n,1,1)`. In this case we also want to use lagged differences of the regressors `w` and `k` as instruments for the levels equations so we need explicit `GMMlevel` entries for those variables. If you want something other than the default treatment for the dependent variable as an instrument for the levels equations, you should give an explicit `GMMlevel` specification for that variable—and in that case the `--system` flag is redundant (but harmless).

For the sake of completeness, note that if you specify at least one `GMMlevel` term, `dpanel` will then include equations in levels, but it will not automatically add a default `GMMlevel` specification for the dependent variable unless the `--system` option is given.

24.4 Cross-country growth example

The previous examples all used the Arellano-Bond dataset; for this example we use the dataset `CEL.gdt`, which is also included in the `gretl` distribution. As with the Arellano-Bond data, there are numerous missing values. Details of the provenance of the data can be found by opening the dataset information window in the `gretl` GUI (Data menu, Dataset info item). This is a subset of the Barro-Lee 138-country panel dataset, an approximation to which is used in [Caselli, Esquivel and Lefort \(1996\)](#) and [Bond, Hoeffler and Temple \(2001\)](#).⁴ Both of these papers explore the dynamic panel-data approach in relation to the issues of growth and convergence of per capita income across countries.

The dependent variable is growth in real GDP per capita over successive five-year periods; the regressors are the log of the initial (five years prior) value of GDP per capita, the log-ratio of investment to GDP, s , in the prior five years, and the log of annual average population growth, n , over the prior five years plus 0.05 as stand-in for the rate of technical progress, g , plus the rate of depreciation, δ (with the last two terms assumed to be constant across both countries and periods). The original model is

$$\Delta_5 y_{it} = \beta y_{i,t-5} + \alpha s_{it} + \gamma(n_{it} + g + \delta) + v_t + \eta_i + \epsilon_{it} \quad (24.7)$$

which allows for a time-specific disturbance v_t . The Solow model with Cobb-Douglas production function implies that $\gamma = -\alpha$, but this assumption is not imposed in estimation. The time-specific disturbance is eliminated by subtracting the period mean from each of the series.

Equation (24.7) can be transformed to an AR(1) dynamic panel-data model by adding $y_{i,t-5}$ to both sides, which gives

$$y_{it} = (1 + \beta)y_{i,t-5} + \alpha s_{it} + \gamma(n_{it} + g + \delta) + \eta_i + \epsilon_{it} \quad (24.8)$$

where all variables are now assumed to be time-demeaned.

In (rough) replication of [Bond *et al.* \(2001\)](#) we now proceed to estimate the following two models: (a) equation (24.8) via GMM-DIF, using as instruments the second and all longer lags of y_{it} , s_{it} and $n_{it} + g + \delta$; and (b) equation (24.8) via GMM-SYS, using $\Delta y_{i,t-1}$, $\Delta s_{i,t-1}$ and $\Delta(n_{i,t-1} + g + \delta)$ as additional instruments in the levels equations. We report robust standard errors throughout. (As a purely notational matter, we now use “ $t - 1$ ” to refer to values five years prior to t , as in [Bond *et al.* \(2001\)](#)).

The `gretl` script to do this job is shown in Listing 24.2. Note that the final transformed versions of the variables (logs, with time-means subtracted) are named `ly` (y_{it}), `linv` (s_{it}) and `lngd` ($n_{it} + g + \delta$).

⁴We say an “approximation” because we have not been able to replicate exactly the OLS results reported in the papers cited, though it seems from the description of the data in [Caselli *et al.* \(1996\)](#) that we ought to be able to do so. We note that [Bond *et al.* \(2001\)](#) used data provided by Professor Caselli yet did not manage to reproduce the latter’s results.

Listing 24.2: GDP growth example [\[Download ▼\]](#)

```

open CEL.gdt

ngd = n + 0.05
ly = log(y)
linv = log(s)
lngd = log(ngd)

# take out time means
loop i=1..8
  smpl (time == i) --restrict --replace
  ly -= mean(ly)
  linv -= mean(linv)
  lngd -= mean(lngd)
endloop

smpl --full
list X = linv lngd
# 1-step GMM-DIF
dpanel 1 ; ly X ; GMM(X,2,99)
# 2-step GMM-DIF
dpanel 1 ; ly X ; GMM(X,2,99) --two-step
# GMM-SYS
dpanel 1 ; ly X ; GMM(X,2,99) GMMlevel(X,1,1) --two-step --sys

```

For comparison we estimated the same two models using Ox/DPD and xtabond2. (In each case we constructed a comma-separated values dataset containing the data as transformed in the gretl script shown above, using a missing-value code appropriate to the target program.) For reference, the commands used with Stata are reproduced in Listing 24.3.

Listing 24.3: Stata commands for GDP growth example

```

#delimit ;
insheet using CEL.csv
tsset unit time;
xtabond2 ly L.ly linv lngd, gmm(L.ly, lag(1 99)) gmm(linv, lag(2 99))
      gmm(lngd, lag(2 99)) rob nolev;
xtabond2 ly L.ly linv lngd, gmm(L.ly, lag(1 99)) gmm(linv, lag(2 99))
      gmm(lngd, lag(2 99)) rob nolev twostep;
xtabond2 ly L.ly linv lngd, gmm(L.ly, lag(1 99)) gmm(linv, lag(2 99))
      gmm(lngd, lag(2 99)) rob nocons twostep;

```

For the GMM-DIF model all three programs find 382 usable observations and 30 instruments, and yield identical parameter estimates and robust standard errors (up to the number of digits printed, or more); see Table 24.1.⁵

Results for GMM-SYS estimation are shown in Table 24.2. In this case we show two sets of gretl

⁵The coefficient shown for $ly(-1)$ in the Tables is that reported directly by the software; for comparability with the original model (eq. 24.7) it is necessary to subtract 1, which produces the expected negative value indicating conditional convergence in per capita income.

	1-step		2-step	
	coeff	std. error	coeff	std. error
ly(-1)	0.577564	0.1292	0.610056	0.1562
linv	0.0565469	0.07082	0.100952	0.07772
lngd	-0.143950	0.2753	-0.310041	0.2980

Table 24.1: GMM-DIF: Barro-Lee data

results: those labeled “gretl(1)” were obtained using `gretl`’s `--dpdstyle` option, while those labeled “gretl(2)” did not use that option—the intent being to reproduce the H matrices used by `Ox/DPD` and `xtabond2` respectively.

	gretl(1)	Ox/DPD	gretl(2)	xtabond2
ly(-1)	0.9237 (0.0385)	0.9167 (0.0373)	0.9073 (0.0370)	0.9073 (0.0370)
linv	0.1592 (0.0449)	0.1636 (0.0441)	0.1856 (0.0411)	0.1856 (0.0411)
lngd	-0.2370 (0.1485)	-0.2178 (0.1433)	-0.2355 (0.1501)	-0.2355 (0.1501)

Table 24.2: 2-step GMM-SYS: Barro-Lee data (standard errors in parentheses)

In this case all three programs use 479 observations; `gretl` and `xtabond2` use 41 instruments and produce the same estimates (when using the same H matrix) while `Ox/DPD` nominally uses 66.⁶ It is noteworthy that with GMM-SYS plus “messy” missing observations, the results depend on the precise array of instruments used, which in turn depends on the details of the implementation of the estimator.

24.5 Auxiliary test statistics

We have concentrated above on parameter estimates and standard errors. Here we add some discussion of the additional test statistics that typically accompany both GMM-DIF and GMM-SYS estimation—tests of overidentification, for first- and second-order autocorrelation, and for the joint significance of regressors.

Overidentification

If a model estimated with the use of instrumental variables is just-identified, the condition of orthogonality of the residuals and the instruments can be satisfied exactly. But if the specification is overidentified (more instruments than endogenous regressors) this condition can only be approximated, and the degree to which orthogonality “fails” serves as a test for the validity of the instruments (and/or the specification). Since dynamic panel models are almost always overidentified such a test is of particular importance.

There are two such tests in the econometric literature, devised respectively by [Sargan \(1958\)](#) and [Hansen \(1982\)](#). They share a common principle: a suitably scaled measure of deviation from perfect orthogonality can be shown to be distributed as $\chi^2(k)$, with k the degree of overidentification, under the null hypothesis of valid instruments and correct specification. Both test statistics can be written as

$$S = \left(\sum_{i=1}^N \hat{\mathbf{v}}_i^{*'} \mathbf{Z}_i \right) \mathbf{A}_N \left(\sum_{i=1}^N \mathbf{Z}_i' \hat{\mathbf{v}}_i^* \right)$$

⁶This is a case of the issue described in section 24.1: the full \mathbf{A}_N matrix turns out to be singular and special measures must be taken to produce estimates.

where the \hat{v}_i^* are the residuals in first differences for unit i , and for that reason they are often rolled together—for example, as “Hansen–Sargan” tests by [Davidson and MacKinnon \(2004\)](#).

The Sargan vs Hansen difference is buried in A_N : Sargan’s original test is the minimized orthogonality score divided by a scalar estimate of the error variance (which is presumed to be homoskedastic), while Hansen’s is the minimized criterion from efficient GMM estimation, in which the scalar variance estimate is replaced by a heteroskedasticity- and autocorrelation-consistent (HAC) estimator of the variance matrix of the error term. These variants correspond to 1-step and 2-step estimates of the given specification.

Up till version 2021d, gretl followed Ox/DPD in presenting a single overidentification statistic under the name “Sargan”—in effect, a Sargan test proper for the 1-step estimator and a Hansen test for 2-step. Subsequently, however, gretl follows xtabond2 in distinguishing between the tests and presenting both statistics, under their original names, when 2-step estimation is selected (and therefore the HAC variance estimator is available). This choice responds to an argument made by [Roodman \(2009b\)](#): the Sargan test is questionable owing to its assumption of homoskedasticity but the Hansen test is seriously weakened by an excessive number of instruments (it may under-reject substantially), so there may be a benefit to taking both tests into consideration.

There are cases where the degrees of freedom for the overidentification test differs between DPD and gretl; this occurs when the A_N matrix is singular (section 24.1). In concept the df equals the number of instruments minus the number of parameters estimated; for the first of these terms gretl uses the rank of A_N , while DPD appears to use the full dimension of this matrix.

Autocorrelation

Negative first-order autocorrelation of the residuals in differences is expected by construction of the dynamic panel estimator, so a significant value for the AR(1) test does not indicate a problem. If the AR(2) test rejects, however, this indicates violation of the maintained assumptions. Note that valid AR tests cannot be produced when the `--asymptotic` option is specified in conjunction with one-step GMM-SYS estimation; if you need the tests, either add the `two-step` option or drop the asymptotic flag (which is recommended in any case).

Wald tests on regressors

Wald tests on the regressors (and separately on the time dummy variables, if included), are based on the estimated variance matrix of the parameter estimates and are generally in agreement across software packages provided the parameter variance is estimated in the same way. One small exception pertains to comparison between Ox/DPD and gretl when the difference estimator is used, a constant term is included, and the `--dpdstyle` option is given with `dpanel` (so the constant is not automatically omitted). In this case DPD includes the constant in the time-dummies Wald test but gretl does not.

24.6 Post-estimation available statistics

After estimation, the `$model` accessor will return a bundle containing several items that may be of interest: most should be self-explanatory, but here’s a partial list:

Key	Content
AR1, AR2	1st and 2nd order autocorrelation test statistics
sargan, sargan_df	Sargan test for overidentifying restrictions and corresponding degrees of freedom
hansen, hansen_df	Hansen test for overidentifying restrictions and corresponding degrees of freedom
wald, wald_df	Wald test for overall significance and corresponding degrees of freedom
GMMinst	The matrix Z of instruments (see equations (24.2) and (24.5))
wgtmat	The matrix A of GMM weights (see equations (24.2) and (24.5))

Note that `hansen` and `hansen_df` are not included when 1-step estimation is selected. Note also that `GMMinst` and `wgtmat` (which may be quite large matrices) are not saved in the `$model` bundle by default; that requires use of the `--keep-extra` option with the `dpanel` command. Listing 24.4 illustrates use of these matrices to replicate via `hansl` commands the calculation of the GMM estimator.

24.7 Memo: `dpanel` options

<i>flag</i>	<i>effect</i>
<code>--asymptotic</code>	Suppresses the use of robust standard errors
<code>--two-step</code>	Calls for 2-step estimation (the default being 1-step)
<code>--system</code>	Calls for GMM-SYS, with default treatment of the dependent variable, as in <code>GMMlevel(y,1,1)</code>
<code>--collapse</code>	Collapse block-diagonal sets of GMM instruments as per Roodman (2009a)
<code>--time-dummies</code>	Includes period-specific dummy variables
<code>--dpdstyle</code>	Compute the H matrix as in DPD; also suppresses differencing of automatic time dummies and omission of intercept in the GMM-DIF case
<code>--verbose</code>	Prints confirmation of the GMM-style instruments used; and when <code>--two-step</code> is selected, prints the 1-step estimates first
<code>--vcv</code>	Calls for printing of the covariance matrix
<code>--quiet</code>	Suppresses the printing of results
<code>--keep-extra</code>	Save additional matrices in <code>\$model</code> bundle (see above)

The time dummies option supports the qualifier `noprint`, as in

```
--time-dummies=noprint
```

This means that although the dummies are included in the specification their coefficients, standard errors and so on are not printed.

Listing 24.4: Manual replication of built-in command [\[Download ▼\]](#)

```
set verbose off
open abdata.gdt

# compose list of regressors
list X = w w(-1) k k(-1)
list Z = w k

dpanel 1 ; n X const ; GMM(Z,2,99) --two-step --dpd --keep-extra

### --- re-do by hand -----

# fetch Z and A from model
A = $model.wgtmat
mZt = $model.GMMinst # note: transposed

# create data matrices
series valid = ok($uhat)
series ddep = diff(n)
series dldep = ddep(-1)
list dreg = diff(X)

smpl valid --dummy

matrix m_reg = {dldep} ~ {dreg} ~ 1
matrix m_dep = {ddep}

matrix uno = mZt * m_reg
matrix due = qform(uno', A)
matrix tre = (uno'A) * (mZt * m_dep)
matrix coef = due\tre

print coef
```

Chapter 25

Nonlinear least squares

25.1 Introduction and examples

Gretl supports nonlinear least squares (NLS) using a variant of the Levenberg-Marquardt algorithm. The user must supply a specification of the regression function; prior to giving this specification the parameters to be estimated must be “declared” and given initial values. Optionally, the user may supply analytical derivatives of the regression function with respect to each of the parameters. If derivatives are not given, the user must instead give a list of the parameters to be estimated (separated by spaces or commas), preceded by the keyword `params`. The tolerance (criterion for terminating the iterative estimation procedure) can be adjusted using the `set` command.

The syntax for specifying the function to be estimated consists of the name of the dependent variable, followed by an expression to generate it. This is illustrated in the following two examples, with accompanying derivatives.

```
# Consumption function from Greene
nls C = alpha + beta * Y^gamma
    deriv alpha = 1
    deriv beta = Y^gamma
    deriv gamma = beta * Y^gamma * log(Y)
end nls

# Nonlinear function from Russell Davidson
nls y = alpha + beta * x1 + (1/beta) * x2
    deriv alpha = 1
    deriv beta = x1 - x2/(beta*beta)
end nls --vcv
```

Note the command words `nls` (which introduces the regression function), `deriv` (which introduces the specification of a derivative), and `end nls`, which terminates the specification and calls for estimation. If the `--vcv` flag is appended to the last line the covariance matrix of the parameter estimates is printed.

25.2 Initializing the parameters

The parameters of the regression function must be given initial values prior to the `nls` command. (In the GUI program this may be done via the menu item “Variable, Define new variable”).

In some cases, where the nonlinear function is a generalization of (or a restricted form of) a linear model, it may be convenient to run an `ols` and initialize the parameters from the OLS coefficient estimates. In relation to the first example above, one might do:

```
ols C 0 Y
alpha = $coeff(0)
beta = $coeff(Y)
gamma = 1
```

And in relation to the second example one might do:

```

ols y 0 x1 x2
alpha = $coeff(0)
beta = $coeff(x1)

```

25.3 NLS dialog window

It is probably most convenient to compose the commands for NLS estimation in the form of a gretl script but you can also do so interactively, by selecting the item “Nonlinear Least Squares” under the “Model, Nonlinear models” menu. This opens a dialog box where you can type the function specification (possibly prefaced by statements to set the initial parameter values) and the derivatives, if available. An example of this is shown in Figure 25.1. Note that in this context you do not have to supply the `nls` and `end nls` tags.

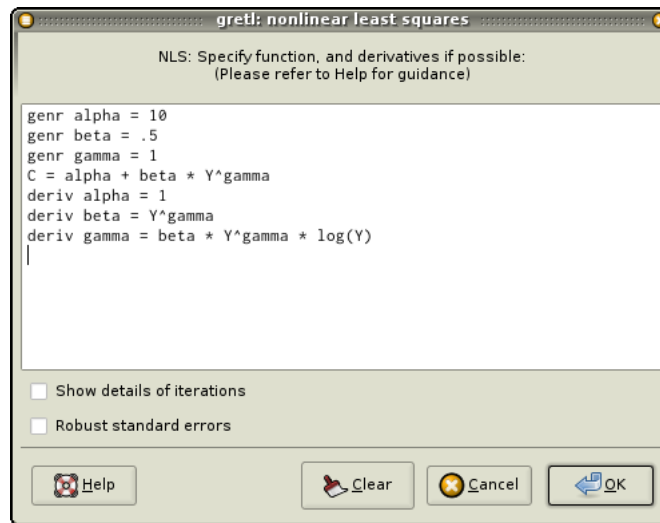


Figure 25.1: NLS dialog box

25.4 Analytical and numerical derivatives

If you are able to figure out the derivatives of the regression function with respect to the parameters, it is advisable to supply those derivatives as shown in the examples above. If that is not possible, gretl will compute approximate numerical derivatives. However, the properties of the NLS algorithm may not be so good in this case (see section 25.8).

This is done by using the `params` statement, which should be followed by a list of identifiers containing the parameters to be estimated. In this case, the examples above would read as follows:

```

# Greene
nls C = alpha + beta * Y^gamma
    params alpha beta gamma
end nls

# Davidson
nls y = alpha + beta * x1 + (1/beta) * x2
    params alpha beta
end nls

```

If analytical derivatives are supplied, they are checked for consistency with the given nonlinear function. If the derivatives are clearly incorrect estimation is aborted with an error message. If the

derivatives are “suspicious” a warning message is issued but estimation proceeds. This warning may sometimes be triggered by incorrect derivatives, but it may also be triggered by a high degree of collinearity among the derivatives.

Note that you cannot mix analytical and numerical derivatives: you should supply expressions for all of the derivatives or none.

25.5 Advanced use

The `nls` block can also contain more sophisticated constructs. First, it can handle intermediate expressions; this makes it possible to construct the conditional mean expression as a multi-step job, thus enhancing modularity and readability of the code. Second, more complex objects, such as lists and matrices, can be used for this purpose.

For example, suppose that we want to estimate a Probit Binary Response model via NLS. The specification is

$$y_i = \Phi[g(\mathbf{x}_i)] + u_i, \quad g(\mathbf{x}_i) = b_0 + b_1 x_{1,i} + b_2 x_{2,i} = \mathbf{b}' \mathbf{x}_i \quad (25.1)$$

Note: this is not the recommended way to estimate a probit model: the u_i term is heteroskedastic by construction and ML estimation is much preferable here. Still, NLS is a consistent estimator of the parameter vector \mathbf{b} , although its covariance matrix will have to be adjusted to compensate for heteroskedasticity: this is accomplished via the `--robust` switch.

Listing 25.1: NLS estimation of a Probit model [\[Download ▼\]](#)

```
open greene25_1.gdt
list X = const age income ownrent selfempl

# initialisation
ols cardhldr X --quiet
matrix b = $coeff / $sigma

# proceed with NLS estimation
nls cardhldr = cnorm(ndx)
    series ndx = lincomb(X, b)
    params b
end nls --robust

# compare with ML probit
probit cardhldr X --p-values
```

The example in script [25.1](#) can be enhanced by using analytical derivatives: since

$$\frac{\partial g(\mathbf{x}_i)}{\partial b_j} = \varphi(\mathbf{b}' \mathbf{x}_i) \cdot x_{ij}$$

one could substitute the `params` line in the script with the two-liner

```
series f = dnorm(ndx)
deriv b = {f} .* {X}
```

and have `nls` use analytically-computed derivatives, which are quicker and usually more reliable.

25.6 Controlling termination

The NLS estimation procedure is an iterative process. Iteration is terminated when the criterion for convergence is met or when the maximum number of iterations is reached, whichever comes first.

Let k denote the number of parameters being estimated. The maximum number of iterations is $100 \times (k + 1)$ when analytical derivatives are given, and $200 \times (k + 1)$ when numerical derivatives are used.

Let ϵ denote a small number. The iteration is deemed to have converged if at least one of the following conditions is satisfied:

- Both the actual and predicted relative reductions in the error sum of squares are at most ϵ .
- The relative error between two consecutive iterates is at most ϵ .

This default value of ϵ is the machine precision to the power $3/4$,¹ but it can be adjusted using the `set` command with the parameter `nls_tol`. For example

```
set nls_tol .0001
```

will relax the value of ϵ to 0.0001.

25.7 Details on the code

The underlying engine for NLS estimation is based on the minpack suite of functions, available from netlib.org. Specifically, the following minpack functions are called:

<code>lmdr</code>	Levenberg-Marquardt algorithm with analytical derivatives
<code>chkder</code>	Check the supplied analytical derivatives
<code>lmdif</code>	Levenberg-Marquardt algorithm with numerical derivatives
<code>fdjac2</code>	Compute final approximate Jacobian when using numerical derivatives
<code>dpmpar</code>	Determine the machine precision

On successful completion of the Levenberg-Marquardt iteration, a Gauss-Newton regression is used to calculate the covariance matrix for the parameter estimates. If the `--robust` flag is given a robust variant is computed. The documentation for the `set` command explains the specific options available in this regard.

Since NLS results are asymptotic, there is room for debate over whether or not a correction for degrees of freedom should be applied when calculating the standard error of the regression (and the standard errors of the parameter estimates). For comparability with OLS, and in light of the reasoning given in [Davidson and MacKinnon \(1993\)](#), the estimates shown in *gretl* *do* use a degrees of freedom correction.

25.8 Numerical accuracy

Table 25.1 shows the results of running the *gretl* NLS procedure on the 27 Statistical Reference Datasets made available by the U.S. National Institute of Standards and Technology (NIST) for testing nonlinear regression software.² For each dataset, two sets of starting values for the parameters are given in the test files, so the full test comprises 54 runs. Two full tests were performed, one

¹On a 32-bit Intel Pentium machine a likely value for this parameter is 1.82×10^{-12} .

²For a discussion of *gretl*'s accuracy in the estimation of linear models, see Appendix C.

using all analytical derivatives and one using all numerical approximations. In each case the default tolerance was used.³

Out of the 54 runs, gretl failed to produce a solution in 4 cases when using analytical derivatives, and in 5 cases when using numeric approximation. Of the four failures in analytical derivatives mode, two were due to non-convergence of the Levenberg–Marquardt algorithm after the maximum number of iterations (on MGH09 and Bennett5, both described by NIST as of “Higher difficulty”) and two were due to generation of range errors (out-of-bounds floating point values) when computing the Jacobian (on BoxBOD and MGH17, described as of “Higher difficulty” and “Average difficulty” respectively). The additional failure in numerical approximation mode was on MGH10 (“Higher difficulty”, maximum number of iterations reached).

The table gives information on several aspects of the tests: the number of outright failures, the average number of iterations taken to produce a solution and two sorts of measure of the accuracy of the estimates for both the parameters and the standard errors of the parameters.

For each of the 54 runs in each mode, if the run produced a solution the parameter estimates obtained by gretl were compared with the NIST certified values. We define the “minimum correct figures” for a given run as the number of significant figures to which the *least accurate* gretl estimate agreed with the certified value, for that run. The table shows both the average and the worst case value of this variable across all the runs that produced a solution. The same information is shown for the estimated standard errors.⁴

The second measure of accuracy shown is the percentage of cases, taking into account all parameters from all successful runs, in which the gretl estimate agreed with the certified value to at least the 6 significant figures which are printed by default in the gretl regression output.

Table 25.1: Nonlinear regression: the NIST tests

	<i>Analytical derivatives</i>	<i>Numerical derivatives</i>
Failures in 54 tests	4	5
Average iterations	32	127
Mean of min. correct figures, parameters	8.120	6.980
Worst of min. correct figures, parameters	4	3
Mean of min. correct figures, standard errors	8.000	5.673
Worst of min. correct figures, standard errors	5	2
Percent correct to at least 6 figures, parameters	96.5	91.9
Percent correct to at least 6 figures, standard errors	97.7	77.3

Using analytical derivatives, the worst case values for both parameters and standard errors were improved to 6 correct figures on the test machine when the tolerance was tightened to $1.0e-14$.

³The data shown in the table were gathered from a pre-release build of gretl version 1.0.9, compiled with gcc 3.3, linked against glibc 2.3.2, and run under Linux on an i686 PC (IBM ThinkPad A21m).

⁴For the standard errors, I excluded one outlier from the statistics shown in the table, namely Lanczos1. This is an odd case, using generated data with an almost-exact fit: the standard errors are 9 or 10 orders of magnitude smaller than the coefficients. In this instance gretl could reproduce the certified standard errors to only 3 figures (analytical derivatives) and 2 figures (numerical derivatives).

Using numerical derivatives, the same tightening of the tolerance raised the worst values to 5 correct figures for the parameters and 3 figures for standard errors, at a cost of one additional failure of convergence.

Note the overall superiority of analytical derivatives: on average solutions to the test problems were obtained with substantially fewer iterations and the results were more accurate (most notably for the estimated standard errors). Note also that the six-digit results printed by gretl are not 100 percent reliable for difficult nonlinear problems (in particular when using numerical derivatives). Having registered this caveat, the percentage of cases where the results were good to six digits or better seems high enough to justify their printing in this form.

Chapter 26

Maximum likelihood estimation

26.1 Generic ML estimation with gretl

Maximum likelihood estimation is a cornerstone of modern inferential procedures. Gretl provides a way to implement this method for a wide range of estimation problems, by use of the `mle` command. We give here a few examples.

To give a foundation for the examples that follow, we start from a brief reminder on the basics of ML estimation. Given a sample of size T , it is possible to define the density function¹ for the whole sample, namely the joint distribution of all the observations $f(\mathbf{Y}; \theta)$, where $\mathbf{Y} = \{y_1, \dots, y_T\}$. Its shape is determined by a k -vector of unknown parameters θ , which we assume is contained in a set Θ , and which can be used to evaluate the probability of observing a sample with any given characteristics.

After observing the data, the values \mathbf{Y} are given, and this function can be evaluated for any legitimate value of θ . In this case, we prefer to call it the *likelihood* function; the need for another name stems from the fact that this function works as a density when we use the y_t s as arguments and θ as parameters, whereas in this context θ is taken as the function's argument, and the data \mathbf{Y} only have the role of determining its shape.

In standard cases, this function has a unique maximum. The location of the maximum is unaffected if we consider the logarithm of the likelihood (or log-likelihood for short): this function will be denoted as

$$\ell(\theta) = \log f(\mathbf{Y}; \theta)$$

The log-likelihood functions that gretl can handle are those where $\ell(\theta)$ can be written as

$$\ell(\theta) = \sum_{t=1}^T \ell_t(\theta)$$

which is true in most cases of interest. The functions $\ell_t(\theta)$ are called the log-likelihood contributions.

Moreover, the location of the maximum is obviously determined by the data \mathbf{Y} . This means that the value

$$\hat{\theta}(\mathbf{Y}) = \underset{\theta \in \Theta}{\text{Argmax}} \ell(\theta) \quad (26.1)$$

is some function of the observed data (a statistic), which has the property, under mild conditions, of being a consistent, asymptotically normal and asymptotically efficient estimator of θ .

Sometimes it is possible to write down explicitly the function $\hat{\theta}(\mathbf{Y})$; in general, it need not be so. In these circumstances, the maximum can be found by means of numerical techniques. These often rely on the fact that the log-likelihood is a smooth function of θ , and therefore on the maximum its partial derivatives should all be 0. The *gradient vector*, or *score vector*, is a function that enjoys many interesting statistical properties in its own right; it will be denoted here as $\mathbf{g}(\theta)$. It is a

¹We are supposing here that our data are a realization of continuous random variables. For discrete random variables, everything continues to apply by referring to the probability function instead of the density. In both cases, the distribution may be conditional on some exogenous variables.

k -vector with typical element

$$g_i(\theta) = \frac{\partial \ell(\theta)}{\partial \theta_i} = \sum_{t=1}^T \frac{\partial \ell_t(\theta)}{\partial \theta_i}$$

Gradient-based methods can be briefly illustrated as follows:

1. pick a point $\theta_0 \in \Theta$;
2. evaluate $\mathbf{g}(\theta_0)$;
3. if $\mathbf{g}(\theta_0)$ is “small”, stop. Otherwise, compute a direction vector $d(\mathbf{g}(\theta_0))$;
4. evaluate $\theta_1 = \theta_0 + d(\mathbf{g}(\theta_0))$;
5. substitute θ_0 with θ_1 ;
6. restart from 2.

Many algorithms of this kind exist; they basically differ from one another in the way they compute the direction vector $d(\mathbf{g}(\theta_0))$, to ensure that $\ell(\theta_1) > \ell(\theta_0)$ (so that we eventually end up on the maximum).

The default method gretl uses to maximize the log-likelihood is a gradient-based algorithm known as the **BFGS** (Broyden, Fletcher, Goldfarb and Shanno) method. This technique is used in most econometric and statistical packages, as it is well-established and remarkably powerful. Clearly, in order to make this technique operational, it must be possible to compute the vector $\mathbf{g}(\theta)$ for any value of θ . In some cases this vector can be written explicitly as a function of \mathbf{Y} . If this is not possible or too difficult the gradient may be evaluated numerically. The alternative **Newton-Raphson** algorithm is also available. This method is more effective under some circumstances but is also more fragile; see section 26.10 and chapter 37 for details.²

The choice of the starting value, θ_0 , is crucial in some contexts and inconsequential in others. In general, however, it is advisable to start the algorithm from “sensible” values whenever possible. If a consistent estimator is available, this is usually a safe and efficient choice: this ensures that in large samples the starting point will be likely close to $\hat{\theta}$ and convergence can be achieved in few iterations.

The maximum number of iterations allowed for the BFGS procedure, and the relative tolerance for assessing convergence, can be adjusted using the `set` command: the relevant variables are `bfgs_maxiter` (default value 500) and `bfgs_tol` (default value, the machine precision to the power 3/4).

26.2 Syntax

ML estimation in gretl is supported by the `mle` command block. This consists of an initial line holding the keyword `mle` plus an equation for the loglikelihood; one or more statements within the block (details below); and a trailer line to close the block: `end mle`. Option flags may be appended to the trailer line.

Listing 26.1 gives a simple but complete example which serves to illustrate the equivalence of MLE and OLS in the context of the normal linear model.

²Note that some of the statements made below (for example, regarding estimation of the covariance matrix) have to be modified when Newton’s method is used.

Listing 26.1: OLS and MLE [\[Download ▼\]](#)

```

open data9-7
list X = const INCOME PRICE
ols QNC X
matrix b = $coeff
scalar s2 = $sigma^2
scalar l2pi = log(2*$pi)
scalar n = $nobs
mle lt = -0.5*l2pi -0.5*log(s2) - 1/(2*s2) * uhat^2
    series uhat = QNC - lincomb(X, b)
    s2 = sum(uhat^2)/n
    params b
end mle

```

Initial line of block

If possible the given expression should evaluate to a series or vector (contribution to the loglikelihood per observation). Failing that, it must evaluate to a scalar (the total loglikelihood). The identifier on the left-hand side (`lt` in Listing 26.1) is up to the user. If the variable in question is defined prior to the `mle` block it can be referenced after ML estimation; otherwise it is treated as a temporary variable and is destroyed after estimation.

Lines within the block

These may take three forms:

1. “Helper” statements that calculate auxiliary quantities (in the example, `uhat` and `s2`). Such statements will be evaluated before the loglikelihood and then re-evaluated on each iteration.
2. Keyword plus parameter, as in “`params b`”, which tells `mle` that the parameter to be adjusted to maximize the loglikelihood is the vector `b`. This sort of statement can also be used to specify analytical derivatives of the loglikelihood with respect to the parameters; see section 26.7 for discussion and examples.
3. Statements employing `print` or `printf` to track the progress of calculation, which can be useful for debugging.

Final line

In the example above this merely terminates the block, but if one wanted standard errors calculated via a numerical approximation to the Hessian (for instance) one could substitute

```
end mle --hessian
```

For a full listing of applicable options see the `mle` entry in the *Gretl Command Reference*.

26.3 Covariance matrix and standard errors

By default the covariance matrix of the parameter estimates is based on the Outer Product of the Gradient (OPG). That is,

$$\widehat{\text{Var}}_{\text{OPG}}(\hat{\theta}) = \left(G'(\hat{\theta}) G(\hat{\theta}) \right)^{-1} \quad (26.2)$$

where $G(\hat{\theta})$ is the $T \times k$ matrix of contributions to the gradient. Other options are available. If the `--hessian` flag is given, the covariance matrix is computed from a numerical approximation to the Hessian at convergence. If the `--robust` option is given the quasi-ML “sandwich” estimator is used:

$$\widehat{\text{Var}}_{\text{QML}}(\hat{\theta}) = H(\hat{\theta})^{-1} G'(\hat{\theta}) G(\hat{\theta}) H(\hat{\theta})^{-1}$$

where H denotes the numerical approximation to the Hessian. A refinement here is that if the `hac` parameter is appended to the `--robust` option, as in

```
end mle --robust=hac
```

the sandwich estimator is augmented in the manner of Newey and West (1987) to allow for serial correlation in the gradient. (Note that this only makes sense for time-series data.) In that case the details of the HAC estimator can be controlled via the `set` command, as described in chapter 22.

Cluster-robust estimation is also available: in order to activate it, use the `--cluster=clustvar`, where `clustvar` should be a discrete series. See section 22.5 for more details.

Note, however, that if the log-likelihood function supplied by the user just returns a scalar value—as opposed to a series or vector holding per-observation contributions—then the OPG method is not applicable and so the covariance matrix must be estimated via a numerical approximation to the Hessian.

26.4 Gamma estimation

Suppose we have a sample of T independent and identically distributed observations from a Gamma distribution with shape parameter k and scale parameter θ . The density function for each observation x_t is

$$f(x_t) = \frac{1}{\Gamma(k)\theta^k} \cdot x_t^{k-1} e^{-x_t/\theta} \quad (26.3)$$

The log-likelihood for the entire sample can be written as the logarithm of the joint density of all the observations. Since these are independent and identical, the joint density is the product of the individual densities, and hence its log is

$$\ell(k, \theta) = \sum_{t=1}^T \log \left[\frac{x_t^{k-1} e^{-x_t/\theta}}{\Gamma(k)\theta^k} \right] = \sum_{t=1}^T \ell_t \quad (26.4)$$

where

$$\ell_t = k \log(x_t/\theta) - \gamma(k) - \log x_t - x_t/\theta$$

and $\gamma(\cdot)$ is the log of the gamma function. In order to estimate the parameters k and θ via ML, we need to maximize (26.4) with respect to them. Here’s a simple snippet of gretl code to do the job.

```
scalar k = 1
scalar theta = 1

mle logl = k*ln(x/theta) - lngamma(k) - ln(x) - x/theta
  params k theta
end mle
```

The first two statements above are necessary to ensure that the variables `k` and `theta` exist before the computation of `logl` is attempted. Inside the `mle` block these variables (which could be either scalars, vectors or a combination of the two—see below for examples) are identified via the `params` keyword as the parameters that should be adjusted to maximize the likelihood. Their values will be changed by the execution of the `mle` command; upon successful completion, they will be replaced by the ML estimates. We set the starting value to 1 for both; this is arbitrary, but does not matter much in this example (more on this later).

The code above can be made more readable, and marginally more efficient, by defining a series to hold x_t/θ , which we'll call y . This command can be embedded in the `mle` block as follows:

```
mle logl = k*ln(y) - lngamma(k) - ln(x) - y
  series y = x/theta
  params k theta
end mle
```

You can insert as many such auxiliary lines as you require before the `params` line, with the restriction that they must contain either (a) commands to generate series, scalars or matrices or (b) `print` commands (which may be used to aid in debugging).

In a simple example like this, the choice of the starting values is almost inconsequential; the algorithm is likely to converge regardless of the initialization. However, consistent method-of-moments estimators of k and θ can easily be recovered from the sample mean m and variance V . It can be shown that

$$E(x_t) = k\theta \quad V(x_t) = k\theta^2$$

hence the following estimators

$$\begin{aligned}\bar{\theta} &= V/m \\ \bar{k} &= m/\theta\end{aligned}$$

are consistent, and therefore suitable to be used as a starting point for the algorithm. The original initializers for k and θ could then be replaced by

```
scalar m = mean(x)
scalar theta = var(x)/m
scalar k = m/theta
```

Another thing to note is that sometimes parameters are constrained within certain boundaries. In this case, for example, both Gamma parameters must be positive numbers. Gretl can't check for this automatically; it's the user's responsibility to ensure that the function is always evaluated at an admissible point in the parameter space during the iterative search for the maximum. An effective technique is to define a scalar variable that checks the validity of the parameters, and set the log-likelihood as undefined (NA) if the check fails. To implement this, the `mle` block above could be modified as follows:

```
mle logl = check ? k*ln(y) - lngamma(k) - ln(x) - y : NA
  series y = x/theta
  scalar check = k > 0 && theta > 0
  params k theta
end mle
```

For reference, Listing 26.2 presents a complete script that generates artificial Gamma data and obtains ML estimates of the parameters, employing the various refinements described above.

26.5 Stochastic frontier cost function

Note: this section has the sole purpose of illustrating the `mle` command. For the estimation of stochastic frontier cost or production functions, you may want to use the `frontier` function package.

When modeling a cost function, it is sometimes worthwhile to incorporate explicitly into the statistical model the notion that firms may be inefficient, so that the observed cost deviates from the theoretical figure not only because of unobserved heterogeneity between firms, but also because two firms could be operating at a different efficiency level, despite being identical in all other respects. In this case we may write

$$C_i = C_i^* + u_i + v_i$$

Listing 26.2: ML estimation of Gamma parameters [\[Download ▼\]](#)

```

# create an empty data set with 200 observations
nulldata 200

# fix a random seed for replicability
set seed 1707138404

# generate a Gamma random variable x with shape k = 3 and scale theta = 2
series x = randgen(G, 3, 2)

# initialize estimates via sample moments
m = mean(x)
theta = var(x) / m
k = m / theta

mle logl = check ? k*ln(y) - lngamma(k) - ln(x) - y : NA
  series y = x/theta
  check = k > 0 && theta > 0
  params k theta
end mle

```

The mle output is:

```

Model 1: ML, using observations 1-200
logl = check ? k*ln(y) - lngamma(k) - ln(x) - y : NA
Standard errors based on Outer Products matrix

```

	estimate	std. error	z	p-value	
k	3.28159	0.309764	10.59	3.18e-26	***
theta	1.86066	0.181566	10.25	1.21e-24	***

Log-likelihood	-504.8970	Akaike criterion	1013.794
Schwarz criterion	1020.391	Hannan-Quinn	1016.463

where C_i is some variable cost indicator, C_i^* is its “theoretical” value, u_i is a zero-mean disturbance term and v_i is the inefficiency term, which is supposed to be nonnegative by its very nature. A linear specification for C_i^* is often chosen. For example, the Cobb–Douglas cost function arises when C_i^* is a linear function of the logarithms of the input prices and the output quantities.

The *stochastic frontier* model is a linear model of the form $y_i = x_i\beta + \varepsilon_i$ in which the error term ε_i is the sum of u_i and v_i .

A common postulate is that $u_i \sim N(0, \sigma_u^2)$ and $v_i \sim |N(0, \sigma_v^2)|$. If independence between u_i and v_i is also assumed, then it is possible to show that the density function of ε_i has the form:

$$f(\varepsilon_i) = \sqrt{\frac{2}{\pi}} \Phi\left(\frac{\lambda \varepsilon_i}{\sigma}\right) \frac{1}{\sigma} \phi\left(\frac{\varepsilon_i}{\sigma}\right) \quad (26.5)$$

where $\Phi(\cdot)$ and $\phi(\cdot)$ are, respectively, the distribution and density function of the standard normal, $\sigma = \sqrt{\sigma_u^2 + \sigma_v^2}$ and $\lambda = \frac{\sigma_u}{\sigma_v}$.

As a consequence, the log-likelihood for one observation takes the form (apart from an irrelevant constant)

$$\ell_t = \log \Phi\left(\frac{\lambda \varepsilon_i}{\sigma}\right) - \left[\log(\sigma) + \frac{\varepsilon_i^2}{2\sigma^2} \right]$$

Therefore, a Cobb–Douglas cost function with stochastic frontier is the model described by the following equations:

$$\begin{aligned} \log C_i &= \log C_i^* + \varepsilon_i \\ \log C_i^* &= c + \sum_{j=1}^m \beta_j \log y_{ij} + \sum_{j=1}^n \alpha_j \log p_{ij} \\ \varepsilon_i &= u_i + v_i \\ u_i &\sim N(0, \sigma_u^2) \\ v_i &\sim |N(0, \sigma_v^2)| \end{aligned}$$

In most cases, one wants to ensure that the homogeneity of the cost function with respect to the prices holds by construction. Since this requirement is equivalent to $\sum_{j=1}^n \alpha_j = 1$, the above equation for C_i^* can be rewritten as

$$\log C_i - \log p_{in} = c + \sum_{j=1}^m \beta_j \log y_{ij} + \sum_{j=2}^n \alpha_j (\log p_{ij} - \log p_{in}) + \varepsilon_i \quad (26.6)$$

The above equation could be estimated by OLS, but it would suffer from two drawbacks: first, the OLS estimator for the intercept c is inconsistent because the disturbance term has a non-zero expected value; second, the OLS estimators for the other parameters are consistent, but inefficient in view of the non-normality of ε_i . Both issues can be addressed by estimating (26.6) by maximum likelihood. Nevertheless, OLS estimation is a quick and convenient way to provide starting values for the MLE algorithm.

Listing 26.3 shows how to implement the model described so far. The `banks91` file contains part of the data used in Lucchetti, Papi and Zazzaro (2001).

The script in example 26.3 is relatively easy to modify to show how one can use vectors (that is, 1-dimensional matrices) for storing the parameters to optimize: example 26.4 holds essentially the same script in which the parameters of the cost function are stored together in a vector. Of course, this makes also possible to use variable lists and other refinements which make the code more compact and readable.

Listing 26.3: Estimation of stochastic frontier cost function (with scalar parameters) [\[Download ▼\]](#)

```

open banks91.gdt

# transformations
series cost = ln(VC)
series q1 = ln(Q1)
series q2 = ln(Q2)
series p1 = ln(P1)
series p2 = ln(P2)
series p3 = ln(P3)

# Cobb-Douglas cost function with homogeneity restrictions
# (for initialization)
series rcost = cost - p1
series rp2 = p2 - p1
series rp3 = p3 - p1

ols rcost const q1 q2 rp2 rp3

# Cobb-Douglas cost function with homogeneity restrictions
# and inefficiency

scalar b0 = $coeff(const)
scalar b1 = $coeff(q1)
scalar b2 = $coeff(q2)
scalar b3 = $coeff(rp2)
scalar b4 = $coeff(rp3)

scalar su = 0.1
scalar sv = 0.1

mle logl = ln(cnorm(e*lambda/ss)) - (ln(ss) + 0.5*(e/ss)^2)
    scalar ss = sqrt(su^2 + sv^2)
    scalar lambda = su/sv
    series e = rcost - b0*const - b1*q1 - b2*q2 - b3*rp2 - b4*rp3
    params b0 b1 b2 b3 b4 su sv
end mle

```

Listing 26.4: Estimation of stochastic frontier cost function (with matrix parameters) [\[Download ▼\]](#)

```
open banks91.gdt

# transformations
series cost = ln(VC)
series q1 = ln(Q1)
series q2 = ln(Q2)
series p1 = ln(P1)
series p2 = ln(P2)
series p3 = ln(P3)

# Cobb-Douglas cost function with homogeneity restrictions
# (for initialization)
series rcost = cost - p1
series rp2 = p2 - p1
series rp3 = p3 - p1
list X = const q1 q2 rp2 rp3

ols rcost X
X = const q1 q2 rp2 rp3
# Cobb-Douglas cost function with homogeneity restrictions
# and inefficiency

matrix b = $coeff
scalar su = 0.1
scalar sv = 0.1

mle logl = ln(cnorm(e*lambda/ss)) - (ln(ss) + 0.5*(e/ss)^2)
  scalar ss = sqrt(su^2 + sv^2)
  scalar lambda = su/sv
  series e = rcost - lincomb(X, b)
  params b su sv
end mle
```

26.6 GARCH models

GARCH models are handled by gretl via a native function. However, it is instructive to see how they can be estimated through the `mle` command.³

The following equations provide the simplest example of a GARCH(1,1) model:

$$\begin{aligned} y_t &= \mu + \varepsilon_t \\ \varepsilon_t &= u_t \cdot \sigma_t \\ u_t &\sim N(0, 1) \\ h_t &= \omega + \alpha \varepsilon_{t-1}^2 + \beta h_{t-1}. \end{aligned}$$

Since the variance of y_t depends on past values, writing down the log-likelihood function is not simply a matter of summing the log densities for individual observations. As is common in time series models, y_t cannot be considered independent of the other observations in our sample, and consequently the density function for the whole sample (the joint density for all observations) is not just the product of the marginal densities.

Maximum likelihood estimation, in these cases, is achieved by considering *conditional* densities, so what we maximize is a conditional likelihood function. If we define the information set at time t as

$$F_t = \{y_t, y_{t-1}, \dots\},$$

then the density of y_t conditional on F_{t-1} is normal:

$$y_t | F_{t-1} \sim N[\mu, h_t].$$

By means of the properties of conditional distributions, the joint density can be factorized as follows

$$f(y_t, y_{t-1}, \dots) = \left[\prod_{t=1}^T f(y_t | F_{t-1}) \right] \cdot f(y_0)$$

If we treat y_0 as fixed, then the term $f(y_0)$ does not depend on the unknown parameters, and therefore the conditional log-likelihood can then be written as the sum of the individual contributions as

$$\ell(\mu, \omega, \alpha, \beta) = \sum_{t=1}^T \ell_t \quad (26.7)$$

where

$$\ell_t = \log \left[\frac{1}{\sqrt{h_t}} \phi \left(\frac{y_t - \mu}{\sqrt{h_t}} \right) \right] = -\frac{1}{2} \left[\log(h_t) + \frac{(y_t - \mu)^2}{h_t} \right]$$

The following script shows a simple application of this technique, which uses the data file `djc1close`; it is one of the example dataset supplied with gretl and contains daily data from the Dow Jones stock index.

```
open djc1close

series y = 100*1diff(djc1close)

scalar mu = 0.0
scalar omega = 1
scalar alpha = 0.4
scalar beta = 0.0

mle ll = -0.5*(log(h) + (e^2)/h)
```

³The *gig* addon, which handles other variants of conditionally heteroskedastic models, uses `mle` as its internal engine.

```

series e = y - mu
series h = var(y)
series h = omega + alpha*(e(-1))^2 + beta*h(-1)
params mu omega alpha beta
end mle

```

26.7 Analytical derivatives

Computation of the score vector is essential for the working of the BFGS method. In all the previous examples, no explicit formula for the computation of the score was given, so the algorithm was fed numerically evaluated gradients. Numerical computation of the score for the i -th parameter is performed via a finite approximation of the derivative, namely

$$\frac{\partial \ell(\theta_1, \dots, \theta_n)}{\partial \theta_i} \simeq \frac{\ell(\theta_1, \dots, \theta_i + h, \dots, \theta_n) - \ell(\theta_1, \dots, \theta_i - h, \dots, \theta_n)}{2h}$$

where h is a small number.

In many situations, this is rather efficient and accurate. A better approximation to the true derivative may be obtained by forcing `mle` to use a technique known as *Richardson Extrapolation*, which gives extremely precise results, but is considerably more CPU-intensive. This feature may be turned on by using the `set` command as in

```
set bfgs_richardson on
```

However, one might want to avoid the approximation and specify an exact function for the derivatives. As an example, consider the following script:

```

nulldata 1000

series x1 = normal()
series x2 = normal()
series x3 = normal()

series ystar = x1 + x2 + x3 + normal()
series y = (ystar > 0)

scalar b0 = 0
scalar b1 = 0
scalar b2 = 0
scalar b3 = 0

mle logl = y*ln(P) + (1-y)*ln(1-P)
  series ndx = b0 + b1*x1 + b2*x2 + b3*x3
  series P = cnorm(ndx)
  params b0 b1 b2 b3
end mle --verbose

```

Here, 1000 data points are artificially generated for an ordinary probit model:⁴ y_t is a binary variable, which takes the value 1 if $y_t^* = \beta_1 x_{1t} + \beta_2 x_{2t} + \beta_3 x_{3t} + \varepsilon_t > 0$ and 0 otherwise. Therefore, $y_t = 1$ with probability $\Phi(\beta_1 x_{1t} + \beta_2 x_{2t} + \beta_3 x_{3t}) = \pi_t$. The probability function for one observation can be written as

$$P(y_t) = \pi_t^{y_t} (1 - \pi_t)^{1-y_t}$$

⁴Again, gretl does provide a native `probit` command (see section 38.1), but a probit model makes for a nice example here.

Since the observations are independent and identically distributed, the log-likelihood is simply the sum of the individual contributions. Hence

$$\ell = \sum_{t=1}^T y_t \log(\pi_t) + (1 - y_t) \log(1 - \pi_t)$$

The `--verbose` switch at the end of the `end mle` statement produces a detailed account of the iterations done by the BFGS algorithm.

In this case, numerical differentiation works rather well; nevertheless, computation of the analytical score is straightforward, since the derivative $\frac{\partial \ell}{\partial \beta_i}$ can be written as

$$\frac{\partial \ell}{\partial \beta_i} = \frac{\partial \ell}{\partial \pi_t} \cdot \frac{\partial \pi_t}{\partial \beta_i}$$

via the chain rule, and it is easy to see that

$$\begin{aligned} \frac{\partial \ell}{\partial \pi_t} &= \frac{y_t}{\pi_t} - \frac{1 - y_t}{1 - \pi_t} \\ \frac{\partial \pi_t}{\partial \beta_i} &= \phi(\beta_1 x_{1t} + \beta_2 x_{2t} + \beta_3 x_{3t}) \cdot x_{it} \end{aligned}$$

The `mle` block in the above script can therefore be modified as follows:

```
mle logl = y*ln(P) + (1-y)*ln(1-P)
  series ndx = b0 + b1*x1 + b2*x2 + b3*x3
  series P = cnorm(ndx)
  series m = dnorm(ndx)*(y/P - (1-y)/(1-P))
  deriv b0 = m
  deriv b1 = m*x1
  deriv b2 = m*x2
  deriv b3 = m*x3
end mle --verbose
```

Note that the `params` statement has been replaced by a series of `deriv` statements; these have the double function of identifying the parameters over which to optimize and providing an analytical expression for their respective score elements.

26.8 Debugging ML scripts

We have discussed above the main sorts of statements that are permitted within an `mle` block, namely

- auxiliary commands to generate helper variables;
- `deriv` statements to specify the gradient with respect to each of the parameters; and
- a `params` statement to identify the parameters in case analytical derivatives are not given.

For the purpose of debugging ML estimators one additional sort of statement is allowed: you can print the value of a relevant variable at each step of the iteration. This facility is more restricted than the regular `print` command. The command word `print` should be followed by the name of just one variable (a scalar, series or matrix).

In the last example above a key variable named `m` was generated, forming the basis for the analytical derivatives. To track the progress of this variable one could add a `print` statement within the ML block, as in

```
series m = dnorm(ndx)*(y/P - (1-y)/(1-P))
print m
```


26.9 Using functions

The `mle` command allows you to estimate models that `gretl` does not provide natively: in some cases, it may be a good idea to wrap up the `mle` block in a user-defined function (see Chapter 14), so as to extend `gretl`'s capabilities in a modular and flexible way.

As an example, we will take a simple case of a model that `gretl` does not yet provide natively: the zero-inflated Poisson model, or ZIP for short.⁵ In this model, we assume that we observe a mixed population: for some individuals, the variable y_t is (conditionally on a vector of exogenous covariates x_t) distributed as a Poisson random variate; for some others, y_t is identically 0. The trouble is, we don't know which category a given individual belongs to.

For instance, suppose we have a sample of women, and the variable y_t represents the number of children that woman t has. There may be a certain proportion, α , of women for whom $y_t = 0$ with certainty (maybe out of a personal choice, or due to physical impossibility). But there may be other women for whom $y_t = 0$ just as a matter of chance — they haven't happened to have any children at the time of observation.

In formulae:

$$\begin{aligned} P(y_t = k | x_t) &= \alpha d_t + (1 - \alpha) \left[e^{-\mu_t} \frac{\mu_t^{y_t}}{y_t!} \right] \\ \mu_t &= \exp(x_t \beta) \\ d_t &= \begin{cases} 1 & \text{for } y_t = 0 \\ 0 & \text{for } y_t > 0 \end{cases} \end{aligned}$$

Writing a `mle` block for this model is not difficult:

```
mle ll = logprob
  series xb = exp(b0 + b1 * x)
  series d = (y=0)
  series poiprob = exp(-xb) * xb^y / gamma(y+1)
  series logprob = (alpha>0) && (alpha<1) ? \
    log(alpha*d + (1-alpha)*poiprob) : NA
  params alpha b0 b1
end mle -v
```

However, the code above has to be modified each time we change our specification by, say, adding an explanatory variable. Using functions, we can simplify this task considerably and eventually be able to write something easy like

```
list X = const x
zip(y, X)
```

Let's see how this can be done. First we need to define a function called `zip()` that will take two arguments: a dependent variable y and a list of explanatory variables X . An example of such function can be seen in script 26.5. By inspecting the function code, you can see that the actual estimation does not happen here: rather, the `zip()` function merely uses the built-in `modprint` command to print out the results coming from another user-written function, namely `zip_estimate()`.

The function `zip_estimate()` is not meant to be executed directly; it just contains the number-crunching part of the job, whose results are then picked up by the end function `zip()`. In turn, `zip_estimate()` calls other user-written functions to perform other tasks. The whole set of "internal" functions is shown in the panel 26.6.

All the functions shown in 26.5 and 26.6 can be stored in a separate `inp` file and executed once, at the beginning of our job, by means of the `include` command. Assuming the name of this script file

⁵The actual ZIP model is in fact a bit more general than the one presented here. The specialized version discussed in this section was chosen for the sake of simplicity. For further details, see [Greene \(2003\)](#).

Listing 26.5: Zero-inflated Poisson Model – user-level function [\[Download ▼\]](#)

```

/*
  user-level function: estimate the model and print out
  the results
*/
function void zip(series y, list X)
  matrix coef_stde = zip_estimate(y, X)
  printf "\nZero-inflated Poisson model:\n"
  string parnames = "alpha,"
  string parnames += varname(X)
  modprint coef_stde parnames
end function

```

Listing 26.6: Zero-inflated Poisson Model — internal functions [\[Download ▼\]](#)

```

/* compute log probabilities for the plain Poisson model */
function series ln_poi_prob(series y, list X, matrix beta)
  series xb = lincomb(X, beta)
  return -exp(xb) + y*xb - lngamma(y+1)
end function

/* compute log probabilities for the zero-inflated Poisson model */
function series ln_zip_prob(series y, list X, matrix beta, scalar p0)
  # check if the probability is in [0,1]; otherwise, return NA
  if p0 > 1 || p0 < 0
    series ret = NA
  else
    series ret = ln_poi_prob(y, X, beta) + ln(1-p0)
    series ret = y==0 ? ln(p0 + exp(ret)) : ret
  endif
  return ret
end function

/* do the actual estimation (silently) */
function matrix zip_estimate(series y, list X)
  # initialize alpha to a "sensible" value: half the frequency
  # of zeros in the sample
  scalar alpha = mean(y==0)/2
  # initialize the coeffs (we assume the first explanatory
  # variable is the constant here)
  matrix coef = zeros(nelem(X), 1)
  coef[1] = mean(y) / (1-alpha)
  # do the actual ML estimation
  mle ll = ln_zip_prob(y, X, coef, alpha)
  params alpha coef
  end mle --hessian --quiet
  return $coeff ~ $stderr
end function

```

is `zip_est.inp`, the following is an example script which (a) includes the script file, (b) generates a simulated dataset, and (c) performs the estimation of a ZIP model on the artificial data.

```
set verbose off

# include the user-written functions
include zip_est.inp

# generate the artificial data
nulldata 1000
set seed 732237
scalar truep = 0.2
scalar b0 = 0.2
scalar b1 = 0.5
series x = normal()
series y = (uniform() < truep) ? 0 : randgen(p, exp(b0 + b1*x))
list X = const x

# estimate the zero-inflated Poisson model
zip(y, X)
```

The results are as follows:

Zero-inflated Poisson model:

	coefficient	std. error	z-stat	p-value	
alpha	0.209738	0.0261746	8.013	1.12e-15	***
const	0.167847	0.0449693	3.732	0.0002	***
x	0.452390	0.0340836	13.27	3.32e-40	***

A further step may then be creating a function package for accessing your new `zip()` function via gretl's graphical interface. For details on how to do this, see section 14.5.

26.10 Advanced use of `mle`: functions, analytical derivatives, algorithm choice

All the techniques described in the previous sections may be combined, and `mle` can be used for solving non-standard estimation problems (provided, of course, that one chooses maximum likelihood as the preferred inference method).

The strategy that, as of this writing, has proven most successful in designing scripts for this purpose is:

- Modularize your code as much as possible.
- Use analytical derivatives whenever possible.
- Choose your optimization method wisely.

In the rest of this section, we will expand on the probit example of section 26.7 to give the reader an idea of what a “heavy-duty” application of `mle` looks like. Most of the code fragments come from `mle-advanced.inp`, which is one of the sample scripts supplied with the standard installation of gretl (see under *File > Script files > Practice File*).

BFGS with and without analytical derivatives

The example in section 26.7 can be made more general by using matrices and user-written functions. Consider the following code fragment:

```

list X = const x1 x2 x3
matrix b = zeros(nelem(X),1)

mle logl = y*ln(P) + (1-y)*ln(1-P)
    series ndx = lincomb(X, b)
    series P = cnorm(ndx)
    params b
end mle

```

In this context, the fact that the model we are estimating has four explanatory variables is totally incidental: the code is written in such a way that we could change the content of the list *X* without having to make any other modification. This was made possible by:

1. gathering the parameters to estimate into a single vector *b* rather than using separate scalars;
2. using the `nelem()` function to initialize *b*, so that its dimension is kept track of automatically;
3. using the `lincomb()` function to compute the index function.

A parallel enhancement could be achieved in the case of analytically computed derivatives: since *b* is now a vector, `mle` expects the argument to the `deriv` keyword to be a matrix, in which each column is the partial derivative to the corresponding element of *b*. It is useful to re-write the score for the *i*-th observation as

$$\frac{\partial \ell_i}{\partial \beta} = m_i \mathbf{x}'_i \quad (26.8)$$

where m_i is the “signed Mills’ ratio”, that is

$$m_i = y_i \frac{\phi(\mathbf{x}'_i \beta)}{\Phi(\mathbf{x}'_i \beta)} - (1 - y_i) \frac{\phi(\mathbf{x}'_i \beta)}{1 - \Phi(\mathbf{x}'_i \beta)},$$

which was computed in section 26.7 via

```

series P = cnorm(ndx)
series m = dnorm(ndx)*(y/P - (1-y)/(1-P))

```

Here, we will code it in a somewhat terser way as

```

series m = y ? invmills(-ndx) : -invmills(ndx)

```

and make use of the conditional assignment operator and of the specialized function `invmills()` for efficiency. Building the score matrix is now easily achieved via

```

mle logl = y*ln(P) + (1-y)*ln(1-P)
    series ndx = lincomb(X, b)
    series P = cnorm(ndx)
    series m = y ? invmills(-ndx) : -invmills(ndx)
    matrix mX = {X}
    deriv b = mX .* {m}
end mle

```

in which the `{}` operator was used to turn series and lists into matrices (see chapter 17). However, proceeding in this way for more complex models than probit may imply inserting into the `mle` block a long series of instructions; the example above merely happens to be short because the score matrix for the probit model is very easy to write in matrix form.

A better solution is writing a user-level function to compute the score and using that inside the `mle` block, as in

```

function matrix score(matrix b, series y, list X)
    series ndx = lincomb(X, b)
    series m = y ? invmills(-ndx) : -invmills(ndx)
    return {m} .* {X}
end function

[...]

mle logl = y*ln(P) + (1-y)*ln(1-P)
    series ndx = lincomb(X, b)
    series P = cnorm(ndx)
    deriv b = score(b, y, X)
end mle

```

In this way, no matter how complex the computation of the score is, the `mle` block remains nicely compact.

Newton's method and the analytical Hessian

As mentioned above, gretl offers the user the option of using Newton's method for maximizing the log-likelihood. In terms of the notation used in section 26.1, the direction for updating the initial parameter vector θ_0 is given by

$$d[\mathbf{g}(\theta_0)] = -\lambda \mathbf{H}(\theta_0)^{-1} \mathbf{g}(\theta_0), \quad (26.9)$$

where $\mathbf{H}(\theta)$ is the Hessian of the total loglikelihood computed at θ and $0 < \lambda < 1$ is a scalar called the *step length*.

The above expression makes a few points clear:

1. At each step, it must be possible to compute not only the score $\mathbf{g}(\theta)$, but also its derivative $\mathbf{H}(\theta)$;
2. the matrix $\mathbf{H}(\theta)$ should be nonsingular;
3. it is assumed that for some positive value of λ , $\ell(\theta_1) > \ell(\theta_0)$; in other words, that going in the direction $d[\mathbf{g}(\theta_0)]$ leads upwards for some step length.

The strength of Newton's method lies in the fact that, if the loglikelihood is globally concave, then (26.9) enjoys certain optimality properties and the number of iterations required to reach the maximum is often much smaller than it would be with other methods, such as BFGS. However, it may have some disadvantages: for a start, the Hessian $\mathbf{H}(\theta)$ may be difficult or very expensive to compute; moreover, the loglikelihood may not be globally concave, so for some values of θ , the matrix $\mathbf{H}(\theta)$ is not negative definite or perhaps even singular. Those cases are handled by gretl's implementation of Newton's algorithm by means of several heuristic techniques⁶, but a number of adverse consequences may occur, which range from *longer* computation time for optimization to non-convergence of the algorithm.

As a consequence, using Newton's method is advisable only when the computation of the Hessian is not too CPU-intensive and the nature of the estimator is such that it is known in advance that the loglikelihood is globally concave. The probit models satisfies both requisites, so we will expand the preceding example to illustrate how to use Newton's method in gretl.

A first example may be given simply by issuing the command

```
set optimizer newton
```

⁶The gist to it is that, if \mathbf{H} is not negative definite, it is substituted by $k \cdot \text{dg}(\mathbf{H}) + (1 - k) \cdot \mathbf{H}$, where k is a suitable scalar; however, if you're interested in the precise details, you'll be much better off looking at the source code: the file you'll want to look at is `lib/src/gretl_bfgs.c`.

before the `mle` block.⁷ This will instruct `gretl` to use Newton's method instead of BFGS. If the `deriv` keyword is used, `gretl` will differentiate the score function numerically; otherwise, if the score has to be computed itself numerically, `gretl` will calculate $\mathbf{H}(\theta)$ by differentiating the loglikelihood numerically twice. The latter solution, though, is generally to be avoided, as may be extremely time-consuming and may yield imprecise results.

A much better option is to calculate the Hessian analytically and have `gretl` use its true value rather than a numerical approximation. In most cases, this is both much faster and numerically stable, but of course comes at the price of having to differentiate the loglikelihood twice to respect with the parameters and translate the resulting expressions into efficient `hansl` code.

Luckily, both tasks are relatively easy in the probit case: the matrix of second derivatives of ℓ_i may be written as

$$\frac{\partial^2 \ell_i}{\partial \beta \partial \beta'} = -m_i (m_i + \mathbf{x}_i' \beta) \mathbf{x}_i \mathbf{x}_i'$$

so the total Hessian is

$$\sum_{i=1}^n \frac{\partial^2 \ell_i}{\partial \beta \partial \beta'} = -X' \begin{bmatrix} w_1 & & & \\ & w_2 & & \\ & & \ddots & \\ & & & w_n \end{bmatrix} X \quad (26.10)$$

where $w_i = m_i (m_i + \mathbf{x}_i' \beta)$. It can be shown that $w_i > 0$, so the Hessian is guaranteed to be negative definite in all sensible cases and the conditions are ideal for applying Newton's method.

A `hansl` translation of equation (26.10) may look like

```
function void Hess(matrix *H, matrix b, series y, list X)
/* computes the negative Hessian for a Probit model */
series ndx = lincomb(X, b)
series m = y ? invmills(-ndx) : -invmills(ndx)
series w = m*(m+ndx)
matrix mX = {X}
H = (mX .* {w})'mX
end function
```

There are two characteristics worth noting of the function above. For a start, it doesn't return anything: the result of the computation is simply stored in the matrix pointed at by the first argument of the function. Second, the result is not the Hessian proper, but rather its negative. This function becomes usable from within an `mle` block by the keyword `hessian`. The syntax is

```
mle ...
...
hessian funcname(&mat_addr, ...)
end mle
```

In other words, the `hessian` keyword must be followed by the call to a function whose first argument is a matrix pointer which is supposed to be filled with the *negative* of the Hessian at θ .

We said above (section 26.1) that the covariance matrix of the parameter estimates is by default estimated using the Outer Product of the Gradient (so long as the log-likelihood function returns the per-observation contributions). However, if you supply a function that computes the Hessian then by default it is used in estimating the covariance matrix. If you wish to impose use of OPG instead, append the `--opg` option to the end of the `mle` block.

Note that `gretl` does not perform any numerical check on whether a user-supplied function computes the Hessian correctly. On the one hand, this means that you can trick `mle` into using alternatives to the Hessian and thereby implement other optimization methods. For example, if you

⁷To go back to BFGS, you use `set optimizer bfgs`.

substitute in equation 26.9 the Hessian \mathbf{H} with the negative of the OPG matrix $-\mathbf{G}'\mathbf{G}$, as defined in (26.2), you get the so-called BHHH optimization method (see [Berndt et al. \(1974\)](#)). Again, the sample file `mle-advanced.inp` provides an example. On the other hand, you may want to perform a check of your analytically-computed \mathbf{H} matrix versus a numerical approximation.

If you have a function that computes the score, this is relatively simple to do by using the `fdjac` function, briefly described in section 37.3, which computes a numerical approximation to a derivative. In practice, you need a function computing $\mathbf{g}(\theta)$ as a row vector and then use `fdjac` to differentiate it numerically with respect to θ . The result can then be compared to your analytically-computed Hessian. The code fragment below shows an example of how this can be done in the probit case:

```
function matrix totalscore(matrix *b, series y, list X)
    /* computes the total score */
    return sumc(score(b, y, X))
end function

function void check(matrix b, series y, list X)
    /* compares the analytical Hessian to its numerical
    approximation obtained via fdjac */
    matrix aH
    Hess(&aH, b, y, X) # stores the analytical Hessian into aH

    matrix nH = fdjac(b, "totalscore(&b, y, X)")
    nH = 0.5*(nH + nH') # force symmetry

    printf "Numerical Hessian\n%16.6f\n", nH
    printf "Analytical Hessian (negative)\n%16.6f\n", aH
    printf "Check (should be zero)\n%16.6f\n", nH + aH
end function
```

26.11 Estimating constrained models

In many cases, you may want to perform ML estimation of a model under some kind of constraint. Mathematically, this amounts to maximizing the log-likelihood $\ell(\theta)$ under some restriction. Assume that the restriction can be represented as $g(\theta) = 0$, where the function $g(\cdot)$ is differentiable. On paper, the most straightforward way to accomplish this task is to set up a Lagrangean

$$\mathcal{L}(\theta) = \ell(\theta) + \lambda' g(\theta)$$

and solve the first-order conditions that arise from differentiating the Lagrangean with respect to θ and λ .

If an explicit solution can be found, then all is well; but in many cases the resulting system of equations cannot be solved explicitly, so that numerical optimisation is necessary. In such cases the approach above is not particularly useful; a different strategy is much more convenient.

The idea is to find an alternative parametrization—a means of expressing the vector θ as a (differentiable) function of a smaller set of parameters ψ . In other words, find a function $h(\cdot)$ such that any admissible value of θ can be written as $\theta = h(\psi)$ and $g[h(\psi)] = 0$ for any value of ψ . Then maximization of the log-likelihood is simply a question of operating on $\ell^*(\psi) = \ell[h(\psi)]$ using an ordinary unconstrained numerical optimization routine.

Once the ML estimate $\hat{\psi}$ is available, it is easy to recover the corresponding constrained vector $\hat{\theta} = h(\hat{\psi})$. Computing the covariance matrix involves an extra step, known as the *delta method*: the asymptotic covariance matrix of $\hat{\theta}$ can be computed as

$$V(\hat{\theta}) = J(\hat{\psi})' V(\hat{\psi}) J(\hat{\psi}) \quad (26.11)$$

where J is the Jacobian matrix, holding the partial derivatives of $h(\psi)$. It is recommended that the Jacobian matrix should be computed analytically whenever possible, but as a fallback strategy, numerical differentiation (available via the function `fdjac` — see section 37.3) is a viable alternative. Note that the matrix produced by this method will be singular by construction.

The example reported in script 26.7 is perhaps a little contrived, but useful to elucidate the technique. Suppose we wish to estimate mean and variance of an iid sample of Gaussian random variables, under the constraint that $V(x_i) = \sigma^2 = \exp[E(x_i)] = \exp(\mu)$. Of course the unconstrained ML estimators $\hat{\mu} = \bar{X}$ and $\hat{\sigma}^2 = n^{-1} \sum_i (x_i - \bar{X})^2$ are not guaranteed to satisfy the constraints (in fact, the probability that they do is 0).

The Lagrangean in this case would be

$$\mathcal{L}(\theta) = K - \frac{n}{2} \log \sigma^2 - \frac{1}{2\sigma^2} \sum_i (x_i - \mu)^2 + \lambda(e^\mu - \sigma^2)$$

and finding an explicit solution by solving the first-order conditions is not at all easy. Fortunately, numerical optimization becomes straightforward by expressing the constrained parameters as

$$\theta = [\mu, \sigma^2]' = [\psi, \exp(\psi)]' = h(\psi);$$

after maximizing the log-likelihood, the covariance matrix for θ can be recovered by computing the Jacobian as

$$J(\psi) = \begin{bmatrix} \frac{d\mu}{d\psi} & \frac{d\sigma^2}{d\psi} \end{bmatrix} = \begin{bmatrix} 1 & \exp(\psi) \end{bmatrix}$$

and applying formula (26.11).

Running the example script should produce the following output:

```
unconstrained estimates: mean = 1.00314, variance = 2.8903
check: vhat - exp(muhat) = 0.163481
```

```
Model 1: ML, using observations 1-1000
loglik = -0.5*log(2*$pi) - 0.5*log(s2) - 0.5*(x-m)^2/s2
Standard errors based on Outer Products matrix
```

	estimate	std. error	z	p-value
-----	-----	-----	-----	-----
psi[1]	1.03763	0.0357311	29.04	2.07e-185 ***
Log-likelihood	-1949.972	Akaike criterion		3901.943
Schwarz criterion	3906.851	Hannan-Quinn		3903.808

```
check: vhat - exp(muhat) = 0
```

	coefficient	std. error	z	p-value
-----	-----	-----	-----	-----
mean	1.03763	0.0357311	29.04	2.07e-185 ***
variance	2.82251	0.100851	27.99	2.35e-172 ***

26.12 Handling non-convergence gracefully

If the numerical aspects of the estimation procedure are complex, it is possible that `mle` fails to find the maximum within the number of iterations stipulated via the `bfgs_maxiter` state variable (which defaults to 500).

In these cases, `mle` will exit with error and it's up to the user to handle the situation appropriately. For example, it is possible that `mle` is used inside a loop and you don't want the loop to stop in case convergence is not achieved. The `catch` command modifier (see also the *Gretl Command Reference*) is an excellent tool for this purpose.

Listing 26.7: Example of ML estimation of a model under constraints [\[Download ▼\]](#)

```

set verbose off
set seed 7120

function matrix h(matrix psi)
    ret = psi[1] | exp(psi[1])
    return ret
end function

function matrix anJacob(matrix psi)
    # the derivative of h
    return 1 ~ exp(psi[1])
end function

nulldata 1000
# generate artificial data from a N(1, e) distribution
series x = 1 + normal() * exp(0.5)

# show that the unconstrained estimates don't satisfy the restriction

scalar muhat = mean(x)
scalar s2hat = sst(x)/$nobs
printf "unconstrained estimates: mean = %g, variance = %g\n", muhat, s2hat
printf "check: vhat - exp(muhat) = %g\n\n", s2hat - exp(muhat)

# now estimate under the constraint exp(mean) = variance

psi = {1}
mle loglik = -0.5*log(2*$pi) - 0.5*log(s2) - 0.5*(x-m)^2/s2
    matrix par = h(psi)
    scalar m = par[1]
    scalar s2 = par[2]
    params psi
end mle

# now map psi to the constrained parametrisation
matrix par = h(psi)

# show that now the constraint holds
printf "check: vhat - exp(muhat) = %g\n\n", par[2] - exp(par[1])

# take care of the covariance matrix
matrix vpar = qform(anJacob(psi)', $vcv)
# alternatively, one could use the numerical Jacobian, as in
# matrix vpar = qform(fdjac(psi, "h(psi)"), $vcv)

# finally, print out the constrained parameters via "modprint"
matrix cs = par ~ sqrt(diag(vpar))
modprint cs "mean variance"

```

The example provided in listing 26.8 illustrates the usage of `catch` in an artificially simple context: we use the `mle` command for estimating mean and variance of a Gaussian rv (of course you don't need the `mle` apparatus for this, but it makes for a nice example). The gist of the example is using the `set bfgs_maxiter` command to force `mle` to abort after a very small number of iterations, so that you can have an idea on how to use the `catch` modifier and the associated `$error` accessor to handle the situation.

You may want to increase the maximum number of BFGS iterations in the example to check what happens if the algorithm is allowed to converge. Note that, upon successful completion of `mle`, a bundle named `$model` is available, containing several quantities that may be of your interest, including the total number of function evaluations.

Listing 26.8: Handling non-convergence via `catch` [\[Download ▼\]](#)

```

set verbose off
nulldata 200
set seed 8118

# generate simulated data from a N(3,4) variate
series x = normal(3,2)

# set starting values
scalar m = 0
scalar s2 = 1

# set iteration limit to a ridiculously low value
set bfgs_maxiter 10

# perform ML estimation; note the "catch" modifier
catch mle loglik = -0.5* (log(2*$pi) + log(s2) + e2/s2)
    series e2 = (x - m)^2
    params m s2
end mle --quiet

# grab the error and proceed as needed
err = $error
if err
    printf "Not converged! (m = %g, s2 = %g)\n", m, s2
else
    printf "Converged after %d iterations\n", $model.grcount
    cs = $coeff ~ sqrt(diag($vcv))
    pn = "m s2"
    modprint cs pn
endif

```

Chapter 27

GMM estimation

27.1 Introduction and terminology

The Generalized Method of Moments (GMM) is a very powerful and general estimation method, which encompasses practically all the parametric estimation techniques used in econometrics. It was introduced in Hansen (1982) and Hansen and Singleton (1982); an excellent and thorough treatment is given in chapter 17 of Davidson and MacKinnon (1993).

The basic principle on which GMM is built is rather straightforward. Suppose we wish to estimate a scalar parameter θ based on a sample x_1, x_2, \dots, x_T . Let θ_0 indicate the “true” value of θ . Theoretical considerations (either of statistical or economic nature) may suggest that a relationship like the following holds:

$$E[x_t - g(\theta)] = 0 \Leftrightarrow \theta = \theta_0, \quad (27.1)$$

with $g(\cdot)$ a continuous and invertible function. That is to say, there exists a function of the data and the parameter, with the property that it has expectation zero if and only if it is evaluated at the true parameter value. For example, economic models with rational expectations lead to expressions like (27.1) quite naturally.

If the sampling model for the x_t s is such that some version of the Law of Large Numbers holds, then

$$\bar{X} = \frac{1}{T} \sum_{t=1}^T x_t \xrightarrow{p} g(\theta_0);$$

hence, since $g(\cdot)$ is invertible, the statistic

$$\hat{\theta} = g^{-1}(\bar{X}) \xrightarrow{p} \theta_0,$$

so $\hat{\theta}$ is a consistent estimator of θ . A different way to obtain the same outcome is to choose, as an estimator of θ , the value that minimizes the objective function

$$F(\theta) = \left[\frac{1}{T} \sum_{t=1}^T (x_t - g(\theta)) \right]^2 = [\bar{X} - g(\theta)]^2; \quad (27.2)$$

the minimum is trivially reached at $\hat{\theta} = g^{-1}(\bar{X})$, since the expression in square brackets equals 0.

The above reasoning can be generalized as follows: suppose θ is an n -vector and we have m relations like

$$E[f_i(x_t, \theta)] = 0 \quad \text{for } i = 1 \dots m, \quad (27.3)$$

where $E[\cdot]$ is a conditional expectation on a set of p variables z_t , called the *instruments*. In the above simple example, $m = 1$ and $f(x_t, \theta) = x_t - g(\theta)$, and the only instrument used is $z_t = 1$. Then, it must also be true that

$$E[f_i(x_t, \theta) \cdot z_{j,t}] = E[f_{i,j,t}(\theta)] = 0 \quad \text{for } i = 1 \dots m \quad \text{and } j = 1 \dots p; \quad (27.4)$$

equation (27.4) is known as an *orthogonality condition*, or *moment condition*. The GMM estimator is defined as the minimum of the quadratic form

$$F(\theta, W) = \tilde{\mathbf{f}}' W \tilde{\mathbf{f}}, \quad (27.5)$$

where $\bar{\mathbf{f}}$ is a $(1 \times m \cdot p)$ vector holding the average of the orthogonality conditions and W is some symmetric, positive definite matrix, known as the *weights* matrix. A necessary condition for the minimum to exist is the order condition $n \leq m \cdot p$.

The statistic

$$\hat{\theta} = \underset{\theta}{\text{Argmin}} F(\theta, W) \quad (27.6)$$

is a consistent estimator of θ whatever the choice of W . However, to achieve maximum asymptotic efficiency W must be proportional to the inverse of the long-run covariance matrix of the orthogonality conditions; if W is not known, a consistent estimator will suffice.

These considerations lead to the following empirical strategy:

1. Choose a positive definite W and compute the *one-step* GMM estimator $\hat{\theta}_1$. Customary choices for W are $I_{m \cdot p}$ or $I_m \otimes (Z'Z)^{-1}$.
2. Use $\hat{\theta}_1$ to estimate $V(f_{i,j,t}(\theta))$ and use its inverse as the weights matrix. The resulting estimator $\hat{\theta}_2$ is called the *two-step* estimator.
3. Re-estimate $V(f_{i,j,t}(\theta))$ by means of $\hat{\theta}_2$ and obtain $\hat{\theta}_3$; iterate until convergence. Asymptotically, these extra steps are unnecessary, since the two-step estimator is consistent and efficient; however, the iterated estimator often has better small-sample properties and should be independent of the choice of W made at step 1.

In the special case when the number of parameters n is equal to the total number of orthogonality conditions $m \cdot p$, the GMM estimator $\hat{\theta}$ is the same for any choice of the weights matrix W , so the first step is sufficient; in this case, the objective function is 0 at the minimum.

If, on the contrary, $n < m \cdot p$, the second step (or successive iterations) is needed to achieve efficiency, and the estimator so obtained can be very different, in finite samples, from the one-step estimator. Moreover, the value of the objective function at the minimum, suitably scaled by the number of observations, yields *Hansen's J statistic*; this statistic can be interpreted as a test statistic that has a χ^2 distribution with $m \cdot p - n$ degrees of freedom under the null hypothesis of correct specification. See Davidson and MacKinnon (1993, section 17.6) for details.

In the following sections we will show how these ideas are implemented in gretl through some examples.

27.2 GMM as Method of Moments

We thank Alecos Papadopoulos, who kindly contributed a document on which this section is based.

A very simple illustration of GMM can be given by dropping the “G”, via an example of the time-honored statistical technique known as the method of moments. Let's see how to estimate the parameters of a gamma distribution, a task which we used to exemplify ML estimation in section 26.4.

Suppose that we have an i.i.d. sample of size T from a gamma distribution. The gamma density can be parameterized in terms of the two parameters k (shape) and θ (scale), both real and positive. In order to estimate them by the method of moments, we need two moment conditions so that we have two equations in the two unknowns (in GMM terms, this amounts to exact identification). The two relations we need are

$$E(x_i) = k \cdot \theta \quad V(x_i) = k \cdot \theta^2$$

Substituting the finite-sample counterparts of the theoretical moments we have

$$\bar{X} = \hat{k} \cdot \hat{\theta} \quad (27.7)$$

$$\hat{V} = \hat{k} \cdot \hat{\theta}^2 \quad (27.8)$$

These two equations are easy to solve analytically, giving $\hat{\theta} = \hat{V}/\bar{X}$ and $\hat{k} = \bar{X}/\hat{\theta}$, (\hat{V} being the sample variance of x_i), but it's instructive to see how the `gmm` command will solve this system of equations numerically.

We feed `gretl` the necessary ingredients for GMM estimation in a command block that starts with `gmm` and ends with `end gmm`. The following elements are compulsory within a `gmm` block:

1. one or more statements to calculate the left-hand side of the orthogonality conditions.
2. one or more `orthog` statements
3. one `weights` statement
4. one `params` statement

These elements should be given in the stated order.

The `orthog` statements are used to specify the orthogonality conditions. They must follow the syntax

```
orthog x ; Z
```

where `x` may be a series, matrix or list of series (given either by name or *in extenso*) `Z` may also be a series, matrix or list. Note the structure of the statement: it is assumed that the term to the left of the semicolon represents a quantity that depends on the estimated parameters (and so must be updated in the process of iterative estimation), while the term on the right is a constant function of the data.

The `weights` statement is used to specify the initial weighting matrix and its syntax is straightforward.

The `params` statement specifies the parameters with respect to which the GMM criterion should be minimized; it follows the same logic and rules as in the `mle` and `nls` commands.

The minimum is found numerically using BFGS (see chapters 37 and 26). The progress of the optimization procedure can be observed by appending the `--verbose` switch to the `end gmm` line.

Equations 27.7 and 27.8 are not yet in the “moment condition” form required by the `gmm` command. We need to transform them and arrive at something looking like $E(e_{j,i}z_{j,i}) = 0$ for $j = 1, 2$. We therefore need two variables e_1 and e_2 with associated instruments z_1 and z_2 ; we can then tell `gretl` that $\hat{E}(e_j z_j) = 0$ must be satisfied (where the $\hat{E}(\cdot)$ notation indicates sample moments).

If we define the instrument as a series of ones, and define a series `e1` such that $e_{1,i} = x_i - k\theta$, we can rewrite the first moment condition as

$$\hat{E}[e_{1,i} \cdot 1] = 0$$

In similar manner we can define a series `e2` such that $e_{2,i} = (x_i - \bar{X})^2 - k\theta^2$ (and set $z_2 = z_1$), so that the second moment condition is

$$\hat{E}[e_{2,i} \cdot 1] = 0$$

Since the built-in `const` is just a series of 1s we could express these moment conditions in the notation that `gretl` expects as

```
orthog e1 ; const
orthog e2 ; const
```

But given that the right-hand side is the same for each the conditions can be combined, using a list on the left:

```
orthog e1 e2 ; const
```

The required weighting matrix can be set to any positive definite 2×2 matrix, since under exact identification the choice doesn't matter and its dimension is determined by the number of orthogonality conditions. So we'll use the I_2 identity matrix. Example code is shown in Listing 27.1, along with the output it produces.

Listing 27.1: MM estimation of Gamma parameters [\[Download ▼\]](#)

```
# create an empty data set with 200 observations
nulldata 200

# fix a random seed for replicability
set seed 1707138404

# generate a Gamma random variable x with shape k = 3 and scale theta = 2
series x = randgen(G, 3, 2)

# declare and initialize the parameter estimates
scalar k = 1
scalar theta = 1

# create the weight matrix as the identity matrix
matrix W = I(2)

# declare two series for use in the orthogonality conditions
series e1 = 0
series e2 = 0

# obtain the sample mean of x
scalar m = mean(x)

gmm
    series e1 = x - k*theta
    series e2 = (x - m)^2 - k*theta^2
    orthog e1 e2 ; const
    weights W
    params k theta
end gmm
```

The gmm output is:

Model 1: 1-step GMM, using observations 1-200

	estimate	std. error	z	p-value	
p	3.08539	0.412149	7.486	7.09e-14	***
theta	1.97898	0.286796	6.900	5.19e-12	***

GMM criterion: Q = 1.19302e-28 (TQ = 2.38604e-26)

In order to use the *unbiased* estimator of the sample variance, we have to modify the second moment condition by substituting

```
series e2 = (x - m)^2 - p*theta^2
```

with

```
scalar adj = $nobs / ($nobs - 1)
series e2 = adj * (x - m)^2 - p*theta^2
```

The output then becomes:

Model 1: 1-step GMM, using observations 1-200

	estimate	std. error	z	p-value	
p	3.06997	0.410088	7.486	7.09e-14	***
theta	1.98892	0.288237	6.900	5.19e-12	***

GMM criterion: Q = 1.66926e-28 (TQ = 3.33852e-26)

In this case both of the point estimates are marginally closer to the true values. But this is a small-sample effect, not something to be expected in large samples.

27.3 OLS as GMM

We now move to an example closer to econometrics proper: the linear model $y_t = x_t\beta + u_t$. Most of us are used to reading it informally as the sum of a “systematic part” and a “disturbance”, but a more rigorous interpretation of this familiar expression rests on the *hypothesis* that the conditional mean $E(y_t|x_t)$ is linear plus the *definition* of u_t as $y_t - E(y_t|x_t)$.

From the definition of u_t , it follows that $E(u_t|x_t) = 0$. The following orthogonality condition is therefore available:

$$E[f(\beta)] = 0, \quad (27.9)$$

where $f(\beta) = (y_t - x_t\beta)x_t$. The definitions given in section 27.1 therefore specialize here to:

- θ is β ;
- the instrument is x_t ;
- $f_{i,j,t}(\theta)$ is $(y_t - x_t\beta)x_t = u_tx_t$; the orthogonality condition is interpretable as the requirement that the regressors should be uncorrelated with the disturbances;
- W can be any symmetric positive definite matrix, since the number of parameters equals the number of orthogonality conditions. Let's say we choose I .
- The function $F(\theta, W)$ is in this case

$$F(\theta, W) = \left[\frac{1}{T} \sum_{t=1}^T (\hat{u}_t x_t) \right]^2$$

and it is easy to see why OLS and GMM coincide here: the GMM objective function has the same minimizer as the objective function of OLS, the residual sum of squares. Note, however, that the two functions are not equal to one another: at the minimum, $F(\theta, W) = 0$ while the minimized sum of squared residuals is zero only in the special case of a perfect linear fit.

The code snippet below uses gretl's `gmm` command to make the above operational. The series `e` holds the “residuals” and the series `x` holds the regressor. If `x` had been a list (or a matrix), the `orthog` statement would have generated one orthogonality condition for each element (or column) of `x`.

```
/* initialize stuff */
series e = 0
```

```

scalar beta = 0
matrix W = I(1)

/* proceed with estimation */
gmm
    series e = y - x*beta
    orthog e ; x
    weights W
    params beta
end gmm

```

27.4 TSLS as GMM

Moving closer to the proper domain of GMM, we now consider two-stage least squares (TSLS) as a case of GMM.

TSLS is employed in the case where one wishes to estimate a linear model of the form $y_t = X_t\beta + u_t$, but where one or more of the variables in the matrix X are potentially endogenous—correlated with the error term, u . We proceed by identifying a set of instruments, Z_t , which are explanatory for the endogenous variables in X but which are plausibly uncorrelated with u . The classic two-stage procedure is (1) regress the endogenous elements of X on Z ; then (2) estimate the equation of interest, with the endogenous elements of X replaced by their fitted values from (1).

An alternative perspective is given by GMM. We define the residual \hat{u}_t as $y_t - X_t\hat{\beta}$, as usual. But instead of relying on $E(u|X) = 0$ as in OLS, we base estimation on the condition $E(u|Z) = 0$. In this case it is natural to base the initial weighting matrix on the covariance matrix of the instruments. Listing 27.2 presents a model from Stock and Watson's *Introduction to Econometrics*. The demand for cigarettes is modeled as a linear function of the logs of price and income; income is treated as exogenous while price is taken to be endogenous and two measures of tax are used as instruments. Since we have two instruments and one endogenous variable the model is over-identified.

In the GMM context, this happens when you have more orthogonality conditions than parameters to estimate. If so, asymptotic efficiency gains can be expected by iterating the procedure once or more. This is accomplished by specifying, after the `end gmm` statement, two mutually exclusive options: `--two-step` or `--iterate`, whose meaning should be obvious. Note that when the problem is over-identified, the weights matrix will influence the solution you get from the 1- and 2-step procedures.

☞ In cases other than one-step estimation the specified weights matrix will be overwritten with the *final* weights on completion of the `gmm` command. If you wish to execute more than one GMM block with a common starting-point it is therefore necessary to reinitialize the weights matrix between runs.

Partial output from this script is shown in 27.3. The estimated standard errors from GMM are robust by default; if we supply the `--robust` option to the `tsls` command we get identical results.¹

After the `end gmm` statement two mutually exclusive options can be specified: `--two-step` or `--iterate`, whose meaning should be obvious.

27.5 Covariance matrix options

The covariance matrix of the estimated parameters depends on the choice of W through

$$\hat{\Sigma} = (J'WJ)^{-1}J'W\Omega WJ(J'WJ)^{-1} \quad (27.10)$$

where J is a Jacobian term

$$J_{ij} = \frac{\partial \bar{f}_i}{\partial \theta_j}$$

¹The data file used in this example is available in the Stock and Watson package for gretl. See http://gretl.sourceforge.net/gretl_data.html.

Listing 27.2: TSLS via GMM [\[Download ▼\]](#)

```
open cig_ch10.gdt

# real avg price including sales tax
ravgprs = avgprs / cpi

# real avg cig-specific tax
rtax = tax / cpi

# real average total tax
rtaxs = taxes / cpi

# real average sales tax
rtaxso = rtaxs - rtax

# logs of consumption, price, income
lpackpc = log(packpc)
lavgprs = log(ravgprs)
perinc = income / (pop*cpi)
lperinc = log(perinc)

# restrict sample to 1995 observations
smpl --restrict year==1995
# Equation (10.16) by tsls
list xlist = const lavgprs lperinc
list zlist = const rtaxso rtax lperinc
tsls lpackpc xlist ; zlist --robust

# setup for gmm
matrix Z = { zlist }
matrix W = inv(Z'Z)
series e = 0
scalar b0 = 1
scalar b1 = 1
scalar b2 = 1

gmm e = lpackpc - b0 - b1*lavgprs - b2*lperinc
    orthog e ; Z
    weights W
    params b0 b1 b2
end gmm
```

Listing 27.3: TSLS via GMM: partial output

Model 1: TSLS estimates using the 48 observations 1-48
 Dependent variable: lpackpc
 Instruments: rtaxso rtax
 Heteroskedasticity-robust standard errors, variant HCO

VARIABLE	COEFFICIENT	STDERROR	T STAT	P-VALUE
const	9.89496	0.928758	10.654	<0.00001 ***
lavgprs	-1.27742	0.241684	-5.286	<0.00001 ***
lperinc	0.280405	0.245828	1.141	0.25401

Model 2: 1-step GMM estimates using the 48 observations 1-48
 e = lpackpc - b0 - b1*lavgprs - b2*lperinc

PARAMETER	ESTIMATE	STDERROR	T STAT	P-VALUE
b0	9.89496	0.928758	10.654	<0.00001 ***
b1	-1.27742	0.241684	-5.286	<0.00001 ***
b2	0.280405	0.245828	1.141	0.25401

GMM criterion = 0.0110046

and Ω is the long-run covariance matrix of the orthogonality conditions.

Gretl computes J by numeric differentiation (there is no provision for specifying a user-supplied analytical expression for J at the moment). As for Ω , a consistent estimate is needed. The simplest choice is the sample covariance matrix of the f_t s:

$$\hat{\Omega}_0(\theta) = \frac{1}{T} \sum_{t=1}^T f_t(\theta) f_t(\theta)' \quad (27.11)$$

This estimator is robust with respect to heteroskedasticity, but not with respect to autocorrelation. A heteroskedasticity- and autocorrelation-consistent (HAC) variant can be obtained using the Bartlett kernel or similar. A univariate version of this is used in the context of the `lrvr()` function—see equation (22.6). The multivariate version is set out in equation (27.12).

$$\hat{\Omega}_k(\theta) = \frac{1}{T} \sum_{t=k}^{T-k} \left[\sum_{i=-k}^k w_i f_t(\theta) f_{t-i}(\theta)' \right], \quad (27.12)$$

Gretl computes the HAC covariance matrix by default when a GMM model is estimated on time series data. You can control the kernel and the bandwidth (that is, the value of k in 27.12) using the `set` command. See chapter 22 for further discussion of HAC estimation. You can also ask gretl *not* to use the HAC version by saying

```
set force_hc on
```

27.6 A real example: the Consumption Based Asset Pricing Model

To illustrate gretl's implementation of GMM, we will replicate the example given in chapter 3 of Hall (2005). The model to estimate is a classic application of GMM, and provides an example of a case when orthogonality conditions do not stem from statistical considerations, but rather from economic theory.

A rational individual who must allocate his income between consumption and investment in a financial asset must in fact choose the consumption path of his whole lifetime, since investment translates into future consumption. It can be shown that an optimal consumption path should satisfy the following condition:

$$pU'(c_t) = \delta^k E[r_{t+k}U'(c_{t+k})|\mathcal{F}_t], \quad (27.13)$$

where p is the asset price, $U(\cdot)$ is the individual's utility function, δ is the individual's subjective discount rate and r_{t+k} is the asset's rate of return between time t and time $t+k$. \mathcal{F}_t is the *information set* at time t ; equation (27.13) says that the utility “lost” at time t by purchasing the asset instead of consumption goods must be matched by a corresponding increase in the (discounted) future utility of the consumption financed by the asset's return. Since the future is uncertain, the individual considers his expectation, conditional on what is known at the time when the choice is made.

We have said nothing about the nature of the asset, so equation (27.13) should hold whatever asset we consider; hence, it is possible to build a system of equations like (27.13) for each asset whose price we observe.

If we are willing to believe that

- the economy as a whole can be represented as a single gigantic and immortal representative individual, and
- the function $U(x) = \frac{x^{\alpha}-1}{\alpha}$ is a faithful representation of the individual's preferences,

then, setting $k = 1$, equation (27.13) implies the following for any asset j :

$$E \left[\delta \frac{r_{j,t+1}}{p_{j,t}} \left(\frac{C_{t+1}}{C_t} \right)^{\alpha-1} \middle| \mathcal{F}_t \right] = 1, \quad (27.14)$$

where C_t is aggregate consumption and α and δ are the risk aversion and discount rate of the representative individual. In this case, it is easy to see that the “deep” parameters α and δ can be estimated via GMM by using

$$e_t = \delta \frac{r_{j,t+1}}{p_{j,t}} \left(\frac{C_{t+1}}{C_t} \right)^{\alpha-1} - 1$$

as the moment condition, while any variable known at time t may serve as an instrument.

In the example code given in 27.4, we replicate selected portions of table 3.7 in Hall (2005). The variable `consrat` is defined as the ratio of monthly consecutive real per capita consumption (services and nondurables) for the US, and `ewr` is the return-price ratio of a fictitious asset constructed by averaging all the stocks in the NYSE. The instrument set contains the constant and two lags of each variable.

The command `set force_hc on` on the second line of the script has the sole purpose of replicating the given example: as mentioned above, it forces `gretl` to compute the long-run variance of the orthogonality conditions according to equation (27.11) rather than (27.12).

We run `gmm` four times: one-step estimation for each of two initial weights matrices, then iterative estimation starting from each set of initial weights. Since the number of orthogonality conditions (5) is greater than the number of estimated parameters (2), the choice of initial weights should make a difference, and indeed we see fairly substantial differences between the one-step estimates (Models 1 and 2). On the other hand, iteration reduces these differences almost to the vanishing point (Models 3 and 4).

Part of the output is given in 27.5. It should be noted that the J test leads to a rejection of the hypothesis of correct specification. This is perhaps not surprising given the heroic assumptions required to move from the microeconomic principle in equation (27.13) to the aggregate system that is actually estimated.

Listing 27.4: Estimation of the Consumption Based Asset Pricing Model [\[Download ▼\]](#)

```

open hall.gdt
set force_hc on

scalar alpha = 0.5
scalar delta = 0.5
series e = 0

list inst = const consrat(-1) consrat(-2) ewr(-1) ewr(-2)

matrix V0 = 100000*I(nelem(inst))
matrix Z = { inst }
matrix V1 = $nobs*inv(Z'Z)

gmm e = delta*ewr*consrat^(alpha-1) - 1
    orthog e ; inst
    weights V0
    params alpha delta
end gmm

gmm e = delta*ewr*consrat^(alpha-1) - 1
    orthog e ; inst
    weights V1
    params alpha delta
end gmm

gmm e = delta*ewr*consrat^(alpha-1) - 1
    orthog e ; inst
    weights V0
    params alpha delta
end gmm --iterate

gmm e = delta*ewr*consrat^(alpha-1) - 1
    orthog e ; inst
    weights V1
    params alpha delta
end gmm --iterate

```

Listing 27.5: Estimation of the Consumption Based Asset Pricing Model – output

Model 1: 1-step GMM estimates using the 465 observations 1959:04-1997:12
 $e = d*ewr*consrat^{(\alpha-1)} - 1$

PARAMETER	ESTIMATE	STDERROR	T STAT	P-VALUE
alpha	-3.14475	6.84439	-0.459	0.64590
d	0.999215	0.0121044	82.549	<0.00001 ***

GMM criterion = 2778.08

Model 2: 1-step GMM estimates using the 465 observations 1959:04-1997:12
 $e = d*ewr*consrat^{(\alpha-1)} - 1$

PARAMETER	ESTIMATE	STDERROR	T STAT	P-VALUE
alpha	0.398194	2.26359	0.176	0.86036
d	0.993180	0.00439367	226.048	<0.00001 ***

GMM criterion = 14.247

Model 3: Iterated GMM estimates using the 465 observations 1959:04-1997:12
 $e = d*ewr*consrat^{(\alpha-1)} - 1$

PARAMETER	ESTIMATE	STDERROR	T STAT	P-VALUE
alpha	-0.344325	2.21458	-0.155	0.87644
d	0.991566	0.00423620	234.070	<0.00001 ***

GMM criterion = 5491.78

J test: Chi-square(3) = 11.8103 (p-value 0.0081)

Model 4: Iterated GMM estimates using the 465 observations 1959:04-1997:12
 $e = d*ewr*consrat^{(\alpha-1)} - 1$

PARAMETER	ESTIMATE	STDERROR	T STAT	P-VALUE
alpha	-0.344315	2.21359	-0.156	0.87639
d	0.991566	0.00423469	234.153	<0.00001 ***

GMM criterion = 5491.78

J test: Chi-square(3) = 11.8103 (p-value 0.0081)

27.7 Caveats

A few words of warning are in order: despite its ingenuity, GMM is possibly the most fragile estimation method in econometrics. The number of non-obvious choices one has to make when using GMM is large, and in finite samples each of these can have dramatic consequences for the eventual output. Some of the factors that may affect the results are:

1. Orthogonality conditions can be written in more than one way: for example, if $E(x_t - \mu) = 0$, then $E(x_t/\mu - 1) = 0$ holds too. It is possible that a different specification of the moment conditions leads to different results.
2. As with all other numerical optimization algorithms, weird things may happen when the objective function is nearly flat in some directions or has multiple minima. BFGS is usually quite good, but there is no guarantee that it always delivers a sensible solution, if one at all.
3. The 1-step and, to a lesser extent, the 2-step estimators may be sensitive to apparently trivial details, like the re-scaling of the instruments. Different choices for the initial weights matrix can also have noticeable consequences.
4. With time-series data, there is no hard rule on the appropriate number of lags to use when computing the long-run covariance matrix (see section 27.5). Our advice is to go by trial and error, since results may be greatly influenced by a poor choice.

One of the consequences of this state of things is that replicating well-known published studies may be extremely difficult. Any non-trivial result is virtually impossible to reproduce unless all details of the estimation procedure are carefully recorded.

Chapter 28

Model selection criteria

28.1 Introduction

In some contexts the econometrician chooses between alternative models based on a formal hypothesis test. For example, one might choose a more general model over a more restricted one if the restriction in question can be formulated as a testable null hypothesis, and the null is rejected on an appropriate test.

In other contexts one sometimes seeks a criterion for model selection that somehow measures the balance between goodness of fit or likelihood, on the one hand, and parsimony on the other. The balancing is necessary because the addition of extra variables to a model cannot reduce the degree of fit or likelihood, and is very likely to increase it somewhat even if the additional variables are not truly relevant to the data-generating process.

The best known such criterion, for linear models estimated via least squares, is the adjusted R^2 ,

$$\bar{R}^2 = 1 - \frac{\text{SSR}/(n - k)}{\text{TSS}/(n - 1)}$$

where n is the number of observations in the sample, k denotes the number of parameters estimated, and SSR and TSS denote the sum of squared residuals and the total sum of squares for the dependent variable, respectively. Compared to the ordinary coefficient of determination or unadjusted R^2 ,

$$R^2 = 1 - \frac{\text{SSR}}{\text{TSS}}$$

the “adjusted” calculation penalizes the inclusion of additional parameters, other things equal.

28.2 Information criteria

A more general criterion in a similar spirit is Akaike’s (1974) “Information Criterion” (AIC). The original formulation of this measure is

$$\text{AIC} = -2\ell(\hat{\theta}) + 2k \quad (28.1)$$

where $\ell(\hat{\theta})$ represents the maximum loglikelihood as a function of the vector of parameter estimates, $\hat{\theta}$, and k (as above) denotes the number of “independently adjusted parameters within the model.” In this formulation, with AIC negatively related to the likelihood and positively related to the number of parameters, the researcher seeks the minimum AIC.

The AIC can be confusing, in that several variants of the calculation are “in circulation.” For example, Davidson and MacKinnon (2004) present a simplified version,

$$\text{AIC} = \ell(\hat{\theta}) - k$$

which is just -2 times the original: in this case, obviously, one wants to maximize AIC.

In the case of models estimated by least squares, the loglikelihood can be written as

$$\ell(\hat{\theta}) = -\frac{n}{2}(1 + \log 2\pi - \log n) - \frac{n}{2} \log \text{SSR} \quad (28.2)$$

Substituting (28.2) into (28.1) we get

$$\text{AIC} = n(1 + \log 2\pi - \log n) + n \log \text{SSR} + 2k$$

which can also be written as

$$\text{AIC} = n \log \left(\frac{\text{SSR}}{n} \right) + 2k + n(1 + \log 2\pi) \quad (28.3)$$

Some authors simplify the formula for the case of models estimated via least squares. For instance, William Greene writes

$$\text{AIC} = \log \left(\frac{\text{SSR}}{n} \right) + \frac{2k}{n} \quad (28.4)$$

This variant can be derived from (28.3) by dividing through by n and subtracting the constant $1 + \log 2\pi$. That is, writing AIC_G for the version given by Greene, we have

$$\text{AIC}_G = \frac{1}{n} \text{AIC} - (1 + \log 2\pi)$$

Finally, Ramanathan gives a further variant:

$$\text{AIC}_R = \left(\frac{\text{SSR}}{n} \right) e^{2k/n}$$

which is the exponential of the one given by Greene.

Gretl began by using the Ramanathan variant, but since version 1.3.1 the program has used the original Akaike formula (28.1), and more specifically (28.3) for models estimated via least squares.

Although the Akaike criterion is designed to favor parsimony, arguably it does not go far enough in that direction. For instance, if we have two nested models with $k - 1$ and k parameters respectively, and if the null hypothesis that parameter k equals 0 is true, in large samples the AIC will nonetheless tend to select the less parsimonious model about 16 percent of the time (see Davidson and MacKinnon, 2004, chapter 15).

An alternative to the AIC which avoids this problem is the Schwarz (1978) “Bayesian information criterion” (BIC). The BIC can be written (in line with Akaike’s formulation of the AIC) as

$$\text{BIC} = -2\ell(\hat{\theta}) + k \log n$$

The multiplication of k by $\log n$ in the BIC means that the penalty for adding extra parameters grows with the sample size. This ensures that, asymptotically, one will not select a larger model over a correctly specified parsimonious model.

A further alternative to AIC, which again tends to select more parsimonious models than AIC, is the Hannan–Quinn criterion or HQC (Hannan and Quinn, 1979). Written consistently with the formulations above, this is

$$\text{HQC} = -2\ell(\hat{\theta}) + 2k \log \log n$$

The Hannan–Quinn calculation is based on the law of the iterated logarithm (note that the last term is the log of the log of the sample size). The authors argue that their procedure provides a “strongly consistent estimation procedure for the order of an autoregression”, and that “compared to other strongly consistent procedures this procedure will underestimate the order to a lesser degree.”

Gretl reports the AIC, BIC and HQC (calculated as explained above) for most sorts of models. The key point in interpreting these values is to know whether they are calculated such that smaller values are better, or such that larger values are better. In gretl, smaller values are better: one wants to minimize the chosen criterion.

Chapter 29

Degrees of freedom correction

29.1 Introduction

This chapter gives a brief account of the issue of correction for degrees of freedom in the context of econometric modeling, leading up to a discussion of the policies adopted in gretl in this regard. We also explain how to supplement the results produced automatically by gretl if you want to apply such a correction where gretl does not, or vice versa.

The first few sections are quite basic; experts are invited to skip to section [29.5](#).

29.2 Back to basics

It's well known that given a sample, $\{x_i\}$, of size n from a normally distributed population, the Maximum Likelihood (ML) estimator of the population variance, σ^2 , is

$$\hat{\sigma}^2 = \frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})^2 \quad (29.1)$$

where \bar{x} is the sample mean, $n^{-1} \sum_{i=1}^n x_i$. It's also well known that $\hat{\sigma}^2$, while it is a consistent estimator, is biased, and it is commonly replaced by the “sample variance”, namely,

$$s^2 = \frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})^2 \quad (29.2)$$

The intuition behind the bias in (29.1) is straightforward. First, the quantity we seek to estimate is defined as

$$\sigma^2 = E[(x_i - \mu)^2]$$

where $\mu = E(x)$. It is clear that if μ were observable, a perfectly good estimator would be

$$\tilde{\sigma}^2 = \frac{1}{n} \sum_{i=1}^n (x_i - \mu)^2.$$

But this is not a practical option: μ is generally unobservable. We therefore substitute \bar{x} for the unknown μ . It is easily shown that \bar{x} is the least-squares estimator of μ , and also (assuming normality) the ML estimator. It is unbiased, but is of course subject to sampling error; in any given sample it is highly unlikely that $\bar{x} = \mu$. Given that \bar{x} is the least-squares estimator, the sum of squared deviations of the x_i from *any* value other than \bar{x} must be greater than the summation in (29.1). But since μ is almost certainly not equal to \bar{x} , the sum of squared deviations of the x_i from μ will surely be greater than the sum of squared deviations in (29.1). It follows that the expected value of $\tilde{\sigma}^2$ falls short of the population variance.

The proof that s^2 is indeed the unbiased estimator can be found in any good statistics textbook, where we also learn that the magnitude $n-1$ in (29.2) can be brought under a general description as the “degrees of freedom” of the calculation at hand. (Given \bar{x} , the n sample values provide only $n-1$ items of information since the n^{th} value can always be deduced via the formula for \bar{x} .)

29.3 Application to OLS regression

The argument above carries over into the usual calculation of standard errors in the context of OLS regression as applied to the linear model $y = X\beta + u$. If the disturbances, u , are assumed to be independently and identically distributed (IID), then the variance of the OLS estimator, $\hat{\beta}$, is given by

$$\text{Var}(\hat{\beta}) = \sigma^2(X'X)^{-1}$$

where σ^2 is the variance of the error term and X is an $n \times k$ matrix of regressors. But how should the unknown σ^2 be estimated? The ML estimator is

$$\hat{\sigma}^2 = \frac{1}{n} \sum_{i=1}^n \hat{u}_i^2 \quad (29.3)$$

where the \hat{u}_i^2 are squared residuals, $u_i = y_i - X_i\beta$. But this estimator is biased and we typically use the unbiased counterpart

$$s^2 = \frac{1}{n-k} \sum_{i=1}^n \hat{u}_i^2 \quad (29.4)$$

in which $n - k$ is the number of degrees of freedom given n residuals from a regression where k parameters are estimated.

The standard estimator of the variance of $\hat{\beta}$ in the context of OLS is then $V = s^2(X'X)^{-1}$. And the standard errors of the individual parameter estimates, $s_{\hat{\beta}_i}$, being the square roots of the diagonal elements of V , inherit a degrees of freedom correction from the estimator s^2 .

Going one step further, consider hypothesis testing in the context of OLS. Since the variance of $\hat{\beta}$ is unknown and must itself be estimated, the sampling distribution of the OLS coefficients is not, strictly speaking, normal. But if the *disturbances* are normally distributed (besides being IID) then, even in small samples, the parameter estimates will follow a distribution that can be specified exactly, namely the Student t distribution with degrees of freedom equal to the value given above, $\nu = n - k$.

That is, besides using a df correction in computing the standard errors of the OLS coefficients, one uses the same ν in selecting the particular distribution to which the “ t -ratio”, $(\hat{\beta}_i - \beta^0)/s_{\hat{\beta}_i}$, should be referred in order to determine the marginal significance level or p -value for the null hypothesis that $\beta_i = \beta^0$. This is the payoff to df correction: we get test statistics that follow a known distribution in small samples. (In big enough samples the point is moot, since the quantitative distinction between $\hat{\sigma}^2$ and s^2 vanishes.)

So far, so good. Everyone expects df correction in plain OLS standard errors just as we expect division by $n - 1$ in the sample variance. And users of econometric software expect that the p -values reported for OLS coefficients will be based on the $t(\nu)$ distribution—although they are not always sufficiently aware that the validity of such statistics in small samples depends on the assumption of normally distributed errors.

29.4 Beyond OLS

The situation is different when we move beyond estimation of the classical linear model via OLS. We may wish to estimate nonlinear models (sometimes by least squares), and many models of interest to econometricians are commonly estimated via maximization of a likelihood function, or via the generalized method of moments (GMM).

In such cases we do not, in general, have exact small-sample results to rely upon; in particular, we cannot assume that coefficient estimates follow the t distribution. Rather, we typically appeal to asymptotic results in statistical theory. We seek *consistent* estimators which, although they may be biased, nonetheless converge in probability to the corresponding parameter values as the sample size goes to infinity. Under the right conditions, laws of large numbers and central limit

theorems entitle us to expect that test statistics will converge to the normal distribution, or the χ^2 distribution for multivariate tests, given big enough samples.

To “correct” or not?

The question arises, should we or should we not apply a df “correction” in reporting variance estimates and standard errors for models that depart from the classical linear specification?

The argument against applying df adjustment is that it lacks a theoretical basis: it does not produce test statistics that follow any known distribution in small samples. In addition, if parameter estimates are obtained via ML, it makes sense to report ML estimates of variances even if these are biased, since it is the ML quantities that are used in computing the criterion function and in forming likelihood-ratio tests.

On the other hand, pragmatic arguments for doing df adjustment are (a) that it makes for closer comparability between regular OLS estimates and nonlinear ones, and (b) that it provides a “pinch of salt” in relation to small-sample results—that is, it inflates standard errors, confidence intervals and p -values somewhat—even if it lacks rigorous justification.

Note that even for fairly small samples, the difference between the biased and unbiased estimators in equations (29.1) and (29.2) above will be small. For example, if $n = 30$ then $s^2 = \frac{30}{29}\hat{\sigma}^2$. In econometric modelling proper, however, the difference can be quite substantial. If $n = 50$ and $k = 10$, the s^2 defined in (29.4) will be $50/40 = 1.25$ as large as the $\hat{\sigma}^2$ in (29.3), and standard errors will be about 12 percent larger.¹ One can make a case for inflating the standard errors obtained via nonlinear estimators as a precaution against taking results to be “more precise than they really are”.

In rejoinder to the last point, one might equally say that savvy econometricians should know to apply a discount factor (albeit an imprecise one) to small-sample estimates outside of the classical, normal linear model—or even that they should distrust such results and insist on large samples before making inferences. This line of thinking suggests that test statistics such as $z = \hat{\beta}_i / \hat{\sigma}_{\hat{\beta}_i}$ should be referred to the distribution to which they conform asymptotically—in this case $N(0, 1)$ for $H_0 : \beta_i = 0$ —if and only if the conditions for appealing to asymptotic results can be considered as met. From this point of view df adjustment may be seen as providing a false sense of security.

29.5 Consistency and awkward cases

Consistency (in the ordinary sense of uniformity of treatment) is a bugbear when dealing with this issue. To give a simple example, suppose an econometrics program follows the policy of applying df correction for OLS estimation but not for ML estimation. One is, of course, free to estimate the classical, normal linear model via ML, in which case $\hat{\beta}$ should be numerically identical to that obtained via OLS. But the user of the software will obtain two different sets of standard errors depending on the estimation method. Admittedly, this example is not very troublesome; presumably one would apply ML to the classical linear model only to make a pedagogical point.

Here is a more awkward case. An unrestricted vector autoregression (VAR) is a system of equations, but the ML estimate of this system, given normal errors, is equivalent to equation-by-equation OLS. Should df correction be applied to VARs? Consistency with OLS argues Yes. However, a popular extension of the VAR methodology is the vector error-correction model (VECM). VECMs are closely related to VARs and one might well be interested in making comparisons across the two, but a VECM is a nonlinear system and the cointegrating vectors that lie at the heart of this model must be estimated via Maximum Likelihood. So perhaps VAR results should *not* be df adjusted, for comparability with VECMs.

¹A fairly typical situation in time-series macroeconometrics would be have between 100 and 200 quarterly observations, and to be estimating up to maybe 30 parameters including lags. In this case df correction would make a difference to standard errors on the order of 10 percent.

Another “grey area” is the class of Feasible Generalized Least Squares (FGLS) estimators—for example, weighted least squares following the estimation of a skedastic function, or estimators designed to handle first-order autocorrelation, such as Cochrane–Orcutt. These depart from the classical linear model, and the theoretical basis for inference in such models is asymptotic, yet according to econometric tradition standard errors are generally df adjusted.

Yet another awkward case: “robust” (heteroskedasticity- and/or autocorrelation-consistent) standard errors in the context of OLS. Such estimators are justified by asymptotic arguments and in general we cannot determine their small-sample distributions. That would argue for referring the associated test statistics to the normal distribution. But comparability with classical standard errors pulls in the other direction. Suppose in a particular case a robust estimator produces a standard error that is numerically indistinguishable from the classical one: if the former is referred to the normal distribution and the latter to the t distribution, switching to robust standard errors will give a smaller p -value for the coefficient in question, making it appear “more significant,” and arguably this is misleading.

29.6 What gretl does

First of all, the third column in gretl model output—following “coefficient” and “std. error”—is labeled either “t-ratio” or “z.” This is your signal: “t-ratio” indicates that the estimated standard error employs a degrees of freedom adjustment and the reported p -value is obtained from the Student t distribution, while “z” indicates that no such adjustment is applied and the p -value comes from the standard normal distribution.

If you see that gretl is applying a df adjustment but you don’t want this, the first point to check is whether you can switch to the asymptotic variant by using an option flag or other command.

- The `ols` and `tsls` commands support a `--no-df-corr` option to suppress degrees of freedom adjustment. In the case of Two-Stage Least Squares it’s certainly arguable that df correction should not be performed by default, however gretl does this, largely for comparability with other software (for example Stata’s `ivreg` command). But you can override the default if you wish.
- The `estimate` command, for systems of equations, also supports the `--no-df-corr` option when the specified estimation method is OLS or TSLS. (For other estimators supported by gretl’s `system` command no df adjustment is applied by default.)
- By default gretl uses the t distribution for statistics based on robust standard errors under OLS. However, users can specify that p -values be calculated using the standard normal distribution whenever the `--robust` option is passed to an estimation command, by means of the following “set” command

```
set robust_z on
```

If these possibilities do not apply, it is fairly straightforward to “purge” regression results of df correction, as illustrated in the following script fragment. We assume that a model has just been estimated, so that the model-related accessors (`$stderr`, `$coeff` and so on) are available.

```
matrix se = $stderr * sqrt($df/$T)
matrix zscore = $coeff ./ se
matrix pv = 2 * pvalue(z, abs(zscore))
matrix M = $coeff ~ se ~ zscore ~ pv
cnameset(M, "coeff stderr z p-value")
print M
```

This will print the original coefficient estimates along with asymptotic standard errors and the associated z -scores and (two-sided) normal p -values. The converse case is left as an exercise for the reader.

VARs

As mentioned above, Vector Autoregressions constitute a particularly awkward case, with considerations of consistency of treatment pulling in two opposite directions. For that reason gretl has adopted an “agnostic” policy in relation to such systems. We do not offer a `$vcv` accessor, but instead accessors named `$xtxin` (the matrix $X'X^{-1}$ for the system as a whole) and `$sigma` (an estimate of the cross-equation variance-covariance matrix, Σ). It's then up to the user to build an estimate of the variance matrix of the parameter estimates—call it V —should that be required.

Note that `$sigma` gives the Maximum Likelihood Estimator (without a degrees of freedom adjustment) so if you do

```
matrix Vml = $sigma ** $xtxin
```

(where “**” represents Kronecker product) you obtain the MLE of the variance matrix of the parameter estimates. But if you want the unbiased estimator you can do

```
matrix S = $sigma * $T/($T-$ncoeff)
matrix Vu = S ** $xtxin
```

to employ a suitably inflated variant of the Σ estimate. (For VARs, and also VECMs, `$ncoeff` gives the number of coefficients per equation.)

The second variant above is such that the vector of standard errors produced by

```
matrix SE = sqrt(diag(Vu))
```

agrees with the standard errors printed as part of the per-equation VAR output.

A fuller example of usage of the `$xtxin` accessor is given in Listing 29.1: this shows how one can replicate the F -tests for Granger causality that are displayed by default by the `var` command, with the refinement that, depending on the setting of the `USE_F` flag, these tests can be done using a small sample correction as in gretl's output or in asymptotic (χ^2) form.

Vector Error Correction Models are more complex than VARs in this respect, since we employ Johansen's variance estimator for the “ β ” terms. This means for example that the `$xtxin` accessor treats each estimated error correction (EC) term as one regressor on its own, such that the sampling uncertainty of the loading coefficients is thereby addressed (after Kronecker-multiplying with `$sigma` as before). The “internals” of the EC terms are of course made up of the integrated (levels) variables, and the special `$jvbeta` accessor is responsible for the variance of the cointegration coefficients, where degrees-of-freedom corrections are not available.

But as soon as the loading coefficients attached to the EC terms are restricted, there is no common set of regressors with freely varying coefficients in the VECM system anymore, and therefore in these cases the formulas above are misleading. The `$xtxin` accessor can still be retrieved (because it does not involve the coefficients), but in the restricted α case it should no longer be used as shown above. The notion of system degrees of freedom then also becomes fuzzier since the number of regressors can vary across equations.

Listing 29.1: Computing statistics to test for Granger causality [\[Download ▼\]](#)

```

open denmark.gdt
list LST = LRM LRY IBO IDE
scalar p = 2 # lags in VAR
scalar USE_F = 1 # small sample correction?

var p LST --quiet

k = nelem(LST)
matrix theta = vec($coeff)
matrix V = $sigma ** $xtxin
if USE_F
    scalar df = $T - $ncoeff
    V *= $T/df
endif

matrix GC = zeros(k, k)
cnameset(GC, LST)
rnameset(GC, LST)

matrix idx = seq(1,p) + 1
loop i = 1..k
    loop j = 1..k
        GC[i,j] = qform(theta[idx]', invpd(V[idx,idx]))
        idx += (j==k)? p+1 : p
    endloop
endloop

if USE_F
    GC /= p
    matrix pvals = pvalue(F, p, df, GC)
else
    matrix pvals = pvalue(X, p, GC)
endif

cnameset(pvals, LST)
rnameset(pvals, LST)
print GC pvals

```

Chapter 30

Time series filters

In addition to the usual application of lags and differences, gretl provides fractional differencing and various filters commonly used in macroeconomics for trend-cycle decomposition: notably the Hodrick–Prescott filter (Hodrick and Prescott, 1997), the Baxter–King bandpass filter (Baxter and King, 1999) and the Butterworth filter (Butterworth, 1930).

30.1 Fractional differencing

The concept of differencing a time series d times is pretty obvious when d is an integer; it may seem odd when d is fractional. However, this idea has a well-defined mathematical content: consider the function

$$f(z) = (1 - z)^{-d},$$

where z and d are real numbers. By taking a Taylor series expansion around $z = 0$, we see that

$$f(z) = 1 + dz + \frac{d(d+1)}{2}z^2 + \dots$$

or, more compactly,

$$f(z) = 1 + \sum_{i=1}^{\infty} \psi_i z^i$$

with

$$\psi_k = \frac{\prod_{i=1}^k (d + i - 1)}{k!} = \psi_{k-1} \frac{d + k - 1}{k}$$

The same expansion can be used with the lag operator, so that if we defined

$$Y_t = (1 - L)^{0.5} X_t$$

this could be considered shorthand for

$$Y_t = X_t - 0.5X_{t-1} - 0.125X_{t-2} - 0.0625X_{t-3} - \dots$$

In gretl this transformation can be accomplished by the syntax

```
Y = fracdiff(X, 0.5)
```

30.2 The Hodrick–Prescott filter

This filter is accessed using the `hpfilt()` function, which takes as its first argument the name of the variable to be processed. (Further optional arguments are explained below.)

A time series y_t may be decomposed into a trend or growth component g_t and a cyclical component c_t .

$$y_t = g_t + c_t, \quad t = 1, 2, \dots, T$$

The Hodrick–Prescott filter effects such a decomposition by minimizing the following:

$$\sum_{t=1}^T (y_t - g_t)^2 + \lambda \sum_{t=2}^{T-1} ((g_{t+1} - g_t) - (g_t - g_{t-1}))^2.$$

The first term above is the sum of squared cyclical components $c_t = y_t - g_t$. The second term is a multiple λ of the sum of squares of the trend component's second differences. This second term penalizes variations in the growth rate of the trend component: the larger the value of λ , the higher is the penalty and hence the smoother the trend series.

Note that the `hpfilt` function in `gretl` produces the cyclical component, c_t , of the original series. If you want the smoothed trend you can subtract the cycle from the original:

```
ct = hpfilt(yt)
gt = yt - ct
```

[Hodrick and Prescott \(1997\)](#) suggest that a value of $\lambda = 1600$ is reasonable for quarterly data. The default value in `gretl` is 100 times the square of the data frequency (which, of course, yields 1600 for quarterly data). The value can be adjusted using an optional second argument to `hpfilt()`, as in

```
ct = hpfilt(yt, 1300)
```

As of version 2018a, the `hpfilt()` function accepts a third, optional Boolean argument. If set to non-zero, what is performed is the so-called *one-sided* version of the filter. See [Section 36.12](#) for further details.

30.3 The Baxter and King filter

This filter is accessed using the `bkfilt()` function, which again takes the name of the variable to be processed as its first argument. The operation of the filter can be controlled via three further optional argument.

Consider the spectral representation of a time series y_t :

$$y_t = \int_{-\pi}^{\pi} e^{i\omega} dZ(\omega)$$

To extract the component of y_t that lies between the frequencies $\underline{\omega}$ and $\overline{\omega}$ one could apply a bandpass filter:

$$c_t^* = \int_{-\pi}^{\pi} F^*(\omega) e^{i\omega} dZ(\omega)$$

where $F^*(\omega) = 1$ for $\underline{\omega} < |\omega| < \overline{\omega}$ and 0 elsewhere. This would imply, in the time domain, applying to the series a filter with an infinite number of coefficients, which is undesirable. The Baxter and King bandpass filter applies to y_t a finite polynomial in the lag operator $A(L)$:

$$c_t = A(L)y_t$$

where $A(L)$ is defined as

$$A(L) = \sum_{i=-k}^k a_i L^i$$

The coefficients a_i are chosen such that $F(\omega) = A(e^{i\omega})A(e^{-i\omega})$ is the best approximation to $F^*(\omega)$ for a given k . Clearly, the higher k the better the approximation is, but since $2k$ observations have to be discarded, a compromise is usually sought. Moreover, the filter has also other appealing

theoretical properties, among which the property that $A(1) = 0$, so a series with a single unit root is made stationary by application of the filter.

In practice, the filter is normally used with monthly or quarterly data to extract the “business cycle” component, namely the component between 6 and 36 quarters. Usual choices for k are 8 or 12 (maybe higher for monthly series). The default values for the frequency bounds are 8 and 32, and the default value for the approximation order, k , is 8. You can adjust these values using the full form of `bkfilt()`, which is

`bkfilt(seriesname, f1, f2, k)`

where $f1$ and $f2$ represent the lower and upper frequency bounds respectively.

30.4 The Butterworth filter

The Butterworth filter ([Butterworth, 1930](#)) is an approximation to an “ideal” square-wave filter. The ideal filter divides the spectrum of a time series into a pass-band (frequencies less than some chosen ω^* for a low-pass filter, or frequencies greater than ω^* for high-pass) and a stop-band; the gain is 1 for the pass-band and 0 for the stop-band. The ideal filter is unattainable in practice since it would require an infinite number of coefficients, but the Butterworth filter offers a remarkably good approximation. This filter is derived and persuasively advocated by [Pollock \(2000\)](#).

For data y , the filtered sequence x is given by

$$x = y - \lambda \Sigma Q (M + \lambda Q' \Sigma Q)^{-1} Q' y \quad (30.1)$$

where

$$\Sigma = \{2I_T - (L_T + L_T^{-1})\}^{T-2} \quad \text{and} \quad M = \{2I_T + (L_T + L_T^{-1})\}^T$$

I_T denotes the identity matrix of order T ; $L_T = [e_1, e_2, \dots, e_{T-1}, 0]$ is the finite-sample matrix version of the lag operator; and Q is defined such that pre-multiplication of a T -vector of data by Q' of order $(T-2) \times T$ produces the second differences of the data. The matrix product

$$Q' \Sigma Q = \{2I_T - (L_T + L_T^{-1})\}^T$$

is a Toeplitz matrix.

The behavior of the Butterworth filter is governed by two parameters: the frequency cutoff ω^* and an integer order, n , which determines the number of coefficients used. The λ that appears in (30.1) is $\tan(\omega^*/2)^{-2n}$. Higher values of n produce a better approximation to the ideal filter in principle (i.e. a sharper cut between the pass-band and the stop-band) but there is a downside: with a greater number of coefficients numerical instability may be an issue, and the influence of the initial values in the sample may be exaggerated.

In `gretl` the Butterworth filter is implemented by the `bwfilt()` function,¹ which takes three arguments: the series to filter, the order n and the frequency cutoff, ω^* , expressed in degrees. The cutoff value must be greater than 0 and less than 180. This function operates as a low-pass filter; for the high-pass variant, subtract the filtered series from the original, as in

```
series bwcycle = y - bwfilt(y, 8, 67)
```

Pollock recommends that the parameters of the Butterworth filter be tuned to the data: one should examine the periodogram of the series in question (possibly after removal of a polynomial trend) in search of a “dead spot” of low power between the frequencies one wishes to exclude and the frequencies one wishes to retain. If ω^* is placed in such a dead spot then the job of separation can be done with a relatively small n , hence avoiding numerical problems. By way of illustration, consider the periodogram for quarterly observations on new cars sales in the US,² 1975:1 to 1990:4 (the upper panel in Figure 30.1).

¹The code for this filter is based on D. S. G. Pollock’s programs IDEOLOG and DETREND. The Pascal source code for

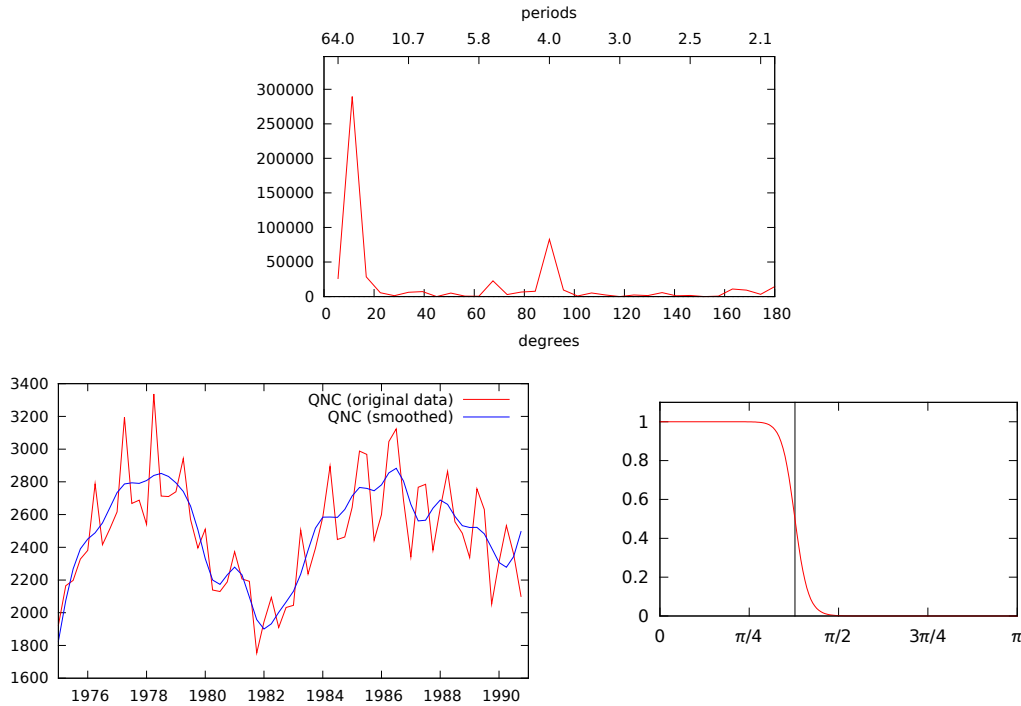


Figure 30.1: The Butterworth filter applied

A seasonal pattern is clearly visible in the periodogram, centered at an angle of 90° or 4 periods. If we set $\omega^* = 68^\circ$ (or thereabouts) we should be able to excise the seasonality quite cleanly using $n = 8$. The result is shown in the lower panel of the Figure, along with the frequency response or gain plot for the chosen filter. Note the smooth and reasonably steep drop-off in gain centered on the nominal cutoff of $68^\circ \approx 3\pi/8$.

The apparatus that supports this sort of analysis in the gretl GUI can be found under the Variable menu in the main window: the items **Periodogram** and **Filter**. In the periodogram dialog box you have the option of expressing the frequency axis in degrees, which is helpful when selecting a Butterworth filter; and in the Butterworth filter dialog you have the option of plotting the frequency response as well as the smoothed series and/or the residual or cycle.

30.5 The discrete Fourier transform

The Fourier transform is not itself a time-series filter, but by providing the bridge between the time and the frequency domain it is a fundamental building block of many filter internals and deserves some detailed comments.

The discrete Fourier transform can be best thought of as a linear, invertible transform of a complex vector. Hence, if \mathbf{x} is an n -dimensional vector whose k -th element is $x_k = a_k + ib_k$, then the output of the discrete Fourier transform is a vector $\mathbf{f} = \mathcal{F}(\mathbf{x})$ whose k -th element is

$$f_k = \sum_{j=0}^{n-1} e^{-i\omega(j,k)} x_j$$

where $\omega(j, k) = 2\pi i \frac{jk}{n}$. Since the transformation is invertible, the vector \mathbf{x} can be recovered from

the former is available from <http://www.le.ac.uk/users/dsgp1> and the C sources for the latter were kindly made available to us by the author.

²This is the variable QNC from the Ramanathan data file data9-7.

\mathbf{f} via the so-called inverse transform

$$x_k = \frac{1}{n} \sum_{j=0}^{n-1} e^{i\omega(j,k)} f_j.$$

The Fourier transform is used in many diverse situations on account of this key property: the convolution of two vectors can be performed efficiently by multiplying the elements of their Fourier transforms and inverting the result. If

$$z_k = \sum_{j=1}^n x_j y_{k-j},$$

then

$$\mathcal{F}(\mathbf{z}) = \mathcal{F}(\mathbf{x}) \odot \mathcal{F}(\mathbf{y}).$$

That is, $\mathcal{F}(\mathbf{z})_k = \mathcal{F}(\mathbf{x})_k \mathcal{F}(\mathbf{y})_k$.

For computing the Fourier transform, gretl uses the external library `fftw3`: see [Frigo and Johnson \(2005\)](#). This guarantees extreme speed and accuracy. In fact, the CPU time needed to perform the transform is $O(n \log n)$ for any n . This is why the array of numerical techniques employed in `fftw3` is commonly known as the *Fast* Fourier Transform.

Gretl provides two matrix functions for performing the Fourier transform and its inverse: `fft` and `ffti`. For example:

```
matrix x1 = { 1 ; 2 ; 3 }
# perform the transform
matrix f = fft(x1)
# perform the inverse transform
matrix x2 = ffti(f)
```

yields

$$x_1 = \begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix} \quad f = \begin{bmatrix} 6 & 0 \\ -1.5 & 0.866 \\ -1.5 & -0.866 \end{bmatrix} \quad x_2 = \begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}$$

Should it be necessary to compute the Fourier transform on several vectors with the same number of elements, it is numerically more efficient to group them into a matrix rather than invoking `fft` for each vector separately.

As an example, consider the multiplication of two polynomials:

$$\begin{aligned} a(x) &= 1 + 0.5x \\ b(x) &= 1 + 0.3x - 0.8x^2 \\ c(x) = a(x) \cdot b(x) &= 1 + 0.8x - 0.65x^2 - 0.4x^3 \end{aligned}$$

The coefficients of the polynomial $c(x)$ are the convolution of the coefficients of $a(x)$ and $b(x)$; the following gretl code fragment illustrates how to compute the coefficients of $c(x)$:

```
# define the two polynomials
a = { 1, 0.5, 0, 0 }'
b = { 1, 0.3, -0.8, 0 }'
# perform the transforms
fa = fft(a)
fb = fft(b)
# multiply the two transforms element by element
fc = fa .* fb
# compute the coefficients of c via the inverse transform
c = ffti(fc)
```

Maximum efficiency would have been achieved by grouping `a` and `b` into a matrix. The computational advantage is so little in this case that the exercise is a bit silly, but the following alternative may be preferable for a large number of rows/columns:

```
# define the two polynomials
a = { 1 ; 0.5; 0 ; 0 }
b = { 1 ; 0.3 ; -0.8 ; 0 }
# perform the transforms jointly
f = fft(a ~ b)
# complex-multiply the two transforms
fc = f[,1] .* f[,2]
# compute the coefficients of c via the inverse transform
c = ffti(fc)
```

Traditionally, the Fourier transform in econometrics has been mostly used in time-series analysis, the periodogram being the best known example. Listing 30.1 shows how to compute the periodogram of a time series via the `fft` function.

Listing 30.1: Periodogram via the Fourier transform [\[Download ▼\]](#)

```
set verbose off
nulldata 50
set seed 76543
# generate an AR(1) process
series e = normal()
series x = 0
x = 0.9*x(-1) + e

# compute the periodogram

F = fft({x}) # note that the series is turned into a matrix on the fly
S = abs(F).^2
S = S[2:($nobs/2)+1] / (2*$pi*$nobs)
sfreq = seq(1,($nobs/2))'
omega = sfreq .* (2*$pi/$nobs)
period = $nobs ./ sfreq
omega = omega ~ sfreq ~ period ~ S

# compare the built-in command
pergm x
print omega
```

Chapter 31

Univariate time series models

31.1 Introduction

Time series models are discussed in this chapter and the next two. Here we concentrate on ARIMA models, unit root tests, and GARCH. The following chapter deals with VARs, and chapter 33 with cointegration and error correction.

31.2 ARIMA models

Representation and syntax

The `arma` command performs estimation of AutoRegressive, Integrated, Moving Average (ARIMA) models. These are models that can be written in the form

$$\phi(L)y_t = \theta(L)\epsilon_t \quad (31.1)$$

where $\phi(L)$, and $\theta(L)$ are polynomials in the lag operator, L , defined such that $L^n x_t = x_{t-n}$, and ϵ_t is a white noise process. The exact content of y_t , of the AR polynomial $\phi()$, and of the MA polynomial $\theta()$, will be explained in the following.

Mean terms

The process y_t as written in equation (31.1) has, without further qualifications, mean zero. If the model is to be applied to real data, it is necessary to include some term to handle the possibility that y_t has non-zero mean. There are two possible ways to represent processes with nonzero mean: one is to define μ_t as the *unconditional* mean of y_t , namely the central value of its marginal distribution. Therefore, the series $\tilde{y}_t = y_t - \mu_t$ has mean 0, and the model (31.1) applies to \tilde{y}_t . In practice, assuming that μ_t is a linear function of some observable variables x_t , the model becomes

$$\phi(L)(y_t - x_t\beta) = \theta(L)\epsilon_t \quad (31.2)$$

This is sometimes known as a “regression model with ARMA errors”; its structure may be more apparent if we represent it using two equations:

$$\begin{aligned} y_t &= x_t\beta + u_t \\ \phi(L)u_t &= \theta(L)\epsilon_t \end{aligned}$$

The model just presented is also sometimes known as “ARMAX” (ARMA + eXogenous variables). It seems to us, however, that this label is more appropriately applied to a different model: another way to include a mean term in (31.1) is to base the representation on the *conditional* mean of y_t , that is the central value of the distribution of y_t *given its own past*. Assuming, again, that this can be represented as a linear combination of some observable variables z_t , the model would expand to

$$\phi(L)y_t = z_t\gamma + \theta(L)\epsilon_t \quad (31.3)$$

The formulation (31.3) has the advantage that γ can be immediately interpreted as the vector of marginal effects of the z_t variables on the conditional mean of y_t . And by adding lags of z_t to

this specification one can estimate *Transfer Function models* (which generalize ARMA by adding the effects of exogenous variable distributed across time).

Gretl provides a way to estimate both forms. Models written as in (31.2) are estimated by maximum likelihood; models written as in (31.3) are estimated by conditional maximum likelihood. (For more on these options see the section on “Estimation” below.)

In the special case when $x_t = z_t = 1$ (that is, the models include a constant but no exogenous variables) the two specifications discussed above reduce to

$$\phi(L)(y_t - \mu) = \theta(L)\epsilon_t \quad (31.4)$$

and

$$\phi(L)y_t = \alpha + \theta(L)\epsilon_t \quad (31.5)$$

respectively. These formulations are essentially equivalent, but if they represent one and the same process μ and α are, fairly obviously, not numerically identical; rather

$$\alpha = (1 - \phi_1 - \dots - \phi_p)\mu$$

The gretl syntax for estimating (31.4) is simply

```
arma p q ; y
```

The AR and MA lag orders, p and q , can be given either as numbers or as pre-defined scalars. The parameter μ can be dropped if necessary by appending the option `--nc` (“no constant”) to the command. If estimation of (31.5) is needed, the switch `--conditional` must be appended to the command, as in

```
arma p q ; y --conditional
```

Generalizing this principle to the estimation of (31.2) or (31.3), you get that

```
arma p q ; y const x1 x2
```

would estimate the following model:

$$y_t - x_t\beta = \phi_1(y_{t-1} - x_{t-1}\beta) + \dots + \phi_p(y_{t-p} - x_{t-p}\beta) + \epsilon_t + \theta_1\epsilon_{t-1} + \dots + \theta_q\epsilon_{t-q}$$

where in this instance $x_t\beta = \beta_0 + x_{t,1}\beta_1 + x_{t,2}\beta_2$. Appending the `--conditional` switch, as in

```
arma p q ; y const x1 x2 --conditional
```

would estimate the following model:

$$y_t = x_t\gamma + \phi_1y_{t-1} + \dots + \phi_py_{t-p} + \epsilon_t + \theta_1\epsilon_{t-1} + \dots + \theta_q\epsilon_{t-q}$$

Ideally, the issue broached above could be made moot by writing a more general specification that nests the alternatives; that is

$$\phi(L)(y_t - x_t\beta) = z_t\gamma + \theta(L)\epsilon_t; \quad (31.6)$$

we would like to generalize the `arma` command so that the user could specify, for any estimation method, whether certain exogenous variables should be treated as x_t s or z_t s, but we’re not yet at that point (and neither are most other software packages).

Seasonal models

A more flexible lag structure is desirable when analyzing time series that display strong seasonal patterns. Model (31.1) can be expanded to

$$\phi(L)\Phi(L^s)y_t = \theta(L)\Theta(L^s)\epsilon_t. \quad (31.7)$$

For such cases, a fuller form of the syntax is available, namely,

```
arma p q ; P Q ; y
```

where p and q represent the non-seasonal AR and MA orders, and P and Q the seasonal orders. For example,

```
arma 1 1 ; 1 1 ; y
```

would be used to estimate the following model:

$$(1 - \phi L)(1 - \Phi L^s)(y_t - \mu) = (1 + \theta L)(1 + \Theta L^s)\epsilon_t$$

If y_t is a quarterly series (and therefore $s = 4$), the above equation can be written more explicitly as

$$y_t - \mu = \phi(y_{t-1} - \mu) + \Phi(y_{t-4} - \mu) - (\phi \cdot \Phi)(y_{t-5} - \mu) + \epsilon_t + \theta\epsilon_{t-1} + \Theta\epsilon_{t-4} + (\theta \cdot \Theta)\epsilon_{t-5}$$

Such a model is known as a “multiplicative seasonal ARMA model”.

Gaps in the lag structure

The standard way to specify an ARMA model in gretl is via the AR and MA orders, p and q respectively. In this case all lags from 1 to the given order are included. In some cases one may wish to include only certain specific AR and/or MA lags. This can be done in either of two ways.

- One can construct a matrix containing the desired lags (positive integer values) and supply the name of this matrix in place of p or q .
- One can give a comma-separated list of lags, enclosed in braces, in place of p or q .

The following code illustrates these options:

```
matrix pvec = {1,4}
arma pvec 1 ; y
arma {1,4} 1 ; y
```

Both forms above specify an ARMA model in which AR lags 1 and 4 are used (but not 2 and 3).

This facility is available only for the non-seasonal component of the ARMA specification.

Differencing and ARIMA

The above discussion presupposes that the time series y_t has already been subjected to all the transformations deemed necessary for ensuring stationarity (see also section 31.3). Differencing is the most common of these transformations, and gretl provides a mechanism to include this step into the `arma` command: the syntax

```
arma p d q ; y
```

would estimate an $\text{ARMA}(p, q)$ model on $\Delta^d y_t$. It is functionally equivalent to

```

series tmp = y
loop i=1..d
    tmp = diff(tmp)
endloop
arma p q ; tmp

```

except with regard to forecasting after estimation (see below).

When the series y_t is differenced before performing the analysis the model is known as ARIMA (“I” for Integrated); for this reason, gretl provides the `arma` command as an alias for `arma`.

Seasonal differencing is handled similarly, with the syntax

```
arma p d q ; P D Q ; y
```

where `D` is the order for seasonal differencing. Thus, the command

```
arma 1 0 0 ; 1 1 1 ; y
```

would produce the same parameter estimates as

```

series dsy = sdiff(y)
arma 1 0 ; 1 1 ; dsy

```

where we use the `sdiff` function to create a seasonal difference (e.g. for quarterly data, $y_t - y_{t-4}$).

In specifying an ARIMA model with exogenous regressors we face a choice which relates back to the discussion of the variant models (31.2) and (31.3) above. If we choose model (31.2), the “regression model with ARMA errors”, how should this be extended to the case of ARIMA? The issue is whether or not the differencing that is applied to the dependent variable should also be applied to the regressors. Consider the simplest case, ARIMA with non-seasonal differencing of order 1. We may estimate either

$$\phi(L)(1-L)(y_t - X_t\beta) = \theta(L)\epsilon_t \quad (31.8)$$

or

$$\phi(L)((1-L)y_t - X_t\beta) = \theta(L)\epsilon_t \quad (31.9)$$

The first of these formulations can be described as a regression model with ARIMA errors, while the second preserves the levels of the X variables. As of gretl version 1.8.6, the default model is (31.8), in which differencing is applied to both y_t and X_t . However, when using the default estimation method (native exact ML, see below), the option `--y-diff-only` may be given, in which case gretl estimates (31.9).¹

Estimation

The default estimation method for ARMA models is exact maximum likelihood estimation (under the assumption that the error term is normally distributed), using a variety of techniques: the main algorithm for evaluating the log-likelihood is AS197 by Melard (1984). Maximization is performed via BFGS and the score is approximated numerically. This method produces results that are directly comparable with many other software packages. The constant, and any exogenous variables, are treated as in equation (31.2). The covariance matrix for the parameters is computed using a numerical approximation to the Hessian at convergence.

The alternative method, invoked with the `--conditional` switch, is conditional maximum likelihood (CML), also known as “conditional sum of squares” (see Hamilton, 1994, p. 132). This method was exemplified in Listing 13.3, and only a brief description will be given here. Given a sample of size T , the CML method minimizes the sum of squared one-step-ahead prediction errors generated

¹Prior to gretl 1.8.6, the default model was (31.9). We changed this for the sake of consistency with other software.

by the model for the observations t_0, \dots, T . The starting point t_0 depends on the orders of the AR polynomials in the model. The numerical maximization method used is BHHH, and the covariance matrix is computed using a Gauss-Newton regression.

The CML method is nearly equivalent to maximum likelihood under the hypothesis of normality; the difference is that the first $(t_0 - 1)$ observations are considered fixed and only enter the likelihood function as conditioning variables. As a consequence, the two methods are asymptotically equivalent under standard conditions—except for the fact, discussed above, that our CML implementation treats the constant and exogenous variables as per equation (31.3).

The two methods can be compared as in the following example

```
open data10-1
arma 1 1 ; r
arma 1 1 ; r --conditional
```

which produces the estimates shown in Table 31.1. As you can see, the estimates of ϕ and θ are quite similar. The reported constants differ widely, as expected—see the discussion following equations (31.4) and (31.5). However, dividing the CML constant by $1 - \phi$ we get 7.38, which is not far from the ML estimate of 6.93.

Table 31.1: ML and CML estimates

Parameter	ML		CML	
μ	6.93042	(0.923882)	1.07322	(0.488661)
ϕ	0.855360	(0.0511842)	0.852772	(0.0450252)
θ	0.588056	(0.0986096)	0.591838	(0.0456662)

Convergence and initialization

The numerical methods used to maximize the likelihood for ARMA models are not guaranteed to converge. Whether or not convergence is achieved, and whether or not the true maximum of the likelihood function is attained, may depend on the starting values for the parameters. Gretl employs one of the following two initialization mechanisms, depending on the specification of the model and the estimation method chosen.

1. Estimate a pure AR model by Least Squares (nonlinear least squares if the model requires it, otherwise OLS). Set the AR parameter values based on this regression and set the MA parameters to a small positive value (0.0001).
2. The Hannan-Rissanen method: First estimate an autoregressive model by OLS and save the residuals. Then in a second OLS pass add appropriate lags of the first-round residuals to the model, to obtain estimates of the MA parameters.

To see the details of the ARMA estimation procedure, add the `--verbose` option to the command. This prints a notice of the initialization method used, as well as the parameter values and log-likelihood at each iteration.

Besides the built-in initialization mechanisms, the user has the option of specifying a set of starting values manually. This is done via the `set` command: the first argument should be the keyword `initvals` and the second should be the name of a pre-specified matrix containing starting values. For example

```
matrix start = { 0, 0.85, 0.34 }
set initvals start
arma 1 1 ; y
```

The specified matrix should have just as many parameters as the model: in the example above there are three parameters, since the model implicitly includes a constant. The constant, if present, is always given first; otherwise the order in which the parameters are expected is the same as the order of specification in the `arma` or `arima` command. In the example the constant is set to zero, ϕ_1 to 0.85, and θ_1 to 0.34.

You can get gretl to revert to automatic initialization via the command `set initvals auto`.

Two variants of the BFGS algorithm are available in gretl. In general we recommend the default variant, which is based on an implementation by Nash (1990), but for some problems the alternative, limited-memory version (L-BFGS-B, see Byrd *et al.*, 1995) may increase the chances of convergence on the ML solution. This can be selected via the `--lbfgs` option to the `arma` command.

Estimation via X-12-ARIMA

As an alternative to estimating ARMA models using “native” code, gretl offers the option of using the external program X-12-ARIMA. This is the seasonal adjustment software produced and maintained by the U.S. Census Bureau; it is used for all official seasonal adjustments at the Bureau. (The current version X13 can also be used, working as a drop-in replacement.)

Gretl includes a module which interfaces with X-12-ARIMA: it translates `arma` commands using the syntax outlined above into a form recognized by X-12-ARIMA, executes the program, and retrieves the results for viewing and further analysis within gretl. To use this facility you have to install X-12-ARIMA separately. Packages for both MS Windows and GNU/Linux are available from the gretl website, <http://gretl.sourceforge.net/>.

To invoke X-12-ARIMA as the estimation engine, append the flag `--x-12-arima`, as in

```
arma p q ; y --x-12-arima
```

As with native estimation, the default is to use exact ML but there is the option of using conditional ML with the `--conditional` flag. However, please note that when X-12-ARIMA is used in conditional ML mode, the comments above regarding the variant treatments of the mean of the process y_t *do not apply*. That is, when you use X-12-ARIMA the model that is estimated is (31.2), regardless of whether estimation is by exact ML or conditional ML. In addition, the treatment of exogenous regressors in the context of ARIMA differencing is always that shown in equation (31.8).

Forecasting

ARMA models are often used for forecasting purposes. The autoregressive component, in particular, offers the possibility of forecasting a process “out of sample” over a substantial time horizon.

Gretl supports forecasting on the basis of ARMA models using the method set out by Box and Jenkins (1976).² The Box and Jenkins algorithm produces a set of integrated AR coefficients which take into account any differencing of the dependent variable (seasonal and/or non-seasonal) in the ARIMA context, thus making it possible to generate a forecast for the level of the original variable. By contrast, if you first difference a series manually and then apply ARMA to the differenced series, forecasts will be for the differenced series, not the level. This point is illustrated in Listing 31.1. The parameter estimates are identical for the two models. The forecasts differ but are mutually consistent: the variable `fcdiff` emulates the ARMA forecast (static, one step ahead within the sample range, and dynamic out of sample).

Lag selection

A variant of the `arma` and `arima` commands is available as an aid to specification. If you give the `--lagselect` option the lag orders p and q —as well as P and Q , if applicable—are taken as

²See in particular their “Program 4” on p. 505ff.

Listing 31.1: ARIMA forecasting [\[Download ▼\]](#)

```

open greene18_2.gdt
# log of quarterly U.S. nominal GNP, 1950:1 to 1983:4
series y = log(Y)
# and its first difference
series dy = diff(y)
# reserve 2 years for out-of-sample forecast
smpl ; 1981:4
# Estimate using ARIMA
arima 1 1 1 ; y
# forecast over full period
smpl --full
fcast fc1
# Return to sub-sample and run ARMA on the first difference of y
smpl ; 1981:4
arma 1 1 ; dy
smpl --full
fcast fc2
series fcdiff = (t<=1982:1)? (fc1 - y(-1)) : (fc1 - fc1(-1))
# compare the forecasts over the later period
smpl 1981:1 1983:4
print y fc1 fc2 fcdiff --byobs

```

The output from the last command is:

	y	fc1	fc2	fcdiff
1981:1	7.964086	7.940930	0.02668	0.02668
1981:2	7.978654	7.997576	0.03349	0.03349
1981:3	8.009463	7.997503	0.01885	0.01885
1981:4	8.015625	8.033695	0.02423	0.02423
1982:1	8.014997	8.029698	0.01407	0.01407
1982:2	8.026562	8.046037	0.01634	0.01634
1982:3	8.032717	8.063636	0.01760	0.01760
1982:4	8.042249	8.081935	0.01830	0.01830
1983:1	8.062685	8.100623	0.01869	0.01869
1983:2	8.091627	8.119528	0.01891	0.01891
1983:3	8.115700	8.138554	0.01903	0.01903
1983:4	8.140811	8.157646	0.01909	0.01909

maxima, and the usual output is replaced by a table showing information criteria and log-likelihood for a range of specifications from zero lags to the maxima. If no seasonal component is given this table has six columns: p and q ; the criteria AIC, BIC and HQC (see Chapter 28); and log-likelihood. In the seasonal case there are eight columns: P and Q are inserted following p and q . Asterisks identify the rows (specifications) on which each information criterion is minimized.

If the input specification includes differencing (non-seasonal and/or seasonal) this is respected but d and D are treated as fixed values rather than maxima. You have the usual choice between exact and conditional ML estimation but the option of using X-12-ARIMA (or X13) is not supported. You also have the usual option of including exogenous regressors (ARMAX).

On successful completion the table of results is available in the form of a matrix via the `$test` accessor. The printed version can be suppressed via the `--quiet` option.

A simple example of usage is shown in Listing 31.2, using annual sunspot data from 1700 to 2021. The table (part of which is elided for brevity) has the three information criteria agreeing on ARMA(4,2) as the optimum among the specifications estimated. The script illustrates how the `$test` matrix can be used to extract the “best” specification.

31.3 Unit root tests

The ADF test

The Augmented Dickey-Fuller (ADF) test is, as implemented in gretl, the t -statistic on φ in the following regression:

$$\Delta y_t = \mu_t + \varphi y_{t-1} + \sum_{i=1}^p \gamma_i \Delta y_{t-i} + \epsilon_t. \quad (31.10)$$

This test statistic is probably the best-known and most widely used unit root test. It is a one-sided test whose null hypothesis is $\varphi = 0$ versus the alternative $\varphi < 0$ (and hence large negative values of the test statistic lead to the rejection of the null). Under the null, y_t must be differenced at least once to achieve stationarity; under the alternative, y_t is already stationary and no differencing is required.

One peculiar aspect of this test is that its limit distribution is non-standard under the null hypothesis: moreover, the shape of the distribution, and consequently the critical values for the test, depends on the form of the μ_t term. A full analysis of the various cases is inappropriate here: [Hamilton \(1994\)](#) contains an excellent discussion, but any recent time series textbook covers this topic. Suffice it to say that gretl allows the user to choose the specification for μ_t among four different alternatives:

μ_t	command option
0	--nc
μ_0	--c
$\mu_0 + \mu_1 t$	--ct
$\mu_0 + \mu_1 t + \mu_1 t^2$	--ctt

These option flags are not mutually exclusive; when they are used together the statistic will be reported separately for each selected case. By default, gretl uses the combination `--c --ct`. For each case, approximate p-values are calculated by means of the algorithm developed in [MacKinnon \(1996\)](#).

The gretl command used to perform the test is `adf`; for example

```
adf 4 x1
```

Listing 31.2: ARMA lag selection [\[Download ▼\]](#)

```

open sunspots.gdt
# ARMA lag selection with maxima of 4 for p and q
arma 4 4 ; sunspots --lagselect
# determine the "best" row per BIC (column 4)
best_row = iminc($test)[4]
# extract this row
spec = $test[best_row,][1:2]
# extract p and q as scalars
scalar p = spec[1]
scalar q = spec[2]
# and estimate the "best" specification
arma p q ; sunspots

```

Part of the lag-selection table:

Estimated using AS 197 (exact ML)
 Dependent variable sunspots, T = 322
 Criteria for ARMA(p, q) specifications

p, q	AIC	BIC	HQC	lnL
<hr/>				
0, 0	3575.2367	3582.7858	3578.2505	-1785.6183
0, 1	3283.7333	3295.0569	3288.2540	-1638.8666
0, 2	3123.6726	3138.7708	3129.7002	-1557.8363
0, 3	3071.8351	3090.7078	3079.3697	-1530.9175
0, 4	3047.0500	3069.6973	3056.0916	-1517.5250
1, 0	3220.3385	3231.6621	3224.8593	-1607.1692
1, 1	3108.4048	3123.5030	3114.4325	-1550.2024
1, 2	3060.3363	3079.2090	3067.8709	-1525.1681
1, 3	3051.2713	3073.9187	3060.3129	-1519.6357
1, 4	3045.1230	3071.5449	3055.6715	-1515.5615
...				
3, 0	3008.6022	3027.4750	3016.1368	-1499.3011
3, 1	3010.5262	3033.1735	3019.5677	-1499.2631
3, 2	2976.3054	3002.7273	2986.8539	-1481.1527
3, 3	2969.6493	2999.8457	2981.7046	-1476.8246
3, 4	2970.5017	3004.4727	2984.0640	-1476.2509
4, 0	3010.5497	3033.1970	3019.5912	-1499.2748
4, 1	3012.3267	3038.7485	3022.8751	-1499.1633
4, 2	2969.5073*	2999.7037*	2981.5626*	-1476.7536
4, 3	2971.2552	3005.2262	2984.8175	-1476.6276
4, 4	2971.1378	3008.8833	2986.2070	-1475.5689

would compute the test statistic as the t -statistic for φ in equation 31.10 with $p = 4$ in the two cases $\mu_t = \mu_0$ and $\mu_t = \mu_0 + \mu_1 t$.

The number of lags (p in equation 31.10) should be chosen as to ensure that (31.10) is a parametrization flexible enough to represent adequately the short-run persistence of Δy_t . Setting p too low results in size distortions in the test, whereas setting p too high leads to low power. As a convenience to the user, the parameter p can be automatically determined. Setting p to a negative number triggers a sequential procedure that starts with p lags and decrements p until the t -statistic for the parameter γ_p exceeds 1.645 in absolute value.

The ADF-GLS test

Elliott, Rothenberg and Stock (1996) proposed a variant of the ADF test which involves an alternative method of handling the parameters pertaining to the deterministic term μ_t : these are estimated first via Generalized Least Squares, and in a second stage an ADF regression is performed using the GLS residuals. This variant offers greater power than the regular ADF test for the cases $\mu_t = \mu_0$ and $\mu_t = \mu_0 + \mu_1 t$.

The ADF-GLS test is available in gretl via the `--gls` option to the `adf` command. When this option is selected the `--nc` and `--ctt` options become unavailable, and only one case can be selected at a time; by default the constant-only model is used but a trend can be added using the `--ct` flag. When a trend is present in this test MacKinnon-type p -values are not available; instead we show critical values from Table 1 in Elliott *et al.* (1996).

The KPSS test

The KPSS test (Kwiatkowski, Phillips, Schmidt and Shin, 1992) is a unit root test in which the null hypothesis is opposite to that in the ADF test: under the null, the series in question is stationary; the alternative is that the series is $I(1)$.

The basic intuition behind this test statistic is very simple: if y_t can be written as $y_t = \mu + u_t$, where u_t is some zero-mean stationary process, then not only does the sample average of the y_t s provide a consistent estimator of μ , but the long-run variance of u_t is a well-defined, finite number. Neither of these properties hold under the alternative.

The test itself is based on the following statistic:

$$\eta = \frac{\sum_{t=1}^T S_t^2}{T^2 \hat{\sigma}^2} \quad (31.11)$$

where $S_t = \sum_{s=1}^t e_s$ and $\hat{\sigma}^2$ is an estimate of the long-run variance of $e_t = (y_t - \bar{y})$. Under the null, this statistic has a well-defined (nonstandard) asymptotic distribution, which is free of nuisance parameters and has been tabulated by simulation. Under the alternative, the statistic diverges.

As a consequence, it is possible to construct a one-sided test based on η , where H_0 is rejected if η is bigger than the appropriate critical value; gretl provides the 90, 95 and 99 percent quantiles. The critical values are computed via the method presented by Sephton (1995), which offers greater accuracy than the values tabulated in Kwiatkowski *et al.* (1992).

Usage example:

```
kpss m y
```

where m is an integer representing the bandwidth or window size used in the formula for estimating the long run variance:

$$\hat{\sigma}^2 = \sum_{i=-m}^m \left(1 - \frac{|i|}{m+1}\right) \hat{\gamma}_i$$

The $\hat{\gamma}_i$ terms denote the empirical autocovariances of e_t from order $-m$ through m . For this estimator to be consistent, m must be large enough to accommodate the short-run persistence of

e_t , but not too large compared to the sample size T . If the supplied m is non-positive a default value is computed, namely the integer part of $4 \left(\frac{T}{100} \right)^{1/4}$.

The above concept can be generalized to the case where y_t is thought to be stationary around a deterministic trend. In this case, formula (31.11) remains unchanged, but the series e_t is defined as the residuals from an OLS regression of y_t on a constant and a linear trend. This second form of the test is obtained by appending the `--trend` option to the `kpss` command:

```
kpss n y --trend
```

Note that in this case the asymptotic distribution of the test is different and the critical values reported by `gretl` differ accordingly.

Panel unit root tests

The most commonly used unit root tests for panel data involve a generalization of the ADF procedure, in which the joint null hypothesis is that a given times series is non-stationary for all individuals in the panel.

In this context the ADF regression (31.10) can be rewritten as

$$\Delta y_{it} = \mu_{it} + \varphi_i y_{i,t-1} + \sum_{j=1}^{p_i} y_{ij} \Delta y_{i,t-j} + \epsilon_{it} \quad (31.12)$$

The model (31.12) allows for maximal heterogeneity across the individuals in the panel: the parameters of the deterministic term, the autoregressive coefficient φ , and the lag order p are all specific to the individual, indexed by i .

One possible modification of this model is to impose the assumption that $\varphi_i = \varphi$ for all i ; that is, the individual time series share a common autoregressive root (although they may differ in respect of other statistical properties). The choice of whether or not to impose this assumption has an important bearing on the hypotheses under test. Under model (31.12) the joint null is $\varphi_i = 0$ for all i , meaning that all the individual time series are non-stationary, and the alternative (simply the negation of the null) is that *at least one* individual time series is stationary. When a common φ is assumed, the null is that $\varphi = 0$ and the alternative is that $\varphi < 0$. The null still says that all the individual series are non-stationary, but the alternative now says that they are *all* stationary. The choice of model should take this point into account, as well as the gain in power from forming a pooled estimate of φ and, of course, the plausibility of assuming a common AR(1) coefficient.³

In `gretl`, the formulation (31.12) is used automatically when the `adf` command is used on panel data. The joint test statistic is formed using the method of [Im, Pesaran and Shin \(2003\)](#). In this context the behavior of `adf` differs from regular time-series data: only one case of the deterministic term is handled per invocation of the command; the default is that μ_{it} includes just a constant but the `--nc` and `--ct` flags can be used to suppress the constant or to include a trend, respectively; and the quadratic trend option `--ctt` is not available.

The alternative that imposes a common value of φ is implemented via the `levinlin` command. The test statistic is computed as per [Levin, Lin and Chu \(2002\)](#). As with the `adf` command, the first argument is the lag order and the second is the name of the series to test; and the default case for the deterministic component is a constant only. The options `--nc` and `--ct` have the same effect as with `adf`. One refinement is that the lag order may be given in either of two forms: if a scalar is given, this is taken to represent a common value of p for all individuals, but you may instead provide a vector holding a set of p_i values, hence allowing the order of autocorrelation of the series to differ by individual. So, for example, given

³If the assumption of a common φ seems excessively restrictive, bear in mind that we routinely assume common slope coefficients when estimating panel models, even if this is unlikely to be literally true.

```
levinlin 2 y
levinlin {2,2,3,3,4,4} y
```

the first command runs a joint ADF test with a common lag order of 2, while the second (which assumes a panel with six individuals) allows for differing short-run dynamics. The first argument to `levinlin` can be given as a set of comma-separated integers enclosed in braces, as shown above, or as the name of an appropriately dimensioned pre-defined matrix (see chapter 17).

Besides variants of the ADF test, the KPSS test also can be used with panel data via the `kpss` command. In this case the test (of the null hypothesis that the given time series is *stationary* for all individuals) is implemented using the method of Choi (2001). This is an application of *meta-analysis*, the statistical technique whereby an overall or composite p-value for the test of a given null hypothesis can be computed from the p-values of a set of separate tests. Unfortunately, in the case of the KPSS test we are limited by the unavailability of precise p-values, although if an individual test statistic falls between the 10 percent and 1 percent critical values we are able to interpolate with a fair degree of confidence. This gives rise to four cases.

1. All the individual KPSS test statistics fall between the 10 percent and 1 percent critical values: the Choi method gives us a plausible composite p-value.
2. Some of the KPSS test statistics exceed the 1 percent value and none fall short of the 10 percent value: we can give an upper bound for the composite p-value by setting the unknown p-values to 0.01.
3. Some of the KPSS test statistics fall short of the 10 percent critical value but none exceed the 1 percent value: we can give a lower bound to the composite p-value by setting the unknown p-values to 0.10.
4. None of the above conditions are satisfied: the Choi method fails to produce any result for the composite KPSS test.

31.4 Cointegration test

The generally recommended test for cointegration is the Johansen test, which is discussed in detail in chapter 33. In this context we just offer a few remarks on the cointegration test of Engle and Granger (1987), because it builds on the univariate ADF test discussed above (section 31.3).

For the Engle–Granger test, the procedure is:

1. Test each series for a unit root using an ADF test.
2. Run a “cointegrating regression” via OLS. For this we select one of the potentially cointegrated variables as dependent, and include the other potentially cointegrated variables as regressors.
3. Perform an ADF test on the residuals from the cointegrating regression.

The idea is that cointegration is supported if (a) the null of non-stationarity is *not* rejected for each of the series individually, in step 1, while (b) the null *is* rejected for the residuals at step 3. That is, each of the individual series is $I(1)$ but some linear combination of the series is $I(0)$.

This test is implemented in gretl by the `coint` command, which requires an integer lag order (for the ADF tests) followed by a list of variables to be tested, the first of which will be taken as dependent in the cointegrating regression. Please see the online help for `coint`, or the *Gretl Command Reference*, for further details.

31.5 ARCH and GARCH

Heteroskedasticity means a non-constant variance of the error term in a regression model. Autoregressive Conditional Heteroskedasticity (ARCH) is a phenomenon specific to time series models, whereby the variance of the error displays autoregressive behavior; for instance, the time series exhibits successive periods where the error variance is relatively large, and successive periods where it is relatively small. This sort of behavior is reckoned to be common in asset markets: an unsettling piece of news can lead to a period of increased volatility in the market.

An ARCH error process of order q can be represented as

$$u_t = \sigma_t \varepsilon_t; \quad \sigma_t^2 \equiv E(u_t^2 | \Omega_{t-1}) = \alpha_0 + \sum_{i=1}^q \alpha_i u_{t-i}^2$$

where the ε_t s are independently and identically distributed (iid) with mean zero and variance 1, and where σ_t is taken to be the positive square root of σ_t^2 . Ω_{t-1} denotes the information set as of time $t-1$ and σ_t^2 is the conditional variance: that is, the variance conditional on information dated $t-1$ and earlier.

It is important to notice the difference between ARCH and an ordinary autoregressive error process. The simplest (first-order) case of the latter can be written as

$$u_t = \rho u_{t-1} + \varepsilon_t; \quad -1 < \rho < 1$$

where the ε_t s are independently and identically distributed with mean zero and variance σ^2 . With an AR(1) error, if ρ is positive then a positive value of u_t will tend to be followed by a positive u_{t+1} . With an ARCH error process, a disturbance u_t of large absolute value will tend to be followed by further large absolute values, but with no presumption that the successive values will be of the same sign. ARCH in asset prices is a “stylized fact” and is consistent with market efficiency; on the other hand autoregressive behavior of asset prices would violate market efficiency.

One can test for ARCH of order q in the following way:

1. Estimate the model of interest via OLS and save the squared residuals, \hat{u}_t^2 .
2. Perform an auxiliary regression in which the current squared residual is regressed on a constant and q lags of itself.
3. Find the TR^2 value (sample size times unadjusted R^2) for the auxiliary regression.
4. Refer the TR^2 value to the χ^2 distribution with q degrees of freedom, and if the p-value is “small enough” reject the null hypothesis of homoskedasticity in favor of the alternative of ARCH(q).

This test is implemented in gretl via the `modtest` command with the `--arch` option, which must follow estimation of a time-series model by OLS (either a single-equation model or a VAR). For example,

```
ols y 0 x
modtest 4 --arch
```

This example specifies an ARCH order of $q = 4$; if the order argument is omitted, q is set equal to the periodicity of the data. In the graphical interface, the ARCH test is accessible from the “Tests” menu in the model window (again, for single-equation OLS or VARs).

GARCH

The simple ARCH(q) process is useful for introducing the general concept of conditional heteroskedasticity in time series, but it has been found to be insufficient in empirical work. The

dynamics of the error variance permitted by ARCH(q) are not rich enough to represent the patterns found in financial data. The generalized ARCH or GARCH model is now more widely used.

The representation of the variance of a process in the GARCH model is somewhat (but not exactly) analogous to the ARMA representation of the level of a time series. The variance at time t is allowed to depend on both past values of the variance and past values of the realized squared disturbance, as shown in the following system of equations:

$$y_t = X_t \beta + u_t \quad (31.13)$$

$$u_t = \sigma_t \varepsilon_t \quad (31.14)$$

$$\sigma_t^2 = \alpha_0 + \sum_{i=1}^q \alpha_i u_{t-i}^2 + \sum_{j=1}^p \delta_j \sigma_{t-j}^2 \quad (31.15)$$

As above, ε_t is an iid sequence with unit variance. X_t is a matrix of regressors (or in the simplest case, just a vector of 1s allowing for a non-zero mean of y_t). Note that if $p = 0$, GARCH collapses to ARCH(q): the generalization is embodied in the δ_j terms that multiply previous values of the error variance.

In principle the underlying innovation, ε_t , could follow any suitable probability distribution, and besides the obvious candidate of the normal or Gaussian distribution the Student's t distribution has been used in this context. Currently gretl only handles the case where ε_t is assumed to be Gaussian. However, when the `--robust` option to the `garch` command is given, the estimator gretl uses for the covariance matrix can be considered Quasi-Maximum Likelihood even with non-normal disturbances. See below for more on the options regarding the GARCH covariance matrix.

Example:

```
garch p q ; y const x
```

where $p \geq 0$ and $q > 0$ denote the respective lag orders as shown in equation (31.15). These values can be supplied in numerical form or as the names of pre-defined scalar variables.

GARCH estimation

Estimation of the parameters of a GARCH model is by no means a straightforward task. (Consider equation 31.15: the conditional variance at any point in time, σ_t^2 , depends on the conditional variance in earlier periods, but σ_t^2 is not observed, and must be inferred by some sort of Maximum Likelihood procedure.) By default gretl uses native code that employs the BFGS maximizer; you also have the option (activated by the `--fcp` command-line switch) of using the method proposed by Fiorentini *et al.* (1996),⁴ which was adopted as a benchmark in the study of GARCH results by McCullough and Renfro (1998). It employs analytical first and second derivatives of the log-likelihood, and uses a mixed-gradient algorithm, exploiting the information matrix in the early iterations and then switching to the Hessian in the neighborhood of the maximum likelihood. (This progress can be observed if you append the `--verbose` option to gretl's `garch` command.)

Several options are available for computing the covariance matrix of the parameter estimates in connection with the `garch` command. At a first level, one can choose between a “standard” and a “robust” estimator. By default, the Hessian is used unless the `--robust` option is given, in which case the QML estimator is used. A finer choice is available via the `set` command, as shown in Table 31.2.

It is not uncommon, when one estimates a GARCH model for an arbitrary time series, to find that the iterative calculation of the estimates fails to converge. For the GARCH model to make sense, there are strong restrictions on the admissible parameter values, and it is not always the case that there exists a set of values inside the admissible parameter space for which the likelihood is maximized.

⁴The algorithm is based on Fortran code deposited in the archive of the *Journal of Applied Econometrics* by the authors, and is used by kind permission of Professor Fiorentini.

Table 31.2: Options for the GARCH covariance matrix

<i>command</i>	<i>effect</i>
set garch_vcv hessian	Use the Hessian
set garch_vcv im	Use the Information Matrix
set garch_vcv op	Use the Outer Product of the Gradient
set garch_vcv qml	QML estimator
set garch_vcv bw	Bollerslev-Wooldridge “sandwich” estimator

The restrictions in question can be explained by reference to the simplest (and much the most common) instance of the GARCH model, where $p = q = 1$. In the GARCH(1, 1) model the conditional variance is

$$\sigma_t^2 = \alpha_0 + \alpha_1 u_{t-1}^2 + \delta_1 \sigma_{t-1}^2 \quad (31.16)$$

Taking the unconditional expectation of (31.16) we get

$$\sigma^2 = \alpha_0 + \alpha_1 \sigma^2 + \delta_1 \sigma^2$$

so that

$$\sigma^2 = \frac{\alpha_0}{1 - \alpha_1 - \delta_1}$$

For this unconditional variance to exist, we require that $\alpha_1 + \delta_1 < 1$, and for it to be positive we require that $\alpha_0 > 0$.

A common reason for non-convergence of GARCH estimates (that is, a common reason for the non-existence of α_i and δ_i values that satisfy the above requirements and at the same time maximize the likelihood of the data) is misspecification of the model. It is important to realize that GARCH, in itself, allows *only* for time-varying volatility in the data. If the *mean* of the series in question is not constant, or if the error process is not only heteroskedastic but also autoregressive, it is necessary to take this into account when formulating an appropriate model. For example, it may be necessary to take the first difference of the variable in question and/or to add suitable regressors, X_t , as in (31.13).

Chapter 32

Vector Autoregressions

Gretl provides a standard set of procedures for dealing with the multivariate time-series models known as VARs (*Vector AutoRegression*). More general models—such as VARMA, nonlinear models or multivariate GARCH models—are not provided as of now, although it is entirely possible to estimate them by writing custom procedures in the gretl scripting language. In this chapter, we will briefly review gretl’s VAR toolbox.

32.1 Notation

A VAR is a structure whose aim is to model the time persistence of a vector of n time series, y_t , via a multivariate autoregression, as in

$$y_t = A_1 y_{t-1} + A_2 y_{t-2} + \cdots + A_p y_{t-p} + Bx_t + \epsilon_t \quad (32.1)$$

The number of lags p is called the *order* of the VAR. The vector x_t , if present, contains a set of exogenous variables, often including a constant, possibly with a time trend and seasonal dummies. The vector ϵ_t is typically assumed to be a vector white noise, with covariance matrix Σ .

Equation (32.1) can be written more compactly as

$$A(L)y_t = Bx_t + \epsilon_t \quad (32.2)$$

where $A(L)$ is a matrix polynomial in the lag operator, or as

$$\begin{bmatrix} y_t \\ y_{t-1} \\ \vdots \\ y_{t-p+1} \end{bmatrix} = \mathbf{A} \begin{bmatrix} y_{t-1} \\ y_{t-2} \\ \vdots \\ y_{t-p} \end{bmatrix} + \begin{bmatrix} B \\ 0 \\ \vdots \\ 0 \end{bmatrix} x_t + \begin{bmatrix} \epsilon_t \\ 0 \\ \vdots \\ 0 \end{bmatrix} \quad (32.3)$$

The matrix \mathbf{A} is known as the “companion matrix” and equals

$$\mathbf{A} = \begin{bmatrix} A_1 & A_2 & \cdots & A_p \\ I & 0 & \cdots & 0 \\ 0 & I & \cdots & 0 \\ \vdots & \vdots & \ddots & \vdots \end{bmatrix}$$

Equation (32.3) is known as the “companion form” of the VAR.

Another representation of interest is the so-called “VMA representation”, which is written in terms of an infinite series of matrices Θ_i defined as

$$\Theta_i = \frac{\partial y_t}{\partial \epsilon_{t-i}} \quad (32.4)$$

The Θ_i matrices may be derived by recursive substitution in equation (32.1): for example, assuming for simplicity that $B = 0$ and $p = 1$, equation (32.1) would become

$$y_t = Ay_{t-1} + \epsilon_t$$

which could be rewritten as

$$y_t = A^{n+1}y_{t-n-1} + \epsilon_t + A\epsilon_{t-1} + A^2\epsilon_{t-2} + \cdots + A^n\epsilon_{t-n}$$

In this case $\Theta_i = A^i$. In general, it is possible to compute Θ_i as the $n \times n$ north-west block of the i -th power of the companion matrix A (so Θ_0 is always an identity matrix).

The VAR is said to be *stable* if all the eigenvalues of the companion matrix A are smaller than 1 in absolute value, or equivalently, if the matrix polynomial $A(L)$ in equation (32.2) is such that $|A(z)| = 0$ implies $|z| > 1$. If this is the case, $\lim_{n \rightarrow \infty} \Theta_n = 0$ and the vector y_t is stationary; as a consequence, the equation

$$y_t - E(y_t) = \sum_{i=0}^{\infty} \Theta_i \epsilon_{t-i} \quad (32.5)$$

is a legitimate Wold representation.

If the VAR is not stable, then the inferential procedures that are called for become somewhat more specialized, except for some simple cases. In particular, if the number of eigenvalues of A with modulus 1 is between 1 and $n - 1$, the canonical tool to deal with these models is the cointegrated VAR model, discussed in chapter 33.

32.2 Estimation

The `gretl` command for estimating a VAR is `var` which, in the command line interface, is invoked in the following manner:

```
[ modelname <- ] var p Ylist [; Xlist]
```

where `p` is a scalar (the VAR order) and `Ylist` is a list of variables specifying the content of y_t . The optional `Xlist` argument can be used to specify a set of exogenous variables. If this argument is omitted, the vector x_t is taken to contain a constant (only); if present, it must be separated from `Ylist` by a semicolon. Note, however, that a few common choices can be obtained in a simpler way: the options `--trend` and `--seasonals` call for inclusion of a linear trend and a set of seasonal dummies respectively. In addition the `--nc` option (no constant) can be used to suppress the standard inclusion of a constant.

The “<-” construct can be used to store the model under a name (see section 3.2), if so desired. To estimate a VAR using the graphical interface, choose “Time Series, Vector Autoregression”, under the Model menu.

The parameters in eq. (32.1) are typically free from restrictions, which implies that multivariate OLS provides a consistent and asymptotically efficient estimator of all the parameters.¹ Given the simplicity of OLS, this is what every software package, including `gretl`, uses; example script 32.1 exemplifies the fact that the `var` command gives you exactly the output you would have from a battery of OLS regressions. The advantage of using the dedicated command is that, after estimation is done, it makes it much easier to access certain quantities and manage certain tasks. For example, the `$coeff` accessor returns the estimated coefficients as a matrix with n columns and `$sigma` returns an estimate of the matrix Σ , the covariance matrix of ϵ_t .

Moreover, for each variable in the system an F test is automatically performed, in which the null hypothesis is that no lags of variable j are significant in the equation for variable i . This is commonly known as a **Granger causality** test.

In addition, two accessors become available for the companion matrix (`$compan`) and the VMA representation (`$vma`). The latter deserves a detailed description: since the VMA representation (32.5) is of infinite order, `gretl` defines a *horizon* up to which the Θ_i matrices are computed automatically.

¹In fact, under normality of ϵ_t OLS is indeed the conditional ML estimator. You may want to use other methods if you need to estimate a VAR in which some parameters are constrained.

Listing 32.1: Estimation of a VAR via OLS [\[Download ▼\]](#)

```

open sw_ch14.gdt
series infl = 400*sdiff(log(PUNEW))

scalar p = 2
list X = LHUR infl
list Xlag = lags(p,X)

loop foreach i X
    ols $i const Xlag
endloop

var p X

```

Output (selected portions):

Model 1: OLS, using observations 1960:3-1999:4 (T = 158)
 Dependent variable: LHUR

	coefficient	std. error	t-ratio	p-value	
const	0.113673	0.0875210	1.299	0.1960	
LHUR_1	1.54297	0.0680518	22.67	8.78e-51	***
LHUR_2	-0.583104	0.0645879	-9.028	7.00e-16	***
infl_1	0.0219040	0.00874581	2.505	0.0133	**
infl_2	-0.0148408	0.00920536	-1.612	0.1090	

Mean dependent var	6.019198	S.D. dependent var	1.502549
Sum squared resid	8.654176	S.E. of regression	0.237830

...

VAR system, lag order 2
 OLS estimates, observations 1960:3-1999:4 (T = 158)
 Log-likelihood = -322.73663
 Determinant of covariance matrix = 0.20382769
 AIC = 4.2119
 BIC = 4.4057
 HQC = 4.2906
 Portmanteau test: LB(39) = 226.984, df = 148 [0.0000]

Equation 1: LHUR

	coefficient	std. error	t-ratio	p-value	
const	0.113673	0.0875210	1.299	0.1960	
LHUR_1	1.54297	0.0680518	22.67	8.78e-51	***
LHUR_2	-0.583104	0.0645879	-9.028	7.00e-16	***
infl_1	0.0219040	0.00874581	2.505	0.0133	**
infl_2	-0.0148408	0.00920536	-1.612	0.1090	

Mean dependent var	6.019198	S.D. dependent var	1.502549
Sum squared resid	8.654176	S.E. of regression	0.237830

Periodicity	horizon
Quarterly	20 (5 years)
Monthly	24 (2 years)
Daily	3 weeks
All other cases	10

Table 32.1: VMA horizon as a function of the dataset periodicity

By default, this is a function of the periodicity of the data (see table 32.1), but it can be set by the user to any desired value via the `set` command with the `horizon` parameter, as in

```
set horizon 30
```

Calling the horizon h , the `$vma` accessor returns an $(h + 1) \times n^2$ matrix, in which the $(i + 1)$ -th row is the vectorized form of Θ_i .

VAR lag-order selection

In order to help the user choose the most appropriate VAR order, `gretl` provides a special variant of the `var` command:

```
var p Ylist [Xlist] --lagselect
```

When the `--lagselect` option is given, estimation is performed for all lags up to p and a table is printed: it displays, for each order, a Likelihood Ratio test for the order p versus $p - 1$, plus an array of information criteria (see chapter 28). For each information criterion in the table, a star indicates what appears to be the “best” choice. The same output can be obtained through the graphical interface via the “Time Series, VAR lag selection” entry under the Model menu.

Warning: in finite samples the choice of the maximum lag, p , may affect the outcome of the procedure. *This is not a bug*, but rather an unavoidable side effect of the way these comparisons should be made. If your sample contains T observations and you invoke the lag selection procedure with maximum order p , `gretl` examines all VARs of order ranging from 1 to p , estimated on a uniform sample of $T - p$ observations. In other words, the comparison procedure does not use all the available data when estimating VARs of order less than p , so as to ensure that all the models in the comparison are estimated on the same data range. Choosing a different value of p may therefore alter the results, although this is unlikely to happen if your sample size is reasonably large.

An example of this unpleasant phenomenon is given in example script 32.2. As can be seen, according to the Hannan-Quinn criterion, order 2 seems preferable to order 1 if the maximum tested order is 4, but the situation is reversed if the maximum tested order is 6.

32.3 Structural VARs

`Gretl`’s built-in `var` command does not support the general class of models known as “Structural VARs”—though it does support the Cholesky decomposition-based approach, the classic and most popular structural VAR variant. If you wish to go beyond that there is a `gretl` “addon” named `SVAR` which will likely meet your needs. `SVAR` is supplied as part of the `gretl` package, you can find its documentation (which is quite detailed) as follows: under the Tools menu in the `gretl` main window, go to “Function packages/On local machine.” (Or use the “*fx*” button on the toolbar at the foot of the main window.) In the function packages window either scroll down or use the search box to find `SVAR`. Then right-click and select “Info.” This opens a window which gives basic information on the package, including a link to `SVAR.pdf`, the full documentation.

The remainder of this section will thus only deal with the Cholesky-based recursive shock identification used by the native `var` command.

Listing 32.2: VAR lag selection via Information Criteria

```
open denmark
list Y = 1 2 3 4
var 4 Y --lagselect
var 6 Y --lagselect
```

Output (selected portions):

VAR system, maximum lag order 4

The asterisks below indicate the best (that is, minimized) values of the respective information criteria, AIC = Akaike criterion, BIC = Schwarz Bayesian criterion and HQC = Hannan-Quinn criterion.

lags	loglik	p(LR)	AIC	BIC	HQC
1	609.15315		-23.104045	-22.346466*	-22.814552
2	631.70153	0.00013	-23.360844*	-21.997203	-22.839757*
3	642.38574	0.16478	-23.152382	-21.182677	-22.399699
4	653.22564	0.15383	-22.950025	-20.374257	-21.965748

VAR system, maximum lag order 6

The asterisks below indicate the best (that is, minimized) values of the respective information criteria, AIC = Akaike criterion, BIC = Schwarz Bayesian criterion and HQC = Hannan-Quinn criterion.

lags	loglik	p(LR)	AIC	BIC	HQC
1	594.38410		-23.444249	-22.672078*	-23.151288*
2	615.43480	0.00038	-23.650400*	-22.260491	-23.123070
3	624.97613	0.26440	-23.386781	-21.379135	-22.625083
4	636.03766	0.13926	-23.185210	-20.559827	-22.189144
5	658.36014	0.00016	-23.443271	-20.200150	-22.212836
6	669.88472	0.11243	-23.260601	-19.399743	-21.795797

IRF and FEVD

Assume that the disturbance in equation (32.1) can be thought of as a linear function of a vector of *structural shocks* u_t , which are assumed to have unit variance and to be mutually uncorrelated, so $V(u_t) = I$. If $\epsilon_t = Ku_t$, it follows that $\Sigma = V(\epsilon_t) = KK'$.

The main object of interest in this setting is the sequence of matrices

$$C_k = \frac{\partial y_t}{\partial u_{t-k}} = \Theta_k K, \quad (32.6)$$

known as the structural VMA representation. From the C_k matrices defined in equation (32.6) two quantities of interest may be derived: the **Impulse Response Function** (IRF) and the **Forecast Error Variance Decomposition** (FEVD).

The IRF of variable i to shock j is simply the sequence of the elements in row i and column j of the C_k matrices. In symbols:

$$I_{i,j,k} = \frac{\partial y_{i,t}}{\partial u_{j,t-k}}$$

As a rule, Impulse Response Functions are plotted as a function of k , and are interpreted as the effect that a shock has on an observable variable through time. Of course, what we observe are the estimated IRFs, so it is natural to endow them with confidence intervals: following common practice, gretl computes the confidence intervals by using the bootstrap;² details are given later in this section.

Another quantity of interest that may be computed from the structural VMA representation is the Forecast Error Variance Decomposition (FEVD). The forecast error variance after h steps is given by

$$\Omega_h = \sum_{k=0}^h C_k C_k'$$

hence the variance for variable i is

$$\omega_i^2 = [\Omega_h]_{i,i} = \sum_{k=0}^h \text{diag}(C_k C_k')_i = \sum_{k=0}^h \sum_{l=1}^n ({}_k c_{i,l})^2$$

where ${}_k c_{i,l}$ is, trivially, the i, l element of C_k . As a consequence, the share of uncertainty on variable i that can be attributed to the j -th shock after h periods equals

$$\mathcal{VD}_{i,j,h} = \frac{\sum_{k=0}^h ({}_k c_{i,j})^2}{\sum_{k=0}^h \sum_{l=1}^n ({}_k c_{i,l})^2}.$$

This makes it possible to quantify which shocks are most important to determine a certain variable in the short and/or in the long run.

Triangularization

The formula 32.6 takes K as known, while of course it has to be estimated. The estimation problem has been the subject of an enormous body of literature we will not even attempt to summarize here: see for example (Lütkepohl, 2005, chapter 9).

Suffice it to say that the most popular choice dates back to Sims (1980), and consists in assuming that K is lower triangular, so its estimate is simply the Cholesky decomposition of the estimate of Σ . The main consequence of this choice is that the ordering of variables within the vector y_t becomes meaningful: since K is also the matrix of Impulse Response Functions at lag 0, the triangularity

²It is possible, in principle, to compute analytical confidence intervals via an asymptotic approximation, but this is not a very popular choice: asymptotic formulae are known to often give a very poor approximation of the finite-sample properties.

assumption means that the first variable in the ordering responds instantaneously only to shock number 1, the second one only to shocks 1 and 2, and so forth. For this reason, each variable is thought to “own” one shock: variable 1 owns shock number 1, and so on.

In this sort of exercise, therefore, the ordering of the y variables is important. To put it differently, if variable `foo` comes before variable `bar` in the Y list, it follows that the shock owned by `foo` affects `bar` instantaneously, but not vice versa.

Impulse Response Functions and the FEVD can be printed out via the command line interface by using the `--impulse-responses` and `--variance-decomp` options, respectively. If you need to store them into matrices, you could compute the structural VMA and proceed from there. For example, the following code snippet shows you how to manually compute a matrix containing the IRFs:

```
open denmark
list Y = 1 2 3 4
scalar n = nelem(Y)
var 2 Y --quiet --impulse-responses

matrix K = cholesky($sigma)
matrix V = $vma
matrix IRF = V * (K ** I(n))
print IRF
```

in which the equality

$$\text{vec}(C_k) = \text{vec}(\Theta_k K) = (K' \otimes I) \text{vec}(\Theta_k)$$

was used.

A more convenient way of obtaining the desired quantities is to use the `irf` and `fevd` functions which can be used in scripts after a VAR (or VECM, see the next chapter) has been estimated. In these functions you must specify the number of the responding (target) variable and the number of the analyzed shock to get the corresponding results as a column vector. The choice of how many periods should be calculated –and thus how long the result vector will be– is determined by previously invoking `set horizon x`, where x is a non-negative integer and the first response concerns the impact effect. As always, it is recommended to consult the function reference under the help menu, where in the case of the `irf` function it is also explained that the implicit shock size is such that the impact response in the same equation is one standard deviation (of the corresponding error term).

IRF bootstrap

The IRFs obtained above are estimates and as such they are uncertain. Mostly due to the fact that they are nonlinear functions of the VAR parameters the standard way of assessing this estimation uncertainty and to derive confidence intervals or bands is to use a bootstrap approach. Again, more advanced options are available with the `SVAR` addon, but the `irf` function used after the built-in `var` (or `vecm`) command also provides the option to run a bootstrap based on resampling from the residuals. (The number of bootstrap iterations can be adjusted through `set boot_iters x`, where x must be larger than 499.) The desired nominal confidence level must be specified after the target and shock numbers as the third argument, and in that case the return vector becomes a three-column matrix where the lower and upper bounds of the confidence intervals are given in the extra two columns.

Menu-driven usage

Almost all the functionality related to the described (recursively identified) structural VARs is also available under the menus in the model window that appears after a VAR is estimated in the GUI.³

³Note that you cannot directly invoke the `SVAR` addon from the model window of an estimated VAR; that menu entry is only present in gretl's *main* window under the Model menu and multivariate time series sub-menu.

- In the “Plots” menu there are a number of menu entries relating to the impulse responses as well as one entry for the forecast error variance decomposition. Selecting any of these will bring up a little specification window where the ordering for the Cholesky decomposition must be chosen, and in case of IRFs the intended bootstrap coverage can be set.
- In the “Analysis” menu there are also entries for IRF and FEVD, which may sometimes be a little confusing. The point is that here the numbers (of the point estimates) will be printed out in a tabular format instead of being plotted.

32.4 Residual-based diagnostic tests

Three diagnostic tests based on residuals are available after estimating a VAR—for normality, autocorrelation and ARCH (Autoregressive Conditional Heteroskedasticity). These are implemented by the `modtest` command, using the options `--normality`, `--autocorr` and `--arch`, respectively.

The (multivariate) normality test is that of [Doornik and Hansen \(1994\)](#); it is based on the skewness and kurtosis of the VAR residuals.

The autocorrelation and ARCH test are also by default multivariate; they are described in detail by [Lütkepohl \(2005\)](#) (see sections 4.4.4 and 16.5.1). Both tests are of the LM type, although the autocorrelation test statistic is referred to a Rao F distribution ([Rao, 1973](#)). These tests may involve estimation of a large number of parameters, depending on the lag horizon chosen, and can fail for lack of degrees of freedom in small samples. As a fallback, the `--univariate` option can be used to specify that the tests be run per-equation rather than in multivariate mode.

Listing 32.3 illustrates the VAR autocorrelation tests, replicating an example given by [Lütkepohl \(2005, p. 174\)](#). Note the difference in the interpretation of the `order` argument to `modtest` with the `--autocorr` option (this also applies to the ARCH test): in the multivariate version `order` is taken as the *maximum* lag order and tests are run from lag 1 up to the maximum; but in the univariate version a single test is run for each equation using just the specified lag order. The example also exposes what exactly is returned by the `$test` and `$pvalue` accessors in the two variants.

Listing 32.3: VAR autocorrelation test from Lütkepohl [\[Download ▼\]](#)

```

open wgmactro.gdt --quiet
list Y = investment income consumption
list dlnY = ldiff(Y)
smp1 1960:4 1978:4
var 2 dlnY
modtest 4 --autocorr
eval $test ~ $pvalue
modtest 4 --autocorr --univariate
eval $test ~ $pvalue

```

Output from tests:

```

? modtest 4 --autocorr
Test for autocorrelation of order up to 4

```

	Rao F	Approx dist.	p-value
lag 1	0.615	F(9, 148)	0.7827
lag 2	0.754	F(18, 164)	0.7507
lag 3	1.143	F(27, 161)	0.2982
lag 4	1.254	F(36, 154)	0.1743

```

? eval $test ~ $pvalue
    0.61524    0.78269
    0.75397    0.75067
    1.1429     0.29820
    1.2544     0.17431

```

```

? modtest 4 --autocorr --univariate
Test for autocorrelation of order 4

```

Equation 1:
 Ljung-Box $Q' = 6.11506$ with p-value = $P(\text{Chi-square}(4) > 6.11506) = 0.191$

Equation 2:
 Ljung-Box $Q' = 1.67136$ with p-value = $P(\text{Chi-square}(4) > 1.67136) = 0.796$

Equation 3:
 Ljung-Box $Q' = 1.59931$ with p-value = $P(\text{Chi-square}(4) > 1.59931) = 0.809$

```

? eval $test ~ $pvalue
    6.1151    0.19072
    1.6714    0.79591
    1.5993    0.80892

```

Chapter 33

Cointegration and Vector Error Correction Models

33.1 Introduction

The twin concepts of cointegration and error correction have drawn a good deal of attention in macroeconometrics over recent years. The attraction of the Vector Error Correction Model (VECM) is that it allows the researcher to embed a representation of economic equilibrium relationships within a relatively rich time-series specification. This approach overcomes the old dichotomy between (a) structural models that faithfully represented macroeconomic theory but failed to fit the data, and (b) time-series models that were accurately tailored to the data but difficult if not impossible to interpret in economic terms.

The basic idea of cointegration relates closely to the concept of unit roots (see section 31.3). Suppose we have a set of macroeconomic variables of interest, and we find we cannot reject the hypothesis that some of these variables, considered individually, are non-stationary. Specifically, suppose we judge that a subset of the variables are individually integrated of order 1, or I(1). That is, while they are non-stationary in their levels, their first differences are stationary. Given the statistical problems associated with the analysis of non-stationary data (for example, the threat of spurious regression), the traditional approach in this case was to take first differences of all the variables before proceeding with the analysis.

But this can result in the loss of important information. It may be that while the variables in question are I(1) when taken individually, there exists a linear combination of the variables that is stationary without differencing, or I(0). (There could be more than one such linear combination.) That is, while the ensemble of variables may be “free to wander” over time, nonetheless the variables are “tied together” in certain ways. And it may be possible to interpret these ties, or *cointegrating vectors*, as representing equilibrium conditions.

For example, suppose we find some or all of the following variables are I(1): money stock, M , the price level, P , the nominal interest rate, R , and output, Y . According to standard theories of the demand for money, we would nonetheless expect there to be an equilibrium relationship between real balances, interest rate and output; for example

$$m - p = \gamma_0 + \gamma_1 y + \gamma_2 r \quad \gamma_1 > 0, \gamma_2 < 0$$

where lower-case variable names denote logs. In equilibrium, then,

$$m - p - \gamma_1 y - \gamma_2 r = \gamma_0$$

Realistically, we should not expect this condition to be satisfied each period. We need to allow for the possibility of short-run disequilibrium. But if the system moves back towards equilibrium following a disturbance, it follows that the vector $x = (m, p, y, r)'$ is bound by a cointegrating vector $\beta' = (\beta_1, \beta_2, \beta_3, \beta_4)$, such that $\beta'x$ is stationary (with a mean of γ_0). Furthermore, if equilibrium is correctly characterized by the simple model above, we have $\beta_2 = -\beta_1$, $\beta_3 < 0$ and $\beta_4 > 0$. These things are testable within the context of cointegration analysis.

There are typically three steps in this sort of analysis:

1. Test to determine the number of cointegrating vectors, the *cointegrating rank* of the system.
2. Estimate a VECM with the appropriate rank, but subject to no further restrictions.

3. Probe the interpretation of the cointegrating vectors as equilibrium conditions by means of restrictions on the elements of these vectors.

The following sections expand on each of these points, giving further econometric details and explaining how to implement the analysis using gretl.

33.2 Vector Error Correction Models as representation of a cointegrated system

Consider a VAR of order p with a deterministic part given by μ_t (typically, a polynomial in time). One can write the n -variate process y_t as

$$y_t = \mu_t + A_1 y_{t-1} + A_2 y_{t-2} + \cdots + A_p y_{t-p} + \epsilon_t \quad (33.1)$$

But since $y_{t-i} \equiv y_{t-1} - (\Delta y_{t-1} + \Delta y_{t-2} + \cdots + \Delta y_{t-i+1})$, we can re-write the above as

$$\Delta y_t = \mu_t + \Pi y_{t-1} + \sum_{i=1}^{p-1} \Gamma_i \Delta y_{t-i} + \epsilon_t, \quad (33.2)$$

where $\Pi = \sum_{i=1}^p A_i - I$ and $\Gamma_i = -\sum_{j=i+1}^p A_j$. This is the VECM representation of (33.1).

The interpretation of (33.2) depends crucially on r , the rank of the matrix Π .

- If $r = 0$, the processes are all I(1) and not cointegrated.
- If $r = n$, then Π is invertible and the processes are all I(0).
- Cointegration occurs in between, when $0 < r < n$ and Π can be written as $\alpha\beta'$. In this case, y_t is I(1), but the combination $z_t = \beta' y_t$ is I(0). If, for example, $r = 1$ and the first element of β was -1 , then one could write $z_t = -y_{1,t} + \beta_2 y_{2,t} + \cdots + \beta_n y_{n,t}$, which is equivalent to saying that

$$y_{1,t} = \beta_2 y_{2,t} + \cdots + \beta_n y_{n,t} - z_t$$

is a long-run equilibrium relationship: the deviations z_t may not be 0 but they are stationary. In this case, (33.2) can be written as

$$\Delta y_t = \mu_t + \alpha\beta' y_{t-1} + \sum_{i=1}^{p-1} \Gamma_i \Delta y_{t-i} + \epsilon_t. \quad (33.3)$$

If β were known, then z_t would be observable and all the remaining parameters could be estimated via OLS. In practice, the procedure estimates β first and then the rest.

The rank of Π is investigated by computing the eigenvalues of a closely related matrix whose rank is the same as Π : however, this matrix is by construction symmetric and positive semidefinite. As a consequence, all its eigenvalues are real and non-negative, and tests on the rank of Π can therefore be carried out by testing how many eigenvalues are 0.

If all the eigenvalues are significantly different from 0, then all the processes are stationary. If, on the contrary, there is at least one zero eigenvalue, then the y_t process is integrated, although some linear combination $\beta' y_t$ might be stationary. At the other extreme, if no eigenvalues are significantly different from 0, then not only is the process y_t non-stationary, but the same holds for any linear combination $\beta' y_t$; in other words, no cointegration occurs.

Estimation typically proceeds in two stages: first, a sequence of tests is run to determine r , the cointegration rank. Then, for a given rank the parameters in equation (33.3) are estimated. The two commands that gretl offers for estimating these systems are `johansen` and `vecm`, respectively.

The syntax for `johansen` is

```
johansen p ylist [ ; xlist [ ; zlist ] ]
```

where p is the number of lags in (33.1); $ylist$ is a list containing the y_t variables; $xlist$ is an optional list of exogenous variables; and $zlist$ is another optional list of exogenous variables whose effects are assumed to be confined to the cointegrating relationships.

The syntax for `vecm` is

```
vecm p r ylist [ ; xlist [ ; zlist ] ]
```

where p is the number of lags in (33.1); r is the cointegration rank; and the lists $ylist$, $xlist$ and $zlist$ have the same interpretation as in `johansen`.

Both commands can be given specific options to handle the treatment of the deterministic component μ_t . These are discussed in the following section.

33.3 Interpretation of the deterministic components

Statistical inference in the context of a cointegrated system depends on the hypotheses one is willing to make on the deterministic terms, which leads to the famous “five cases.”

In equation (33.2), the term μ_t is usually understood to take the form

$$\mu_t = \mu_0 + \mu_1 \cdot t.$$

In order to have the model mimic as closely as possible the features of the observed data, there is a preliminary question to settle. Do the data appear to follow a deterministic trend? If so, is it linear or quadratic?

Once this is established, one should impose restrictions on μ_0 and μ_1 that are consistent with this judgement. For example, suppose that the data do not exhibit a discernible trend. This means that Δy_t is on average zero, so it is reasonable to assume that its expected value is also zero. Write equation (33.2) as

$$\Gamma(L)\Delta y_t = \mu_0 + \mu_1 \cdot t + \alpha z_{t-1} + \epsilon_t, \quad (33.4)$$

where $z_t = \beta' y_t$ is assumed to be stationary and therefore to possess finite moments. Taking unconditional expectations, we get

$$0 = \mu_0 + \mu_1 \cdot t + \alpha m_z.$$

Since the left-hand side does not depend on t , the restriction $\mu_1 = 0$ is a safe bet. As for μ_0 , there are just two ways to make the above expression true: either $\mu_0 = 0$ with $m_z = 0$, or μ_0 equals $-\alpha m_z$. The latter possibility is less restrictive in that the vector μ_0 may be non-zero, but is constrained to be a linear combination of the columns of α . In that case, μ_0 can be written as $\alpha \cdot c$, and one may write (33.4) as

$$\Gamma(L)\Delta y_t = \alpha \begin{bmatrix} \beta' & c \end{bmatrix} \begin{bmatrix} y_{t-1} \\ 1 \end{bmatrix} + \epsilon_t.$$

The long-run relationship therefore contains an intercept. This type of restriction is usually written

$$\alpha'_\perp \mu_0 = 0,$$

where α_\perp is the left null space of the matrix α .

An intuitive understanding of the issue can be gained by means of a simple example. Consider a series x_t which behaves as follows

$$x_t = m + x_{t-1} + \varepsilon_t$$

where m is a real number and ε_t is a white noise process: x_t is then a random walk with drift m . In the special case $m = 0$, the drift disappears and x_t is a pure random walk.

Consider now another process y_t , defined by

$$y_t = k + x_t + u_t$$

where, again, k is a real number and u_t is a white noise process. Since u_t is stationary by definition, x_t and y_t cointegrate: that is, their difference

$$z_t = y_t - x_t = k + u_t$$

is a stationary process. For $k = 0$, z_t is simple zero-mean white noise, whereas for $k \neq 0$ the process z_t is white noise with a non-zero mean.

After some simple substitutions, the two equations above can be represented jointly as a VAR(1) system

$$\begin{bmatrix} y_t \\ x_t \end{bmatrix} = \begin{bmatrix} k + m \\ m \end{bmatrix} + \begin{bmatrix} 0 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} y_{t-1} \\ x_{t-1} \end{bmatrix} + \begin{bmatrix} u_t + \varepsilon_t \\ \varepsilon_t \end{bmatrix}$$

or in VECM form

$$\begin{aligned} \begin{bmatrix} \Delta y_t \\ \Delta x_t \end{bmatrix} &= \begin{bmatrix} k + m \\ m \end{bmatrix} + \begin{bmatrix} -1 & 1 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} y_{t-1} \\ x_{t-1} \end{bmatrix} + \begin{bmatrix} u_t + \varepsilon_t \\ \varepsilon_t \end{bmatrix} = \\ &= \begin{bmatrix} k + m \\ m \end{bmatrix} + \begin{bmatrix} -1 \\ 0 \end{bmatrix} \begin{bmatrix} 1 & -1 \end{bmatrix} \begin{bmatrix} y_{t-1} \\ x_{t-1} \end{bmatrix} + \begin{bmatrix} u_t + \varepsilon_t \\ \varepsilon_t \end{bmatrix} = \\ &= \mu_0 + \alpha \beta' \begin{bmatrix} y_{t-1} \\ x_{t-1} \end{bmatrix} + \eta_t = \mu_0 + \alpha z_{t-1} + \eta_t, \end{aligned}$$

where β is the cointegration vector and α is the “loadings” or “adjustments” vector.

We are now ready to consider three possible cases:

1. $m \neq 0$: In this case x_t is trended, as we just saw; it follows that y_t also follows a linear trend because on average it keeps at a fixed distance k from x_t . The vector μ_0 is unrestricted.
2. $m = 0$ and $k \neq 0$: In this case, x_t is not trended and as a consequence neither is y_t . However, the mean distance between y_t and x_t is non-zero. The vector μ_0 is given by

$$\mu_0 = \begin{bmatrix} k \\ 0 \end{bmatrix}$$

which is not null and therefore the VECM shown above does have a constant term. The constant, however, is subject to the restriction that its second element must be 0. More generally, μ_0 is a multiple of the vector α . Note that the VECM could also be written as

$$\begin{bmatrix} \Delta y_t \\ \Delta x_t \end{bmatrix} = \begin{bmatrix} -1 \\ 0 \end{bmatrix} \begin{bmatrix} 1 & -1 & -k \end{bmatrix} \begin{bmatrix} y_{t-1} \\ x_{t-1} \\ 1 \end{bmatrix} + \begin{bmatrix} u_t + \varepsilon_t \\ \varepsilon_t \end{bmatrix}$$

which incorporates the intercept into the cointegration vector. This is known as the “restricted constant” case.

3. $m = 0$ and $k = 0$: This case is the most restrictive: clearly, neither x_t nor y_t are trended, and the mean distance between them is zero. The vector μ_0 is also 0, which explains why this case is referred to as “no constant.”

In most cases, the choice between these three possibilities is based on a mix of empirical observation and economic reasoning. If the variables under consideration seem to follow a linear trend

then we should not place any restriction on the intercept. Otherwise, the question arises of whether it makes sense to specify a cointegration relationship which includes a non-zero intercept. One example where this is appropriate is the relationship between two interest rates: generally these are not trended, but the VAR might still have an intercept because the difference between the two (the “interest rate spread”) might be stationary around a non-zero mean (for example, because of a risk or liquidity premium).

The previous example can be generalized in three directions:

1. If a VAR of order greater than 1 is considered, the algebra gets more convoluted but the conclusions are identical.
2. If the VAR includes more than two endogenous variables the cointegration rank r can be greater than 1. In this case, α is a matrix with r columns, and the case with restricted constant entails the restriction that μ_0 should be some linear combination of the columns of α .
3. If a linear trend is included in the model, the deterministic part of the VAR becomes $\mu_0 + \mu_1 t$. The reasoning is practically the same as above except that the focus now centers on μ_1 rather than μ_0 . The counterpart to the “restricted constant” case discussed above is a “restricted trend” case, such that the cointegration relationships include a trend but the first differences of the variables in question do not. In the case of an unrestricted trend, the trend appears in both the cointegration relationships and the first differences, which corresponds to the presence of a quadratic trend in the variables themselves (in levels).

In order to accommodate the five cases, gretl provides the following options to the `johansen` and `vecm` commands:

μ_t	option flag	description
0	--nc	no constant
$\mu_0, \alpha'_\perp \mu_0 = 0$	--rc	restricted constant
μ_0	--uc	unrestricted constant
$\mu_0 + \mu_1 t, \alpha'_\perp \mu_1 = 0$	--crt	constant + restricted trend
$\mu_0 + \mu_1 t$	--ct	constant + unrestricted trend

Note that for this command the above options are mutually exclusive. In addition, you have the option of using the `--seasonals` options, for augmenting μ_t with centered seasonal dummies. In each case, p-values are computed via the approximations devised by [Doornik \(1998\)](#).

33.4 The Johansen cointegration tests

The two Johansen tests for cointegration are used to establish the rank of β , or in other words the number of cointegrating vectors. These are the “ λ -max” test, for hypotheses on individual eigenvalues, and the “trace” test, for joint hypotheses. Suppose that the eigenvalues λ_i are sorted from largest to smallest. The null hypothesis for the λ -max test on the i -th eigenvalue is that $\lambda_i = 0$. The corresponding trace test, instead, considers the hypothesis $\lambda_j = 0$ for all $j \geq i$.

The gretl command `johansen` performs these two tests. The corresponding menu entry in the GUI is “Model, Time Series, Cointegration Test, Johansen”.

As in the ADF test, the asymptotic distribution of the tests varies with the deterministic component μ_t one includes in the VAR (see section 33.3 above). The following code uses the `denmark` data file, supplied with gretl, to replicate Johansen’s example found in his 1995 book.

```
open denmark
johansen 2 LRM LRY IBO IDE --rc --seasonals
```

In this case, the vector y_t in equation (33.2) comprises the four variables LRM, LRY, IBO, IDE. The number of lags equals p in (33.2) (that is, the number of lags of the model written in VAR form). Part of the output is reported below:

```
Johansen test:
Number of equations = 4
Lag order = 2
Estimation period: 1974:3 - 1987:3 (T = 53)

Case 2: Restricted constant
Rank Eigenvalue Trace test p-value Lmax test p-value
0 0.43317 49.144 [0.1284] 30.087 [0.0286]
1 0.17758 19.057 [0.7833] 10.362 [0.8017]
2 0.11279 8.6950 [0.7645] 6.3427 [0.7483]
3 0.043411 2.3522 [0.7088] 2.3522 [0.7076]
```

Both the trace and λ -max tests accept the null hypothesis that the smallest eigenvalue is 0 (see the last row of the table), so we may conclude that the series are in fact non-stationary. However, some linear combination may be $I(0)$, since the λ -max test rejects the hypothesis that the rank of Π is 0 (though the trace test gives less clear-cut evidence for this, with a p-value of 0.1284).

33.5 Identification of the cointegration vectors

The core problem in the estimation of equation (33.2) is to find an estimate of Π that has by construction rank r , so it can be written as $\Pi = \alpha\beta'$, where β is the matrix containing the cointegration vectors and α contains the “adjustment” or “loading” coefficients whereby the endogenous variables respond to deviation from equilibrium in the previous period.

Without further specification, the problem has multiple solutions (in fact, infinitely many). The parameters α and β are under-identified: if all columns of β are cointegration vectors, then any arbitrary linear combinations of those columns is a cointegration vector too. To put it differently, if $\Pi = \alpha_0\beta'_0$ for specific matrices α_0 and β_0 , then Π also equals $(\alpha_0 Q)(Q^{-1}\beta'_0)$ for any conformable non-singular matrix Q . In order to find a unique solution, it is therefore necessary to impose some restrictions on α and/or β . It can be shown that the minimum number of restrictions that is necessary to guarantee identification is r^2 . Normalizing one coefficient per column to 1 (or -1 , according to taste) is a trivial first step, which also helps in that the remaining coefficients can be interpreted as the parameters in the equilibrium relations, but this only suffices when $r = 1$.

The method that gretl uses by default is known as the “Phillips normalization”, or “triangular representation”.¹ The starting point is writing β in partitioned form as in

$$\beta = \begin{bmatrix} \beta_1 \\ \beta_2 \end{bmatrix}$$

where β_1 is an $r \times r$ matrix and β_2 is $(n - r) \times r$. Assuming that β_1 has full rank, β can be post-multiplied by β_1^{-1} , giving

$$\hat{\beta} = \begin{bmatrix} I \\ \beta_2\beta_1^{-1} \end{bmatrix} = \begin{bmatrix} I \\ -B \end{bmatrix}.$$

The coefficients that gretl produces are $\hat{\beta}$, with B known as the matrix of unrestricted coefficients. In terms of the underlying equilibrium relationship, the Phillips normalization expresses the system

¹For comparison with other studies, you may wish to normalize β differently. Using the `set` command you can do `set vecm_norm diag` to select a normalization that simply scales the columns of the original β such that $\beta_{ij} = 1$ for $i = j$ and $i \leq r$, as used in the empirical section of Boswijk and Doornik (2004). Another alternative is `set vecm_norm first`, which scales β such that the elements on the first row equal 1. To suppress normalization altogether, use `set vecm_norm none`. (To return to the default: `set vecm_norm phillips`.)

of r equilibrium relations as

$$\begin{aligned} y_{1,t} &= b_{1,r+1}y_{r+1,t} + \dots + b_{1,n}y_{n,t} \\ y_{2,t} &= b_{2,r+1}y_{r+1,t} + \dots + b_{2,n}y_{n,t} \\ &\vdots \\ y_{r,t} &= b_{r,r+1}y_{r+1,t} + \dots + b_{r,n}y_{n,t} \end{aligned}$$

where the first r variables are expressed as functions of the remaining $n - r$.

Although the triangular representation ensures that the statistical problem of estimating β is solved, the resulting equilibrium relationships may be difficult to interpret. In this case, the user may want to achieve identification by specifying manually the system of r^2 constraints that gretl will use to produce an estimate of β .

As an example, consider the money demand system presented in section 9.6 of Verbeek (2004). The variables used are *m* (the log of real money stock M1), *infl* (inflation), *cpr* (the commercial paper rate), *y* (log of real GDP) and *tbr* (the Treasury bill rate).²

Estimation of β can be performed via the commands

```
open money.gdt
smp1 1954:1 1994:4
vecm 6 2 m infl cpr y tbr --rc
```

and the relevant portion of the output reads

```
Maximum likelihood estimates, observations 1954:1-1994:4 (T = 164)
Cointegration rank = 2
Case 2: Restricted constant

beta (cointegrating vectors, standard errors in parentheses)

m          1.0000      0.0000
           (0.0000)    (0.0000)
infl       0.0000      1.0000
           (0.0000)    (0.0000)
cpr        0.56108     -24.367
           (0.10638)   (4.2113)
y          -0.40446    -0.91166
           (0.10277)   (4.0683)
tbr        -0.54293     24.786
           (0.10962)   (4.3394)
const      -3.7483     16.751
           (0.78082)   (30.909)
```

Interpretation of the coefficients of the cointegration matrix β would be easier if a meaning could be attached to each of its columns. This is possible by hypothesizing the existence of two long-run relationships: a money demand equation

$$m = c_1 + \beta_1 \text{infl} + \beta_2 y + \beta_3 \text{tbr}$$

and a risk premium equation

$$\text{cpr} = c_2 + \beta_4 \text{infl} + \beta_5 y + \beta_6 \text{tbr}$$

²This data set is available in the verbeek data package; see http://gretl.sourceforge.net/gretl_data.html.

which imply that the cointegration matrix can be normalized as

$$\beta = \begin{bmatrix} -1 & 0 \\ \beta_1 & \beta_4 \\ 0 & -1 \\ \beta_2 & \beta_5 \\ \beta_3 & \beta_6 \\ c_1 & c_2 \end{bmatrix}$$

This renormalization can be accomplished by means of the `restrict` command, to be given after the `vecm` command or, in the graphical interface, by selecting the “Test, Linear Restrictions” menu entry. The syntax for entering the restrictions should be fairly obvious:³

```
restrict
  b[1,1] = -1
  b[1,3] = 0
  b[2,1] = 0
  b[2,3] = -1
end restrict
```

which produces

Cointegrating vectors (standard errors in parentheses)

m	-1.0000	0.0000
	(0.0000)	(0.0000)
infl	-0.023026	0.041039
	(0.0054666)	(0.027790)
cpr	0.0000	-1.0000
	(0.0000)	(0.0000)
y	0.42545	-0.037414
	(0.033718)	(0.17140)
tbr	-0.027790	1.0172
	(0.0045445)	(0.023102)
const	3.3625	0.68744
	(0.25318)	(1.2870)

33.6 Over-identifying restrictions

One purpose of imposing restrictions on a VECM system is simply to achieve identification. If these restrictions are simply normalizations, they are not testable and should have no effect on the maximized likelihood. In addition, however, one may wish to formulate constraints on β and/or α that derive from the economic theory underlying the equilibrium relationships; substantive restrictions of this sort are then testable via a likelihood-ratio statistic.

Gretl is capable of testing general linear restrictions of the form

$$R_b \text{vec}(\beta) = q \quad (33.5)$$

and/or

$$R_a \text{vec}(\alpha) = 0 \quad (33.6)$$

Note that the β restriction may be non-homogeneous ($q \neq 0$) but the α restriction must be homogeneous. Nonlinear restrictions are not supported, and neither are restrictions that cross between β

³Note that in this context we are bending the usual matrix indexation convention, using the leading index to refer to the *column* of β (the particular cointegrating vector). This is standard practice in the literature, and defensible insofar as it is the columns of β (the cointegrating relations or equilibrium errors) that are of primary interest.

and α . When $r > 1$, such restrictions may be in common across all the columns of β (or α) or may be specific to certain columns of these matrices. For useful discussions of this point see [Boswijk \(1995\)](#) and [Boswijk and Doornik \(2004\)](#), section 4.4.

The restrictions (33.5) and (33.6) may be written in explicit form as

$$\text{vec}(\beta) = H\phi + h_0 \quad (33.7)$$

and

$$\text{vec}(\alpha') = G\psi \quad (33.8)$$

respectively, where ϕ and ψ are the free parameter vectors associated with β and α respectively. We may refer to the free parameters collectively as θ (the column vector formed by concatenating ϕ and ψ). Gretl uses this representation internally when testing the restrictions.

If the list of restrictions that is passed to the `restrict` command contains more constraints than necessary to achieve identification, then an LR test is performed. In addition, the `restrict` command can be given the `--full` switch, in which case full estimates for the restricted system are printed (including the Γ_i terms) and the system thus restricted becomes the “current model” for the purposes of further tests. Thus you are able to carry out cumulative tests, as in Chapter 7 of [Johansen \(1995\)](#).

Syntax

The full syntax for specifying the restriction is an extension of that exemplified in the previous section. Inside a `restrict...end restrict` block, valid statements are of the form

$$\textit{parameter linear combination} = \textit{scalar}$$

where a parameter linear combination involves a weighted sum of individual elements of β or α (but not both in the same combination); the scalar on the right-hand side must be 0 for combinations involving α , but can be any real number for combinations involving β . Below, we give a few examples of valid restrictions:

$$\begin{aligned} b[1,1] &= 1.618 \\ b[1,4] + 2*b[2,5] &= 0 \\ a[1,3] &= 0 \\ a[1,1] - a[1,2] &= 0 \end{aligned}$$

Special syntax is used when a certain constraint should be applied to all columns of β : in this case, one index is given for each `b` term, and the square brackets are dropped. Hence, the following syntax

```
restrict
  b1 + b2 = 0
end restrict
```

corresponds to

$$\beta = \begin{bmatrix} \beta_{11} & \beta_{21} \\ -\beta_{11} & -\beta_{21} \\ \beta_{13} & \beta_{23} \\ \beta_{14} & \beta_{24} \end{bmatrix}$$

The same convention is used for α : when only one index is given for an “`a`” term the restriction is presumed to apply to all r columns of α , or in other words the variable associated with the given row of α is weakly exogenous. For instance, the formulation

```

restrict
  a3 = 0
  a4 = 0
end restrict

```

specifies that variables 3 and 4 do not respond to the deviation from equilibrium in the previous period.⁴

A variant on the single-index syntax for common restrictions on α and β is available: you can replace the index number with the name of the corresponding variable, in square brackets. For example, instead of `a3 = 0` one could write `a[cpr] = 0`, if the third variable in the system is named `cpr`.

Finally, a shortcut (or anyway an alternative) is available for setting up complex restrictions (but currently only in relation to β): you can specify R_b and q , as in $R_b \text{vec}(\beta) = q$, by giving the names of previously defined matrices. For example,

```

matrix I4 = I(4)
matrix vR = I4**(I4~zeros(4,1))
matrix vq = mshape(I4,16,1)
restrict
  R = vR
  q = vq
end restrict

```

which manually imposes Phillips normalization on the β estimates for a system with cointegrating rank 4.

There are two points to note in relation to this option. First, $\text{vec}(\beta)$ is taken to include the coefficients on all terms within the cointegration space, including the restricted constant or trend, if any, as well as any restricted exogenous variables. Second, it is acceptable to give an `R` matrix with a number of columns equal to the number of *rows* of β ; this variant is taken to specify a restriction that is in common across all the columns of β .

An example

[Brand and Cassola \(2004\)](#) propose a money demand system for the Euro area, in which they postulate three long-run equilibrium relationships:

money demand	$m = \beta_l l + \beta_y y$
Fisher equation	$\pi = \phi l$
Expectation theory of interest rates	$l = s$

where m is real money demand, l and s are long- and short-term interest rates, y is output and π is inflation.⁵ (The names for these variables in the `gretl` data file are `m_p`, `r_l`, `r_s`, `y` and `infl`, respectively.)

The cointegration rank assumed by the authors is 3 and there are 5 variables, giving 15 elements in the β matrix. $3 \times 3 = 9$ restrictions are required for identification, and a just-identified system would have $15 - 9 = 6$ free parameters. However, the postulated long-run relationships feature only three free parameters, so the over-identification rank is 3.

⁴Note that when two indices are given in a restriction on α the indexation is consistent with that for β restrictions: the leading index denotes the cointegrating vector and the trailing index the equation number.

⁵A traditional formulation of the Fisher equation would reverse the roles of the variables in the second equation, but this detail is immaterial in the present context; moreover, the expectation theory of interest rates implies that the third equilibrium relationship should include a constant for the liquidity premium. However, since in this example the system is estimated with the constant term unrestricted, the liquidity premium gets absorbed into the system intercept and disappears from z_t .

Listing 33.1: Estimation of a money demand system with constraints on β [\[Download ▼\]](#)

```

open brand_cassola.gdt

# perform a few transformations
m_p = m_p*100
y = y*100
infl = infl/4
rs = rs/4
r1 = r1/4

# replicate table 4, page 824
vecm 2 3 m_p infl r1 rs y -q
l10 = $lnl

restrict --full
  b[1,1] = 1
  b[1,2] = 0
  b[1,4] = 0
  b[2,1] = 0
  b[2,2] = 1
  b[2,4] = 0
  b[2,5] = 0
  b[3,1] = 0
  b[3,2] = 0
  b[3,3] = 1
  b[3,4] = -1
  b[3,5] = 0
end restrict
l11 = $rlnl

```

Partial output:

```

Unrestricted loglikelihood (lu) = 116.60268
Restricted loglikelihood (lr) = 115.86451
2 * (lu - lr) = 1.47635
P(Chi-Square(3) > 1.47635) = 0.68774

```

beta (cointegrating vectors, standard errors in parentheses)

m_p	1.0000	0.0000	0.0000
	(0.0000)	(0.0000)	(0.0000)
infl	0.0000	1.0000	0.0000
	(0.0000)	(0.0000)	(0.0000)
r1	1.6108	-0.67100	1.0000
	(0.62752)	(0.049482)	(0.0000)
rs	0.0000	0.0000	-1.0000
	(0.0000)	(0.0000)	(0.0000)
y	-1.3304	0.0000	0.0000
	(0.030533)	(0.0000)	(0.0000)

Listing 33.1 replicates Table 4 on page 824 of the Brand and Cassola article.⁶ Note that we use the `$lnl` accessor after the `vecm` command to store the unrestricted log-likelihood and the `$rlnl` accessor after `restrict` for its restricted counterpart.

The example continues in script 33.2, where we perform further testing to check whether (a) the income elasticity in the money demand equation is 1 ($\beta_y = 1$) and (b) the Fisher relation is homogeneous ($\phi = 1$). Since the `--full` switch was given to the initial `restrict` command, additional restrictions can be applied without having to repeat the previous ones. (The second script contains a few `printf` commands, which are not strictly necessary, to format the output nicely.) It turns out that both of the additional hypotheses are rejected by the data, with p-values of 0.002 and 0.004.

Listing 33.2: Further testing of money demand system

```
restrict
  b[1,5] = -1
end restrict
ll_uie = $rlnl

restrict
  b[2,3] = -1
end restrict
ll_hfh = $rlnl

# replicate table 5, page 824
printf "Testing zero restrictions in cointegration space:\n"
printf "  LR-test, rank = 3: chi^2(3) = %6.4f [%6.4f]\n", 2*(ll0-ll1), \
  pvalue(X, 3, 2*(ll0-ll1))

printf "Unit income elasticity: LR-test, rank = 3:\n"
printf "  chi^2(4) = %g [%6.4f]\n", 2*(ll0-ll_uie), \
  pvalue(X, 4, 2*(ll0-ll_uie))

printf "Homogeneity in the Fisher hypothesis:\n"
printf "  LR-test, rank = 3: chi^2(4) = %6.3f [%6.4f]\n", 2*(ll0-ll_hfh), \
  pvalue(X, 4, 2*(ll0-ll_hfh))
```

Output:

```
Testing zero restrictions in cointegration space:
  LR-test, rank = 3: chi^2(3) = 1.4763 [0.6877]
Unit income elasticity: LR-test, rank = 3:
  chi^2(4) = 17.2071 [0.0018]
Homogeneity in the Fisher hypothesis:
  LR-test, rank = 3: chi^2(4) = 15.547 [0.0037]
```

Another type of test that is commonly performed is the “weak exogeneity” test. In this context, a variable is said to be weakly exogenous if all coefficients on the corresponding row in the α matrix are zero. If this is the case, that variable does not adjust to deviations from any of the long-run equilibria and can be considered an autonomous driving force of the whole system.

The code in Listing 33.3 performs this test for each variable in turn, thus replicating the first column of Table 6 on page 825 of Brand and Cassola (2004). The results show that weak exogeneity might perhaps be accepted for the long-term interest rate and real GDP (p-values 0.07 and 0.08 respectively).

⁶Modulo what appear to be a few typos in the article.

Listing 33.3: Testing for weak exogeneity

```

restrict
    a1 = 0
end restrict
ts_m = 2*(l10 - $rln1)

restrict
    a2 = 0
end restrict
ts_p = 2*(l10 - $rln1)

restrict
    a3 = 0
end restrict
ts_l = 2*(l10 - $rln1)

restrict
    a4 = 0
end restrict
ts_s = 2*(l10 - $rln1)

restrict
    a5 = 0
end restrict
ts_y = 2*(l10 - $rln1)

loop foreach i m p l s y
    printf "Delta $i\t%6.3f [%6.4f]\n", ts_$i, pvalue(X, 6, ts_$i)
endloop

```

Output (variable, LR test, p-value):

Delta m	18.111	[0.0060]
Delta p	21.067	[0.0018]
Delta l	11.819	[0.0661]
Delta s	16.000	[0.0138]
Delta y	11.335	[0.0786]

Identification and testability

One point regarding VECM restrictions that can be confusing at first is that identification (does the restriction identify the system?) and testability (is the restriction testable?) are quite separate matters. Restrictions can be identifying but not testable; less obviously, they can be testable but not identifying.

This can be seen quite easily in relation to a rank-1 system. The restriction $\beta_1 = 1$ is identifying (it pins down the scale of β) but, being a pure scaling, it is not testable. On the other hand, the restriction $\beta_1 + \beta_2 = 0$ is testable—the system with this requirement imposed will almost certainly have a lower maximized likelihood—but it is not identifying; it still leaves open the scale of β .

We said above that the number of restrictions must equal at least r^2 , where r is the cointegrating rank, for identification. This is a necessary and not a sufficient condition. In fact, when $r > 1$ it can be quite tricky to assess whether a given set of restrictions is identifying. Gretl uses the method suggested by Doornik (1995), where identification is assessed via the rank of the information matrix.

It can be shown that for restrictions of the sort (33.7) and (33.8) the information matrix has the same rank as the Jacobian matrix

$$J(\theta) = \left[(I_p \otimes \beta)G : (\alpha \otimes I_{p_1})H \right]$$

A sufficient condition for identification is that the rank of $J(\theta)$ equals the number of free parameters. The rank of this matrix is evaluated by examination of its singular values at a randomly selected point in the parameter space. For practical purposes we treat this condition as if it were both necessary and sufficient; that is, we disregard the special cases where identification could be achieved without this condition being met.⁷

33.7 Numerical solution methods

In general, the ML estimator for the restricted VECM problem has no closed-form solution, hence the maximum must be found via numerical methods.⁸ In some cases convergence may be difficult, and gretl provides several choices to solve the problem.

Switching and LBFGS

Two maximization methods are available in gretl. The default is the switching algorithm set out in Boswijk and Doornik (2004). The alternative is a limited-memory variant of the BFGS algorithm (LBFGS), using analytical derivatives. This is invoked using the `--lbfgs` flag with the `restrict` command.

The switching algorithm works by explicitly maximizing the likelihood at each iteration, with respect to $\hat{\phi}$, $\hat{\psi}$ and $\hat{\Omega}$ (the covariance matrix of the residuals) in turn. This method shares a feature with the basic Johansen eigenvalues procedure, namely, it can handle a set of restrictions that does not fully identify the parameters.

LBFGS, on the other hand, requires that the model be fully identified. When using LBFGS, therefore, you may have to supplement the restrictions of interest with normalizations that serve to identify the parameters. For example, one might use all or part of the Phillips normalization (see section 33.5).

Neither the switching algorithm nor LBFGS is guaranteed to find the global ML solution.⁹ The

⁷See Boswijk and Doornik (2004), pp. 447–8 for discussion of this point.

⁸The exception is restrictions that are homogeneous, common to all β or all α (in case $r > 1$), and involve either β only or α only. Such restrictions are handled via the modified eigenvalues method set out by Johansen (1995). We solve directly for the ML estimator, without any need for iterative methods.

⁹In developing gretl's VECM-testing facilities we have considered a fair number of “tricky cases” from various sources. We'd like to thank Luca Fanelli of the University of Bologna and Sven Schreiber of Goethe University Frankfurt for their help in devising torture-tests for gretl's VECM code.

optimizer may end up at a local maximum (or, in the case of the switching algorithm, at a saddle point).

The solution (or lack thereof) may be sensitive to the initial value selected for θ . By default, gretl selects a starting point using a deterministic method based on Boswijk (1995), but two further options are available: the initialization may be adjusted using simulated annealing, or the user may supply an explicit initial value for θ .

The default initialization method is:

1. Calculate the unrestricted ML $\hat{\beta}$ using the Johansen procedure.
2. If the restriction on β is non-homogeneous, use the method proposed by Boswijk:

$$\phi_0 = -[(I_r \otimes \hat{\beta}_\perp)' H]^+ (I_r \otimes \hat{\beta}_\perp)' h_0 \quad (33.9)$$

where $\hat{\beta}_\perp' \hat{\beta} = 0$ and A^+ denotes the Moore-Penrose inverse of A . Otherwise

$$\phi_0 = (H' H)^{-1} H' \text{vec}(\hat{\beta}) \quad (33.10)$$

3. $\text{vec}(\beta_0) = H\phi_0 + h_0$.
4. Calculate the unrestricted ML $\hat{\alpha}$ conditional on β_0 , as per Johansen:

$$\hat{\alpha} = S_{01}\beta_0(\beta_0' S_{11}\beta_0)^{-1} \quad (33.11)$$

5. If α is restricted by $\text{vec}(\alpha') = G\psi$, then $\psi_0 = (G'G)^{-1}G' \text{vec}(\hat{\alpha}')$ and $\text{vec}(\alpha'_0) = G\psi_0$.

Alternative initialization methods

As mentioned above, gretl offers the option of adjusting the initialization using **simulated annealing**. This is invoked by adding the `--jitter` option to the `restrict` command.

The basic idea is this: we start at a certain point in the parameter space, and for each of n iterations (currently $n = 4096$) we randomly select a new point within a certain radius of the previous one, and determine the likelihood at the new point. If the likelihood is higher, we jump to the new point; otherwise, we jump with probability P (and remain at the previous point with probability $1 - P$). As the iterations proceed, the system gradually “cools”—that is, the radius of the random perturbation is reduced, as is the probability of making a jump when the likelihood fails to increase.

In the course of this procedure many points in the parameter space are evaluated, starting with the point arrived at by the deterministic method, which we'll call θ_0 . One of these points will be “best” in the sense of yielding the highest likelihood: call it θ^* . This point may or may not have a greater likelihood than θ_0 . And the procedure has an end point, θ_n , which may or may not be “best”.

The rule followed by gretl in selecting an initial value for θ based on simulated annealing is this: use θ^* if $\theta^* > \theta_0$, otherwise use θ_n . That is, if we get an improvement in the likelihood via annealing, we make full use of this; on the other hand, if we fail to get an improvement we nonetheless allow the annealing to randomize the starting point. Experiments indicate that the latter effect can be helpful.

Besides annealing, a further alternative is **manual initialization**. This is done by passing a predefined vector to the `set` command with parameter `initvals`, as in

```
set initvals myvec
```

The details depend on whether the switching algorithm or LBFGS is used. For the switching algorithm, there are two options for specifying the initial values. The more user-friendly one (for most people, we suppose) is to specify a matrix that contains $\text{vec}(\beta)$ followed by $\text{vec}(\alpha)$. For example:

```

open denmark.gdt
vecm 2 1 LRM LRY IBO IDE --rc --seasonals

matrix BA = {1, -1, 6, -6, -6, -0.2, 0.1, 0.02, 0.03}
set initvals BA
restrict
  b[1] = 1
  b[1] + b[2] = 0
  b[3] + b[4] = 0
end restrict

```

In this example—from [Johansen \(1995\)](#)—the cointegration rank is 1 and there are 4 variables. However, the model includes a restricted constant (the `--rc` flag) so that β has 5 elements. The α matrix has 4 elements, one per equation. So the matrix BA may be read as

$$(\beta_1, \beta_2, \beta_3, \beta_4, \beta_5, \alpha_1, \alpha_2, \alpha_3, \alpha_4)$$

The other option, which is compulsory when using LBFGS, is to specify the initial values in terms of the free parameters, ϕ and ψ . Getting this right is somewhat less obvious. As mentioned above, the implicit-form restriction $R\text{vec}(\beta) = q$ has explicit form $\text{vec}(\beta) = H\phi + h_0$, where $H = R_\perp$, the right nullspace of R . The vector ϕ is shorter, by the number of restrictions, than $\text{vec}(\beta)$. The savvy user will then see what needs to be done. The other point to take into account is that if α is unrestricted, the *effective* length of ψ is 0, since it is then optimal to compute α using Johansen’s formula, conditional on β (equation 33.11 above). The example above could be rewritten as:

```

open denmark.gdt
vecm 2 1 LRM LRY IBO IDE --rc --seasonals

matrix phi = {-8, -6}
set initvals phi
restrict --lbfgs
  b[1] = 1
  b[1] + b[2] = 0
  b[3] + b[4] = 0
end restrict

```

In this more economical formulation the initializer specifies only the two free parameters in ϕ (5 elements in β minus 3 restrictions). There is no call to give values for ψ since α is unrestricted.

Scale removal

Consider a simpler version of the restriction discussed in the previous section, namely,

```

restrict
  b[1] = 1
  b[1] + b[2] = 0
end restrict

```

This restriction comprises a substantive, testable requirement—that β_1 and β_2 sum to zero—and a normalization or scaling, $\beta_1 = 1$. The question arises, might it be easier and more reliable to maximize the likelihood without imposing $\beta_1 = 1$?¹⁰ If so, we could record this normalization, remove it for the purpose of maximizing the likelihood, then reimpose it by scaling the result.

Unfortunately it is not possible to say in advance whether “scale removal” of this sort will give better results for any particular estimation problem. However, this does seem to be the case more often than not. Gretl therefore performs scale removal where feasible, unless you

¹⁰As a numerical matter, that is. In principle this should make no difference.

- explicitly forbid this, by giving the `--no-scaling` option flag to the `restrict` command; or
- provide a specific vector of initial values; or
- select the LBFGS algorithm for maximization.

Scale removal is deemed infeasible if there are any cross-column restrictions on β , or any non-homogeneous restrictions involving more than one element of β .

In addition, experimentation has suggested to us that scale removal is inadvisable if the system is just identified with the normalization(s) included, so we do not do it in that case. By “just identified” we mean that the system would not be identified if any of the restrictions were removed. On that criterion the above example is not just identified, since the removal of the second restriction would not affect identification; and `gretl` would in fact perform scale removal in this case unless the user specified otherwise.

Chapter 34

Multivariate models

By a multivariate model we mean one that includes more than one dependent variable. Certain specific types of multivariate model for time-series data are discussed elsewhere: chapter 32 deals with VARs and chapter 33 with VECMs. Here we discuss two general sorts of multivariate model, implemented in gretl via the `system` command: SUR systems (Seemingly Unrelated Regressions), in which all the regressors are taken to be exogenous and interest centers on the covariance of the error term across equations; and simultaneous systems, in which some regressors are assumed to be endogenous.

In this chapter we give an account of the syntax and use of the `system` command and its companions, `restrict` and `estimate`; we also explain the options and accessors available in connection with multivariate models.

34.1 The `system` command

The specification of a multivariate system takes the form of a block of statements, starting with `system` and ending with `end system`. Once a system is specified it can be estimated via various methods, using the `estimate` command, with or without restrictions, which may be imposed via the `restrict` command.

Starting a system block

The first line of a system block may be augmented in either (or both) of two ways:

- An estimation method is specified for the system. This is done by following `system` with an expression of the form `method=estimator`, where *estimator* must be one of `ols` (Ordinary Least Squares), `tsls` (Two-Stage Least Squares), `sur` (Seemingly Unrelated Regressions), `3sls` (Three-Stage Least Squares), `liml` (Limited Information Maximum Likelihood) or `fiml` (Full Information Maximum Likelihood). Two examples:

```
system method=sur
system method=fiml
```

OLS, TSLS and LIML are, of course, single-equation methods rather than true system estimators; they are included to facilitate comparisons.

- The system is assigned a name. This is done by giving the name first, followed by a back-arrow, “<-”, followed by `system`. If the name contains spaces it must be enclosed in double-quotes. Here are two examples:

```
sys1 <- system
"System 1" <- system
```

Note, however, that this naming method is not available within a user-defined function, only in the main body of a gretl script.

If the initial `system` line is augmented in the first way, the effect is that the system is estimated as soon as its definition is completed, using the specified method. The effect of the second option is

that the system can then be referenced by the assigned name for the purposes of the `restrict` and `estimate` commands; in the gretl GUI an additional effect is that an icon for the system is added to the “Session view”.

These two possibilities can be combined, as in

```
msysys <- system method=3sls
```

In this example the system is estimated immediately via Three-Stage Least Squares, and is also available for subsequent use under the name `msysys`.

If the system is not named via the back-arrow mechanism, it is still available for subsequent use via `restrict` and `estimate`; in this case you should use the generic name `$system` to refer to the last-defined multivariate system.

The body of a system block

The most basic element in the body of a `system` block is the `equation` statement, which is used to specify each equation within the system. This takes the same form as the regression specification for single-equation estimators, namely a list of series with the dependent variable given first, followed by the regressors, with the series given either by name or by ID number (order in the dataset). A system block must contain at least two `equation` statements, and for systems without endogenous regressors these statements are all that is required. So, for example, a minimal SUR specification might look like this:

```
system method=sur
  equation y1 const x1
  equation y2 const x2
end system
```

For simultaneous systems it is necessary to determine which regressors are endogenous and which exogenous. By default all regressors are treated as exogenous, except that any variable that appears as the dependent variable in one equation is automatically treated as endogenous if it appears as a regressor elsewhere. However, an explicit list of endogenous regressors may be supplied following the `equations` lines: this takes the form of the keyword `endog` followed by the names or ID numbers of the relevant regressors.

When estimation is via TSLS or 3SLS it is possible to specify a particular set of instruments for each equation. This is done by giving the `equation` lists in the format used with the `tsls` command: first the dependent variable, then the regressors, then a semicolon followed by the instruments, as in

```
system method=3sls
  equation y1 const x11 x12 ; const x11 z1
  equation y2 const x21 x22 ; const x21 z2
end system
```

An alternative way of specifying instruments is to insert an extra line starting with `instr`, followed by the list of variables acting as instruments. This is especially useful for specifying the system with the `equations` keyword; see the following subsection. As in `tsls`, any regressors that are not also listed as instruments are treated as endogenous, so in the example above `x11` and `x21` are treated as exogenous while `x21` and `x22` are endogenous, and instrumented by `z1` and `z2` respectively.

One more sort of statement is allowed in a `system` block: that is, the keyword `identity` followed by an equation that defines an accounting relationship, rather than a stochastic one, between variables. For example,

```
identity Y = C + I + G + X
```

There can be more than one `identity` in a system block. But note that these statements are specific to estimation via FIML; they are ignored for other estimators.

34.2 Equation systems within functions

It is also possible to define a multivariate system in a programmatic way. This is useful if the precise specification of the system depends on some input parameters that are not known in advance, but are given when the script is actually run.

The relevant syntax is given by the `equations` keyword (note the plural), which replaces the block of `equation` lines in the standard form. This keyword must be followed by two arguments. The first is a named list containing all series on the left-hand side of the system, which determines the number of equations in the system. The nature of the second argument depends on whether or not the list of regressors is in common for all equations (as in SUR):

- Common regressors: a second named list.
- Differing regressors: an array of lists, one per equation.

The first case is straightforward; the second requires a little more explanation. Suppose we have a two-equation system with regressors given by the lists `xlist1` and `xlist2`. We can then define a suitable array as follows:

```
lists Xlists = defarray(xlist1, xlist2)
```

(See section 11.8 for alternative ways of building an array.)

Therefore, specifying a system generically in this way just involves building the necessary list arguments, as shown in the following example:

```
open denmark
list LHS = LRM LRY
list RHS1 = const LRM(-1) IBO(-1) IDE(-1)
list RHS2 = const LRY(-1) IBO(-1)
lists RHS = defarray(RHS1, RHS2)
system method=ols
    equations LHS RHS
end system
```

As mentioned above, the option of assigning a specific name to a system is not available within functions, but the generic identifier `$system` can be used to similar effect. The following example illustrates how one can define a system, estimate it via two methods, apply a restriction, then re-estimate it subject to the restriction.

```
function void anonsys(series x, series y)
    system
        equation x const
        equation y const
    end system
    estimate $system method=ols
    estimate $system method=sur
    restrict $system
        b[1,1] - b[2,1] = 0
    end restrict
    estimate $system method=ols
end function
```


34.3 Restriction and estimation

The behavior of the `restrict` command is a little different for multivariate systems as compared with single-equation models.

In the single-equation case, `restrict` refers to the last-estimated model, and once the command is completed the restriction is tested. In the multivariate case, you must give the name of the system to which the restriction is to be applied (or `$system` to refer to the last-defined system), and the effect of the command is just to attach the restriction to the system; testing is not done until the next `estimate` command is given. In addition, in the system case the default is to produce full estimates of the restricted model; if you are not interested in the full estimates and just want the test statistic you can append the `--quiet` option to `estimate`.

A given system restriction remains in force until it is replaced or removed. To return a system to its unrestricted state you can give an empty `restrict` block, as in

```
restrict sysname
end restrict
```

As illustrated above, you can use the `method` tag to specify an estimation method with the `estimate` command. If the system has already been estimated you can omit this tag and the previous method is used again.

The `estimate` command is the main locus for options regarding the details of estimation. The available options are as follows:

- If the estimation method is SUR or 3SLS and the `--iterate` flag is given, the estimator will be iterated. In the case of SUR, if the procedure converges the results are maximum likelihood estimates. Iteration of three-stage least squares, however, does not in general converge on the full-information maximum likelihood results. This flag is ignored for other estimators.
- If the equation-by-equation estimators OLS or TSLS are chosen, the default is to apply a degrees of freedom correction when calculating standard errors. This can be suppressed using the `--no-df-corr` flag. This flag has no effect with the other estimators; no degrees of freedom correction is applied in any case.
- By default, the formula used in calculating the elements of the cross-equation covariance matrix is

$$\hat{\sigma}_{ij} = \frac{\hat{u}_i' \hat{u}_j}{T}$$

where T is the sample size and \hat{u}_i is the vector of residuals from equation i . But if the `--geomean` flag is given, a degrees of freedom correction is applied: the formula is

$$\hat{\sigma}_{ij} = \frac{\hat{u}_i' \hat{u}_j}{\sqrt{(T - k_i)(T - k_j)}}$$

where k_i denotes the number of independent parameters in equation i .

- If an iterative method is specified, the `--verbose` option calls for printing of the details of the iterations.
- When the system estimator is SUR or 3SLS the cross-equation covariance matrix is initially estimated via OLS or TSLS, respectively. In the case of a system subject to restrictions the question arises: should the initial single-equation estimator be restricted or unrestricted? The default is the former, but the `--unrestrict-init` flag can be used to select unrestricted initialization. (Note that this is unlikely to make much difference if the `--iterate` option is given.)

34.4 System accessors

After system estimation various matrices may be retrieved for further analysis. Let g denote the number of equations in the system and let K denote the total number of estimated parameters ($K = \sum_i k_i$). The accessors `$uhat` and `$yhat` get $T \times g$ matrices holding the residuals and fitted values respectively. The accessor `$coeff` gets the stacked K -vector of parameter estimates; `$vcv` gets the $K \times K$ variance matrix of the parameter estimates; and `$sigma` gets the $g \times g$ cross-equation covariance matrix, $\hat{\Sigma}$.

A test statistic for the hypothesis that Σ is diagonal can be retrieved as `$diagtest` and its p-value as `$diagpval`. This is the Breusch-Pagan test except when the estimator is (unrestricted) iterated SUR, in which case it's a Likelihood Ratio test. The Breusch-Pagan test is computed as

$$\text{LM} = T \sum_{i=2}^g \sum_{j=1}^{i-1} r_{ij}^2$$

where $r_{ij} = \hat{\sigma}_{ij} / \sqrt{\hat{\sigma}_{ii}\hat{\sigma}_{jj}}$; the LR test is

$$\text{LR} = T \left(\sum_{i=1}^g \log \hat{\sigma}_i^2 - \log |\hat{\Sigma}| \right)$$

where $\hat{\sigma}_i^2$ is $\hat{u}_i' \hat{u}_i / T$ from the individual OLS regressions. In both cases the test statistic is distributed asymptotically as χ^2 with $g(g-1)/2$ degrees of freedom.

All these quantities can also be retrieved if necessary via the `$system` accessor: after successful completion of the estimation procedure, it will contain a bundle holding various quantities that describe the estimated system.

Structural and reduced forms for forecasting and simulation

Systems of simultaneous systems can be represented in structural form as

$$\Gamma y_t = A_1 y_{t-1} + A_2 y_{t-2} + \cdots + A_p y_{t-p} + B x_t + \epsilon_t$$

where y_t represents the vector of endogenous variables in period t , x_t denotes the vector of exogenous variables, and p is the maximum lag of the endogenous regressors. The structural-form matrices can be retrieved as `$sysGamma`, `$sysA` and `$sysB` respectively, or as elements of the returned `$system` bundle. If y_t is $m \times 1$ and x_t is $n \times 1$, then Γ is $m \times m$ and B is $m \times n$. If the system contains no lags of the endogenous variables then the A matrix is not defined, otherwise A is the horizontal concatenation of A_1, \dots, A_p , and is therefore $m \times mp$.

From the structural form it is straightforward to obtain the reduced form, namely,

$$y_t = \Gamma^{-1} \left(\sum_{i=1}^p A_i y_{t-i} \right) + \Gamma^{-1} B x_t + v_t \quad (34.1)$$

where $v_t \equiv \Gamma^{-1} \epsilon_t$.

As is well known, the reduced form can be used any time one has to calculate the values of the endogenous variables given the exogenous ones; this is typically necessary in two cases: forecasting or simulation.

Forecasts for multi-equation systems are generated natively by `gretl` in response to the `fcast` command. This means that—in contrast to single-equation estimation—the values produced via `fcast` for a static, within-sample forecast will in general differ from the fitted values retrieved via `$yhat`. The fitted values for equation i represent the expectation of y_{ti} conditional on the contemporaneous values of all the regressors, while the `fcast` values are conditional on the exogenous and predetermined variables only.

The above account has to be qualified for the case where a system is set up for estimation via TSLS or 3SLS using a specific list of instruments per equation, as described in section 34.1. In that case it is possible to include more endogenous regressors than explicit equations (although, of course, there must be sufficient instruments to achieve identification). In such systems endogenous regressors that have no associated explicit equation are treated “as if” exogenous when constructing the structural-form matrices. This means that forecasts are conditional on the observed values of the “extra” endogenous regressors rather than solely on the values of the exogenous and predetermined variables.

On the contrary, gretl does not provide a native command for generating simulated data from a multi-equation system, but this is relatively easily accomplished by means of scripting: script 34.1 gives an example on a 3-variable system.¹ All equations contain lagged endogenous variables, but the equation for consumption at time t also contains income at time t as an explanatory variable. This makes the system simultaneous, so we use FIML as the estimation method.

Once the system is estimated, we store its results to a bundle named `sys`, so as to make it easier to retrieve certain quantities used in the remainder of the script.

First, we compute the reduced form matrices by using the `Gamma`, `A` and `B` bundle elements. Of course, simulation needs values for the exogenous variable, which are easy to create in a system such as this where all the exogenous variables are deterministic. The simulation horizon is set for this example at 12 periods.

Subsequently, structural-form disturbances are drawn randomly from a multivariate normal distribution with mean 0 and variance equal to the estimated covariance matrix $\hat{\Sigma}$, available as the `sigma` element of the `sys` bundle. These are then mapped to reduced-form innovations via the relationship $v_t \equiv \Gamma^{-1}\epsilon_t$.

Finally, all these ingredients are combined to produce the simulated values with the `varsimul` function. Note that initial values for the VAR recursion are taken from the latest available data. Running the script should produce the following set of simulated values:

Sim (14 x 3)

13.887	12.874	14.508
13.889	12.877	14.515
13.893	12.880	14.520
13.895	12.885	14.518
13.895	12.894	14.517
13.900	12.902	14.520
13.907	12.908	14.525
13.917	12.910	14.534
13.920	12.911	14.539
13.919	12.906	14.547
13.934	12.910	14.567
13.935	12.908	14.575
13.942	12.913	14.581
13.944	12.916	14.583

¹Note: the system of equations that is being estimated here is not meant to stand for a realistic model of the European economy. It is just set up in such a way to provide a simple example.

Listing 34.1: Simulation from a simultaneous equation system [\[Download ▼\]](#)

```

set verbose off
set seed 131020

### -----
### load the data and generate the variables
### -----

open AWM18.gdt --quiet
Con = log(PCR)
Inv = log(GCR)
Inc = log(YER)
list EX0 = const time

### -----
### estimate the system via FIML
### -----

system method=fiml
    equation Con EX0 Con(-1) Inc(0 to -1)
    equation Inv EX0 Inv(-1) Inc(-1)
    equation Inc EX0 Inc(-1 to -2) Inv(-1)
end system

bundle sys = $system    # save the estimated system to a bundle

### -----
### compute the reduced form VAR representation
### -----

matrix iG = inv(sys.Gamma)
matrix rfA = iG * sys.A
matrix rfB = iG * sys.B

### -----
### produce the simulation
### -----

scalar horizon = 12

### retrieve a few magnitudes from the estimated system
scalar g = sys.neqns          # number of equations
scalar p = cols(sys.A) / g    # maximum lag

### future values of the exogenous variable
matrix SimExo = 1 ~ seq($nobs + 1, $nobs + horizon)'
matrix X = SimExo * rfB'

### simulated disturbances
E = mnormal(horizon, g) * cholesky(sys.sigma)' # reduced form disturbances
V = E * iG'                                     # structural form disturbances

### initial values
list ENDO = Con Inv Inc
matrix init = {ENDO}[$nobs-p+1:,]

### perform simulation
Sim = varsimul(rfA, X + V, init)

print Sim

```

Chapter 35

Forecasting

35.1 Introduction

In some econometric contexts forecasting is the prime objective: one wants estimates of the future values of certain variables to reduce the uncertainty attaching to current decision making. In other contexts where real-time forecasting is not the focus prediction may nonetheless be an important moment in the analysis. For example, out-of-sample prediction can provide a useful check on the validity of an econometric model. In other cases we are interested in questions of “what if”: for example, how might macroeconomic outcomes have differed over a certain period if a different policy had been pursued? In the latter cases “prediction” need not be a matter of actually projecting into the future but in any case it involves generating fitted values from a given model. The term “postdiction” might be more accurate but it is not commonly used; we tend to talk of prediction even when there is no true forecast in view.

This chapter offers an overview of the methods available within gretl for forecasting or prediction (whether forward in time or not) and explicates some of the finer points of the relevant commands.

35.2 Saving and inspecting fitted values

In the simplest case, the “predictions” of interest are just the (within sample) fitted values from an econometric model. For the single-equation linear model, $y_t = X_t\beta + u_t$, these are $\hat{y}_t = X_t\hat{\beta}$.

In command-line mode, the \hat{y} series can be retrieved, after estimating a model, using the accessor `$yhat`, as in

```
series yh = $yhat
```

If the model in question takes the form of a system of equations, `$yhat` returns a matrix, each column of which contains the fitted values for a particular dependent variable. To extract the fitted series for, e.g., the dependent variable in the second equation, do

```
matrix Yh = $yhat
series yh2 = Yh[,2]
```

Having obtained a series of fitted values, you can use the `fcstats` function to produce a vector of statistics that characterize the accuracy of the predictions (see section [35.4](#) below).

The gretl GUI offers several ways of accessing and examining within-sample predictions. In the model display window the Save menu contains an item for saving fitted values, the Graphs menu allows plotting of fitted versus actual values, and the Analysis menu offers a display of actual, fitted and residual values.

35.3 The `fcast` command

The `fcast` command (and its equivalent GUI invocation, see below) generates predictions based on the last estimated model. Several questions arise here: How to control the range over which predictions are generated? How to control the forecasting method (where a choice is available)? How to control the printing and/or saving of the results? Basic answers can be found in the *Gretl Command Reference*; we add some more details here.

The forecast range

The range defaults to the currently defined sample range. If this remains unchanged following estimation of the model in question, the forecast will be “within sample” and (with some qualifications noted below) it will essentially duplicate the information available via the retrieval of fitted values (see section 35.2 above).

A common situation is that a model is estimated over a given sample and then forecasts are wanted for a subsequent out-of-sample range. The simplest way to accomplish this is via the `--out-of-sample` option to `fcast`. For example, assuming we have a quarterly time-series dataset containing observations from 1980:1 to 2008:4, four of which are to be reserved for forecasting:

```
# reserve the last 4 observations
smpl 1980:1 2007:4
ols y 0 xlist
fcast --out-of-sample
```

This will generate a forecast from 2008:1 to 2008:4.

There are two other ways of adjusting the forecast range, offering finer control:

- Use the `smpl` command to adjust the sample range prior to invoking `fcast`.
- Use the optional *startobs* and *endobs* arguments to `fcast` (which should come right after the command word). These values set the forecast range independently of the sample range.

What if one wants to generate a true forecast that goes beyond the available data? In that case one can use the `dataset` command with the `addobs` parameter to add extra observations before forecasting. For example:

```
# use the entire dataset, which ends in 2008:4
ols y 0 xlist
dataset addobs 4
fcast 2009:1 2009:4
```

But this will work as stated only if the set of regressors in `xlist` does not contain any stochastic regressors other than lags of `y`. The `dataset addobs` command attempts to detect and extrapolate certain common deterministic variables (e.g., time trend, periodic dummy variables). In addition, lagged values of the dependent variable can be supported via a dynamic forecast (see below for discussion of the static/dynamic distinction). But “future” values of any other included regressors must be supplied before such a forecast is possible. Note that specific values in a series can be set directly by date, for example: `x1[2009:1] = 120.5`. Or, if the assumption of no change in the regressors is warranted, one can do something like this:

```
loop t=2009:1..2009:4
  loop foreach i xlist
    $i[t] = $i[2008:4]
  endloop
endloop
```

In single-equation OLS models a `--recursive` forecast option is also available, expanding the estimation sample one-by-one and re-calculating the forecasts again and again for the constantly updated information set. In this case a number must be given of how many periods ahead should be forecast for each of the estimation samples. Note that only this *k*-steps-ahead forecast will be printed (or accessible in `$fcast`), not the interim values from step 1 through *k* – 1 (if *k* > 1). If those interim values are also needed, then several `fcast ... --recursive` rounds would have to be done with different steps-ahead numbers.

Static and dynamic forecasts

The distinction between static and dynamic forecasts applies only to dynamic models, i.e., those that feature one or more lags of the dependent variable. The simplest case is the AR(1) model,

$$y_t = \alpha_0 + \alpha_1 y_{t-1} + \epsilon_t \quad (35.1)$$

In some cases the presence of a lagged dependent variable is implicit in the dynamics of the error term, for example

$$\begin{aligned} y_t &= \beta + u_t \\ u_t &= \rho u_{t-1} + \epsilon_t \end{aligned}$$

which implies that

$$y_t = (1 - \rho)\beta + \rho y_{t-1} + \epsilon_t$$

Suppose we want to forecast y for period s using a dynamic model, say (35.1) for example. If we have data on y available for period $s - 1$ we could form a fitted value in the usual way: $\hat{y}_s = \hat{\alpha}_0 + \hat{\alpha}_1 y_{s-1}$. But suppose that data are available only up to $s - 2$. In that case we can apply the chain rule of forecasting:

$$\begin{aligned} \hat{y}_{s-1} &= \hat{\alpha}_0 + \hat{\alpha}_1 y_{s-2} \\ \hat{y}_s &= \hat{\alpha}_0 + \hat{\alpha}_1 \hat{y}_{s-1} \end{aligned}$$

This is what is called a dynamic forecast. A static forecast, on the other hand, is simply a fitted value (even if it happens to be computed out-of-sample).

Printing, displaying, and saving forecasts

When working from the GUI, the way to perform and access forecasts is to first estimate a model with some inherently dynamic features, and then in the model window navigate to the Forecasts entry in the Analysis menu. If some out-of-sample observations are already available (see above) a dialog window is presented where the discussed forecasting options can be chosen by pointing and clicking. Executing the forecasts then automatically yields two result windows: one with a time-series plot of the forecasts along with their confidence bands (if those were chosen), and another one with tabular output.

The produced plot can be saved to the current session or exported like any other plot in gretl by right-clicking. Notice that in the textual result window there is a “+” button at the top which offers to save the point forecasts and their standard errors as new series to the active dataset.

In a command line context the `fcast` command automatically prints out the tables with the produced forecasts, their standard errors, and associated confidence intervals—unless you wish to suppress this verbose output with the options `--stats-only` or `--quiet`. The former option restricts output to the forecast evaluation statistics as explained in the next section; the latter option silences output altogether. Another accepted syntax variant is to supply the name of a new series for the point forecasts after the `fcast` command, as for example in `fcast Yfc --out-of-sample`. At the same time this also suppresses printout.

Accessing and saving the produced forecast time series along with the estimated standard errors also works through the `$fcast` and `$fcse` accessors available after `fcast` execution. These return vectors as gretl matrix objects, not series, so if you want to add the results to the dataset in this way you would have to set the active sample to the forecast range first. (You can of course first access and store the matrices and then later after resetting the sample assign them to series.) Note that the estimated standard errors do not incorporate parameter uncertainty in the case of dynamic models.

But if you want to create forecast plots within a script the relevant option already has to be appended to the `fcast` command. As explained in the command reference, specify `--plot=<filename>`

(without the < > symbols) to save the plot file directly to disc, namely by default to the active working directory if no full path is specified.¹

35.4 Univariate forecast evaluation statistics

Let y_t be the value of a variable of interest at time t and let f_t be a forecast of y_t . We define the forecast error as $e_t = y_t - f_t$. Given a series of T observations and associated forecasts we can construct several measures of the overall accuracy of the forecasts. Some commonly used measures are the Mean Error (ME), Root Mean Squared Error (RMSE), Mean Absolute Error (MAE), Mean Percentage Error (MPE) and Mean Absolute Percentage Error (MAPE). These are defined as follows.

$$\begin{aligned} \text{ME} &= \frac{1}{T} \sum_{t=1}^T e_t & \text{RMSE} &= \sqrt{\frac{1}{T} \sum_{t=1}^T e_t^2} & \text{MAE} &= \frac{1}{T} \sum_{t=1}^T |e_t| \\ \text{MPE} &= \frac{1}{T} \sum_{t=1}^T 100 \frac{e_t}{y_t} & \text{MAPE} &= \frac{1}{T} \sum_{t=1}^T 100 \left| \frac{e_t}{y_t} \right| \end{aligned}$$

A further relevant statistic is Theil's U , of which there are two variants: U_1 [Theil \(1961\)](#) and U_2 [\(Theil, 1966\)](#). The first is defined thus

$$U_1 = \left[\frac{1}{T} \sum_{t=1}^T (y_t - f_t)^2 \right]^{0.5} \cdot \left[\left(\frac{1}{T} \sum_{t=1}^T y_t^2 \right)^{0.5} + \left(\frac{1}{T} \sum_{t=1}^T f_t^2 \right)^{0.5} \right]^{-1}$$

and is bounded by 0 and 1. Value close to zero indicate high forecast accuracy; U_1 approaches 1 as the forecast errors grow arbitrarily large. The second is defined as the positive square root of

$$U_2^2 = \frac{1}{T} \sum_{t=1}^{T-1} \left(\frac{f_{t+1} - y_{t+1}}{y_t} \right)^2 \cdot \left[\frac{1}{T} \sum_{t=1}^{T-1} \left(\frac{y_{t+1} - y_t}{y_t} \right)^2 \right]^{-1}$$

U_2 depends on the data having a natural ordering and is applicable only for time series data. It can be interpreted as the ratio of the RMSE of the proposed forecasting model to the RMSE of a naïve model which simply predicts $y_{t+1} = y_t$ for all t . The naïve model yields $U_2 = 1$; values less than 1 indicate an improvement relative to this benchmark and values greater than 1 a deterioration.

In addition, Theil (1966, pp. 33-36) proposed a decomposition of the MSE which can be useful in evaluating a set of forecasts. He showed that the MSE could be broken down into three non-negative components as follows

$$\text{MSE} = (\bar{f} - \bar{y})^2 + (s_f - r s_y)^2 + (1 - r^2) s_y^2$$

where \bar{f} and \bar{y} are the sample means of the forecasts and the observations, s_f and s_y are the respective standard deviations (using T in the denominator), and r is the sample correlation between y and f . Dividing through by MSE we get

$$\frac{(\bar{f} - \bar{y})^2}{\text{MSE}} + \frac{(s_f - r s_y)^2}{\text{MSE}} + \frac{(1 - r^2) s_y^2}{\text{MSE}} = 1 \quad (35.2)$$

Theil labeled the three terms on the left-hand side of (35.2) the bias proportion (U^M), regression proportion (U^R) and disturbance proportion (U^D), respectively. If y and f represent the in-sample observations of the dependent variable and the fitted values from a linear regression then the first two components, U^M and U^R , will be zero (apart from rounding error), and the entire MSE will be accounted for by the unsystematic part, U^D . In the case of out-of-sample prediction, however (or

¹Being a single plot, this is currently not available for forecasts based on multiple equation systems. If the path contains spaces it must be enclosed in quotes.

“prediction” over a sub-sample of the data used in the regression), U^M and U^R are not necessarily close to zero. U^M differs from zero if and only if the mean of the forecasts differs from the mean of the realizations, and U^R is non-zero if and only if the slope of a simple regression of the realizations on the forecasts differs from 1.

The above-mentioned statistics are printed as part of the output of the `fcast` command. They can also be retrieved in the form of a column vector using the function `fcstats`, which takes two series arguments corresponding to y and f . The vector returned is

$$\left(\text{ME} \quad \text{RMSE} \quad \text{MAE} \quad \text{MPE} \quad \text{MAPE} \quad U \quad U^M \quad U^R \quad U^D \right)'$$

where U is U_2 for time series data, U_1 otherwise. (Note that the MSE is not included since it can easily be obtained given the RMSE.) The series given as arguments to `fcstats` must not contain any missing values in the current sample range; use the `smp1` command to adjust the range if needed. See the *Gretl Command Reference* for more detail on `fcstats`.

35.5 Forecasts based on VAR models

The interface for forecasting from a VAR is similar to that for a single equation. Here's an example via scripting. The code:

```
# open sample data file
open sw_ch14.gdt --quiet
# generate the "inflation" series
series INFL = 100 * sdiff(log(PUNEW))
# put last year aside for out-of-sample forecast
smp1 ; -4
# estimate a 5-lag VAR
var 5 LHUR INFL --silent
# store fitted values (note: result is a 2-column matrix)
YH = $yhat
# perform out-of-sample forecast (both versions)
fcast LHUR --static --out-of-sample
# note that omission of the variable specification means "all"
fcast --dynamic --out-of-sample
```

yields

For 95% confidence intervals, $t(140, 0.025) = 1.977$

	LHUR	prediction	std. error	95% interval
1999:1	4.300000	4.335004	0.222784	3.894549 - 4.775460
1999:2	4.300000	4.243244	0.222784	3.802788 - 4.683699
1999:3	4.233333	4.290981	0.222784	3.850525 - 4.731436
1999:4	4.100000	4.178030	0.222784	3.737575 - 4.618486

Forecast evaluation statistics

Mean Error	-0.028481
Root Mean Squared Error	0.058861
Mean Absolute Error	0.05686
Mean Percentage Error	-0.68977
Mean Absolute Percentage Error	1.3497
Theil's U2	0.75027
Bias proportion, UM	0.23414
Regression proportion, UR	0.0081804
Disturbance proportion, UD	0.75768

For 95% confidence intervals, $t(140, 0.025) = 1.977$

	LHUR	prediction	std. error	95% interval
1999:1	4.300000	4.335004	0.222784	3.894549 - 4.775460
1999:2	4.300000	4.312724	0.401960	3.518028 - 5.107421
1999:3	4.233333	4.272764	0.539582	3.205982 - 5.339547
1999:4	4.100000	4.223213	0.642001	2.953943 - 5.492482

Forecast evaluation statistics

Mean Error	-0.052593
Root Mean Squared Error	0.067311
Mean Absolute Error	0.052593
Mean Percentage Error	-1.2616
Mean Absolute Percentage Error	1.2616
Theil's U2	0.87334
Bias proportion, UM	0.61049
Regression proportion, UR	0.29203
Disturbance proportion, UD	0.097478

	INFL	prediction	std. error	95% interval
1999:1	1.651245	1.812250	0.431335	0.959479 - 2.665022
1999:2	2.048545	2.088185	0.777834	0.550366 - 3.626004
1999:3	2.298952	2.266445	1.075855	0.139423 - 4.393467
1999:4	2.604836	2.610037	1.409676	-0.176969 - 5.397043

Forecast evaluation statistics

Mean Error	-0.043335
Root Mean Squared Error	0.084525
Mean Absolute Error	0.059588
Mean Percentage Error	-2.6178
Mean Absolute Percentage Error	3.3248
Theil's U2	0.095932
Bias proportion, UM	0.26285
Regression proportion, UR	0.45311
Disturbance proportion, UD	0.28404

One of the main differences is that specifying a variable name after the `fcast` command does not mean to save something under that name, but now it serves to pick one of the N variables of the VAR for printing out the forecasts. That leaves only the `$fcast` and `$fcse` accessors to obtain and save the produced forecasts—in this system case the returned matrix objects will have as many columns as equations.

In the GUI the relevant menu entry is again Forecasts in the Analysis menu in the window of the estimated VAR model. Here the user must pick the variable of interest, after which a dialog window with relevant options is presented. As in the single-equation context a plot and a textual output windows are created. Again, forecast series can be added to the dataset through the “+” button, and the plot can be saved or exported.

Special VAR cases: exogenous variables, cointegration

It may be worth noting that when a VAR is specified with additional (non-deterministic) exogenous regressors a similar issue as with single equations arises: the forecast is conditional and requires some assumptions about the development of those regressors out of sample. As before, these

values can be easily filled in after the dataset has been extended with the observations for the forecasting sample, but naturally only the user, not gretl, can and must decide what those values should be. This includes hand-crafted deterministic variables like shift dummies; but on the other hand standard deterministic terms like trends and seasonals will be extrapolated by gretl automatically.

Using a cointegrated VAR model with gretl's `vecm` command does not change the way a forecast is obtained afterwards. The VECM can be internally represented as a VAR (in levels) that automatically contains the reduced-rank restrictions of cointegration, and this VAR form is then used to calculate the forecasts. Providing forecast standard errors and the associated confidence bands is also straightforward since only the innovation uncertainty is captured in those. This ease of use also carries over to the situation when a VECM with additional exogenous terms is used for forecasting—provided that future values of the exogenous variables are specified, of course.

35.6 Forecasting from simultaneous systems

To be interesting for a forecasting application, a simultaneous-equation system must be dynamic, including some lags of endogenous variables as regressors. Otherwise we would be conducting a scenario analysis purely conditional on assumed exogenous developments. For the following discussion we therefore presuppose that we are dealing with such a dynamic system. Then the difference between such a model set up with gretl's `system` block and a VAR system concerns mainly two aspects: First, a VAR model is already given as a so-called reduced form and as such is ready to be used for forward simulation a.k.a. forecasting. In contrast, a simultaneous system can come in a structural form with some contemporaneous endogenous variables as regressors in the equations; the future values of those regressors are unknown, however. Second, a plain VAR is estimated by OLS, whereas a simultaneous system can be estimated with different methods for reasons of efficiency.

Neither of these differences present any deep challenge for forecasting, however.

- As explained at the end of the previous chapter on multivariate models (see the subsection titled “Structural and reduced forms”), it is easy to obtain the reduced form of any such simultaneous equation system. This reduced form is used by gretl to simulate the system forward in time, just as with a VAR model. The slight complication for computing the forecast variances is merely that the estimated error term ϵ_t from the structural form must be mapped to the reduced-form innovations v_t using the (inverse of the) estimated structural relations matrix Γ . This is automatically taken into account.
- The estimation method through which the coefficient values of the system are determined does not matter for forecasting. The prediction algorithm can simply take these point estimates as given, use these for calculating the associated reduced form, and use that representation to iterate the model forward over the desired forecasting horizon. It should nonetheless be obvious that different estimators entail different forecast values.

As a consequence of these considerations, the way to handle forecasts from simultaneous systems in gretl is exactly as discussed before in the context of VARs (possibly with exogenous regressors). This applies to the command-line interface as well as the GUI.

Chapter 36

State Space Modeling

36.1 Introduction

This chapter describes the handling of linear state space models in gretl 2022b and higher.¹ Here is a brief high-level overview of gretl's Kalman apparatus.

- To obtain a Kalman structure—in the form of a bundle—you use the `ksetup` function.
- Having obtained such a bundle you can then adjust its contents, as described in detail below.
- You then “do things” with your state space model via the functions `kfilter` (forecasting), `ksmooth` (state smoothing), `kdsmooth` (disturbance smoothing), and/or `ksimul` (simulation).

36.2 Notation

In this document our basic representation of a state space model is given by the following pair of equations:

$$y_t = Z_t \alpha_t + \varepsilon_t \quad (36.1)$$

$$\alpha_{t+1} = T_t \alpha_t + \eta_t \quad (36.2)$$

where (36.1) is the observation or measurement equation and (36.2) is the state transition equation. The state vector, α_t , is $(r \times 1)$ and the vector of observables, y_t , is $(n \times 1)$. The $(n \times 1)$ vector ε_t and the $(r \times 1)$ vector η_t are assumed to be vector Gaussian white noise:

$$E(\varepsilon_t \varepsilon_s') = \Sigma_t \text{ for } t = s, \text{ otherwise } \mathbf{0}$$

$$E(\eta_t \eta_s') = \Omega_t \text{ for } t = s, \text{ otherwise } \mathbf{0}$$

The number of time-series observations is denoted by N . In the case where $Z_t = Z$, $T_t = T$, $\Sigma_t = \Sigma$ and $\Omega_t = \Omega$ for all t the model is said to be *time-invariant*. We assume time-invariance in much of what follows but discuss the time-varying case—along with other extensions of the basic model—in section 36.9.

36.3 Defining the model as a bundle

The `ksetup` function is used to initialize a state space model by specifying only its indispensable elements: the observables and their link to the unobserved state vector, plus the law of motion for the latter and the covariance matrix of its innovations. Therefore, the function takes a minimum of four arguments. The corresponding bundle keys are as follows:

¹The user interface was substantially different prior to version 2017a. For example, be aware that Lucchetti (2011) is based on the old syntax. If anyone needs documentation for the original interface it can be found at http://gretl.sourceforge.net/papers/kalman_old.pdf. Additional functionality relating to “exact diffuse” initialization of the Kalman filter was added in version 2022b.

Symbol	Dimensions	Reserved key
y	$N \times n$	<code>obsy</code>
Z	$n \times r$	<code>obsymat</code>
T	$r \times r$	<code>statemat</code>
Ω	$r \times r$	<code>statevar</code>

☞ Please note that the matrix Z in the observation equation must be given in *transposed* form. This is required to preserve compatibility with gretl versions prior to 2022a. Correspondingly, if you retrieve this matrix using its key, `obsymat`, it's the transpose you actually obtain.

The names of these input matrices don't matter; in fact they may be anonymous matrices constructed on the fly. But if and when you wish to copy them out of the bundle you must use the specified keys, as in

```
matrix Z = SSmod.obsymat'
matrix T = SSmod.statemat
```

Although all the arguments are in principle matrices, as a convenience you may give `obsy` as a series or list of series, and the other arguments can be given as scalars if in context they are 1×1 .

If applicable you may specify any of the following optional input matrices:²

Symbol	Dimensions	Key	If omitted...
Σ	$n \times n$	<code>obsvar</code>	no disturbance term in observation equation
α_0	$r \times 1$	<code>inistate</code>	α_0 is a zero vector
P_0	$r \times r$	<code>inivar</code>	P_0 is set automatically

These matrices are not passed to `ksetup`, rather you add them to the bundle returned by `ksetup` (under their reserved keys) as you usually add elements to a bundle, for example:

```
SSmod.obsvar = Veps
```

Naturally, the arguments you pass to `ksetup` must have mutually compatible dimensions, otherwise an error is returned. Once setup is complete the dimensions of the model— r , n and N —become available as scalar members of the bundle (under their own names).

In case `inivar` is not specified the matrix $P_{1|0}$ will be automatically initialized by gretl only if all the eigenvalues of T lie inside the unit circle and the model is stationary. In this case the variance for the marginal distribution of α_t is well defined and the initializer is computed using

$$\text{vec}(P_{1|0}) = [I - T \otimes T]^{-1} \text{vec}(\Omega)$$

If the above condition is not satisfied you will have to make a choice on which technique to use for “diffuse” initialization.

In Section 36.8 we provide a fuller discussion of the various options, but here's what is probably the bottom line for many users. In earlier versions of gretl a rather crude solution was adopted, initializing $P_{1|0}$ to a “numerically large” matrix. This was accomplished by setting a value of 1 on the bundle under the (reserved) key `diffuse`. From gretl version 2022b on, if you have scripts where you set `diffuse=1` on your Kalman bundle you can now try `diffuse=2` instead. This invokes the new “exact initial” method for state space models with a diffuse initializer. Don't expect identical results from the new code, but to the extent results differ the new ones should be somewhat more accurate. (If results differ wildly you've probably found a bug; please report it!) You may also find that the new code is faster; it should be less likely to get hung up on numerical problems that delay or prevent convergence of ML estimation.

²Additional optional matrices are described in section 36.9 below.

36.4 Special features of state-space bundles

A bundle created by `ksetup` works in most ways like any other `gretl` bundle but some differences should be noted. With an ordinary bundle you can replace or delete members at will; with a state-space bundle there are certain constraints.

- You can replace the coefficient matrices `obsymat`, `statemat`, `statevar` and (if applicable) `obsvar` in a given bundle if you wish—but only on condition that the replacement matrix has the same dimensions as the original. In other words, the dimensions r and n are set once and for all by the `ksetup` call (section 36.3).
- You can replace the data matrix `obsy` subject to the condition that the number of columns, n , is unchanged; the time-series length, N , is mutable.
- None of the input matrices just mentioned can be deleted from the bundle.
- Output matrices that are automatically added to the bundle by the functions described in the following sections *can* be deleted (if you don't need them and want to save on storage). But they cannot be replaced by arbitrary user content under the same key.
- The only other “special” member that can be deleted is the function call (string) that is discussed in section 36.9.

Nonetheless, in the “user area” of the bundle (that is, under keys other than the reserved ones noted in this chapter) the usual rules apply.

For all the “k” functions described below the first argument (and in most cases the only argument) must be a pointer to a bundle obtained via `ksetup`. Any old bundle will not do. A “pointer to bundle” is specified by prefixing the name of the bundle with an ampersand, as in “&SSmod”. Passing the argument in this form allows these functions to modify the content of the bundle.

36.5 The `kfilter` function

Once a model is established as described in the previous section, `kfilter` can be used to run a forward, forecasting pass. This function takes a single argument, namely a bundle-pointer, and it returns a scalar code: 0 for successful completion or non-zero if numerical problems were encountered. The forward iteration is as follows.

$$\begin{aligned} v_t &= y_t - Z_t \alpha_t \\ F_t &= Z_t P_t Z_t' + \Sigma_t \\ M_t &= T_t P_t Z_t' \\ \alpha_{t+1} &= T_t \alpha_t + K_t v_t \\ P_{t+1} &= T_t P_t T_t' + \Omega_t - C_t \end{aligned}$$

where $K_t = M_t F_t^{-1}$ is the Kalman gain, and $C_t = M_t F_t^{-1} M_t'$.

On successful completion several elements are added to the input bundle (or updated if they're already present). A scalar under the key `lnl` gives the overall loglikelihood under the joint normality assumption,

$$\ell = -\frac{1}{2} \left[nN \log(2\pi) + \sum_{t=1}^N \log |F_t| + \sum_{t=1}^N v_t' F_t^{-1} v_t \right]$$

while the key `llt` gives access to a N -vector, element t of which is

$$\ell_t = -\frac{1}{2} \left[n \log(2\pi) + \log |F_t| + v_t' F_t^{-1} v_t \right]$$

In addition the scalar `s2` holds the scale factor,

$$\hat{\sigma}^2 = \frac{1}{nN - d} \sum_{t=1}^N v_t' F_t^{-1} v_t$$

where d denotes the number of elements in the state vector subject to a diffuse initialization. This is as in SsfPack 2.2 (Koopman *et al.*, 1999).

Five additional matrices also become available. Each of these has N rows, one for each time-step; the contents of the rows are as follows.

1. Forecast errors for the observable variables, v_t' , n columns: key `prederr`.
2. Variance matrix for the forecast errors, $\text{vech}(F_t)'$, $n(n+1)/2$ columns: key `pevar`.
3. Estimate of the state vector, $\hat{\alpha}_{t|t-1}'$, r columns: key `state`.
4. MSE of estimate of the state vector, $\text{vech}(P_{t|t-1})'$, $r(r+1)/2$ columns: key `stvar`.
5. Kalman gain, $\text{vec}(K_t)'$, rn columns: key `gain`.

The Kalman gain is rarely required by the user as such. However, since it is a key quantity in the filtering algorithm we make it available under a dedicated key for diagnostic purposes in case numerical problems should arise. For example, the following retrieves the gain after a filtering operation:

```
kfilter(&SSmod)
matrix G = SSmod.gain
```

Then if you want to retrieve, for example, the matrix K at time 10, you need to reshape the tenth row of `G` into the appropriate dimensions:

```
matrix K10 = mshape(G[10,], SSmod.r, SSmod.n)
```

36.6 The `ksmooth` function

Like `kfilter` this function takes a single bundle-pointer argument and returns an integer error code (0 indicating success). It runs a forward, filtering pass followed by a backward pass which computes a smoothed estimate of the state and its MSE using the method of Anderson and Moore.

Note that since `ksmooth` starts with a forward pass, it can be run without a prior call to `kfilter`. This may appear to be useless duplication, but in fact it enables an efficient scripting option. The main utility of the forward pass lies in the calculation of the log-likelihood in the context of estimation, but if a state space model contains no parameters that have to be estimated, the model setup can be followed directly by a call to `ksmooth`. (And the same goes for `kdsMOOTH` below.)

The backward-pass algorithm is as follows: for $t = N, \dots, 1$

$$\begin{aligned} L_t &= T_t - K_t Z_t' \\ u_{t-1} &= Z_t F_t^{-1} v_t + L_t' u_t \\ U_{t-1} &= Z_t F_t^{-1} Z_t' + L_t' U_t L_t \\ \hat{\alpha}_{t|T} &= \hat{\alpha}_{t|t-1} + P_{t|t-1} u_{t-1} \\ P_{t|T} &= P_{t|t-1} - P_{t|t-1} U_{t-1} P_{t|t-1} \end{aligned}$$

with initial values $u_N = 0$ and $U_N = 0$.

On successful completion all the quantities computed by `kfilter` are available as bundle members (see section 36.5), but the keys `state` and `stvar` now give the smoothed estimates. That is, row t of the `state` matrix holds $\hat{\alpha}_{t|T}'$ and row t of `stvar` holds $P_{t|T}$, in transposed `vech` form with $r(r+1)/2$ elements.

36.7 The ksmooth function

As with `ksmooth`, this function requires a bundle-pointer argument and returns an integer error code (0 indicating success). It runs a forward, filtering pass followed by a backward pass which computes a smoothed estimate of the disturbances along with a dispersion measure, using the methods described in [Koopman \(1993\)](#) and [Koopman et al. \(1999\)](#).

Upon successful execution of the function the bundle will contain under the key `smdist` an $N \times (r + n)$ matrix holding smoothed estimates of η_t and ε_t . That is, a matrix whose t -th row contains

$$(\hat{\eta}'_t, \hat{\varepsilon}'_t) = E[(\eta'_t, \varepsilon'_t) | \mathcal{Y}_1, \dots, \mathcal{Y}_T]$$

(This assumes the observation equation has a stochastic component; if it does not, then `smdist` is just $N \times r$.) Once the smoothed disturbances are obtained the smoothed state can be calculated quickly and easily, so a call to `ksmooth` updates the `state` member of the bundle passed as argument. However, the variance of the state (`stvar`) is *not* updated by `ksmooth`; only `ksmooth` does that.

An associated dispersion measure is provided under the key `smdisterr`. The precise definition of this matrix depends on a second, optional Boolean parameter. Before describing the action of this parameter we need to give a brief account of the two variance measures that are found in the literature on disturbance smoothing. Our account runs in terms of the state disturbance, η_t , but it applies equally to the observation disturbance, ε_t , if present.

Two measures of variance

One measure of variance is the mean square distance of the inferred disturbances from zero (that is, from their unconditional expectation). Let us call this $V_t^{(1)}$:

$$V_t^{(1)} = E(\hat{\eta}_t \hat{\eta}'_t)$$

This measure is used in computing the so-called *auxiliary residuals*, which are advocated in [Durbin and Koopman \(2012\)](#) as useful diagnostic tools. Auxiliary residuals for the state equation are obtained by dividing $\hat{\eta}_t$ by the square roots of the associated diagonal elements of $V_t^{(1)}$. In computing this matrix we use the formulae given in [Koopman et al. \(1999, section 4.4\)](#).

A second measure of variance is the mean squared distance of the inferred disturbances from their true values, or in other words the mean squared error, which we'll write as $V_t^{(2)}$.

$$V_t^{(2)} = E[(\hat{\eta}_t - \eta_t)(\hat{\eta}_t - \eta_t)' | \mathcal{Y}_1, \dots, \mathcal{Y}_T]$$

We calculate this matrix using the formulae given in [Durbin and Koopman \(2012, section 4.5.2\)](#). Its diagonal elements can be used to form confidence intervals for the true disturbances.

We are now ready to state what `gretl` provides under the key `smdisterr`. If the optional second argument to `ksmooth` is present and non-zero the results are based on $V_t^{(2)}$, otherwise (that is, by default) they are based on $V_t^{(1)}$. In either case row t of `smdisterr` contains the square roots of the diagonal elements of the matrix in question: the first r elements pertain to the state disturbances and the following n elements to the observation equation (if applicable). Like `smdist`, `smdisterr` has N rows and either $r + n$ or just r columns depending on whether or not there's a disturbance term in the observation equation. We return standard deviations rather than variances since most of the time it's the former that users will actually want.

Section [36.12](#) presents a script which exercises the disturbance smoother and illustrates the difference between $V_t^{(1)}$ and $V_t^{(2)}$.

36.8 Diffuse initialization of the state vector

We describe a state space model as “diffuse” if it is impossible to pin down the variance of α_t , which is usually denoted by P_t . This may happen either because the model is non-stationary (in

which case P_t is not even defined) or simply out of lack of information.

In that case there are two possible approaches. The “traditional” one, used by gretl up to version 2022a, is to ascribe a very large variance to the initial P_t , as in $P_0 = \kappa \times I_r$ where κ is, say, 10^7 . You can impose this diffuse prior by setting

```
SSmod.diffuse = 1
```

In some cases this strategy may lead to numerical problems. It may then be helpful to specify a diffuse initializer via `inivar` using a somewhat smaller value of κ , as in

```
SSmod.inivar = 1.0e5 * I(stdim)
```

where `stdim` is the dimension of the state.

While the “ $\kappa \times I$ ” approach works fairly well in many cases it is nowadays generally deprecated in favor of one or other “exact initial” method. Such methods depend on derivation of the properties of the Kalman filter (and smoother) in the limit, as the aforementioned “very large” variance tends to infinity. In libgretl we have implemented two such methods: the “univariate approach to multivariate observable” advocated by Durbin and Koopman (2012) and the augmented Kalman method set out by de Jong (1991) and de Jong and Chu-Chun-Lin (2003).³ We’ll refer to them via the labels `univariate` and `dejong`, respectively.

Exact diffuse methods

The `univariate` approach handles a vector observable by “unpacking” it and substituting scalar calculations for matrix ones so far as possible. Durbin and Koopman claim it is faster than the alternatives. It is also able to deal in a straightforward way with incomplete observations (where some but not all elements of y_t are missing at time t): it can utilize any non-missing elements while ignoring the missing ones. However, it runs into complications if (a) the variance matrix of the observation disturbances is not diagonal, and/or (b) the disturbances are correlated between the state and observation equations. Case (a) can be handled at the cost of some extra preliminary computation—transforming y and Z to induce a diagonal variance matrix—and this is automatically carried out by gretl if needed. Handling case (b) is more bothersome, requiring augmentation of the state; at present this is not supported in gretl.

The `dejong` approach has no problem with the variance cases (a) and (b) mentioned above. However, it’s not clear how incomplete observations can be handled and at present observations with any missing elements are ignored.

In short, there are cases where `univariate` may work best, and other cases that are not handled by `univariate` but where `dejong` works fine. Hence our decision to implement both methods.

Table 36.1 sets out the various cases that arise via combination of “code” (where `legacy` indicates the Kalman code as of gretl 2022a) and “diffuse status” (i.e. whether the model is diffuse, and if so how it is handled). (Note that although the primary virtue of `univariate` and `dejong` is their handling of the exact diffuse case, these methods can handle the non-diffuse case and the traditional “ κ -diffuse” case).

The case used depends on various points, the primary one being the `diffuse` integer member of the state space bundle, which defaults to 0 but can be set to 1 or 2.

- `diffuse=0`: case 1 is the default (for backward compatibility) but case 4 or 7 can be selected, by adding `univariate=1` or `dejong=1` to the bundle.
- `diffuse=1`: case 2 is the default but case 5 or 8 can be selected as above.

³The first of these is used in the KFAS package for R (Helske, 2017) and the second by the `sspace` command in Stata. See <https://www.stata.com/manuals/tsspace.pdf>.

	non-diffuse	κ -diffuse	exact diffuse
code	diffuse=0	diffuse=1	diffuse=2
legacy	1	2	–
univariate	4	5	6
dejong	7	8	9

Table 36.1: Cross-tabulation of code-path and diffuse status. Numbers in cells are used for reference in the text; “legacy” indicates gretl 2022a or earlier.

- diffuse=2: the default is 6 but can be switched to 9 via `dejong=1`.

For cases in the same column—namely {1,4,7}, {2,5,8} and {6,9}—results from `kfilter()`, `ksmooth()` and `kdsMOOTH()` should in principle be the same across the code-paths but in practice there are bound to be slight differences due to the different algorithms employed. And note that slight differences at that level may be somewhat amplified by iterated filtering as in ML estimation.

36.9 Extensions and refinements

Regressors in the observation equation

The observation equation (36.1) can be augmented to allow for the effect of a k -vector of observable exogenous variables, x_t , in addition to that of the unobserved state, as in

$$y_t = B_t x_t + Z_t \alpha_t + \varepsilon_t$$

This specification can be added to a bundle previously obtained via `ksetup` by use of the keys `obsx` (for x) and `obsxmat` (for B'). In that case `obsx` must be an $N \times k$ matrix and B must be $n \times k$. (But please note: as with the case of Z described above, backward compatibility dictates that `obsxmat` be given in transposed form.)

An exception to this dimensionality rule is granted for convenience. If the observation equation includes a constant but no additional exogenous variables, you can give B as $n \times 1$ without having to specify `obsx`. More generally, if the column dimension of B is 1 greater than k it is assumed that the first element of B is associated with an implicit column of ones.

Intercept in the state equation

In some applications it may be useful to have an “intercept” in the state transition equation, thus generalizing equation (36.2) to

$$\alpha_{t+1} = \mu_t + T_t \alpha_t + \eta_t$$

The term μ is never strictly necessary: the system (36.1) and (36.2) can absorb it as an extra (non time-varying) element in the state vector. However, this comes at the cost of expanding all the matrices that touch the state (α , T , η , Ω , Z), making the model relatively awkward to formulate and forecasts more expensive to compute. We therefore adopt the convention above on practical grounds.

The $(r \times 1)$ vector μ can be added to a bundle under the key `stconst`. Despite its name this matrix can be specified as time-varying as explained in the next section.

Time-varying matrices

Any or all of the matrices `obsymat`, `obsxmat`, `obsvar`, `statemat`, `statevar` and `stconst` may be time-varying. In that case you must supply the name of a function to be called to update the matrix or matrices in question: you add this to the bundle as a string, under the key `timevar_call`.⁴ For

⁴The choice of the name for the function itself is of course totally up to the user.

example, if just `obsymat` (Z_t) should be updated, by a function named `TV_Z`, you would write

```
SSmod.timevar_call = "TV_Z"
```

The function that plays this role will be called at each time-step of the filtering or simulation operation, prior to performing any calculations. It should have a single bundle-pointer parameter, by means of which it will be passed a pointer to the Kalman bundle to which the call is attached. Its return value (if any) will not be used, so generally it returns nothing (is of type `void`). However, you can use `gretl's funcerr` keyword to raise an error if things seem to be going wrong; see chapter 14 for details.

Besides the bundle members noted above, a time variation function has access to the current (1-based) time step, under the reserved key `t`, and the n -vector containing the forecast error from the previous time step, v_{t-1} , under the key `uhat`; when $t = 1$ the latter will be a zero vector.

If any additional information is needed for performing the update it can be placed in the bundle under a user-specified key. So, for example, a simple updater for a (1×1) Z matrix might look like this:

```
function void TV_Z (bundle *b)
    b.obsymat = b.Zvals[b.t]
end function
```

where `b.Zvals` is a bundled N -vector. An updater that operates on both Z ($n \times r$) and T ($r \times r$) might be

```
function void update_2 (bundle *b)
    b.obsymat = mshape(b.Zvals[b.t,], b.r, b.n)
    b.statemat = unvech(b.Tvals[b.t,])
end function
```

where in this case we assume that `b.Zvals` is $N \times rn$, with row t holding the (transposed) vec of Z_t , and `b.Tvals` is $N \times r(r+1)/2$, with row t holding the vech of T_t . Simpler variants (e.g. just one element of a relevant matrix in question is changed) and more complex variants—say, involving some sort of conditionality—are also possible in this framework.

It is worth noting that this setup lends itself to a much wider scope than time-varying system matrices. In fact, this syntax allows for the possibility of executing user-defined operations at each step. The function that goes under `timevar_call` can read all the elements of the model bundle and can modify several of them: the system matrices (which can therefore be made time-varying) as well as the user-defined elements.

An extended example of use of the time-variation facility is presented in section 36.12.

Cross-correlated disturbances

The formulation given in equations (36.1) and (36.2) assumes mutual independence of the disturbances in the state and observation equations, ε_t and η_t . This assumption holds good in many practical applications, but in some cases one may wish to allow for cross-correlation.

More generally, we note three common representations of the variance of the disturbances in (36.1) and (36.2).

1. The “basic” representation: ε_t and η_t are assumed to be mutually uncorrelated, and we write their respective (possibly time-varying) variance matrices as $V(\varepsilon_t)$ ($n \times n$) and $V(\eta_t)$ ($r \times r$).
2. The “de Jong” representation: write $\varepsilon_t = G_t v_t$ and $\eta_t = H_t v_t$, where G_t is $n \times r$, H_t is $r \times p$ and p is the length of the underlying disturbance vector v_t . This formulation allows for correlation of the disturbances across the equations, if $H_t G_t'$ is non-zero.

3. The “Durbin-Koopman” representation: as in the first case assume that the disturbances are uncorrelated across the equations, but write $\eta_t = R_t \xi_t$ and $V(\eta_t) = R_t Q_t R_t'$, where R_t is a selection matrix and $Q_t = V(\xi_t)$. Let $m \leq r$ denote the dimension of ξ_t . Then Q_t is $m \times m$ and R_t is $r \times m$. This allows for the possibility that there are fewer disturbances to the state than elements of the state vector.

With the de Jong representation, in place of (36.1)–(36.2) we may write

$$\begin{aligned} y_t &= Z_t \alpha_t + G_t v_t \\ \alpha_{t+1} &= T_t \alpha_t + H_t v_t. \end{aligned}$$

In that case we may re-express the variance matrices from section 36.2 above as

$$\begin{aligned} \Sigma_t &= G_t G_t' \\ \Omega_t &= H_t H_t' \end{aligned}$$

with the addition of

$$\text{Cov}(\eta_t, \varepsilon_t) = H_t G_t'$$

You can select the de Jong or Durbin-Koopman representation by supplying extra arguments to the `ksetup` function. For the de Jong version, in place of giving Ω you should give the two matrices identified above as H and G , as in

```
bundle SSxmod = ksetup(y, Z, T, H, G),
```

and in case you wish to retrieve or update information on the variance of the disturbances, note that in the cross-correlated case the bundle keys `statevar` and `obsvar` are taken to designate the factors H and G respectively.

To select the Durbin-Koopman representation a sixth, boolean argument must be used. If that has a non-zero value `statevar` is taken to be Q and the fifth argument is taken to be R . Note that in this case `obsvar` should be added separately as in the basic case.

The following statements illustrate the three cases.

```
# basic
bundle kb1 = ksetup(y, Z', T, Veta)
kb1.obsvar = Veps # if wanted

# de Jong
bundle kb2 = ksetup(y, Z', T, H, G)

# Durbin-Koopman
bundle kb3 = ksetup(y, Z', T, Q, R, 1)
kb3.obsvar = Veps # if wanted
```

36.10 The `ksimul` function

This simulation function has as its required arguments a pointer to a Kalman bundle and a matrix containing artificial disturbances, and it returns a matrix of simulation results. An optional trailing Boolean argument is supported, the purpose of which is explained below.

If you are calling `ksimul` as a follow-up to other state-space computations you will presumably have a Kalman bundle to hand to serve as the first argument. If you're doing simulation from scratch you need to create such a bundle, but note that in this case the first argument to `ksetup` (the matrix of observables) is really just a place-holder: a $2 \times n$ zero matrix will suffice (two rows being the minimum required for this matrix). The number of simulated observations is set by the row dimension of the second argument to `ksimul`.

If the disturbances are not cross-correlated, the matrix argument must be either $N \times r$, if there is no disturbance in the observation equation, or $N \times (r + n)$ if the Σ (`obsvar`) matrix is specified. Row t holds either η'_t or $(\eta'_t, \varepsilon'_t)$. Note that if Ω (`statevar`) is not simply an identity matrix you will have to scale the artificial state disturbances appropriately; the same goes for Σ and the observation disturbances, if present. Given a matrix U containing standard normal variates, in the general case this requires finding a matrix A such that

$$AA' = \Lambda \equiv \begin{pmatrix} \Omega & 0_{r \times n} \\ 0_{n \times r} & \Sigma \end{pmatrix}$$

and post-multiplying U by A' (although it's not necessary to form A explicitly if the disturbance variance matrices are diagonal). This is not particularly onerous if Λ is time-invariant; gretl's `psdroot` function can be used to form A if it's needed. If Ω and/or Σ are time-varying, however, this scaling can become quite burdensome. As a convenience, the ancillary function `ksimdata` can be used to pre-process the U matrix automatically. Here's an example (we assume that a bundle named `b` has been obtained via `ksetup`):

```
matrix N = mnormal(500, b.r + b.n)
matrix E = ksimdata(&b, N)
matrix sim = ksimul(&b, E)
```

or if you have no need to store the disturbances:

```
matrix sim = ksimul(&b, ksimdata(&b, mnormal(500, b.r + b.n)))
```

Time-variation or no, `ksimdata` will ensure that the disturbances are scaled to the variances specified by Ω_t and Σ_t .

If the disturbances are cross-correlated (see section 36.9) then the matrix argument to `ksimul` should be $N \times p$, each row holding v'_t . In this case no prior scaling is required since it is assumed that $v_t \sim N(0, I)$ and the disturbances for the respective equations, $H_t v_t$ and $G_t v_t$, are computed internally, with regard to time-variation if applicable.

As mentioned above, for the purposes of `ksimul` the time-series length, N , is defined by the number of rows of the supplied disturbance matrix. This need not equal the original N value (set from `obsy` in the initial call to `ksetup`), since `obsy` is ignored under simulation. However, if the model includes exogenous variables in the observation equation (`obsx`) and the simulation length is greater than the original N , the simulation will run out of data and fail unless you supply a larger `x` matrix. This can be done in either of two ways. You can add a suitably sized matrix to the Kalman bundle under the key `simx`; if present, this will be used in preference to `obsx` for simulation. Or if you don't mind over-writing the original `obsx` you can substitute another matrix with the required number of rows under that key.

By default, the value returned by `ksimul` is a $(N \times n)$ matrix holding simulated values for the vector of observables at each time step; that is, row t holds \tilde{y}'_t , where the tilde indicates a simulated quantity. To obtain a record of the simulated state, supply a non-zero value for the final, optional argument. In that case the returned matrix is $N \times (r + n)$ and contains both the simulated state and the simulated observable; row t holds $(\tilde{\alpha}'_t, \tilde{y}'_t)$.

Note that the original `obsy` member of the bundle is not overwritten by `ksimul`, nor is `state` or any other user-accessible output matrix. On exit from `ksimul` the prior value of N is restored.

The initial state under simulation

The recursion that yields \tilde{y} and $\tilde{\alpha}$ is as follows: for $t = 1, \dots, N$

$$\begin{aligned}\tilde{y}_t &= Z_t \tilde{\alpha}_t + \varepsilon_t \\ \tilde{\alpha}_{t+1} &= T_t \tilde{\alpha}_t + \eta_t\end{aligned}$$

This implies that a value for $\tilde{\alpha}_1$ is required to get things started. You can add such a value to a Kalman bundle under the reserved key `simstart`. If this member is not present in the bundle, $\tilde{\alpha}_1$ defaults to the value given under the key `inistate`, or if that in turn is not present, to a zero vector.

Alternatively, the starting point can be made stochastic. To do this you can emulate the procedure followed by `SsfPack`, namely setting

$$\alpha_1 = a + Av_0$$

where a is a non-stochastic r -vector, v_0 is an r -vector of standard normal random numbers, and A is a matrix such that $AA' = P_0$.

Let's say we have a state-space bundle `b`, on which we have already set suitable values of `inistate` (corresponding to a above) and `inivar` (P_0). To perform a simulation with a stochastic starting point we can set α_1 thus:

```
matrix A = psdroot(b.inivar)
b.simstart = b.inistate + A * mnormal(b.r, 1)
```

36.11 Numerical optimization

If the object of using a state space model is to produce maximum likelihood estimates of some parameters of interest, note that the loglikelihood surface may be quite awkward (far from globally concave), posing a challenge for numerical methods such as BFGS, the default maximizer under `gretl's` `mle` command. Symptoms may include failure of convergence—typically due to an excessive computed gradient even as the maximizer cannot find an improvement in the objective function—or an excessive number of iterations. In such cases it is worth considering the following points.

- In some cases, scaling the observables may help: if the order of magnitude of y_t is too small or too large, floating-point precision may become an issue for estimating variances.
- If you can obtain plausible initial values for the parameters, things are likely to go better than starting with arbitrary values.
- The limited-memory version of BFGS (L-BFGS) may work better than the standard version in some cases. To engage this, issue the command

```
set lbfgs on
prior to ML estimation.
```

- It may be helpful to employ a more accurate (but computationally more expensive) method for computing the gradient, namely Richardson extrapolation. Here the command is

```
set bfgs_richardson on
```

36.12 Example scripts

This section presents a selection of short sample scripts to illustrate the most important points covered in this chapter.

ARMA estimation

Functions illustrated in this example: `ksetup`, `kfilter`.

As is well known, the Kalman filter provides a very efficient way to compute the likelihood of ARMA models; as an example, take an ARMA(1,1) model

$$y_t = \phi y_{t-1} + \varepsilon_t + \theta \varepsilon_{t-1}$$

Listing 36.1: ARMA estimation [\[Download ▼\]](#)

```

function void arma11_via_kalman (series y)
  /* parameter initialization */
  scalar phi = 0
  scalar theta = 0
  scalar sigma = 1

  /* state-space model setup */
  matrix Z = {1, theta}
  matrix T = {phi, 0; 1, 0}
  matrix Q = {sigma^2, 0; 0, 0}
  bundle kb = ksetup(y, Z', T, Q)

  /* maximum likelihood estimation */
  mle logl = ERR ? NA : kb.llt
  kb.obsymat[2] = theta
  kb.statemat[1,1] = phi
  kb.statevar[1,1] = sigma^2
  ERR = kfilter(&kb)
  params phi theta sigma
end mle --hessian
end function

# ----- main -----

open arma.gdt          # open the "arma" example dataset
arma11_via_kalman(y)   # estimate an arma(1,1) model
arma 1 1 ; y --nc      # check via native command

```

One of the ways the above equation can be cast in state-space form is by defining a latent process $\alpha_t = (1 - \phi L)^{-1} \varepsilon_t$. The observation equation corresponding to (36.1) is then

$$y_t = \alpha_t + \theta \alpha_{t-1} \quad (36.3)$$

and the state transition equation corresponding to (36.2) is

$$\begin{bmatrix} \alpha_t \\ \alpha_{t-1} \end{bmatrix} = \begin{bmatrix} \phi & 0 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} \alpha_{t-1} \\ \alpha_{t-2} \end{bmatrix} + \begin{bmatrix} \varepsilon_t \\ 0 \end{bmatrix}$$

The hansl syntax for a corresponding filter would be

```
matrix Z = {1, theta}
matrix T = {phi, 0; 1, 0}
matrix Q = {s^2, 0; 0, 0}
bundle kb = ksetup(y, Z', T, Q)
```

or, if you prefer, just a one-liner:

```
bundle kb = ksetup(y, {1; theta}, {phi, 0; 1, 0}, {s^2, 0; 0, 0})
```

Note that the observation equation (36.3) does not include an “error term”; this is equivalent to saying that $\text{var}(\varepsilon_t) = 0$ and there is therefore no need to add an obsvar element to the bundle.

Once the filter is set up, all it takes to compute the log-likelihood for given values of ϕ , θ and σ_ε^2 is to execute the `kfilter` function and read the Kalman bundle’s `lnl` member (which holds the total loglikelihood) or—more appropriately if the likelihood has to be maximized through `mle—llt`, which gives the series of contributions to the log-likelihood per observation. An example is shown in script 36.1.

The Hodrick–Prescott filter

Functions illustrated in this example: `ksetup`, `kfilter`, `ksmooth`.

The Hodrick–Prescott (HP) filter can be obtained as the solution of a prediction problem, that is obtaining estimates of the latent time series μ_t in

$$\begin{aligned} x_t &= \mu_t + \varepsilon_t \\ \Delta^2 \mu_t &= \eta_t, \end{aligned}$$

where x_t is an observable time series and ε_t and η_t are mutually uncorrelated white noise processes; the ratio between the two variances is the “smoothing” parameter: $\lambda = \frac{V(\varepsilon_t)}{V(\eta_t)}$. This is normally calibrated rather than estimated, and a common choice for macro data is to make it a function of the data periodicity: $\lambda = 100 \cdot p^2$, where p is the number of subperiods in a year. See [Harvey and Jaeger \(1993\)](#) and [King and Rebelo \(1993\)](#) for details.

The most common use of the HP filter is to obtain an estimate of the trend μ_t using all the available data, so that the estimate for each period t uses future as well as prior values of x_t . But in some uses (such as forecasting) this is clearly undesirable, and we may wish to construct $\hat{\mu}_t$ as a function of x_t, x_{t-1}, \dots only. This point was famously made by [Stock and Watson \(1999\)](#), and the resulting estimator is known as the one-sided HP filter.

A possible space-state representation of the model above is

$$\begin{aligned} x_t &= [1 \quad 0] \begin{bmatrix} \mu_t \\ \mu_{t-1} \end{bmatrix} + \varepsilon_t \\ \begin{bmatrix} \mu_t \\ \mu_{t-1} \end{bmatrix} &= \begin{bmatrix} 2 & -1 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} \mu_{t-1} \\ \mu_{t-2} \end{bmatrix} + \eta_t. \end{aligned}$$

Listing 36.2: HP filter [\[Download ▼\]](#)

```

function series hp_via_kalman(series y, scalar lambda[0], bool onside[0])
    if lambda == 0
        lambda = 100 * $pd^2
    endif
    # State transition matrix
    matrix T = {2, -1; 1, 0}
    # Observation matrix
    matrix Z = {1, 0}
    # Covariance matrix in the state equation
    matrix Q = {1/sqrt(lambda), 0; 0, 0}
    matrix my = {y}

    string desc = ""
    if onside
        matrix my = my | 0
        desc = "1-sided "
    endif

    ssm = ksetup(my, Z', T, Q)
    ssm.obsvar = sqrt(lambda)
    ssm.inistate = {2*y[1]-y[2] ; 3*y[1]-2*y[2]}
    ssm.diffuse = 1

    err = onside ? kfilter(&ssm) : ksmooth(&ssm)
    if err
        series ret = NA
    else
        mu = onside ? ssm.state[2:,2] : ssm.state[,1]
        series ret = y - mu
    endif

    string d = sprintf("%sHP-filtered %s (lambda = %g)", desc, argname(y), lambda)
    setinfo ret --description="@d"
    return ret
end function

# --- example -----

clear
open fedstl.bin
data houst
y = log(houst)

# one-sided, built-in then hansl
n1c = hpfilt(y, 1600, 1)
series h1c = hp_via_kalman(y, 1600, 1)
ols n1c const h1c --simple-print

# two-sided, built-in then hansl
n2c = hpfilt(y, 1600)
series h2c = hp_via_kalman(y, 1600)
ols n2c const h2c --simple-print

```

Estimates for μ_t can be obtained by running a forward filter for the one-sided version, plus a smoothing pass for the two-sided one. Code implementing the filter is shown in script 36.2, along with an example using the “housing starts” series from the St. Louis Fed database. The example also compares the result of the function to that from gretl’s native `hpfilt()` function.

Note that in the case of the one-sided filter a little trick is required in order to get the desired result: the state matrix stored by the `kfilter()` function is the estimate of $\hat{\alpha}_{t|t-1}$, whereas what we require is in fact $\hat{\alpha}_{t|t}$. To work around this we add an extra observation to the end of the series and retrieve the *one-step-ahead* estimate of the *lagged* state.

Local level model

Functions illustrated in this example: `ksetup`, `kfilter`, `ksmooth`.

Suppose we have a series $y_t = \mu_t + \varepsilon_t$, where μ_t is a random walk with normal increments of variance σ_1^2 and ε_t is normal white noise with variance σ_2^2 , independent of μ_t . This is known as the “local level” model, and it can be cast in state-space form as equations (36.1)–(36.2) with $T = 1$, $\eta_t \sim N(0, \sigma_1^2)$, $Z = 1$ and $\varepsilon_t \sim N(0, \sigma_2^2)$.⁵ The translation to `hansl` is

```
bundle llmod = ksetup(y, 1, 1, s1)
llmod.obsvar = s2
llmod.diffuse = 1
```

The two unknown parameters σ_1^2 and σ_2^2 can be estimated via maximum likelihood. Listing 36.3 provides an example of simulation and estimation of such a model. Since simulating the local level model is trivial using ordinary gretl commands, we don’t use `ksimul` in this context.⁶

Time-varying models

To illustrate state space models with time-varying system matrices we will use time-varying OLS. Suppose the DGP for an observable time series y_t is given by

$$y_t = \beta_0 + \beta_{1,t}x_t + \varepsilon_t \quad (36.4)$$

where the slope coefficient β_1 evolves through time according to

$$\beta_{1,t+1} = \beta_{1,t} + \eta_t \quad (36.5)$$

It is easy to see that the pair of equations above define a state space model, with equation (36.4) as the measurement equation and (36.5) as the state transition equation. The unobservable state is $\beta_{1,t}$, $T = 1$ and $\Omega = \sigma_\eta^2$. As for the measurement equation, $\Sigma = \sigma_\varepsilon^2$, while the matrix multiplying $\beta_{1,t}$, and hence playing the role of Z_t , is the time-varying x_t .

Once the system is framed as a state-space model, estimation of the three unknown parameters β_0 , σ_ε^2 and σ_η^2 can proceed by maximum likelihood in a manner similar to example 36.1 and 36.3. The sequence of slope coefficients $\beta_{1,t}$ can then be estimated by running the smoother, which also yields a consistent estimate of the dispersion of the estimated state.

Listing 36.4 presents an example in which data from the AWM database are used to estimate a Phillips Curve with time-varying slope:

$$\text{INFQ}_t = \beta_0 + \beta_{1,t}\text{URX}_t + \varepsilon_t$$

⁵Note that the local level model, plus other common “Structural Time Series” models are implemented in the *StrucTiSM* function package.

⁶Warning: as the script stands, there is an “off-by-one” misalignment between the state vector and the observable series. For convenience, the script is written as if equation (36.2) was modified into the equivalent formulation

$$\alpha_t = T\alpha_{t-1} + \eta_t$$

We kept the script as simple as possible so that the reader can focus on the interesting aspects.

Listing 36.3: Local level model [\[Download ▼\]](#)

```
nulldata 200
set seed 101010
setobs 1 1 --special-time-series

/* set the true variance parameters */
true_s1 = 0.5
true_s2 = 0.25

/* and simulate some data */
v = normal() * sqrt(true_s1)
w = normal() * sqrt(true_s2)
mu = 2 + cum(v)
y = mu + w

/* starting values for variance estimates */
s1 = 1
s2 = 1

/* state-space model set-up */
bundle kb = ksetup(y, 1, 1, s1)
kb.obsvar = s2
kb.diffuse = 1

/* ML estimation of variances */
mle ll = ERR ? NA : kb.llt
    ERR = kfilter(&kb)
    params kb.statevar kb.obsvar
end mle

/* compute the smoothed state */
ksmooth(&kb)
series muhat = kb.state
```

Listing 36.4: Phillips curve on Euro data with time-varying slope [\[Download ▼\]](#)

```

function void at_each_step(bundle *b)
    b.observmat = transp(b.mX[b.t,:])
end function

open AWM.gdt --quiet
smp1 1974:1 1994:1

/* parameter initialization */
scalar b0 = mean(INFQ)
scalar s_obs = 0.1
scalar s_state = 0.1

/* bundle setup */
bundle B = ksetup(INFQ, 1, 1, 1)
matrix B.mX = {URX}
matrix B.depvar = {INFQ}
B.timevar_call = "at_each_step"
B.diffuse = 1

/* ML estimation of intercept and the two variances */
mle LL = err ? NA : B.llt
    B.observ = B.depvar - b0
    B.observvar = s_obs^2
    B.statevar = s_state^2
    err = kfilter(&B)
    params b0 s_obs s_state
end mle

/* display the smoothed time-varying slope */
ksmooth(&B)
series tvar_b1hat = B.state[,1]
series tvar_b1se = sqrt(B.stvar[,1])
gnuplot tvar_b1hat --time-series --with-lines --output=display \
    --band=tvar_b1hat,tvar_b1se,1.96 --band-style=fill

```

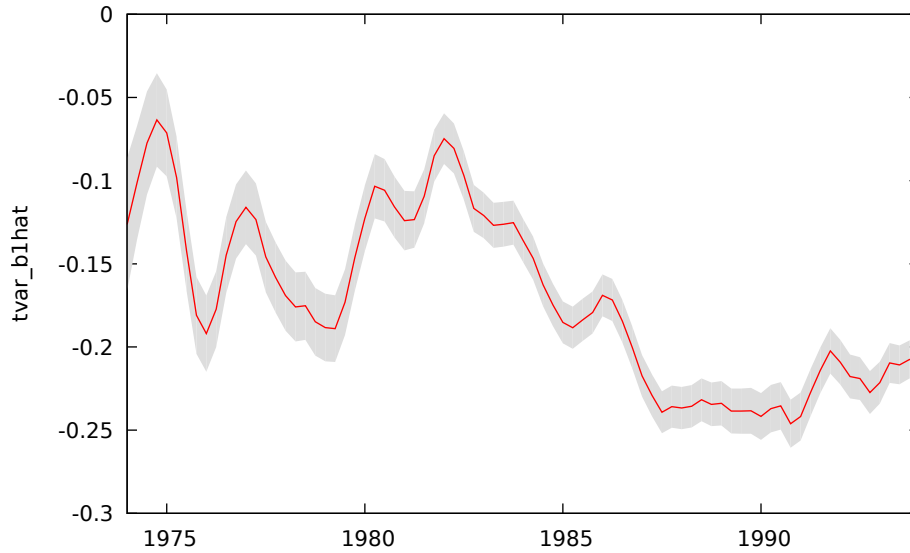


Figure 36.1: Phillips Curve on Euro data: time-varying slope and 95% confidence interval

where INFQ is a measure of quarterly inflation and URX a measure of unemployment. At the end of the script the evolution of the slope coefficient over time is plotted along with a 95% confidence band—see Figure 36.1.

Disturbance smoothing

Functions illustrated in this example: `ksetup`, `kdsMOOTH`.

In section 36.7 we noted that the `kdsMOOTH` function can produce two different measures of the dispersion of the smoothed disturbances, depending on the value of the (optional) trailing Boolean parameter. Here we show what these two measures are good for, using the famous Nile flow data that have been much analysed in the state-space literature. We focus on the state equation; that is, the random-walk component of the observed series.

Our script is shown in Listing 36.5. This is an instance of the Local Level model and the ML variance estimates are obtained as in Listing 36.3. In the first call to `kdsMOOTH` we omit the optional switch and therefore compute $E(\hat{\eta}_t \hat{\eta}_t')$ for each t . This quantity is suitable for constructing the auxiliary residuals shown in the top panel of Figure 36.2 (for similar plots see [Koopman et al., 1999](#); [Pelagatti, 2011](#)). This plot suggests the presence of a structural break shortly prior to 1900, as various authors have observed.

In the second `kdsMOOTH` call we ask `gretl` to compute instead $E[(\hat{\eta}_t - \eta_t)(\hat{\eta}_t - \eta_t)' | \mathcal{Y}_1, \dots, \mathcal{Y}_T]$, the MSE of $\hat{\eta}_t$ considered as an estimator of η_t . And in the lower panel of the Figure we plot $\hat{\eta}_t$ along with a 90% confidence band (roughly, ± 1.64 times the RMSE). This reveals that, given the sampling variance of $\hat{\eta}_t$, we're not really sure that any of the η_t values were truly different from zero. The resolution of the seeming conflict here is commonly reckoned to be that there was in fact a change in mean around 1900, but besides that event there's little evidence for a non-zero σ_η^2 . Or in other words the standard local level model is not really applicable to the data.

36.13 Graphical interface

By this point, the reader will have gathered that setting up a state space model can be quite a complex undertaking, and the only general way to accomplish it is by writing a script. However, some cases are simple enough to lend themselves to a standardized treatment, and so can be

Listing 36.5: Working with smoothed disturbances – Nile data [\[Download ▼\]](#)

```
open nile.gdt

# ML variance estimates
scalar s2_eta = 1468.49
scalar s2_eps = 15099.7

bundle LLM = ksetup(nile, 1, 1, s2_eta)
LLM.obsvar = s2_eps
LLM.diffuse = 1

kdsmooth(&LLM)
series eta_aux = LLM.smdist[,1] ./ LLM.smdisterr[,1]
series zero = 0
plot eta_aux
    options time-series with-lines band=zero,const,2
    literal unset ylabel
    literal set title 'Auxiliary residual, state equation'
end plot --output=display

kdsmooth(&LLM, 1)
series etahat = LLM.smdist[,1]
series sdeta = LLM.smdisterr[,1]

plot etahat
    options time-series with-lines band=etahat,sdeta,1.64485
    literal unset ylabel
    literal set title 'State disturbance with 90% confidence band'
end plot --output=display
```

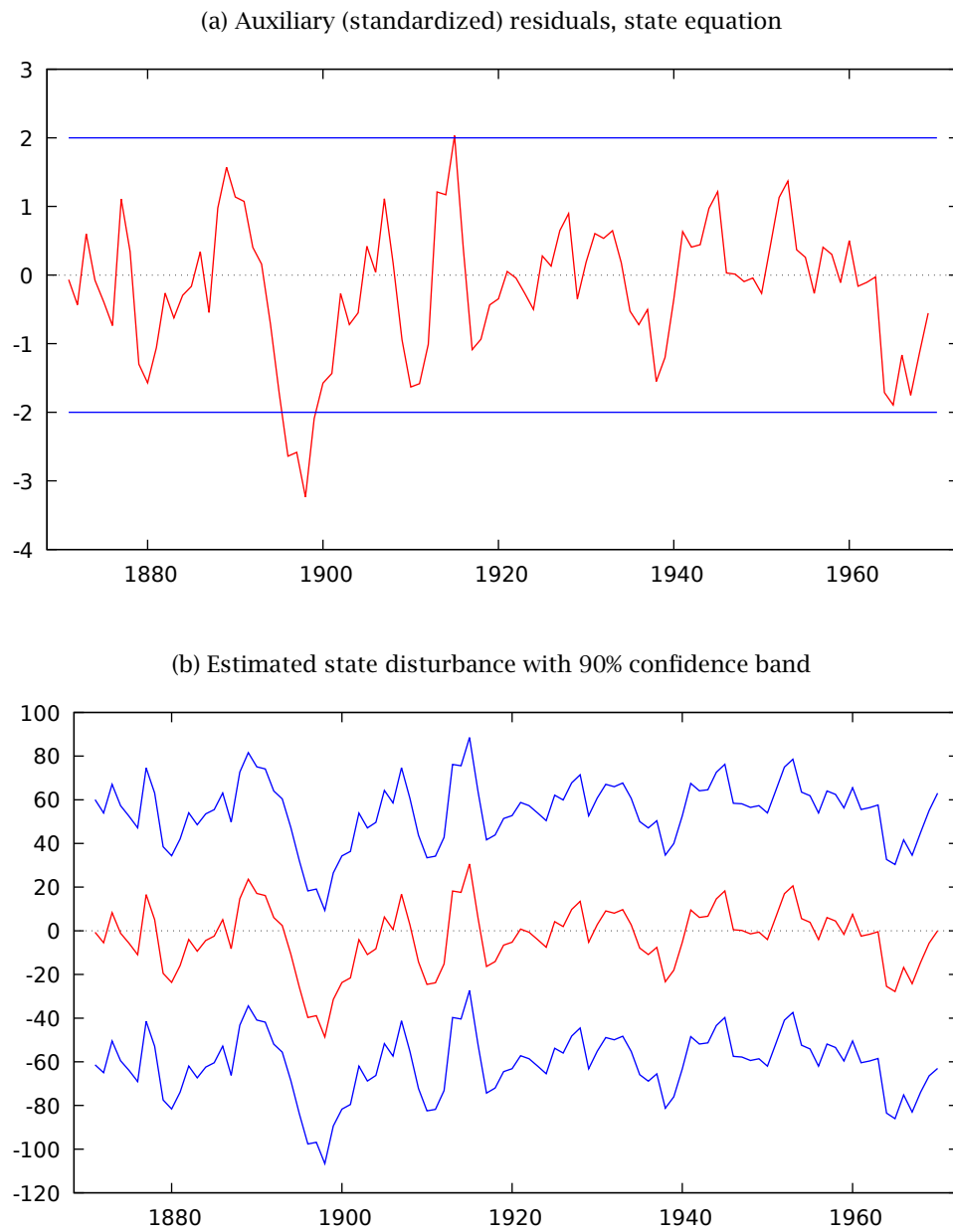


Figure 36.2: Nile data: auxiliary residuals and $\hat{\eta}_t$ from disturbance smoother

handled via a relatively streamlined graphical interface. As of version 2022a, gretl provides just this: a GUI for estimating a subset of state space models that, while limited, may still be useful for pedagogical purposes, sparing the user from the intricacies of scripting. In this section, we describe the GUI and the class of models it supports.

The GUI can be used for performing ML estimation of models of the kind

$$y_t = Z\alpha_t + \varepsilon_t \quad (36.6)$$

$$\alpha_{t+1} = T\alpha_t + R\eta_t \quad (36.7)$$

where y_t is a vector of observables, $V(\varepsilon_t)$ is a diagonal matrix—or possibly 0, in which case the last term of equation (36.6) is dropped. As for the covariance matrix of the shocks to equation (36.7), it is assumed that η_t is an IID sequence of normal random variates with diagonal covariance matrix Σ_η . Therefore, the covariance matrix denoted by Ω in the previous sections of this chapter (whose corresponding key in the Kalman bundle is `statevar`) is assumed to be $\Omega = R\Sigma_\eta R'$. Note that R can have fewer columns than r , thereby making Ω singular. In the graphical interface, this is called the “state variance factor”.

The system matrices Z , T and R are assumed to be time-invariant and known, so estimation only concerns the variances of ε_t and η_t . Clearly, this is a limited subset of the range of models that gretl can handle, but it may be of some value to users.

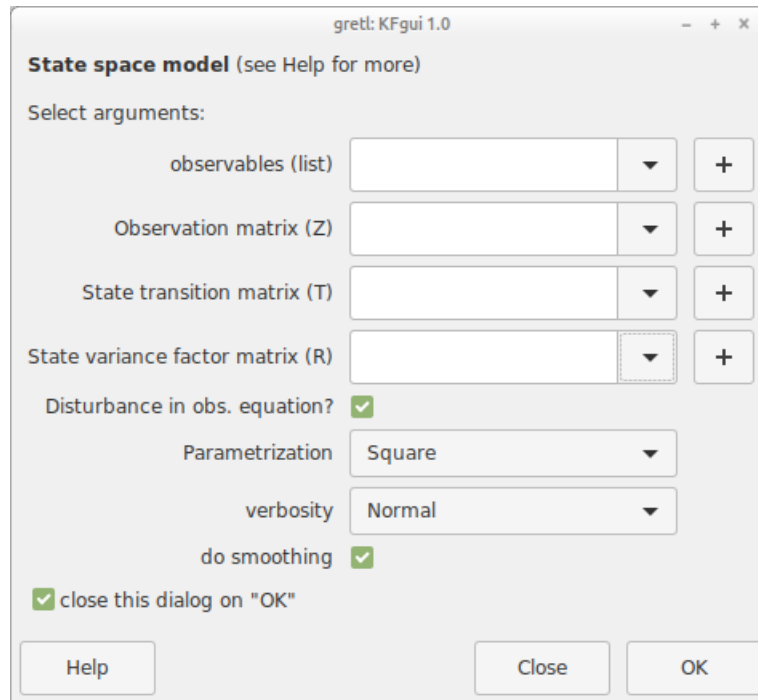


Figure 36.3: GUI hook for state space models

ML estimation is carried out internally using the `mle` command with the limited-memory version of the BFGS optimizer, and the user is given the option of tracking the optimization process via a “verbosity” option. For reasons of numerical performance, it is convenient to have the choice of representing variances as transformations of the BFGS parameters in one of the three following ways:

Absolute value maximization is performed on the variances: $\sigma^2 = |\theta|$

Square maximization is performed on the standard deviations: $\sigma^2 = \theta^2$

Exponential maximization is performed on the log standard deviations: $\sigma^2 = \exp(2 \cdot \theta)$

Normally, this choice should make no difference for well-behaved data, although numerical problems may occur sometimes. In these cases, it may be helpful to rescale the data by multiplying y_t by some scalar (such as 100 or 0.0001) so as to make the order of magnitude of the parameters less prone to finite-precision issues. In any case, the function reports the estimates of the standard errors whatever the parametrization type. Once the parameters are estimated the user has the choice of performing smoothing of the states.

The GUI is shown in figure 36.3. The “observables” box is used for specifying a list of series (or a single series) for y_t . The next two boxes handle the Z and T matrices, respectively. These can be pre-existing matrices or may be created “on the fly”. The same applies for the next box, dedicated to the R matrix. However, the R matrix can be omitted, in which case it is implicitly assumed $R = I$. The remaining GUI elements should hopefully be self-explanatory.

The function returns a bundle which includes a sub-bundle called `kmod` with all the state-space internals; a matrix called `state` holding the estimated states; and matrices `coeff` and `vcv` holding, respectively, the coefficients and standard errors obtained via ML estimation.

Example: Random walk plus noise

The model here is

$$y_t = \alpha_t + \varepsilon_t \quad \alpha_{t+1} = \alpha_t + \eta_t$$

so that $Z = T = R = 1$.

The following script simulates the DGP above with $V(\varepsilon_t) = 1$ and $V(\eta_t) = 1/16$, and sets up the two matrices Z and T , ready to be entered into the second and third boxes of the GUI helper, respectively; obviously, the first box should contain the string `y`. Note that the first box expects as argument a named list, thereby allowing for multivariate models.

```
clear
set verbose off
set seed 280921

nulldata 256
setobs 1 1 --special

# example 1: random walk plus noise

series m = cum(normal() * 0.25)
series y = m + normal()
Z = {1}
T = {1}
```

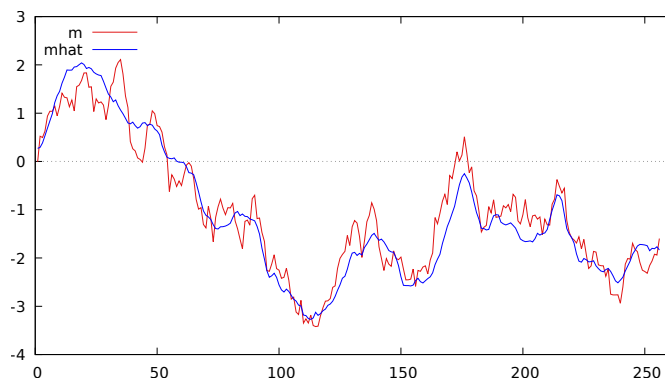


Figure 36.4: Estimated state

Once this is done, clicking on the “OK” button should result in the output shown below; by clicking on the “Graph” icon the picture shown in Figure 36.4 should be produced.

Observation equation

	coefficient	std. error	z	p-value
-----	-----	-----	-----	-----
stdev[1]	0.939311	0.0496287	18.93	6.86e-80 ***

State transition equation

	coefficient	std. error	z	p-value
-----	-----	-----	-----	-----
stdev[1]	0.274650	0.0488920	5.617	1.94e-08 ***

Log-likelihood = -388.946

Example: Random walk plus noise plus seasonal

The model here is

$$y_t = \mu_t + s_t + \varepsilon_t,$$

where $\mu_t = \mu_{t-1} + \eta_{1,t}$ is a random walk, as in the previous example, and s_t is a seasonal component, implicitly defined by the property

$$s_t = - \sum_{j=1}^{S-1} s_{t-j} + \eta_{2,t},$$

S being the number of subperiods. This model is amenable to the representation used in this section by defining the state vector as

$$\alpha_t = [\mu_t, s_t, s_{t-1}, s_{t-2}]'.$$

For example, with quarterly data the system matrices would be equal to

$$Z = \begin{bmatrix} 1 & 1 & 0 & 0 \end{bmatrix} \quad T = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & -1 & -1 & -1 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix} \quad R = \begin{bmatrix} 1 & 0 \\ 0 & 1 \\ 0 & 0 \\ 0 & 0 \end{bmatrix}$$

The following script applies this model to one of the series in the gretl example dataset data9-3.gdt:

```
open data9-3
y = log(reskwh)

Z = ones(2,1) | zeros(2,1)
SeasMat = -ones(1,3) | I(2,3)
T = diagcat(1, SeasMat)
R = I(2) | zeros(2,2)
```

Again, filling the GUI boxes in the obvious way and clicking “OK” will produce the output below:

Observation equation

	coefficient	std. error	z	p-value
--	-------------	------------	---	---------

```
-----
stdev[1]    0.0173633    0.00448117    3.875    0.0001    ***
```

State transition equation

```
-----
            coefficient    std. error    z    p-value
-----
stdev[1]    0.0269790    0.00409457    6.589    4.43e-11    ***
stdev[2]    0.00648082    0.00202576    3.199    0.0014    ***
```

Log-likelihood = 121.33

Note that the output window will contain a few icons on the top bar. By clicking on the second one from the left, it is possible to save to the gretl workspace one or more elements from the returned bundle. For example, the `kmod` key corresponds to the estimated kalman bundle. Saving it under the name `kb` and running the code below will produce the plot shown in Figure 36.5.

```
series trend = kb.state[,1]
series seas  = kb.state[,2]
```

```
scatters y trend seas
```

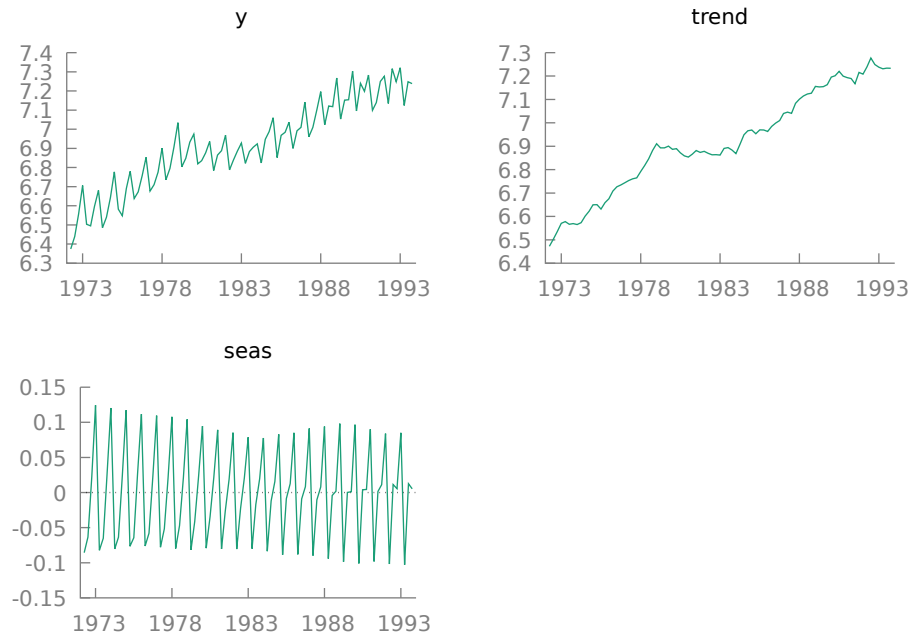


Figure 36.5: Estimated trend and seasonal component

Chapter 37

Numerical methods

Several functions are available to aid in the construction of special-purpose estimators: their purpose is to find numerically approximate solutions to problems that in principle could be solved analytically, but in practice cannot be, for one reason or another. In this chapter, we illustrate the tools that gretl offers for optimization of functions, differentiation and integration.

37.1 Derivative-based optimization methods

In some cases, the function we want to optimize is differentiable and has a maximum in the interior of the search space. In these cases, you will want to use algorithms that exploit this feature, such as BFGS or Newton-Raphson. If this is not the case, you may want to use derivative-free methods, which are illustrated in section [37.2](#).

BFGS

The BFGSmax function has two required arguments: a vector holding the initial values of a set of parameters, and a call to a function that calculates the (scalar) criterion to be maximized, given the current parameter values and any other relevant data. If the object is in fact minimization, this function should return the negative of the criterion. On successful completion, BFGSmax returns the maximized value of the criterion and the vector given via the first argument holds the parameter values which produce the maximum. It is assumed here that the objective function is a user-defined function (see Chapter [14](#)) with the following general set-up:

```
function scalar ObjFunc (const matrix theta, matrix *X)
    scalar val = ... # do some computation
    return val
end function
```

The first argument contains the parameter vector (which should not be modified within the function) and the second may be used to hold “extra” values that are necessary to compute the objective function, but are not the variables of the optimization problem. Here the pointer form is chosen for the argument, but depending on the problem it could also be passed as a plain argument, with or without the `const` modifier. For example, if the objective function were a log-likelihood, the first argument would contain the parameters and the second one the data. Or, for more economic-theory inclined readers, if the objective function were the utility of a consumer, the first argument might contain the quantities of goods and the second one their prices and disposable income.

The operation of BFGS can be adjusted using the `set` variables `bfgs_maxiter` and `bfgs_tol` (see Chapter [26](#)). In addition you can provoke verbose output from the maximizer by setting `max_verbose` to `on`, again via the `set` command (alternatively, you could have set it to `full` and get even richer output).

The Rosenbrock function is often used as a test problem for optimization algorithms. It is also known as “Rosenbrock’s Valley” or “Rosenbrock’s Banana Function”, on account of the fact that its contour lines are banana-shaped. It is defined by:

$$f(x, y) = (1 - x)^2 + 100(y - x^2)^2$$

Listing 37.1: Finding the minimum of the Rosenbrock function [\[Download ▼\]](#)

```

function scalar Rosenbrock(const matrix param)
    scalar x = param[1]
    scalar y = param[2]
    return -(1-x)^2 - 100 * (y - x^2)^2
end function

matrix theta = {0, 0}
set max_verbose on
M = BFGSmax(&theta, Rosenbrock(theta))
print theta

```

The function has a global minimum at $(x, y) = (1, 1)$ where $f(x, y) = 0$. Listing 37.1 shows a gretl script that discovers the minimum using BFGSmax (giving a verbose account of progress). Note that, in this particular case, the function to be maximized only depends on the parameters, so the second parameter is omitted from the definition of the function Rosenbrock.

Supplying analytical derivatives for BFGS

An optional third argument to the BFGSmax function enables the user to supply analytical derivatives of the criterion function with respect to the parameters (without which a numerical approximation to the gradient is computed). This argument is similar to the second one in that it specifies a function call. In this case the function that is called must have the following signature.

Its first argument should be a pre-defined matrix correctly dimensioned to hold the gradient; that is, if the parameter vector contains k elements, the gradient matrix must also be a k -vector. This matrix argument must be given in “pointer” form so that its content can be modified by the function. (Note that unlike the parameter vector, where the choice of initial values can be important, the initial values given to the gradient are immaterial and do not affect the results.)

In addition the gradient function must have as one of its argument the parameter vector. This may be given in pointer form (which enhances efficiency) but that is not required. Additional arguments may be specified if necessary.

Given the current parameter values, the function call must fill out the gradient vector appropriately. It is not required that the gradient function returns any value directly; if it does, that value is ignored.

Listing 37.2 illustrates, showing how the Rosenbrock script can be modified to use analytical derivatives. (Note that since this is a minimization problem the values written into `g[1]` and `g[2]` in the function Rosen_grad are in fact the derivatives of the negative of the Rosenbrock function.)

Limited-memory variant and constrained optimization

As an alternative to “standard” BFGS gretl offers the limited-memory variant, L-BFGS-B. This is described by Byrd *et al.* (1995) and Zhu *et al.* (1997). Gretl uses version 3.0 of this code, which features improvements described by Morales and Nocedal (2011). Some problems that defeat standard BFGS may be amenable to solution by L-BFGS-B. To see if this is the case, gretl code that uses BFGS can be pushed into using the alternative algorithm via the `set` command, as follows:

```
set lbfgs on
```

The primary case for using L-BFGS-B, however, is constrained optimization: this algorithm supports constraints on the parameters in the form of minima and/or maxima. In gretl this is implemented

Listing 37.2: Rosenbrock function with analytical gradient [\[Download ▼\]](#)

```

function scalar Rosenbrock (const matrix param)
    scalar x = param[1]
    scalar y = param[2]
    return -(1-x)^2 - 100 * (y - x^2)^2
end function

function void Rosen_grad (matrix *g, const matrix param)
    scalar x = param[1]
    scalar y = param[2]
    g[1] = 2*(1-x) + 2*x*(200*(y-x^2))
    g[2] = -200*(y - x^2)
end function

matrix theta = {0, 0}
matrix grad = {0, 0}
set max_verbose 1
M = BFGSmax(&theta, Rosenbrock(theta), Rosen_grad(&grad, theta))
print theta
print grad

```

by the function `BFGScmax` ('c' for constrained). The syntax is basically similar to that of `BFGSmax`, except that the first argument must be followed by specification of a “bounds” matrix. This matrix should have three columns and as many rows as there are constrained elements of the parameter vector. Each row should hold the (1-based) index of the constrained parameter, followed by lower and upper bounds. The values `-$huge` and `$huge` should be used to indicate that the parameter is unconstrained downward or upward, respectively. For example, the following code constructs a matrix to specify that the second element of the parameter vector must be non-negative, and the fourth must lie between 0 and 1:

```
matrix bounds = {2, 0, $huge; 4, 0, 1}
```

Newton-Raphson

BFGS, discussed above, is an excellent all-purpose maximizer, and about as robust as possible given the limitations of digital computer arithmetic. The Newton-Raphson maximizer is not as robust, but may converge much faster than BFGS for problems where the maximand is reasonably well behaved—in particular, where it is anything like quadratic (see below). The case for using Newton-Raphson is enhanced if it is possible to supply a function to calculate the Hessian analytically.

The `gretl` function `NRmax`, which implements the Newton-Raphson method, has a maximum of four arguments. The first two (required) arguments are exactly as for BFGS: an initial parameter vector, and a function call which returns the maximand given the parameters. The (optional) third argument is again as in BFGS: a function call that calculates the gradient. Specific to `NRmax` is an optional fourth argument, namely a function call to calculate the (negative) Hessian. The first argument of this function must be a pre-defined matrix of the right dimension to hold the Hessian—that is, a $k \times k$ matrix, where k is the length of the parameter vector—given in “pointer” form. The second argument should be the parameter vector (optionally in pointer form). Other data may be passed as additional arguments as needed. Similarly to the case with the gradient, if the fourth argument to `NRmax` is omitted then a numerical approximation to the Hessian is constructed.

What is ultimately required in Newton-Raphson is the negative inverse of the Hessian. Note that if you give the optional fourth argument, your function should compute the negative Hessian, but

should not invert it; NRmax takes care of inversion, with special handling for the case where the matrix is not negative definite, which can happen far from the maximum.

Listing 37.3 extends the Rosenbrock example, using NRmax with a function Rosen_hess to compute the Hessian. The functions Rosenbrock and Rosen_grad are just the same as in Listing 37.2 and are omitted for brevity.

Listing 37.3: Rosenbrock function via Newton-Raphson

```
function void Rosen_hess (matrix *H, const matrix param)
    scalar x = param[1]
    scalar y = param[2]
    H[1,1] = 2 - 400*y + 1200*x^2
    H[1,2] = -400*x
    H[2,1] = -400*x
    H[2,2] = 200
end function

matrix theta = {0, 0}
matrix grad = {0, 0}
matrix H = zeros(2, 2)
set max_verbose 1
M = NRmax(&theta, Rosenbrock(theta), Rosen_grad(&grad, theta),
          Rosen_hess(&H, theta))
print theta
print grad
```

The idea behind Newton-Raphson is to exploit a quadratic approximation to the maximand, under the assumption that it is concave. If this is true, the method is very effective. However, if the algorithm happens to evaluate the function at a point where the Hessian is not negative definite, things may go wrong. Script 37.4 exemplifies this by using a normal density, which is concave in the interval $(-1, 1)$ and convex elsewhere. If the algorithm is started from within the interval everything goes well and NR is (slightly) more effective than BFGS. If, however, the Hessian is positive at the starting point BFGS converges with only little more difficulty, while Newton-Raphson fails.

37.2 Derivative-free optimization methods

Golden section search method

Suppose you have a function $f(x)$ of a scalar argument, that is known to have a unique maximum. The golden section method is rather effective at finding it quickly without making use of derivatives (see [Press et al. \(2007\)](#), section 10.2 for a thorough description). The gretl function implementing this method is called GSSmax.

The idea is, roughly, to take an interval $[x_0, x_1]$ (also known as the “bracket”) that should contain the maximizing value. Once $y_0 = f(x_0)$ and $y_1 = f(x_1)$ are computed, the algorithm sets a new point x_2 that replaces the end of the previous interval for which the function takes the worse value. So for example, if $y_0 < y_1$, then x_0 is replaced and the interval becomes $[x_1, x_2]$. The width of the interval shrinks progressively, so after a few iterations you should end close to the maximum.

As an illustration, consider the function $f(x) = 50 \cdot x^{3/2} e^{-x}$, which is maximized at $x = 1.5$. In Listing 37.5 we set as the initial interval the range $[0, 10]$ and observe the progress of the algorithm.

As you can see from the output, the bracket shrinks progressively; the center of the interval when the algorithm stops is $x = 1.49996$. Figure 37.1 depicts the process.

Listing 37.4: Maximization of a Gaussian density [\[Download ▼\]](#)

```

function scalar ND(matrix x)
    scalar z = x[1]
    return exp(-0.5*z*z)
end function

set max_verbose 1

x = {0.75}
A = BFGSmax(&x, ND(x))

x = {0.75}
A = NRmax(&x, ND(x))

x = {1.5}
A = BFGSmax(&x, ND(x))

x = {1.5}
A = NRmax(&x, ND(x))

```

Listing 37.5: Golden section example

```

function scalar g(scalar x)
    return 50 * x^(1.5) * exp(-x)
end function

set max_verbose on
m = {5, 0, 10}
y = GSSmax(&m, g(m[1]))
printf "\nf(%g) = %g\n", m[1], y

```

The output is

```

1: bracket={3.81966,6.18034}, values={8.18747,1.59001}
2: bracket={2.36068,3.81966}, values={17.1118,8.18747}
3: bracket={1.45898,2.36068}, values={20.4841,17.1118}
4: bracket={0.901699,1.45898}, values={17.3764,20.4841}
...
20: bracket={1.50017,1.50042}, values={20.4958,20.4958}
21: bracket={1.50001,1.50017}, values={20.4958,20.4958}

f(1.49996) = 20.4958

```

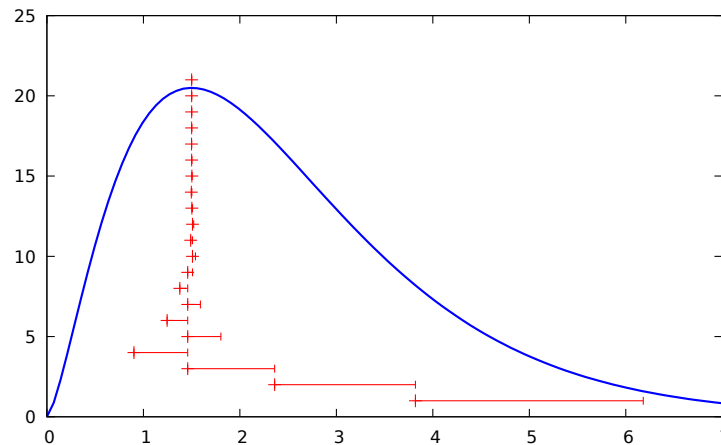



Figure 37.1: Golden section search: the blue line shows the function to be maximized and the red segments show successive choices for the bracket.

Simulated Annealing

Simulated annealing—as implemented by the gretl function `simann`—is not a full-blown maximization method in its own right, but can be a useful auxiliary tool in problems where convergence depends sensitively on the initial values of the parameters. The idea is that you supply initial values and the simulated annealing mechanism tries to improve on them via controlled randomization.

The `simann` function takes up to three arguments. The first two (required) are the same as for `BFGSmax` and `NRmax`: an initial parameter vector and a function that computes the maximand. The optional third argument is a positive integer giving the maximum number of iterations, n , which defaults to 1024.

Starting from the specified point in the parameter space, for each of n iterations we select at random a new point within a certain radius of the previous one and determine the value of the criterion at the new point. If the criterion is higher we jump to the new point; otherwise, we jump with probability P (and remain at the previous point with probability $1 - P$). As the iterations proceed, the system gradually “cools”—that is, the radius of the random perturbation is reduced, as is the probability of making a jump when the criterion fails to increase.

In the course of this procedure $n + 1$ points in the parameter space are evaluated: call them θ_i , $i = 0, \dots, n$, where θ_0 is the initial value given by the user. Let θ^* denote the “best” point among $\theta_1, \dots, \theta_n$ (highest criterion value). The value written into the parameter vector on completion is then θ^* if θ^* is better than θ_0 , otherwise θ_n . In other words, failing an actual improvement in the criterion, `simann` randomizes the starting point, which may be helpful in tricky optimization problems.

Listing 37.6 shows `simann` at work as a helper for `BFGSmax` in finding the maximum of a bimodal function. Unaided, `BFGSmax` requires 60 function evaluations and 55 evaluations of the gradient, while after simulated annealing the maximum is found with 7 function evaluations and 6 evaluations of the gradient.¹

Nelder-Mead

The Nelder-Mead derivative-free simplex maximizer (also known as the “amoeba” algorithm) is implemented by the function `NMmax`. The argument list of this function is essentially the same as for `simann`: the required arguments are an initial parameter vector and a function-call to compute the maximand, while an optional third argument can be used to set the maximum number of

¹Your mileage may vary: these figures are somewhat compiler- and machine-dependent.

Listing 37.6: BFGS with initialization via Simulated Annealing [\[Download ▼\]](#)

```

function scalar bimodal (matrix x, matrix A)
    scalar ret = exp(-qform((x-1)', A))
    ret += 2*exp(-qform((x+4)', A))
    return ret
end function

set seed 12334
set max_verbose on

scalar k = 2
matrix A = 0.1 * I(k)
matrix x0 = {3; -5}

x = x0
u = BFGSmax(&x, bimodal(x, A))
print x

x = x0
u = simann(&x, bimodal(x, A), 1000)
print x
u = BFGSmax(&x, bimodal(x, A))
print x

```

function evaluations (default value: 2000).

This method is unlikely to produce as close an approximation to the “true” optimum as derivative-based methods such as BFGS and Newton-Raphson, but it is more robust than the latter. It may succeed in some cases where derivative-based methods fail, and it may be useful, like `simann`, for improving the starting point for an optimization problem so that a derivative-based method can then take over successfully.

NMmax includes an internal “convergence” check—namely, verification that the best value achieved for the objective function at termination of the algorithm is at least a local optimum—but by default it doesn’t flag an error if this condition is not satisfied. This permits a mode of usage where you set a fairly tight budget of function evaluations (for example, 200) and just take any improvement in the objective function that is available, without worrying about whether an optimum has truly been reached. However, if you want the convergence check to be enforced you can flag this by setting a negative value for the maximum function evaluations argument; in that case the absolute value of the argument is taken and an error is provoked on non-convergence.

If the task for this function is actually minimization, you can either have the function-call return the negative of the actual criterion or, if you prefer, call NMmax under the alias NMmin.

Here is an example of use: minimization of the Powell quartic function, which is problematic for BFGS. (The true minimum is zero, obtained for `x` a 4-vector of zeros.)

```

function scalar powell (const matrix x)
    fx1 = x[1] + 10 * x[2]
    fx2 = x[3] - x[4]
    fx3 = x[2] - 2 * x[3]
    fx4 = x[1] - x[4]
    return fx1^2 + 5.0 * fx2^2 + fx3^4 + 10.0 * fx4^4
end function

```

```

matrix x = {3, -1, 0, 1}'
printf "Initial f(X) = %g\n", powell(x)
fmin = NMmin(x, powell(x))
printf "Estimate of optimal X*:\n%14f\n", x
printf "f(X*) = %g\n", fmin

```

37.3 Numerical differentiation

Computing a Jacobian

Gretl offers the possibility of differentiating numerically a user-defined function via the `fdjac` function.

This function takes two arguments: an $n \times 1$ matrix holding initial parameter values and a function call that calculates and returns an $m \times 1$ matrix, given the current parameter values and any other relevant data. On successful completion it returns an $m \times n$ matrix holding the Jacobian. For example,

```
matrix Jac = fdjac(theta, SumOC(&theta, &X))
```

where we assume that `SumOC` is a user-defined function with the following structure:

```

function matrix SumOC (matrix *theta, matrix *X)
    matrix V = ... # do some computation
    return V
end function

```

This may come in handy in several cases: for example, if you use `BFGSmax` to estimate a model, you may wish to calculate a numerical approximation to the relevant Jacobian to construct a covariance matrix for your estimates.

Another example is the delta method: if you have a consistent estimator of a vector of parameters $\hat{\theta}$, and a consistent estimate of its covariance matrix Σ , you may need to compute estimates for a nonlinear continuous transformation $\psi = g(\theta)$. In this case, a standard result in asymptotic theory is that

$$\left\{ \begin{array}{c} \hat{\theta} \xrightarrow{p} \theta \\ \sqrt{T}(\hat{\theta} - \theta) \xrightarrow{d} N(0, \Sigma) \end{array} \right\} \Rightarrow \left\{ \begin{array}{c} \hat{\psi} = g(\hat{\theta}) \xrightarrow{p} \psi = g(\theta) \\ \sqrt{T}(\hat{\psi} - \psi) \xrightarrow{d} N(0, J\Sigma J') \end{array} \right\}$$

where T is the sample size and J is the Jacobian $\left. \frac{\partial g(x)}{\partial x} \right|_{x=\theta}$.

Script 37.7 exemplifies such a case: the example is taken from [Greene \(2003\)](#), section 9.3.1. The slight differences between the results reported in the original source and what `gretl` returns are due to the fact that the Jacobian is computed numerically, rather than analytically as in the book.

On the subject of numerical versus analytical derivatives, one may wonder what difference it makes to use one method or another. Simply put, the answer is: analytical derivatives may be painful to derive and to translate into code, but in most cases they are much faster than using `fdjac`; as a consequence, if you need to use derivatives as part of an algorithm that requires iteration (such as numerical optimization, or a Monte Carlo experiment), you'll definitely want to use analytical derivatives.

Analytical derivatives are also, in most cases, more precise than numerical ones, but this advantage may or may not be negligible in practice depending on the practical details: the two fundamental aspects to take in consideration are nonlinearity and machine precision.

As an example, consider the derivative of a highly nonlinear function such as the matrix inverse. In order to keep the example simple, let's focus on 2×2 matrices and define the function

```

function matrix vecinv(matrix x)
    A = mshape(x,2,2)

```

Listing 37.7: Delta Method [\[Download ▼\]](#)

```

function matrix MPC(matrix *param, matrix *Y)
    beta = param[2]
    gamma = param[3]
    y = Y[1]
    return beta*gamma*y^(gamma-1)
end function

# William Greene, Econometric Analysis, 5e, Chapter 9
set echo off
set messages off
open greene5_1.gdt

# Use OLS to initialize the parameters
ols realcons 0 realdpi --quiet
a = $coeff(0)
b = $coeff(realdpi)
g = 1.0

# Run NLS with analytical derivatives
nls realcons = a + b * (realdpi^g)
    deriv a = 1
    deriv b = realdpi^g
    deriv g = b * realdpi^g * log(realdpi)
end nls

matrix Y = realdpi[2000:4]
matrix theta = $coeff
matrix V = $vcv

mpc = MPC(&theta, &Y)
matrix Jac = fdjac(theta, MPC(&theta, &Y))
Sigma = qform(Jac, V)

printf "\nmpc = %g, std.err = %g\n", mpc, sqrt(Sigma)
scalar teststat = (mpc-1)/sqrt(Sigma)
printf "\nTest for MPC = 1: %g (p-value = %g)\n", \
    teststat, pvalue(n,abs(teststat))

```

```

    return vec(inv(A))'
end function

```

which, given $\text{vec}(A)$, returns $\text{vec}(A^{-1})$. As is well known (see for example [Magnus and Neudecker \(1988\)](#)),

$$\frac{\partial \text{vec}(A^{-1})}{\partial \text{vec}(A)} = -(A^{-1})' \otimes (A^{-1}),$$

which is rather easy to code in `hansl` as

```

function matrix grad(matrix x)
    iA = inv(mshape(x,2,2))
    return -iA' ** iA
end function

```

Using the `fdjac` function to obtain the same result is even easier: you just invoke it like

```
fdjac(a, "vecinv(a)")
```

In order to see what the difference is, in terms of precision, between analytical and numerical Jacobians, let's start from $A = \begin{bmatrix} 2 & 1 \\ 1 & 1 \end{bmatrix}$. The following code

```

a = {2; 1; 1; 1}
ia = vecinv(a)
ag = grad(a)
ng = fdjac(a, "vecinv(a)")
dg = ag - ng
print ag ng dg

```

gives

```
ag (4 x 4)
```

```

-1    1    1   -1
 1   -2   -1    2
 1   -1   -2    2
-1    2    2   -4

```

```
ng (4 x 4)
```

```

-1    1    1   -1
 1   -2   -1    2
 1   -1   -2    2
-1    2    2   -4

```

```
dg (4 x 4)
```

```

-3.3530e-08 -3.7251e-08 -3.7251e-08 -3.7255e-08
 2.6079e-08  5.2150e-08  3.7251e-08  6.7060e-08
 2.6079e-08  3.7251e-08  5.2150e-08  6.7060e-08
-2.2354e-08 -5.9600e-08 -5.9600e-08 -1.4902e-07

```

in which the analytically-computed derivative and its numerical approximation are essentially the same. If, however, you set $A = \begin{bmatrix} 1.0001 & 1 \\ 1 & 1 \end{bmatrix}$ you end up evaluating the function at a point in which the function itself is considerably more nonlinear since the matrix is much closer to being singular. As a consequence, the numerical approximation becomes much less satisfactory:

ag (4 x 4)

```
-1.0000e+08  1.0000e+08  1.0000e+08 -1.0000e+08
 1.0000e+08 -1.0001e+08 -1.0000e+08  1.0001e+08
 1.0000e+08 -1.0000e+08 -1.0001e+08  1.0001e+08
-1.0000e+08  1.0001e+08  1.0001e+08 -1.0002e+08
```

ng (4 x 4)

```
-9.9985e+07  1.0001e+08  1.0001e+08 -9.9985e+07
 9.9985e+07 -1.0002e+08 -1.0001e+08  9.9995e+07
 9.9985e+07 -1.0001e+08 -1.0002e+08  9.9995e+07
-9.9985e+07  1.0002e+08  1.0002e+08 -1.0001e+08
```

dg (4 x 4)

```
-14899.      -14901.      -14901.      -14900.
 14899.       14903.       14901.       14902.
 14899.       14901.       14903.       14902.
-14899.      -14903.      -14903.      -14903.
```

Moreover, machine precision may have its impact: if you take $A = 0.00001 \times \begin{bmatrix} 2 & 1 \\ 1 & 1 \end{bmatrix}$, the matrix itself is not singular at all, but the order of magnitude of its elements is close enough to machine precision to provoke problems:

ag (4 x 4)

```
-1.0000e+10  1.0000e+10  1.0000e+10 -1.0000e+10
 1.0000e+10 -2.0000e+10 -1.0000e+10  2.0000e+10
 1.0000e+10 -1.0000e+10 -2.0000e+10  2.0000e+10
-1.0000e+10  2.0000e+10  2.0000e+10 -4.0000e+10
```

ng (4 x 4)

```
-1.0000e+10  1.0000e+10  1.0000e+10 -1.0000e+10
 1.0000e+10 -2.0000e+10 -1.0000e+10  2.0000e+10
 1.0000e+10 -1.0000e+10 -2.0000e+10  2.0000e+10
-1.0000e+10  2.0000e+10  2.0000e+10 -4.0000e+10
```

dg (4 x 4)

```
-488.30      -390.60      -390.60      -195.33
 634.79       781.21       390.60       585.98
 634.79       488.26       683.55       585.98
-781.27      -976.52      -781.21      -1367.3
```

Computing a Hessian

In principle, you can use the `fdjac` function repeatedly to evaluate higher-order derivatives. However, you should be aware that you may encounter rather serious numerical issues. For this reason, `gretl` provides a function, similar to `fdjac`, for computing a Hessian directly, called `numhess`.

An example follows:

```
function scalar quad(matrix x, matrix A )
    return 0.5*qform(x', A)
end function
```

```

function matrix coljac(matrix x, matrix A)
    return fdjac(x, quad(x, A))'
end function

A = {23, -11; -11, 118}
x = {1;1}

set fdjac_quality 2
H0 = fdjac(x, "coljac(x, A)")
H1 = numhess(x, "quad(x, A)")
printf "\n%14.8f", H0
printf "\n%14.8f", H1

```

In this example, we use the function `quad` for evaluating a simple quadratic form $f(x) = \frac{1}{2}x'Ax$, for which the Hessian is trivially the matrix A . The matrix `H0` is obtained by using `fdjac` twice (at its best quality, that is with Richardson extrapolation on); the matrix `H1`, instead, is obtained directly via the `numhess` function. The result of the above script is:

```

22.99788411  -10.99983724
-10.99902343  117.99161784

23.00000000  -11.00000000
-11.00000000  118.00000000

```

which makes it apparent how much better the second result is (note that `H0` is not even symmetric, as it should be).

37.4 Numerical integration

The main tool that `gretl` offers in this area is integration via Gaussian quadrature. In practice, the evaluation of an integral of the kind

$$C = \int_A f(x) \omega(x) dx \quad (37.1)$$

is approximated via a suitable linear combination of the form

$$C \simeq \sum_{i=1}^q f(x_i) w(x_i), \quad (37.2)$$

where the q “quadrature points” x_1, x_2, \dots, x_q are suitably chosen and the corresponding weights $w(x_i)$ ensure that the approximation is optimal.

The `quadtable` function provides quadrature points and weights for the following list of problems:

Integral	Technique	Note
$\int_{-\infty}^{\infty} f(x) e^{-x^2} dx$	Gauss-Hermite	see below for the relationship with the Gaussian distribution
$\int_0^{\infty} f(x) e^{-x} dx$	Gauss-Laguerre	can be used for evaluating Laplace transforms numerically
$\int_a^b f(x) dx$	Gauss-Legendre	by default, $a = -1$ and $b = 1$

The `quadtable` function returns a $q \times 2$ matrix with the x_i points in the first column and the corresponding weights w_i in the second, so in practice you compute the desired integral of $f(x)$ by applying that function to the first column and then computing the inner product of the result by the second column.

In econometrics, Gaussian quadrature is most commonly used for evaluating expectations of functions of Gaussian random variables, that is, integrals of the form

$$E[f(X)] = \int_{-\infty}^{\infty} f(x)\varphi(x)dx$$

In this case, Gauss-Hermite quadrature can be readily applied, provided one modifies the integral above via a suitable change of variable, namely by defining $z = x/\sqrt{2}$ so that

$$\int_{-\infty}^{\infty} f(x) \frac{1}{\sqrt{2\pi}} e^{-x^2/2} dx = \frac{1}{\sqrt{\pi}} \int_{-\infty}^{\infty} f(\sqrt{2} \cdot z) \cdot e^{-z^2} dz$$

For example, consider the following script, in which we evaluate $E(e^X)$ and $E[\cos(X)]$ via Gaussian quadrature.

```
q = 10
Q = quadtable(q)

x = exp(sqrt(2) * Q[,1])
w = Q[,2] ./ sqrt($pi)
printf "E(exp(x)) = %16.14f (exact = %16.14f)\n", x'w, exp(0.5)

x = cos(sqrt(2) * Q[,1])
w = Q[,2] ./ sqrt($pi)
printf "E(cos(x)) = %16.14f (exact = %16.14f)\n", x'w, exp(-0.5)
```

The result is

```
E(exp(x)) = 1.64872127069823 (exact = 1.64872127070013)
E(cos(x)) = 0.60653065971146 (exact = 0.60653065971263)
```

Higher values of q will give a more precise approximation.

In fact, the full form of `quadtable`—which supports three optional arguments besides the required q —provides a shortcut which saves you the hassle of having to recalculate the integral with the change of variable. Suppose you want something like

$$C = E[f(X)] \quad X \sim N(\mu, \sigma^2)$$

Then you can use the syntax `quadtable(q, 1, m, s)`, where the 1 indicates Gauss-Hermite integration and the two final arguments give the mean and standard deviation. So for example if you want to compute $E(X^2)$, where $X \sim N(1, 0.25)$, you could use

```
# Note: no rescaling needed
Q = quadtable(q, 1, 1, 0.5)
printf "E(X^2) = %6.4f (exact = %6.4f)\n", (Q[,1].^2)'Q[,2], 1.25
```

which yields

```
E(X^2) = 1.2500 (exact = 1.2500)
```

See the *Gretl Command Reference* for more details.

Chapter 38

Discrete and censored dependent variables

This chapter deals with models for dependent variables that are discrete or censored or otherwise limited (as in event counts or durations, which must be positive) and that therefore call for estimation methods other than the classical linear model. We discuss several estimators (mostly based on the Maximum Likelihood principle), adding some details and examples to complement the material on these methods in the *Gretl Command Reference*.

38.1 Logit and probit models

It often happens that one wants to specify and estimate a model in which the dependent variable is not continuous, but discrete. A typical example is a model in which the dependent variable is the occupational status of an individual (1 = employed, 0 = unemployed). A convenient way of formalizing this situation is to consider the variable y_i as a Bernoulli random variable and analyze its distribution conditional on the explanatory variables x_i . That is,

$$y_i = \begin{cases} 1 & P_i \\ 0 & 1 - P_i \end{cases} \quad (38.1)$$

where $P_i = P(y_i = 1|x_i)$ is a given function of the explanatory variables x_i .

In most cases, the function P_i is a cumulative distribution function F , applied to a linear combination of the x_i s. In the probit model, the normal cdf is used, while the logit model employs the logistic function $\Lambda(\cdot)$. Therefore, we have

$$\text{probit} \quad P_i = F(z_i) = \Phi(z_i) \quad (38.2)$$

$$\text{logit} \quad P_i = F(z_i) = \Lambda(z_i) = \frac{1}{1 + e^{-z_i}} \quad (38.3)$$

$$z_i = \sum_{j=1}^k x_{ij}\beta_j \quad (38.4)$$

where z_i is commonly known as the *index* function. Note that in this case the coefficients β_j cannot be interpreted as the partial derivatives of $E(y_i|x_i)$ with respect to x_{ij} . However, for a given value of x_i it is possible to compute the vector of “slopes”, that is

$$\text{slope}_j(\tilde{x}) = \left. \frac{\partial F(z)}{\partial x_j} \right|_{z=\tilde{z}}$$

Gretl automatically computes the slopes, setting each explanatory variable at its sample mean.

Another, equivalent way of thinking about this model is in terms of an unobserved variable y_i^* which can be described thus:

$$y_i^* = \sum_{j=1}^k x_{ij}\beta_j + \varepsilon_i = z_i + \varepsilon_i \quad (38.5)$$

We observe $y_i = 1$ whenever $y_i^* > 0$ and $y_i = 0$ otherwise. If ε_i is assumed to be normal, then we have the probit model. The logit model arises if we assume that the density function of ε_i is

$$\lambda(\varepsilon_i) = \frac{\partial \Lambda(\varepsilon_i)}{\partial \varepsilon_i} = \frac{e^{-\varepsilon_i}}{(1 + e^{-\varepsilon_i})^2}$$

Both the probit and logit model are estimated in gretl via maximum likelihood, where the log-likelihood can be written as

$$L(\beta) = \sum_{y_i=0} \ln[1 - F(z_i)] + \sum_{y_i=1} \ln F(z_i), \quad (38.6)$$

which is always negative, since $0 < F(\cdot) < 1$. Since the score equations do not have a closed form solution, numerical optimization is used. However, in most cases this is totally transparent to the user, since usually only a few iterations are needed to ensure convergence. The `--verbose` switch can be used to track the maximization algorithm.

By way of example, the commands below reproduce results given in chapter 21 of [Greene \(2000\)](#), regarding the effectiveness of a program for teaching economics.

```
open greene19_1
logit GRADE const GPA TUCE PSI
probit GRADE const GPA TUCE PSI
```

The binary dependent variable, GRADE, equals 1 if a student's grade improved over a certain period, 0 otherwise. The independent variables are PSI (= 1 if the student participated in the program in question, otherwise 0) plus two controls, the student's initial Grade Point Average (GPA) and score on a prior economics test (TUCE). Output is shown in Table 38.1. Note that for the probit model a conditional moment test on skewness and kurtosis ([Bera, Jarque and Lee, 1984](#)) is printed automatically as a test for normality.

In this context, the `$uhat` accessor function takes a special meaning: it returns generalized residuals as defined in [Gourieroux, Monfort, Renault and Trognon \(1987\)](#), which can be interpreted as unbiased estimators of the latent disturbances ε_i . These are defined as

$$u_i = \begin{cases} y_i - \hat{P}_i & \text{for the logit model} \\ y_i \cdot \frac{\phi(\hat{z}_i)}{\Phi(\hat{z}_i)} - (1 - y_i) \cdot \frac{\phi(\hat{z}_i)}{1 - \Phi(\hat{z}_i)} & \text{for the probit model} \end{cases} \quad (38.7)$$

Among other uses, generalized residuals are often used for diagnostic purposes. For example, it is very easy to set up an omitted variables test equivalent to the familiar LM test in the context of a linear regression; example 38.1 shows how to perform a variable addition test.

Listing 38.1: Variable addition test in a probit model [\[Download ▼\]](#)

```
open greene19_1

probit GRADE const GPA PSI
series u = $uhat
ols u const GPA PSI TUCE -q
printf "Variable addition test for TUCE:\n"
printf "Rsq * T = %g (p. val. = %g)\n", $trsqr, pvalue(X,1,$trsqr)
```

Odds ratios

A noteworthy feature of the binary logit model is that the regression coefficients have an interpretation as log odds ratios, where the odds ratio is $0 < P(y = 1)/P(y = 0) < \infty$. In the logit example above the coefficient on TUCE has a value of 0.095. The corresponding odds ratio is then $e^{0.095} = 1.10$, meaning that the estimated effect of a unit increase in TUCE is to move the odds ratio by 10 percent in favor of GRADE = 1.

Model 1: Logit estimates using the 32 observations 1-32
Dependent variable: GRADE

VARIABLE	COEFFICIENT	STDERROR	T STAT	SLOPE (at mean)
const	-13.0213	4.93132	-2.641	
GPA	2.82611	1.26294	2.238	0.533859
TUCE	0.0951577	0.141554	0.672	0.0179755
PSI	2.37869	1.06456	2.234	0.449339

Mean of GRADE = 0.344

Number of cases 'correctly predicted' = 26 (81.2%)

$f(\beta'x)$ at mean of independent vars = 0.189

McFadden's pseudo-R-squared = 0.374038

Log-likelihood = -12.8896

Likelihood ratio test: Chi-square(3) = 15.4042 (p-value 0.001502)

Akaike information criterion (AIC) = 33.7793

Schwarz Bayesian criterion (BIC) = 39.6422

Hannan-Quinn criterion (HQC) = 35.7227

		Predicted	
		0	1
Actual	0	18	3
	1	3	8

Model 2: Probit estimates using the 32 observations 1-32
Dependent variable: GRADE

VARIABLE	COEFFICIENT	STDERROR	T STAT	SLOPE (at mean)
const	-7.45232	2.54247	-2.931	
GPA	1.62581	0.693883	2.343	0.533347
TUCE	0.0517288	0.0838903	0.617	0.0169697
PSI	1.42633	0.595038	2.397	0.467908

Mean of GRADE = 0.344

Number of cases 'correctly predicted' = 26 (81.2%)

$f(\beta'x)$ at mean of independent vars = 0.328

McFadden's pseudo-R-squared = 0.377478

Log-likelihood = -12.8188

Likelihood ratio test: Chi-square(3) = 15.5459 (p-value 0.001405)

Akaike information criterion (AIC) = 33.6376

Schwarz Bayesian criterion (BIC) = 39.5006

Hannan-Quinn criterion (HQC) = 35.581

		Predicted	
		0	1
Actual	0	18	3
	1	3	8

Test for normality of residual -

Null hypothesis: error is normally distributed

Test statistic: Chi-square(2) = 3.61059

with p-value = 0.164426

Table 38.1: Example logit and probit output

When a binary logit model is estimated via the gretl GUI, the Analysis menu in the model output window includes an “Odds ratios” item. This opens a window showing the odds ratios along with standard errors (obtained via the delta method) plus a 95 percent confidence interval, as illustrated below.

95% confidence intervals
 $z(0.025) = 1.9600$

	odds ratio	std. error	low	high
GPA	16.8797	21.3181	1.42019	200.624
TUCE	1.09983	0.155686	0.833365	1.45150
PSI	10.7907	11.4874	1.33934	86.9380

Note, however, that confidence intervals shown are not calculated using the delta-method standard errors; rather, the bounds are obtained by exponentiating the bounds of regular confidence intervals for the coefficients. This makes sense on the assumption that the coefficients themselves are more likely to be normally distributed than their exponentials.

Odds ratio information can also be retrieved following binary logit estimation via scripting. In this case it takes the form of a matrix, provided by the `$oddsratios` accessor or as `$model.oddsratios`.

The perfect prediction problem

One curious characteristic of logit and probit models is that (quite paradoxically) estimation is not feasible if a model fits the data perfectly; this is called the *perfect prediction problem*. The reason why this problem arises is easy to see by considering equation (38.6): if for some vector β and scalar k it's the case that $z_i < k$ whenever $y_i = 0$ and $z_i > k$ whenever $y_i = 1$, the same thing is true for any multiple of β . Hence, $L(\beta)$ can be made arbitrarily close to 0 simply by choosing enormous values for β . As a consequence, the log-likelihood has no maximum, despite being bounded.

Gretl has a mechanism for preventing the algorithm from iterating endlessly in search of a non-existent maximum. One sub-case of interest is when the perfect prediction problem arises because of a single binary explanatory variable. In this case, the offending variable is dropped from the model and estimation proceeds with the reduced specification. Nevertheless, it may happen that no single “perfect classifier” exists among the regressors, in which case estimation is simply impossible and the algorithm stops with an error. This behavior is triggered during the iteration process if

$$\max_{i:y_i=0} z_i < \min_{i:y_i=1} z_i$$

If this happens, unless your model is trivially mis-specified (like predicting if a country is an oil exporter on the basis of oil revenues), it is normally a small-sample problem: you probably just don't have enough data to estimate your model. You may want to drop some of your explanatory variables.

This problem is well analyzed in [Stokes \(2004\)](#); the results therein are replicated in the example script `murder_rates.inp`.

38.2 Ordered response models

These models constitute a simple variation on ordinary logit/probit models, and are usually applied when the dependent variable is a discrete and ordered measurement—not simply binary, but on an ordinal rather than an interval scale. For example, this sort of model may be applied when the dependent variable is a qualitative assessment such as “Good”, “Average” and “Bad”.

In the general case, consider an ordered response variable, y , that can take on any of the $J+1$ values $0, 1, 2, \dots, J$. We suppose, as before, that underlying the observed response is a latent variable,

$$y^* = X\beta + \varepsilon = z + \varepsilon$$

Now define “cut points”, $\alpha_1 < \alpha_2 < \dots < \alpha_J$, such that

$$\begin{aligned} y &= 0 & \text{if } y^* \leq \alpha_1 \\ y &= 1 & \text{if } \alpha_1 < y^* \leq \alpha_2 \\ &\vdots \\ y &= J & \text{if } y^* > \alpha_J \end{aligned}$$

For example, if the response takes on three values there will be two such cut points, α_1 and α_2 .

The probability that individual i exhibits response j , conditional on the characteristics x_i , is then given by

$$P(y_i = j | x_i) = \begin{cases} P(y^* \leq \alpha_1 | x_i) = F(\alpha_1 - z_i) & \text{for } j = 0 \\ P(\alpha_j < y^* \leq \alpha_{j+1} | x_i) = F(\alpha_{j+1} - z_i) - F(\alpha_j - z_i) & \text{for } 0 < j < J \\ P(y^* > \alpha_J | x_i) = 1 - F(\alpha_J - z_i) & \text{for } j = J \end{cases} \quad (38.8)$$

The unknown parameters α_j are estimated jointly with the β s via maximum likelihood. The $\hat{\alpha}_j$ estimates are reported by gretl as `cut1`, `cut2` and so on. For the probit variant, a conditional moment test for normality constructed in the spirit of [Chesher and Irish \(1987\)](#) is also included.

Note that the α_j parameters can be shifted arbitrarily by adding a constant to z_i , so the model is under-identified if there is some linear combination of the explanatory variables which is constant. The most obvious case in which this occurs is when the model contains a constant term; for this reason, gretl drops automatically the intercept if present. However, it may happen that the user inadvertently specifies a list of regressors that may be combined in such a way to produce a constant (for example, by using a full set of dummy variables for a discrete factor). If this happens, gretl will also drop any offending regressors.

In order to apply these models in gretl, the dependent variable must either take on only non-negative integer values, or be explicitly marked as discrete. (In case the variable has non-integer values, it will be recoded internally.) Note that gretl does not provide a separate command for ordered models: the `logit` and `probit` commands automatically estimate the ordered version if the dependent variable is acceptable, but not binary.

Listing 38.2 reproduces the results presented in section 15.10 of [Wooldridge \(2002a\)](#). The question of interest in this analysis is what difference it makes, to the allocation of assets in pension funds, whether individual plan participants have a choice in the matter. The response variable is an ordinal measure of the weight of stocks in the pension portfolio. Having reported the results of estimation of the ordered model, Wooldridge illustrates the effect of the choice variable by reference to an “average” participant. The example script shows how one can compute this effect in gretl.

After estimating ordered models, the `$uhat` accessor yields generalized residuals as in binary models; additionally, the `$yhat` accessor function returns \hat{z}_i , so it is possible to compute an unbiased estimator of the latent variable y_i^* simply by adding the two together.

38.3 Multinomial logit

When the dependent variable is not binary and does not have a natural ordering, *multinomial* models are used. Multinomial logit is supported in gretl via the `--multinomial` option to the `logit` command. Simple models can also be handled via the `mle` command (see chapter 26). We give here an example of such a model. Let the dependent variable, y_i , take on integer values $0, 1, \dots, p$. The probability that $y_i = k$ is given by

$$P(y_i = k | x_i) = \frac{\exp(x_i \beta_k)}{\sum_{j=0}^p \exp(x_i \beta_j)}$$

Listing 38.2: Ordered probit model [\[Download ▼\]](#)

```

/*
Replicate the results in Wooldridge, Econometric Analysis of Cross
Section and Panel Data, section 15.10, using pension-plan data from
Papke (AER, 1998).

The dependent variable, pctstck (percent stocks), codes the asset
allocation responses of "mostly bonds", "mixed" and "mostly stocks"
as {0, 50, 100}.

The independent variable of interest is "choice", a dummy indicating
whether individuals are able to choose their own asset allocations.
*/

open pension.gdt

# demographic characteristics of participant
list DEMOG = age educ female black married
# dummies coding for income level
list INCOME = finc25 finc35 finc50 finc75 finc100 finc101

# Papke's OLS approach
ols pctstck const choice DEMOG INCOME wealth89 prftshr
# save the OLS choice coefficient
choice_ols = $coeff(choice)

# estimate ordered probit
probit pctstck choice DEMOG INCOME wealth89 prftshr

k = $ncoeff
matrix b = $coeff[1:k-2]
a1 = $coeff[k-1]
a2 = $coeff[k]

/*
Wooldridge illustrates the 'choice' effect in the ordered probit
by reference to a single, non-black male aged 60, with 13.5 years
of education, income in the range $50K - $75K and wealth of $200K,
participating in a plan with profit sharing.
*/
matrix X = {60, 13.5, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 200, 1}

# with 'choice' = 0
scalar Xb = (0 ~ X) * b
P0 = cdf(N, a1 - Xb)
P50 = cdf(N, a2 - Xb) - P0
P100 = 1 - cdf(N, a2 - Xb)
E0 = 50 * P50 + 100 * P100

# with 'choice' = 1
Xb = (1 ~ X) * b
P0 = cdf(N, a1 - Xb)
P50 = cdf(N, a2 - Xb) - P0
P100 = 1 - cdf(N, a2 - Xb)
E1 = 50 * P50 + 100 * P100

printf "\nWith choice, E(y) = %.2f, without E(y) = %.2f\n", E1, E0
printf "Estimated choice effect via ML = %.2f (OLS = %.2f)\n", E1 - E0,
choice_ols

```

For the purpose of identification one of the outcomes must be taken as the “baseline”; it is usually assumed that $\beta_0 = 0$, in which case

$$P(y_i = k|x_i) = \frac{\exp(x_i\beta_k)}{1 + \sum_{j=1}^p \exp(x_i\beta_j)}$$

and

$$P(y_i = 0|x_i) = \frac{1}{1 + \sum_{j=1}^p \exp(x_i\beta_j)}.$$

Listing 38.3: Multinomial logit

```
open keane.gdt
smpl year==87 --restrict
logit status 0 educ exper expersq black --multinomial
```

Output (selected portions):

```
Model 1: Multinomial Logit, using observations 1-1738 (n = 1717)
Missing or incomplete observations dropped: 21
Dependent variable: status
Standard errors based on Hessian
```

	coefficient	std. error	z	p-value	

status = 2					
const	10.2779	1.13334	9.069	1.20e-19	***
educ	-0.673631	0.0698999	-9.637	5.57e-22	***
exper	-0.106215	0.173282	-0.6130	0.5399	
expersq	-0.0125152	0.0252291	-0.4961	0.6199	
black	0.813017	0.302723	2.686	0.0072	***
status = 3					
const	5.54380	1.08641	5.103	3.35e-07	***
educ	-0.314657	0.0651096	-4.833	1.35e-06	***
exper	0.848737	0.156986	5.406	6.43e-08	***
expersq	-0.0773003	0.0229217	-3.372	0.0007	***
black	0.311361	0.281534	1.106	0.2687	

Mean dependent var	2.691322	S.D. dependent var	0.573502
Log-likelihood	-907.8572	Akaike criterion	1835.714
Schwarz criterion	1890.198	Hannan-Quinn	1855.874

```
Number of cases 'correctly predicted' = 1366 (79.6%)
Likelihood ratio test: Chi-square(8) = 583.722 [0.0000]
```

Listing 38.3 reproduces Table 15.2 in [Wooldridge \(2002a\)](#), based on data on career choice from [Keane and Wolpin \(1997\)](#). The dependent variable is the occupational status of an individual (0 = in school; 1 = not in school and not working; 2 = working), and the explanatory variables are education and work experience (linear and square) plus a “black” binary variable. The full data set is a panel; here the analysis is confined to a cross-section for 1987.

38.4 Bivariate probit

The bivariate probit model is a two-equation system in which each equation is a probit model and the two disturbance terms may not be independent. In formulae,

$$y_{1,i}^* = \sum_{j=1}^{k_1} x_{ij}\beta_j + \varepsilon_{1,i} \quad y_{1,i} = 1 \iff y_{1,i}^* > 0 \quad (38.9)$$

$$y_{2,i}^* = \sum_{j=1}^{k_2} z_{ij}\gamma_j + \varepsilon_{2,i} \quad y_{2,i} = 1 \iff y_{2,i}^* > 0 \quad (38.10)$$

$$\begin{bmatrix} \varepsilon_{1,i} \\ \varepsilon_{2,i} \end{bmatrix} \sim N \left[0, \begin{pmatrix} 1 & \rho \\ \rho & 1 \end{pmatrix} \right] \quad (38.11)$$

If ρ were 0, ML estimation of the parameters β_j and γ_j could be accomplished by estimating the two equations separately. In the general case, however, joint estimation is required for maximal efficiency.

The gretl command for this model is `biprobit`, which performs ML estimation via numerical optimization using the Newton-Raphson method with analytical derivatives. An example of usage is provided in the `biprobit.inp` sample script. The command takes either three or four arguments, the first three being series names for y_1 and y_2 and a list of explanatory variables. In the common case when the regressors are the same for the two equations this is sufficient, but if z differs from x a second list should be appended following a semicolon, as in:

```
biprobit y1 y2 X ; Z
```

Output from estimation includes a Likelihood Ratio test for the hypothesis $\rho = 0$.¹ This can be retrieved in the form of a bundle named `independence_test` under the `$model` accessor, as in

```
? eval $model.independence_test
bundle:
  dfn = 1
  test = 204.066
  pvalue = 2.70739e-46
```

Since `biprobit` estimates a two-equation system, the `$uhat` and `$yhat` accessors provide matrices rather than series as usual. Specifically, `$uhat` gives a two-column matrix containing the generalized residuals, while `$yhat` contains four columns holding the estimated probabilities of the possible joint outcomes: $(y_{1,i}, y_{1,i}) = (1, 1)$ in column 1, $(y_{1,i}, y_{2,i}) = (1, 0)$ in column 2, $(y_{1,i}, y_{2,i}) = (0, 1)$ in column 3 and $(y_{1,i}, y_{2,i}) = (0, 0)$ in column 4.

38.5 Panel estimators

When your dataset is a panel, the traditional choice for binary dependent variable models was, for many years, to use logit with fixed effects and probit with random effects (see 23.1 for a brief discussion of this dichotomy in the context of linear models). Nowadays the choice is somewhat wider but the two traditional models are by and large what practitioners use as routine tools.

Gretl provides FE logit via the function package `felogit`,² RE probit natively. Provided your dataset has a panel structure, the latter option can be obtained by adding the `--random` option to the `probit` command:

¹Note that if the `--robust` option is given to `biprobit`—and therefore the estimator is meant to be QMLE—this test may not be valid, even asymptotically.

²See http://gretl.sourceforge.net/current_fnfiles/felogit.gfn.


```
probit depvar const indvar1 indvar2 --random
```

as exemplified in the `reprobit.inp` sample script. The numerical technique used for this particular estimator is *Gauss-Hermite quadrature*, which we'll now briefly describe. Generalizing equation (38.5) to a panel context, we get

$$y_{i,t}^* = \sum_{j=1}^k x_{ijt} \beta_j + \alpha_i + \varepsilon_{i,t} = z_{i,t} + \omega_{i,t} \quad (38.12)$$

in which we assume that the individual effect, α_i , and the disturbance term, $\varepsilon_{i,t}$, are mutually independent zero-mean Gaussian random variables. The composite error term, $\omega_{i,t} = \alpha_i + \varepsilon_{i,t}$, is therefore a normal r. v. with mean zero and variance $1 + \sigma_\alpha^2$. Because of the individual effect, α_i , observations for the same unit are not independent; the likelihood therefore has to be evaluated on a per-unit basis, as

$$\ell_i = \log P[y_{i,1}, y_{i,2}, \dots, y_{i,T}].$$

and there's no way to write the above as a product of individual terms.

However, the above probability *could* be written as a product if we were to treat α_i as a constant; in that case we would have

$$\ell_i | \alpha_i = \sum_{t=1}^T \Phi \left[(2y_{i,t} - 1) \frac{x_{ijt} \beta_j + \alpha_i}{\sqrt{1 + \sigma_\alpha^2}} \right]$$

so that we can compute ℓ_i by integrating α_i out as

$$\ell_i = E(\ell_i | \alpha_i) = \int_{-\infty}^{\infty} (\ell_i | \alpha_i) \frac{\varphi(\alpha_i)}{\sqrt{1 + \sigma_\alpha^2}} d\alpha_i$$

The technique known as Gauss-Hermite quadrature is simply a way of approximating the above integral via a sum of carefully chosen terms:³

$$\ell_i \simeq \sum_{k=1}^m (\ell_i | \alpha_i = n_k) w_k$$

where the numbers n_k and w_k are known as *quadrature points* and *weights*, respectively. Of course, accuracy improves with higher values of m , but so does CPU usage. Note that this technique can also be used in more general cases by using the `quadtable()` function and the `mle` command via the apparatus described in chapter 26. Here, however, the calculations were hard-coded in C for maximal speed and efficiency.

Experience shows that a reasonable compromise can be achieved in most cases by choosing m in the order of 20 or so; gretl uses 32 as a default value, but this can be changed via the `--quadpoints` option, as in

```
probit y const x1 x2 x3 --random --quadpoints=48
```

38.6 The Tobit model

The Tobit model is used when the dependent variable of a model is *censored*. Assume a latent variable y_i^* can be described as

$$y_i^* = \sum_{j=1}^k x_{ij} \beta_j + \varepsilon_i,$$

³Some have suggested using a more refined method called *adaptive* Gauss-Hermite quadrature; this is not implemented in gretl.

where $\varepsilon_i \sim N(0, \sigma^2)$. If y_i^* were observable, the model's parameters could be estimated via ordinary least squares. On the contrary, suppose that we observe y_i , defined as

$$y_i = \begin{cases} a & \text{for } y_i^* \leq a \\ y_i^* & \text{for } a < y_i^* < b \\ b & \text{for } y_i^* \geq b \end{cases} \quad (38.13)$$

In most cases found in the applied literature, $a = 0$ and $b = \infty$, so in practice negative values of y_i^* are not observed and are replaced by zeros.

In this case, regressing y_i on the x_i s does not yield consistent estimates of the parameters β , because the conditional mean $E(y_i|x_i)$ is not equal to $\sum_{j=1}^k x_{ij}\beta_j$. It can be shown that restricting the sample to non-zero observations would not yield consistent estimates either. The solution is to estimate the parameters via maximum likelihood. The syntax is simply

```
tobit depvar indvars
```

As usual, progress of the maximization algorithm can be tracked via the `--verbose` switch, while `$uhat` returns the generalized residuals. Note that in this case the generalized residual is defined as $\hat{u}_i = E(\varepsilon_i|y_i = 0)$ for censored observations, so the familiar equality $\hat{u}_i = y_i - \hat{y}_i$ only holds for uncensored observations, that is, when $y_i > 0$.

An important difference between the Tobit estimator and OLS is that the consequences of non-normality of the disturbance term are much more severe: non-normality implies inconsistency for the Tobit estimator. For this reason, the output for the Tobit model includes the [Chesher and Irish \(1987\)](#) normality test by default.

The general case in which a is nonzero and/or b is finite can be handled by using the options `--llimit` and `--rlimit`. So, for example,

```
tobit depvar indvars --llimit=10
```

would tell gretl that the left bound a is set to 10.

38.7 Interval regression

The interval regression model arises when the dependent variable is unobserved for some (possibly all) observations; what we observe instead is an interval in which the dependent variable lies. In other words, the data generating process is assumed to be

$$y_i^* = x_i\beta + \varepsilon_i$$

but we only know that $m_i \leq y_i^* \leq M_i$, where the interval may be left- or right-unbounded (but not both). If $m_i = M_i$, we effectively observe y_i^* and no information loss occurs. In practice, each observation belongs to one of four categories:

1. left-unbounded, when $m_i = -\infty$,
2. right-unbounded, when $M_i = \infty$,
3. bounded, when $-\infty < m_i < M_i < \infty$ and
4. point observations when $m_i = M_i$.

It is interesting to note that this model bears similarities to other models in several special cases:

- When all observations are point observations the model trivially reduces to the ordinary linear regression model.

- The interval model could be thought of as an ordered probit model (see 38.2) in which the cut points (the α_j coefficients in eq. 38.8) are observed and don't need to be estimated.
- The Tobit model (see 38.6) is a special case of the interval model in which m_i and M_i do not depend on i , that is, the censoring limits are the same for all observations. As a matter of fact, gretl's `tobit` command is handled internally as a special case of the interval model.

The gretl command `intreg` estimates interval models by maximum likelihood, assuming normality of the disturbance term ϵ_i . Its syntax is

```
intreg minvar maxvar X
```

where `minvar` contains the m_i series, with NAs for left-unbounded observations, and `maxvar` contains M_i , with NAs for right-unbounded observations. By default, standard errors are computed using the negative inverse of the Hessian. If the `--robust` flag is given, then QML or Huber-White standard errors are calculated instead. In this case the estimated covariance matrix is a “sandwich” of the inverse of the estimated Hessian and the outer product of the gradient.

If the model specification contains regressors other than just a constant, the output includes a chi-square statistic for testing the joint null hypothesis that none of these regressors has any effect on the outcome. This is a Wald statistic based on the estimated covariance matrix. If you wish to construct a likelihood ratio test, this is easily done by estimating both the full model and the null model (containing only the constant), saving the log-likelihood in both cases via the `$lnl` accessor, and then referring twice the difference between the two log-likelihoods to the chi-square distribution with k degrees of freedom, where k is the number of additional regressors (see the `pvalue` command in the *Gretl Command Reference*). Also included is a conditional moment normality test, similar to those provided for the probit, ordered probit and Tobit models (see above). An example is contained in the sample script `wtp.inp`, provided with the gretl distribution.

As with the probit and Tobit models, after a model has been estimated the `$uhat` accessor returns the generalized residual, which is an estimate of ϵ_i : more precisely, it equals $y_i - x_i\hat{\beta}$ for point observations and $E(\epsilon_i|m_i, M_i, x_i)$ otherwise. Note that it is possible to compute an unbiased predictor of y_i^* by summing this estimate to $x_i\hat{\beta}$. Listing 38.4 shows an example. As a further similarity with Tobit, the interval regression model may deliver inconsistent estimates if the disturbances are non-normal; hence, the Chesher and Irish (1987) test for normality is included by default here too.

38.8 Sample selection model

In the sample selection model (also known as “Tobit II” model), there are two latent variables:

$$y_i^* = \sum_{j=1}^k x_{ij}\beta_j + \epsilon_i \quad (38.14)$$

$$s_i^* = \sum_{j=1}^p z_{ij}\gamma_j + \eta_i \quad (38.15)$$

and the observation rule is given by

$$y_i = \begin{cases} y_i^* & \text{for } s_i^* > 0 \\ \blacklozenge & \text{for } s_i^* \leq 0 \end{cases} \quad (38.16)$$

In this context, the \blacklozenge symbol indicates that for some observations we simply do not have data on y : y_i may be 0, or missing, or anything else. A dummy variable d_i is normally used to set censored observations apart.

Listing 38.4: Interval model on artificial data [\[Download ▼\]](#)

```

nulldata 100
# generate artificial data
set seed 201449
x = normal()
epsilon = 0.2*normal()
ystar = 1 + x + epsilon
lo_bound = floor(ystar)
hi_bound = ceil(ystar)

# run the interval model
intreg lo_bound hi_bound const x

# estimate ystar
gen_resid = $uhat
yhat = $yhat + gen_resid
corr ystar yhat

```

Output (selected portions):

Model 1: Interval estimates using the 100 observations 1-100
 Lower limit: lo_bound, Upper limit: hi_bound

	coefficient	std. error	t-ratio	p-value
const	0.993762	0.0338325	29.37	1.22e-189 ***
x	0.986662	0.0319959	30.84	8.34e-209 ***

Chi-square(1)	950.9270	p-value	8.3e-209
Log-likelihood	-44.21258	Akaike criterion	94.42517
Schwarz criterion	102.2407	Hannan-Quinn	97.58824

```

sigma = 0.223273
Left-unbounded observations: 0
Right-unbounded observations: 0
Bounded observations: 100
Point observations: 0

```

...

```

corr(ystar, yhat) = 0.98960092
Under the null hypothesis of no correlation:
t(98) = 68.1071, with two-tailed p-value 0.0000

```

One of the most popular applications of this model in econometrics is a wage equation coupled with a labor force participation equation: we only observe the wage for the employed. If y_i^* and s_i^* were (conditionally) independent, there would be no reason not to use OLS for estimating equation (38.14); otherwise, OLS does not yield consistent estimates of the parameters β_j .

Since conditional independence between y_i^* and s_i^* is equivalent to conditional independence between ε_i and η_i , one may model the co-dependence between ε_i and η_i as

$$\varepsilon_i = \lambda\eta_i + v_i;$$

substituting the above expression in (38.14), you obtain the model that is actually estimated:

$$y_i = \sum_{j=1}^k x_{ij}\beta_j + \lambda\hat{\eta}_i + v_i,$$

so the hypothesis that censoring does not matter is equivalent to the hypothesis $H_0 : \lambda = 0$, which can be easily tested.

The parameters can be estimated via maximum likelihood under the assumption of joint normality of ε_i and η_i ; however, a widely used alternative method yields the so-called *Heckit* estimator, named after Heckman (1979). The procedure can be briefly outlined as follows: first, a probit model is fit on equation (38.15); next, the generalized residuals are inserted in equation (38.14) to correct for the effect of sample selection.

Gretl provides the `heckit` command to carry out estimation; its syntax is

```
heckit y X ; d Z
```

where y is the dependent variable, X is a list of regressors, d is a dummy variable holding 1 for uncensored observations and Z is a list of explanatory variables for the censoring equation.

Since in most cases maximum likelihood is the method of choice, by default gretl computes ML estimates. The 2-step Heckit estimates can be obtained by using the `--two-step` option. After estimation, the `$uhat` accessor contains the generalized residuals. As in the ordinary Tobit model, the residuals equal the difference between actual and fitted y_i only for uncensored observations (those for which $d_i = 1$).

Listing 38.5: Heckit model [\[Download ▼\]](#)

```
open mroz87.gdt

series EXP2 = AX^2
series WA2 = WA^2
series KIDS = (KL6+K618)>0

# Greene's specification

list X = const AX EXP2 WE CIT
list Z = const WA WA2 FAMINC KIDS WE

heckit WW X ; LFP Z --two-step
heckit WW X ; LFP Z

# Wooldridge's specification

series NWINC = FAMINC - WW*WHRS
series lww = log(WW)
list X = const WE AX EXP2
list Z = X NWINC WA KL6 K618

heckit lww X ; LFP Z --two-step
```

Listing 38.5 shows two estimates from the dataset used in Mroz (1987): the first one replicates Table 22.7 in Greene (2003),⁴ while the second one replicates table 17.1 in Wooldridge (2002a).

⁴Note that the estimates given by gretl do not coincide with those found in the printed volume. They do, however,

38.9 Count data

Here the dependent variable is assumed to be a non-negative integer—for example, the number of Nobel Prize winners in a given country per year, the number of vehicles crossing a certain intersection per hour, the number of bank failures per year. A probabilistic description of such a variable must hinge on some discrete distribution and the one most commonly employed is the Poisson, according to which, for a random variable Y and a specific realization y ,

$$P(Y = y) = \frac{e^{-\lambda} \lambda^y}{y!}, \quad y = 0, 1, 2 \dots$$

where the single parameter λ is both the mean and the variance of Y . In an econometric context we generally want to treat λ as specific to the observation, i , and driven by covariates X_i via a parameter vector β . The standard way of allowing for this is the exponential mean function,

$$\lambda_i \equiv \exp(X_i \beta)$$

hence leading to

$$P(Y_i = y) = \frac{\exp(-\exp(X_i \beta)) (\exp(X_i \beta))^y}{y!}$$

Given this model the log-likelihood for n observations can be written as

$$\ell = \sum_{i=1}^n (-\exp(X_i \beta) + y_i X_i \beta - \log y_i!)$$

Maximization of this quantity is quite straightforward, and is carried out in gretl using the syntax

```
poisson depvar indep
```

In some cases, an “offset” variable is needed: the count of occurrences of the outcome of interest in a given time is assumed to be strictly proportional to the offset variable t_i . In the epidemiology literature, the offset is known as “population at risk”. In this case λ is modeled as

$$\lambda_i = t_i \exp(X_i \beta)$$

The log-likelihood is not greatly complicated thereby. Here’s another way of thinking about the offset variable: its natural log is just another explanatory variable whose coefficient is constrained to equal 1.

If an offset variable is needed, it should be specified at the end of the command, separated from the list of explanatory variables by a semicolon, as in

```
poisson depvar indep ; offset
```

Overdispersion

As mentioned above, in the Poisson model $E(Y_i|X_i) = V(Y_i|X_i) = \lambda_i$, that is, the conditional mean equals the conditional variance by construction. In many cases this feature is at odds with the data; the conditional variance is often larger than the mean, a phenomenon known as overdispersion. The output from the `poisson` command includes a conditional moment test for overdispersion (as per Davidson and MacKinnon (2004), section 11.5), which is printed automatically after estimation.

Overdispersion can be attributed to unmodeled heterogeneity between individuals. Two data points with the same observable characteristics $X_i = X_j$ may differ because of some unobserved scale factor $s_i \neq s_j$ so that

$$E(Y_i|X_i, s_i) = \lambda_i s_i \neq \lambda_j s_j = E(Y_i|X_j, s_j)$$

match those found on the errata web page for Greene’s book: <http://pages.stern.nyu.edu/~wgreene/Text/Errata/ERRATA5.htm>.

even though $\lambda_i = \lambda_j$. In other words, Y_i is a Poisson random variable conditional on both X_i and s_i , but since s_i is unobservable, the only thing we can use, $P(Y_i|X_i)$, will *not* conform to the Poisson distribution.

It is often assumed that s_i can be represented as a gamma random variable with mean 1 and variance α . The parameter α , which measures the degree of heterogeneity between individuals, is then estimated jointly with the vector β .

In this case, the conditional probability that $Y_i = y$ given X_i can be shown to be

$$P(Y_i = y|X_i) = \frac{\Gamma(y + \alpha^{-1})}{\Gamma(\alpha^{-1})\Gamma(y + 1)} \left[\frac{\lambda_i}{\lambda_i + \alpha^{-1}} \right]^y \left[\frac{\alpha^{-1}}{\lambda_i + \alpha^{-1}} \right]^{\alpha^{-1}} \quad (38.17)$$

which is known as the Negative Binomial Model. The conditional mean is still $E(Y_i|X_i) = \lambda_i$, but the variance is $V(Y_i|X_i) = \lambda_i (1 + \lambda_i \alpha)$.

To estimate the Negative Binomial model in gretl, just substitute the keyword `negbin` for `poisson` in the commands shown above.

To be precise, the model 38.17 is that labeled NEGBIN2 by [Cameron and Trivedi \(1986\)](#). There's also a lesser-used NEGBIN1 variant, in which the conditional variance is a scalar multiple of the conditional mean; that is, $V(Y_i|X_i) = \lambda_i (1 + \gamma)$. This can be invoked in gretl by appending the option `--model1` to the `negbin` command.⁵

The two accessors `$yhat` and `$uhat` return the predicted values and generalized residuals, respectively. Note that `$uhat` is *not* equal to the difference between the dependent variable and `$yhat`.

Examples

Among the sample scripts supplied with gretl you can find `camtriv.inp`. This exemplifies the count-data estimators described above, based on a dataset analysed by [Cameron and Trivedi \(1998\)](#). The gretl package also contains a relevant dataset used by [McCullagh and Nelder \(1983\)](#), namely `mccullagh.gdt`, on which the Poisson and Negative Binomial estimators may be tried.

38.10 Duration models

In some contexts we wish to apply econometric methods to measurements of the duration of certain states. Classic examples include the following:

- From engineering, the “time to failure” of electronic or mechanical components: how long do, say, computer hard drives last until they malfunction?
- From the medical realm: how does a new treatment affect the time from diagnosis of a certain condition to exit from that condition (where “exit” might mean death or full recovery)?
- From economics: the duration of strikes, or of spells of unemployment.

In each case we may be interested in how the durations are distributed, and how they are affected by relevant covariates. There are several approaches to this problem; the one we discuss here—which is currently the only one supported by gretl—is estimation of a parametric model by means of Maximum Likelihood. In this approach we hypothesize that the durations follow some definite probability law and we seek to estimate the parameters of that law, factoring in the influence of covariates.

We may express the density of the durations as $f(t, X, \theta)$, where t is the length of time in the state in question, X is a matrix of covariates, and θ is a vector of parameters. The likelihood for a sample

⁵The “1” and “2” in these labels indicate the power to which λ_i is raised in the conditional variance expression.

of n observations indexed by i is then

$$L = \prod_{i=1}^n f(t_i, x_i, \theta)$$

Rather than working with the density directly, however, it is standard practice to factor $f(\cdot)$ into two components, namely a *hazard function*, λ , and a *survivor function*, S . The survivor function gives the probability that a state lasts at least as long as t ; it is therefore $1 - F(t, X, \theta)$ where F is the CDF corresponding to the density $f(\cdot)$. The hazard function addresses this question: given that a state has persisted as long as t , what is the likelihood that it ends within a short increment of time beyond t —that is, it ends between t and $t + \Delta$? Taking the limit as Δ goes to zero, we end up with the ratio of the density to the survivor function:⁶

$$\lambda(t, X, \theta) = \frac{f(t, X, \theta)}{S(t, X, \theta)} \quad (38.18)$$

so the log-likelihood can be written as

$$\ell = \sum_{i=1}^n \log f(t_i, x_i, \theta) = \sum_{i=1}^n \log \lambda(t_i, x_i, \theta) + \log S(t_i, x_i, \theta) \quad (38.19)$$

One point of interest is the shape of the hazard function, in particular its dependence (or not) on time since the state began. If λ does not depend on t we say the process in question exhibits *duration independence*: the probability of exiting the state at any given moment neither increases nor decreases based simply on how long the state has persisted to date. The alternatives are positive duration dependence (the likelihood of exiting the state rises, the longer the state has persisted) or negative duration dependence (exit becomes less likely, the longer it has persisted). Finally, the behavior of the hazard with respect to time need not be monotonic; some parameterizations allow for this possibility and some do not.

Since durations are inherently positive the probability distribution used in modeling must respect this requirement, giving a density of zero for $t \leq 0$. Four common candidates are the exponential, Weibull, log-logistic and log-normal, the Weibull being the most common choice. The table below displays the density and the hazard function for each of these distributions as they are commonly parameterized, written as functions of t alone. (ϕ and Φ denote, respectively, the Gaussian PDF and CDF.)

	density, $f(t)$	hazard, $\lambda(t)$
Exponential	$\gamma \exp(-\gamma t)$	γ
Weibull	$\alpha \gamma^\alpha t^{\alpha-1} \exp[-(\gamma t)^\alpha]$	$\alpha \gamma^\alpha t^{\alpha-1}$
Log-logistic	$\gamma \alpha \frac{(\gamma t)^{\alpha-1}}{[1 + (\gamma t)^\alpha]^2}$	$\gamma \alpha \frac{(\gamma t)^{\alpha-1}}{[1 + (\gamma t)^\alpha]}$
Log-normal	$\frac{1}{\sigma t} \phi[(\log t - \mu)/\sigma]$	$\frac{1}{\sigma t} \frac{\phi[(\log t - \mu)/\sigma]}{\Phi[-(\log t - \mu)/\sigma]}$

The hazard is constant for the exponential distribution. For the Weibull, it is monotone increasing in t if $\alpha > 1$, or monotone decreasing for $\alpha < 1$. (If $\alpha = 1$ the Weibull collapses to the exponential.) The log-logistic and log-normal distributions allow the hazard to vary with t in a non-monotonic fashion.

Covariates are brought into the picture by allowing them to govern one of the parameters of the density, so that durations are not identically distributed across cases. For example, when using

⁶For a fuller discussion see, for example, Davidson and MacKinnon (2004).

the log-normal distribution it is natural to make μ , the expected value of $\log t$, depend on the covariates, X . This is typically done via a linear index function: $\mu = X\beta$.

Note that the expressions for the log-normal density and hazard contain the term $(\log t - \mu)/\sigma$. Replacing μ with $X\beta$ this becomes $(\log t - X\beta)/\sigma$. As in [Kalbfleisch and Prentice \(2002\)](#), we define a shorthand label for this term:

$$w_i \equiv (\log t_i - x_i\beta)/\sigma \quad (38.20)$$

It turns out that this constitutes a useful simplifying change of variables for all of the distributions discussed here. The interpretation of the scale factor, σ , in the expression above depends on the distribution. For the log-normal, σ represents the standard deviation of $\log t$; for the Weibull and the log-logistic it corresponds to $1/\alpha$; and for the exponential it is fixed at unity. For distributions other than the log-normal, $X\beta$ corresponds to $-\log \gamma$, or in other words $\gamma = \exp(-X\beta)$.

With this change of variables, the density and survivor functions may be written compactly as follows (the exponential is the same as the Weibull).

	density, $f(w_i)$	survivor, $S(w_i)$
Weibull	$\exp(w_i - e^{w_i})$	$\exp(-e^{w_i})$
Log-logistic	$e^{w_i} (1 + e^{w_i})^{-2}$	$(1 + e^{w_i})^{-1}$
Log-normal	$\phi(w_i)$	$\Phi(-w_i)$

In light of the above we may think of the generic parameter vector θ , as in $f(t, X, \theta)$, as composed of the coefficients on the covariates, β , plus (in all cases but the exponential) the additional parameter σ .

A complication in estimation of θ is posed by “incomplete spells”. That is, in some cases the state in question may not have ended at the time the observation is made (e.g. some workers remain unemployed, some components have not yet failed). If we use t_i to denote the time from entering the state to either (a) exiting the state or (b) the observation window closing, whichever comes first, then all we know of the “right-censored” cases (b) is that the duration was at least as long as t_i . This can be handled by rewriting the the log-likelihood (compare [38.19](#)) as

$$\ell_i = \sum_{i=1}^n \delta_i \log S(w_i) + (1 - \delta_i) [-\log \sigma + \log f(w_i)] \quad (38.21)$$

where δ_i equals 1 for censored cases (incomplete spells), and 0 for complete observations. The rationale for this is that the log-density equals the sum of the log hazard and the log survivor function, but for the incomplete spells only the survivor function contributes to the likelihood. So in [\(38.21\)](#) we are adding up the log survivor function alone for the incomplete cases, plus the full log density for the completed cases.

Implementation in gretl and illustration

The `duration` command accepts a list of series on the usual pattern: dependent variable followed by covariates. If right-censoring is present in the data this should be represented by a dummy variable corresponding to δ_i above, separated from the covariates by a semicolon. For example,

```
duration durat 0 X ; cens
```

where `durat` measures durations, 0 represents the constant (which is required for such models), `X` is a named list of regressors, and `cens` is the censoring dummy.

By default the Weibull distribution is used; you can substitute any of the other three distributions discussed here by appending one of the option flags `--exponential`, `--loglogistic` or `--lognormal`.

Interpreting the coefficients in a duration model requires some care, and we will work through an illustrative case. The example comes from section 20.3 of Wooldridge (2002a) and it concerns criminal recidivism.⁷ The data (filename `recid.gdt`) pertain to a sample of 1,445 convicts released from prison between July 1, 1977 and June 30, 1978. The dependent variable is the time in months until they are again arrested. The information was gathered retrospectively by examining records in April 1984; the maximum possible length of observation is 81 months. Right-censoring is important: when the data were compiled about 62 percent had not been rearrested. The dataset contains several covariates, which are described in the data file; we will focus below on interpretation of the `married` variable, a dummy which equals 1 if the respondent was married when imprisoned.

Listing 38.6 shows the `gretl` commands for Weibull and log-normal models along with most of the output. Consider first the Weibull scale factor, σ . The estimate is 1.241 with a standard error of 0.048. (We don't print a z score and p -value for this term since $H_0 : \sigma = 0$ is not of interest.) Recall that σ corresponds to $1/\alpha$; we can be confident that α is less than 1, so recidivism displays negative duration dependence. This makes sense: it is plausible that if a past offender manages to stay out of trouble for an extended period his risk of engaging in crime again diminishes. (The exponential model would therefore not be appropriate in this case.)

On a priori grounds, however, we may doubt the monotonic decline in hazard that is implied by the Weibull specification. Even if a person is liable to return to crime, it seems relatively unlikely that he would do so straight out of prison. In the data, we find that only 2.6 percent of those followed were rearrested within 3 months. The log-normal specification, which allows the hazard to rise and then fall, may be more appropriate. Using the `duration` command again with the same covariates but the `--lognormal` flag, we get a log-likelihood of -1597 as against -1633 for the Weibull, confirming that the log-normal gives a better fit.

Let us now focus on the `married` coefficient, which is positive in both specifications but larger and more sharply estimated in the log-normal variant. The first thing is to get the interpretation of the sign right. Recall that $X\beta$ enters negatively into the intermediate variable w (equation 38.20). The Weibull hazard is $\lambda(w_i) = e^{w_i}$, so being married reduces the hazard of re-offending, or in other words lengthens the expected duration out of prison. The same qualitative interpretation applies for the log-normal.

To get a better sense of the married effect, it is useful to show its impact on the hazard across time. We can do this by plotting the hazard for two values of the index function $X\beta$: in each case the values of all the covariates other than `married` are set to their means (or some chosen values) while `married` is set first to 0 then to 1. Listing 38.7 provides a script that does this, and the resulting plots are shown in Figure 38.1. Note that when computing the hazards we need to multiply by the Jacobian of the transformation from t_i to $w_i = \log(t_i - x_i\beta)/\sigma$, namely $1/t$. Note also that the estimate of σ is available via the accessor `$sigma`, but it is also present as the last element in the coefficient vector obtained via `$coeff`.

A further difference between the Weibull and log-normal specifications is illustrated in the plots. The Weibull is an instance of a *proportional hazard* model. This means that for any sets of values of the covariates, x_i and x_j , the ratio of the associated hazards is invariant with respect to duration. In this example the Weibull hazard for unmarried individuals is always 1.1637 times that for married. In the log-normal variant, on the other hand, this ratio gradually declines from 1.6703 at one month to 1.1766 at 100 months.

Alternative representations of the Weibull model

One point to watch out for with the Weibull duration model is that the estimates may be represented in different ways. The representation given by `gretl` is sometimes called the *accelerated failure-time* (AFT) metric. An alternative that one sometimes sees is the *log relative-hazard* metric; in fact this is the metric used in Wooldridge's presentation of the recidivism example. To get from AFT estimates to log relative-hazard form it is necessary to multiply the coefficients by $-\sigma^{-1}$. For example, the

⁷Germán Rodríguez of Princeton University has a page discussing this example and displaying estimates from Stata at <http://data.princeton.edu/pop509/recid1.html>.

Listing 38.6: Models for recidivism data [\[Download ▼\]](#)

```

open recid.gdt
list X = workprg priors tserve felon alcohol drugs \
      black married educ age
duration durat 0 X ; cens
duration durat 0 X ; cens --lognormal

```

Partial output:

Model 1: Duration (Weibull), using observations 1-1445
 Dependent variable: durat

	coefficient	std. error	z	p-value	
const	4.22167	0.341311	12.37	3.85e-35	***
workprg	-0.112785	0.112535	-1.002	0.3162	
priors	-0.110176	0.0170675	-6.455	1.08e-10	***
tserve	-0.0168297	0.00213029	-7.900	2.78e-15	***
felon	0.371623	0.131995	2.815	0.0049	***
alcohol	-0.555132	0.132243	-4.198	2.69e-05	***
drugs	-0.349265	0.121880	-2.866	0.0042	***
black	-0.563016	0.110817	-5.081	3.76e-07	***
married	0.188104	0.135752	1.386	0.1659	
educ	0.0289111	0.0241153	1.199	0.2306	
age	0.00462188	0.000664820	6.952	3.60e-12	***
sigma	1.24090	0.0482896			

Chi-square(10)	165.4772	p-value	2.39e-30
Log-likelihood	-1633.032	Akaike criterion	3290.065

Model 2: Duration (log-normal), using observations 1-1445
 Dependent variable: durat

	coefficient	std. error	z	p-value	
const	4.09939	0.347535	11.80	4.11e-32	***
workprg	-0.0625693	0.120037	-0.5213	0.6022	
priors	-0.137253	0.0214587	-6.396	1.59e-10	***
tserve	-0.0193306	0.00297792	-6.491	8.51e-11	***
felon	0.443995	0.145087	3.060	0.0022	***
alcohol	-0.634909	0.144217	-4.402	1.07e-05	***
drugs	-0.298159	0.132736	-2.246	0.0247	**
black	-0.542719	0.117443	-4.621	3.82e-06	***
married	0.340682	0.139843	2.436	0.0148	**
educ	0.0229194	0.0253974	0.9024	0.3668	
age	0.00391028	0.000606205	6.450	1.12e-10	***
sigma	1.81047	0.0623022			

Chi-square(10)	166.7361	p-value	1.31e-30
Log-likelihood	-1597.059	Akaike criterion	3218.118

Listing 38.7: Create plots showing conditional hazards [\[Download ▼\]](#)

```

open recid.gdt -q

# leave 'married' separate for analysis
list X = workprg priors tserve felon alcohol drugs \
      black educ age

# Weibull variant
duration durat 0 X married ; cens
# coefficients on all Xs apart from married
matrix beta_w = $coeff[1:$ncoeff-2]
# married coefficient
scalar mc_w = $coeff[$ncoeff-1]
scalar s_w = $sigma

# Log-normal variant
duration durat 0 X married ; cens --lognormal
matrix beta_n = $coeff[1:$ncoeff-2]
scalar mc_n = $coeff[$ncoeff-1]
scalar s_n = $sigma

list allX = 0 X
# evaluate X\beta at means of all variables except marriage
scalar Xb_w = meanc({allX}) * beta_w
scalar Xb_n = meanc({allX}) * beta_n

# construct two plot matrices
matrix mat_w = zeros(100, 3)
matrix mat_n = zeros(100, 3)

loop t=1..100
  # first column, duration
  mat_w[t, 1] = t
  mat_n[t, 1] = t
  wi_w = (log(t) - Xb_w)/s_w
  wi_n = (log(t) - Xb_n)/s_n
  # second col: hazard with married = 0
  mat_w[t, 2] = (1/t) * exp(wi_w)
  mat_n[t, 2] = (1/t) * pdf(z, wi_n) / cdf(z, -wi_n)
  wi_w = (log(t) - (Xb_w + mc_w))/s_w
  wi_n = (log(t) - (Xb_n + mc_n))/s_n
  # third col: hazard with married = 1
  mat_w[t, 3] = (1/t) * exp(wi_w)
  mat_n[t, 3] = (1/t) * pdf(z, wi_n) / cdf(z, -wi_n)
endloop

cnameset(mat_w, "months unmarried married")
cnameset(mat_n, "months unmarried married")

gnuplot 2 3 1 --with-lines --supp --matrix=mat_w --output=weibull.plt
gnuplot 2 3 1 --with-lines --supp --matrix=mat_n --output=lognorm.plt

```

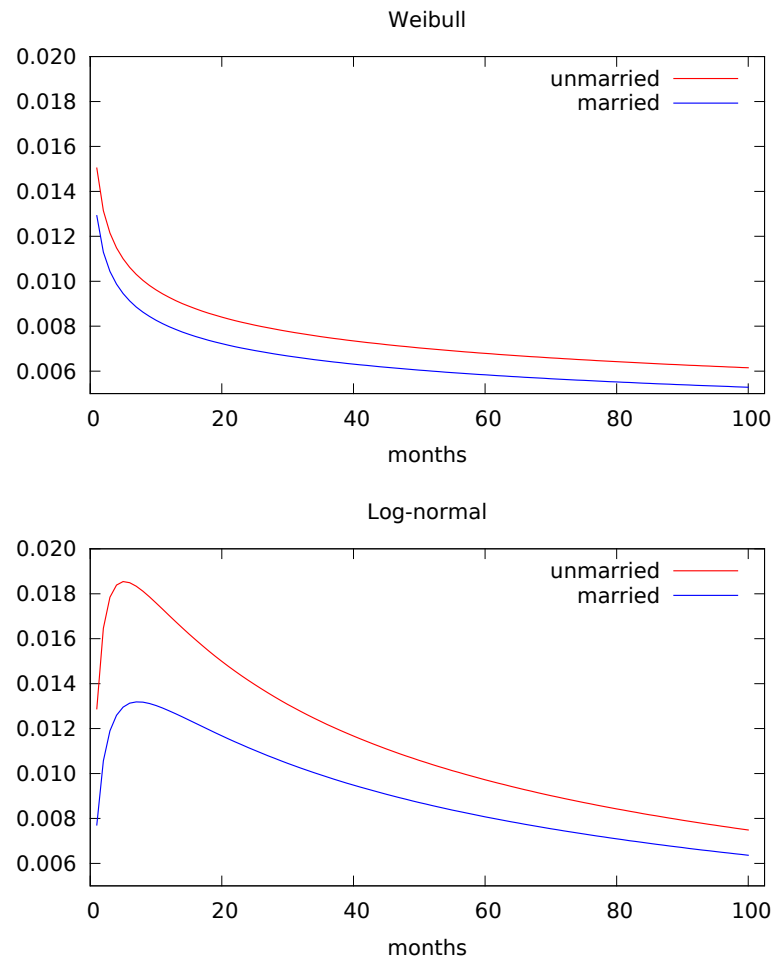


Figure 38.1: Recidivism hazard estimates for married and unmarried ex-convicts

married coefficient in the Weibull specification as shown here is 0.188104 and $\hat{\sigma}$ is 1.24090, so the alternative value is -0.152 , which is what Wooldridge shows (2002a, Table 20.1).

Fitted values and residuals

By default, gretl computes fitted values (accessible via `$yhat`) as the conditional mean of duration. The formulae are shown below (where Γ denotes the gamma function, and the exponential variant is just Weibull with $\sigma = 1$).

Weibull	Log-logistic	Log-normal
$\exp(X\beta)\Gamma(1 + \sigma)$	$\exp(X\beta)\frac{\pi\sigma}{\sin(\pi\sigma)}$	$\exp(X\beta + \sigma^2/2)$

The expression given for the log-logistic mean, however, is valid only for $\sigma < 1$; otherwise the expectation is undefined, a point that is not noted in all software.⁸

Alternatively, if the `--medians` option is given, gretl's `duration` command will produce conditional medians as the content of `$yhat`. For the Weibull the median is $\exp(X\beta)(\log 2)^\sigma$; for the log-logistic and log-normal it is just $\exp(X\beta)$.

The values we give for the accessor `$uhat` are generalized (Cox-Snell) residuals, computed as the integrated hazard function, which equals the negative log of the survivor function:

$$\epsilon_i = \Lambda(t_i, x_i, \theta) = -\log S(t_i, x_i, \theta)$$

Under the null of correct specification of the model these generalized residuals should follow the unit exponential distribution, which has mean and variance both equal to 1 and density $\exp(-\epsilon)$. See chapter 18 of Cameron and Trivedi (2005) for further discussion.

⁸The `predict` adjunct to the `streg` command in Stata 10, for example, gaily produces large negative values for the log-logistic mean in duration models with $\sigma > 1$.

Chapter 39

Quantile regression

39.1 Introduction

In Ordinary Least Squares (OLS) regression, the fitted values, $\hat{y}_i = X_i\hat{\beta}$, represent the *conditional mean* of the dependent variable—conditional, that is, on the regression function and the values of the independent variables. In median regression, by contrast and as the name implies, fitted values represent the *conditional median* of the dependent variable. It turns out that the principle of estimation for median regression is easily stated (though not so easily computed), namely, choose $\hat{\beta}$ so as to minimize the sum of absolute residuals. Hence the method is known as Least Absolute Deviations or LAD. While the OLS problem has a straightforward analytical solution, LAD is a linear programming problem.

Quantile regression is a generalization of median regression: the regression function predicts the conditional τ -quantile of the dependent variable—for example the first quartile ($\tau = .25$) or the ninth decile ($\tau = .90$).

If the classical conditions for the validity of OLS are satisfied—that is, if the error term is independently and identically distributed, conditional on X —then quantile regression is redundant: all the conditional quantiles of the dependent variable will march in lockstep with the conditional mean. Conversely, if quantile regression reveals that the conditional quantiles behave in a manner quite distinct from the conditional mean, this suggests that OLS estimation is problematic.

Gretl has offered quantile regression functionality since version 1.7.5 (in addition to basic LAD regression, which has been available since early in gretl's history via the `lad` command).¹

39.2 Basic syntax

The basic invocation of quantile regression is

```
quantreg tau reglist
```

where

- *reglist* is a standard gretl regression list (dependent variable followed by regressors, including the constant if an intercept is wanted); and
- *tau* is the desired conditional quantile, in the range 0.01 to 0.99, given either as a numerical value or the name of a pre-defined scalar variable (but see below for a further option).

Estimation is via the Frisch–Newton interior point solver (Portnoy and Koenker, 1997), which is substantially faster than the “traditional” Barrodale–Roberts (1974) simplex approach for large problems.

¹We gratefully acknowledge our borrowing from the `quantreg` package for GNU R (version 4.17). The core of the package is composed of Fortran code written by Roger Koenker; this is accompanied by various driver and auxiliary functions written in the R language by Koenker and Martin Mächler. The latter functions have been re-worked in C for gretl. We have added some guards against potential numerical problems in small samples.

By default, standard errors are computed according to the asymptotic formula given by [Koenker and Bassett \(1978\)](#). Alternatively, if the `--robust` option is given, we use the sandwich estimator developed in [Koenker and Zhao \(1994\)](#).²

39.3 Confidence intervals

An option `--intervals` is available. When this is given we print confidence intervals for the parameter estimates instead of standard errors. These intervals are computed using the rank inversion method and in general they are asymmetrical about the point estimates—that is, they are not simply “plus or minus so many standard errors”. The specifics of the calculation are inflected by the `--robust` option: without this, the intervals are computed on the assumption of IID errors ([Koenker, 1994](#)); with it, they use the heteroskedasticity-robust estimator developed by [Koenker and Machado \(1999\)](#).

By default, 90 percent intervals are produced. You can change this by appending a confidence value (expressed as a decimal fraction) to the intervals option, as in

```
quantreg tau reglist --intervals=.95
```

When the confidence intervals option is selected, the parameter estimates are calculated using the Barrodale–Roberts method. This is simply because the Frisch–Newton code does not currently support the calculation of confidence intervals.

Two further details. First, the mechanisms for generating confidence intervals for quantile estimates require that the model has at least two regressors (including the constant). If the `--intervals` option is given for a model containing only one regressor, an error is flagged. Second, when a model is estimated in this mode, you can retrieve the confidence intervals using the accessor `$coeff_ci`. This produces a $k \times 2$ matrix, where k is the number of regressors. The lower bounds are in the first column, the upper bounds in the second. See also section 39.5 below.

39.4 Multiple quantiles

As a further option, you can give *tau* as a matrix—either the name of a predefined matrix or in numerical form, as in `{.05, .25, .5, .75, .95}`. The given model is estimated for all the τ values and the results are printed in a special form, as shown below (in this case the `--intervals` option was also given).

Model 1: Quantile estimates using the 235 observations 1–235

Dependent variable: foodexp

With 90 percent confidence intervals

VARIABLE	TAU	COEFFICIENT	LOWER	UPPER
const	0.05	124.880	98.3021	130.517
	0.25	95.4835	73.7861	120.098
	0.50	81.4822	53.2592	114.012
	0.75	62.3966	32.7449	107.314
	0.95	64.1040	46.2649	83.5790
income	0.05	0.343361	0.343327	0.389750
	0.25	0.474103	0.420330	0.494329
	0.50	0.560181	0.487022	0.601989
	0.75	0.644014	0.580155	0.690413
	0.95	0.709069	0.673900	0.734441

²These correspond to the `iid` and `nid` options in R’s `quantreg` package, respectively.

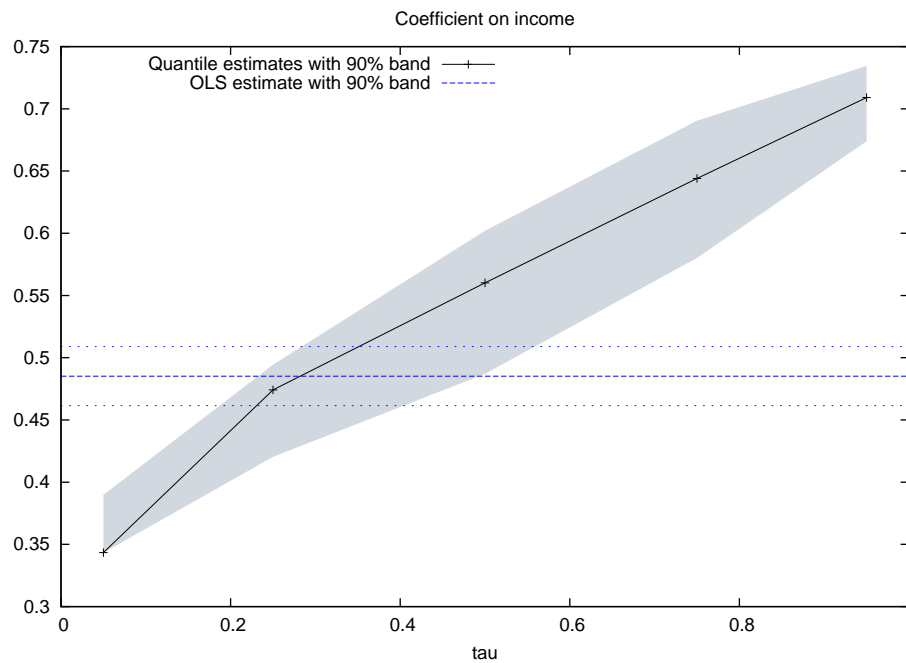


Figure 39.1: Regression of food expenditure on income; Engel’s data

The `gretl` GUI has an entry for Quantile Regression (under `/Model/Robust estimation`), and you can select multiple quantiles there too. In that context, just give space-separated numerical values (as per the predefined options, shown in a drop-down list).

When you estimate a model in this way most of the standard menu items in the model window are disabled, but one extra item is available—graphs showing the τ sequence for a given coefficient in comparison with the OLS coefficient. An example is shown in Figure 39.1. This sort of graph provides a simple means of judging whether quantile regression is redundant (OLS is fine) or informative.

In the example shown—based on data on household income and food expenditure gathered by Ernst Engel (1821–1896)—it seems clear that simple OLS regression is potentially misleading. The “crossing” of the OLS estimate by the quantile estimates is very marked.

However, it is not always clear what implications should be drawn from this sort of conflict. With the Engel data there are two issues to consider. First, Engel’s famous “law” claims an income-elasticity of food consumption that is less than one, and talk of elasticities suggests a logarithmic formulation of the model. Second, there are two apparently anomalous observations in the data set: household 105 has the third-highest income but unexpectedly low expenditure on food (as judged from a simple scatter plot), while household 138 (which also has unexpectedly low food consumption) has much the highest income, almost twice that of the next highest.

With $n = 235$ it seems reasonable to consider dropping these observations. If we do so, and adopt a log-log formulation, we get the plot shown in Figure 39.2. The quantile estimates still cross the OLS estimate, but the “evidence against OLS” is much less compelling: the 90 percent confidence bands of the respective estimates overlap at all the quantiles considered.

A script to produce the results discussed above is presented in listing 39.1.

39.5 Large datasets

As noted above, when you give the `--intervals` option with the `quantreg` command, which calls for estimation of confidence intervals via rank inversion, `gretl` switches from the default Frisch-

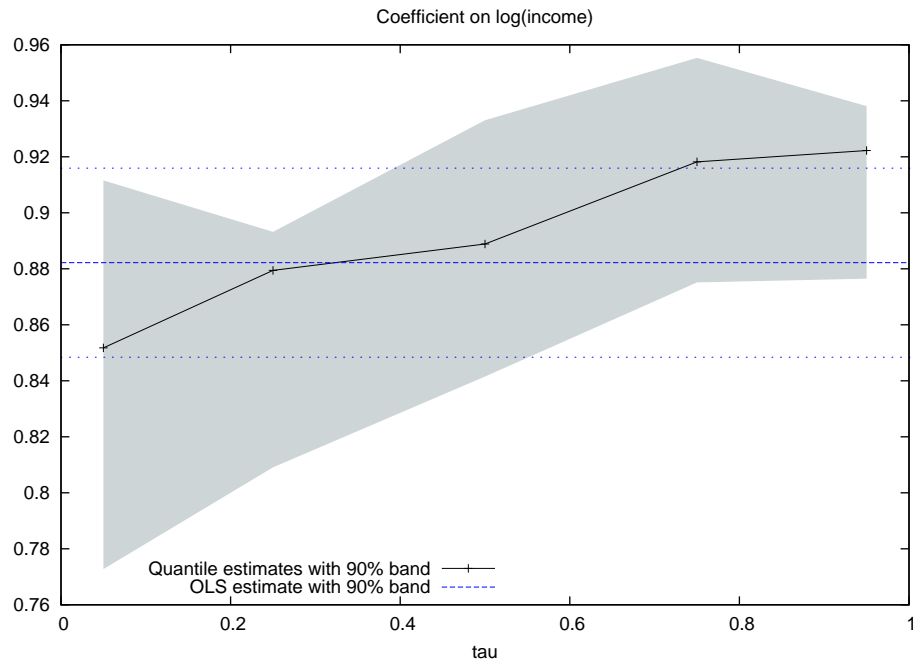


Figure 39.2: Log-log regression; 2 observations dropped from full Engel data set.

Listing 39.1: Food expenditure and income, Engel data [\[Download ▼\]](#)

```
# this data file is supplied with gretl
open engel.gdt

# specify some quantiles
matrix tau = {.05, .25, .5, .75, .95}

# use levels of variables
QM1 <- quantreg tau foodexp 0 income --intervals

# use log-log specification, with two outliers removed
logs foodexp income
smpl obs!=105 && obs!=138 --restrict
QM2 <- quantreg tau l_foodexp 0 l_income --intervals
```

The script saves the two models “as icons”. Double-clicking on a model’s icon opens a window to display the results, and the Graph menu in this window gives access to a tau-sequence plot.

Newton algorithm to the Barrodale–Roberts simplex method.

This is OK for moderately large datasets (up to, say, a few thousand observations) but on very large problems the simplex algorithm may become seriously bogged down. For example, [Koenker and Hallock \(2001\)](#) present an analysis of the determinants of birth weights, using 198377 observations and with 15 regressors. Generating confidence intervals via Barrodale–Roberts for a single value of τ took about half an hour on a Lenovo Thinkpad T60p with 1.83GHz Intel Core 2 processor.

If you want confidence intervals in such cases, you are advised not to use the `--intervals` option, but to compute them using the method of “plus or minus so many standard errors”. (One Frisch–Newton run took about 8 seconds on the same machine, showing the superiority of the interior point method.) The script below illustrates:

```
quantreg .10 y 0 xlist
scalar crit = qnorm(.95)
matrix ci = $coeff - crit * $stderr
ci = ci~($coeff + crit * $stderr)
print ci
```

The matrix `ci` will contain the lower and upper bounds of the (symmetrical) 90 percent confidence intervals.

To avoid a situation where `gretl` becomes unresponsive for a very long time we have set the maximum number of iterations for the Barrodale–Roberts algorithm to the (somewhat arbitrary) value of 1000. We will experiment further with this, but for the meantime if you really want to use this method on a large dataset, and don’t mind waiting for the results, you can increase the limit using the `set` command with parameter `rq_maxiter`, as in

```
set rq_maxiter 5000
```

Chapter 40

Nonparametric methods

The main focus of gretl is on parametric estimation, but we offer a selection of nonparametric methods. The most basic of these

- various tests for difference in distribution (Sign test, Wilcoxon rank-sum test, Wilcoxon signed-rank test);
- the Runs test for randomness; and
- nonparametric measures of association: Spearman's rho and Kendall's tau.

Details on the above can be found by consulting the help for the commands `diffstest`, `runs`, `corr` and `spearman`. In the GUI program these items are found under the Tools menu and the Robust estimation item under the Model menu.

In this chapter we concentrate on two relatively complex methods for nonparametric curve-fitting and prediction, namely William Cleveland's "loess" (also known as "lowess") and the Nadaraya-Watson estimator.

40.1 Locally weighted regression (loess)

Loess (Cleveland, 1979) is a nonparametric smoother employing locally weighted polynomial regression. It is intended to yield an approximation to $g(\cdot)$ when the dependent variable, y , can be expressed as

$$y_i = g(x_i) + \epsilon_i$$

for some smooth function $g(\cdot)$.

Given a sample of n observations on the variables y and x , the procedure is to run a weighted least squares regression (a polynomial of order $d = 0, 1$ or 2 in x) localized to each data point, i . In each such regression the sample consists of the r nearest neighbors (in the x dimension) to the point i , with weights that are inversely related to the distance $|x_i - x_k|$, $k = 1, \dots, r$. The predicted value \hat{y}_i is then obtained by evaluating the estimated polynomial at x_i . The most commonly used order is $d = 1$.

A bandwidth parameter $0 < q \leq 1$ controls the proportion of the total number of data points used in each regression; thus $r = qn$ (rounded up to an integer). Larger values of q lead to a smoother fitted series, smaller values to a series that tracks the actual data more closely; $0.25 \leq q \leq 0.5$ is often a suitable range.

In gretl's implementation of loess the weighting scheme is that given by Cleveland, namely,

$$w_k(x_i) = W(h_i^{-1}(x_k - x_i))$$

where h_i is the distance between x_i and its r^{th} nearest neighbor, and $W(\cdot)$ is the tricube function,

$$W(x) = \begin{cases} (1 - |x|^3)^3 & \text{for } |x| < 1 \\ 0 & \text{for } |x| \geq 1 \end{cases}$$

The local regression can be made robust via an adjustment based on the residuals, $e_i = y_i - \hat{y}_i$. Robustness weights, δ_k , are defined by

$$\delta_k = B(e_k/6s)$$

where s is the median of the $|e_i|$ and $B(\cdot)$ is the bisquare function,

$$B(x) = \begin{cases} (1 - x^2)^2 & \text{for } |x| < 1 \\ 0 & \text{for } |x| \geq 1 \end{cases}$$

The polynomial regression is then re-run using weight $\delta_k w_k(x_i)$ at (x_k, y_k) .

The `loess()` function in `gretl` takes up to five arguments as follows: the y series, the x series, the order d , the bandwidth q , and a Boolean switch to turn on the robust adjustment. The last three arguments are optional: if they are omitted the default values are $d = 1$, $q = 0.5$ and no robust adjustment. An example of a full call to `loess()` is shown below; in this case a quadratic in x is specified, three quarters of the data points will be used in each local regression, and robustness is turned on:

```
series yh = loess(y, x, 2, 0.75, 1)
```

An illustration of loess is provided in Listing 40.1: we generate a series that has a deterministic sine wave component overlaid with noise uniformly distributed on $(-1, 1)$. Loess is then used to retrieve a good approximation to the sine function. The resulting graph is shown in Figure 40.1.

Listing 40.1: Loess script [\[Download ▼\]](#)

```
nulldata 120
series x = index
scalar n = $nobs
series y = sin(2*pi*x/n) + uniform(-1, 1)
series yh = loess(y, x, 2, 0.75, 0)
gnuplot y yh x --output=display --with=lines=yh
```

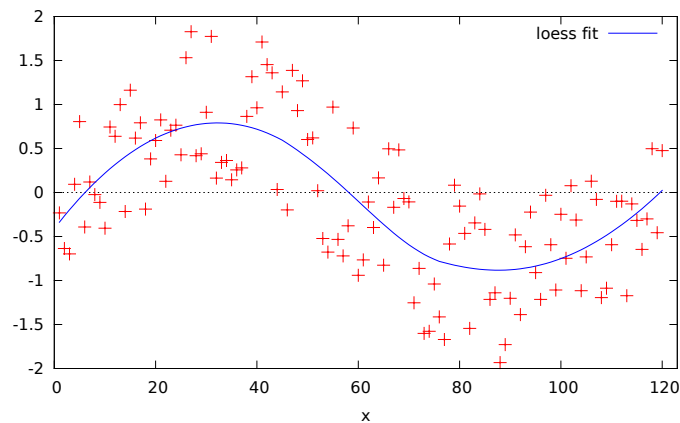


Figure 40.1: Loess: retrieving a sine wave

40.2 The Nadaraya–Watson estimator

The Nadaraya–Watson nonparametric estimator (Nadaraya, 1964; Watson, 1964) is an estimator for the conditional mean of a variable Y , available in a sample of size n , for a given value of a conditioning variable X , and is defined as

$$m(X) = \frac{\sum_{j=1}^n y_j \cdot K_h(X - x_j)}{\sum_{j=1}^n K_h(X - x_j)}$$

where $K_h(\cdot)$ is the so-called *kernel function*, which is usually some simple transform of a density function that depends on a scalar, h , known as the *bandwidth*. The one used by gretl is

$$K_h(x) = \exp\left(-\frac{x^2}{2h}\right)$$

for $|x| < \tau$ and zero otherwise. Larger values of h produce a smoother function. The scalar τ , known as the trim parameter, is used to prevent numerical problems when the kernel function is evaluated too far away from zero.

A common variant of Nadaraya–Watson is the so-called “leave-one-out” estimator, which omits the i -th observation when evaluating $m(x_i)$. The formula therefore becomes

$$m(x_i) = \frac{\sum_{j \neq i} y_j \cdot K_h(x_i - x_j)}{\sum_{j \neq i} K_h(x_i - x_j)}$$

This makes the estimator more robust numerically and its usage is often advised for inference purposes.

The `nadarwat()` function in gretl takes up to five arguments as follows: the dependent series y , the independent series x , the bandwidth h , a Boolean switch to turn on “leave-one-out”, and a value for the trim parameter τ , expressed as a multiple of h . The last three arguments are optional; if they are omitted the default values are, respectively, an automatic data-determined value for h (see below), leave-one-out not activated, and $\tau = 4$. The default value of τ offers a relatively safe guard against numerical problems; in some cases a larger τ may produce more sensible values in regions of X with sparse support.

Choice of bandwidth

As mentioned above, larger values of h lead to a smoother $m(\cdot)$ function; smaller values make the $m(\cdot)$ function follow the y_i values more closely, so that the function appears more “jagged”. In fact, as $h \rightarrow \infty$, $m(x_i) \rightarrow \bar{Y}$; on the contrary, if $h \rightarrow 0$, observations for which $x_i \neq X$ are not taken into account at all when computing $m(X)$. Also, the statistical properties of $m(\cdot)$ vary with h : its variance can be shown to be decreasing in h , while its squared bias is increasing in h . It can be shown that choosing $h \sim n^{-1/5}$ minimizes the RMSE, so that value is customarily taken as a reference point.

If the argument h is omitted or set to 0, gretl uses the following data-determined value:

$$h = 0.9 \cdot \min\left[s, \frac{r}{1.349}\right] \cdot n^{-1/5}$$

where s is the sample standard deviation of x and r is its interquartile range.

Example and prediction

By way of example, Listing 40.2 produces the graph shown in Figure 40.2 (after some slight editing). Although X could be, in principle, any value, in the typical usage of this estimator you want to compute $m(X)$ for X equal to one or more values actually observed in your sample, that is $m(x_i)$.

Listing 40.2: Nadaraya-Watson example [\[Download ▼\]](#)

```
# Nonparametric regression example: husband's age on wife's age
open mroz87.gdt

# initial value for the bandwidth
scalar h = $nobs^(-0.2)
# three increasingly smooth estimates
series m0 = nadarwat(HA, WA, h)
series m1 = nadarwat(HA, WA, h * 5)
series m2 = nadarwat(HA, WA, h * 10)

# produce the graph
dataset sortby WA
gnuplot HA m0 m1 m2 WA --output=display --with-lines=m0,m1,m2
```

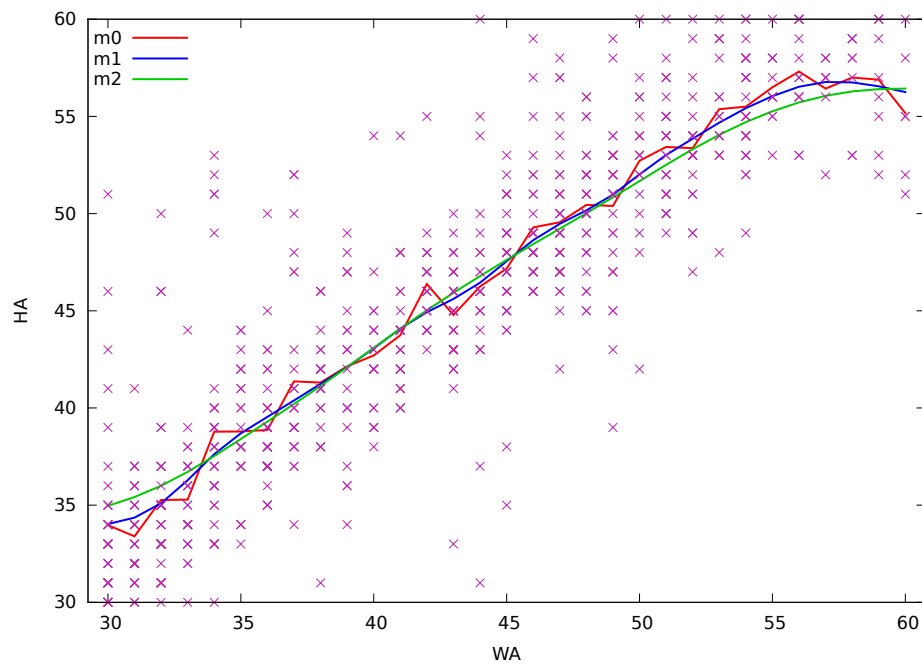


Figure 40.2: Nadaraya-Watson example for several choices of the bandwidth parameter

If you need a point estimate of $m(X)$ for some value of X which is not present among the valid observations of your dependent variable, you may want to add some “fake” observations to your dataset in which y is missing and x contains the values you want $m(x)$ evaluated at. For example, the following script evaluates $m(x)$ at regular intervals between -2.0 and 2.0 :

```

nulldata 120
set seed 120496

# first part of the sample: actual data
smp1 1 100
x = normal()
y = x^2 + sin(x) + normal()

# second part of the sample: fake x data
smp1 101 120
x = (obs-110) / 5

# compute the Nadaraya-Watson estimate
# with bandwidth equal to 0.4 (note that
#  $100^{(-0.2)} = 0.398$ )
smp1 full
m = nadarwat(y, x, 0.4)

# show  $m(x)$  for the fake x values only
smp1 101 120
print x m -o

```

and running it produces

	x	m
101	-1.8	1.165934
102	-1.6	0.730221
103	-1.4	0.314705
104	-1.2	0.026057
105	-1.0	-0.131999
106	-0.8	-0.215445
107	-0.6	-0.269257
108	-0.4	-0.304451
109	-0.2	-0.306448
110	0.0	-0.238766
111	0.2	-0.038837
112	0.4	0.354660
113	0.6	0.908178
114	0.8	1.485178
115	1.0	2.000003
116	1.2	2.460100
117	1.4	2.905176
118	1.6	3.380874
119	1.8	3.927682
120	2.0	4.538364

Chapter 41

MIDAS models

The acronym MIDAS stands for “Mixed Data Sampling”. MIDAS models can essentially be described as models where one or more independent variables are observed at a higher frequency than the dependent variable, and possibly an ad-hoc parsimonious parameterization is adopted. See [Ghysels *et al.*, 2004](#); [Ghysels, 2015](#); [Armesto *et al.*, 2010](#) for a fuller introduction. Naturally, these models require easy handling of multiple-frequency data. The way this is done in gretl is explained in [Chapter 20](#); in this chapter, we concentrate on the numerical aspects of estimation.

41.1 Parsimonious parameterizations

The simplest MIDAS regression specification—known as “unrestricted MIDAS” or U-MIDAS—simply includes p lags of a high-frequency regressor, each with its own parameter to be estimated. A typical case can be written as

$$y_t = \beta_0 + \alpha y_{t-1} + \sum_{i=1}^p \delta_i x_{\tau-i} + \varepsilon_t \quad (41.1)$$

where τ represents the reference point of the sequence of high-frequency lags in “high-frequency time”.¹ Obvious generalizations of this specification include a higher AR order for y and inclusion of additional low- and/or high-frequency regressors.

Estimation of (41.1) can be accomplished via OLS. However, it is more common to enforce parsimony by making the individual coefficients on lagged high-frequency terms a function of a relatively small number of hyperparameters, as in

$$y_t = \beta_0 + \alpha y_{t-1} + yW(x_{\tau-1}, x_{\tau-2}, \dots, x_{\tau-p}; \theta) + \varepsilon_t \quad (41.2)$$

where $W(\cdot)$ is the weighting function associated with a given parameterization and θ is a k -vector of hyperparameters, $k < p$.

This presents a couple of computational questions: how to calculate the per-lag coefficients given the values of the hyperparameters, and how best to estimate the value of the hyperparameters? Gretl can handle natively four commonly used parameterizations: normalized exponential Almon, normalized beta (with or without a zero last coefficient), and plain (non-normalized) Almon polynomial. The Almon variants take one or more parameters (two being a common choice). The beta variants take either two or three parameters. Full details on the forms taken by the $W(\cdot)$ function are provided in [section 41.3](#).

All variants are handled by the functions `mweights` and `mgradient`, which work as follows.

- `mweights` takes three arguments: the number of lags required (p), the k -vector of hyperparameters (θ), and an integer code or string indicating the method (see [Table 41.1](#)). It returns a p -vector containing the coefficients.
- `mgradient` takes three arguments, just like `mweights`. However, this function returns a $p \times k$ matrix holding the (analytical) gradient of the p coefficients or weights with respect to the k elements of θ .

¹For discussion of the placement of this reference point relative to low-frequency time, see [section 20.3](#) above.

<i>Parameterization</i>	<i>code</i>	<i>string</i>
Normalized exponential Almon	1	"nealmon"
Normalized beta, zero last lag	2	"beta0"
Normalized beta, non-zero last lag	3	"betan"
Almon polynomial	4	"almonp"
One-parameter beta	5	"beta1"

Table 41.1: MIDAS parameterizations

In the case of the non-normalized Almon polynomial the γ coefficient in (41.2) is identically 1.0 and is omitted. The "beta1" case is the the same as the two-parameter "beta0" except that θ_1 is constrained to equal 1, leaving θ_2 as the only free parameter. Ghysels and Qian (2016) make a case for use of this particularly parsimonious version.²

An additional function is provided for convenience: it is named `m1incomb` and it combines `mweights` with the `lincomb` function, which takes a list (of series) argument followed by a vector of coefficients and produces a series result, namely a linear combination of the elements of the list. If we have a suitable list `X` available, we can do, for example,

```
series foo = m1incomb(X, theta, "beta0")
```

This is equivalent to

```
series foo = lincomb(X, mweights(nelem(X), theta, "beta0"))
```

but saves a little typing and some CPU cycles.

41.2 Estimating MIDAS models

Gretl offers a dedicated command, `midasreg`, for estimation of MIDAS models. (There's a corresponding item, MIDAS, under the Time series section of the Model menu in the gretl GUI.) We begin by discussing that, then move on to possibilities for defining your own estimator.

The syntax of `midasreg` looks like this:

```
midasreg depvar xlist ; midas-terms [ options ]
```

The `depvar` slot takes the name (or series ID number) of the dependent variable, and `xlist` is the list of regressors that are observed at the same frequency as the dependent variable; this list may contain lags of the dependent variable. The `midas-terms` slot accepts one or more specification(s) for high-frequency terms. Each of these specifications must conform to one or other of the following patterns:

- 1 `mds(mlist, minlag, maxlag, type, theta)`
- 2 `mdsl(l1list, type, theta)`

In case 1 `mlist` must be a **MIDAS list**, as defined in section 20.2, which contains a full set of per-period series but no lags. Lags will be generated automatically, governed by the `minlag` and `maxlag` (integer) arguments, which may be given as numerical values or the names of predefined scalar variables. The integer (or string) `type` argument represents the type of parameterization; in addition to the values 1 to 4 defined in Table 41.1 a value of 0 (or the string "umidas") indicates unrestricted MIDAS.

In case 2 `l1list` is assumed to be a list that already contains the required set of high-frequency lags—as may be obtained via the `hflags` function described in section 20.3—hence `minlag` and `maxlag` are not wanted.

²Note, however, that at present "beta1" cannot be mixed with other parameterizations in a single model.

The final *theta* argument is optional in most cases (implying an automatic initialization of the hyperparameters). If this argument is given it must take one of the following forms:

1. The name of a matrix (vector) holding initial values for the hyperparameters, or a simple expression which defines a matrix using scalars, such as {1, 5}.
2. The keyword `null`, indicating that an automatic initialization should be used (as happens when this argument is omitted).
3. An integer value (in numerical form), indicating how many hyperparameters should be used (which again calls for automatic initialization).

The third of these forms is required if you want automatic initialization in the Almon polynomial case, since we need to know how many terms you wish to include. (In the normalized exponential Almon case we default to the usual two hyperparameters if *theta* is omitted or given as `null`.)

The `midasreg` syntax allows the user to specify multiple high-frequency predictors, if wanted: these can have different lag specifications, different parameterizations and/or different frequencies.

The options accepted by `midasreg` include `--quiet` (suppress printed output), `--verbose` (show detail of iterations, if applicable) and `--robust` (use a HAC estimator of the Newey–West type in computing standard errors). Two additional specialized options are described below.

Examples of usage

Suppose we have a dependent variable named `dy` and a MIDAS list named `dX`, and we wish to run a MIDAS regression using one lag of the dependent variable and high-frequency lags 1 to 10 of the series in `dX`. The following will produce U-MIDAS estimates:

```
midasreg dy const dy(-1) ; mds(dX, 1, 10, 0)
```

The next lines will produce estimates for the normalized exponential Almon parameterization with two coefficients, both initialized to zero:

```
midasreg dy const dy(-1) ; mds(dX, 1, 10, "nealmon", {0,0})
```

In the examples above, the required lags will be added to the dataset automatically then deleted after use. If you are estimating several models using a single set of MIDAS lags it is more efficient to create the lags once and use the `mdsl` specifier. For example, the following estimates three variant parameterizations (exponential Almon, beta with zero last lag, and beta with non-zero last lag) on the same data:

```
list dXL = hflags(1, 10, dX)
midasreg dy 0 dy(-1) ; mdsl(dXL, "nealmon", {0,0})
midasreg dy 0 dy(-1) ; mdsl(dXL, "beta0", {1,5})
midasreg dy 0 dy(-1) ; mdsl(dXL, "betan", {1,1,0})
```

Any additional MIDAS terms should be separated by spaces, as in

```
midasreg dy const dy(-1) ; mds(dX,1,9,1,theta1) mds(Z,1,6,3,theta2)
```

Replication exercise

We give a substantive illustration of `midasreg` in Listing 41.1. This replicates the first practical example discussed by Ghysels in the user's guide titled *MIDAS Matlab Toolbox*,³ The dependent

³See Ghysels (2015). This document announces itself as Version 2.0 of the guide and is dated November 1, 2015. The example we're looking at appears on pages 24–26; the associated Matlab code can be found in the program `appADLMIDAS1.m`.

variable is the quarterly log-difference of real GDP, named `dy` in our script. The independent variables are the first lag of `dy` and monthly lags 3 to 11 of the monthly log-difference of non-farm payroll employment (named `dXL` in our script). Therefore, in this case equation (41.2) becomes

$$y_t = \alpha + \beta y_{t-1} + \gamma W(x_{t-3}, x_{t-4}, \dots, x_{t-11}; \theta) + \varepsilon_t$$

and in the U-MIDAS case the model comes down to

$$y_t = \alpha + \beta y_{t-1} + \sum_{i=1}^9 \delta_i x_{t-i-2} + \varepsilon_t$$

The script exercises all five of the parameterizations mentioned above,⁴ and in each case the results of 9 pseudo-out-of-sample forecasts are recorded so that their Root Mean Square Errors can be compared.

The data file used in the replication, `gdp_midas.gdt`, was constructed as described in section 20.1 (and as noted there, it is included in the current `gretl` package). Part of the output from the replication script is shown in Listing 41.2. The γ coefficient is labeled `HF_slope` in the `gretl` output.

For reference, output from Matlab (version R2016a for Linux) is available at http://gretl.sourceforge.net/midas/matlab_output.txt. For the most part (in respect of regression coefficients and auxiliary statistics such as R^2 and forecast RMSEs), `gretl`'s output agrees with that of Matlab to the extent that one can reasonably expect on nonlinear problems—that is, to at least 4 significant digits in all but a few instances.⁵ Standard errors are not quite so close across the two programs, particularly for the hyperparameters of the beta and exponential Almon functions. We show these in Table 41.2.

	2-param beta		3-param beta		Exp Almon	
	Matlab	gretl	Matlab	gretl	Matlab	gretl
const	0.135	0.140	0.143	0.146	0.135	0.140
dy(-1)	0.116	0.118	0.116	0.119	0.116	0.119
HF slope	0.559	0.575	0.566	0.582	0.562	0.575
θ_1	0.067	0.106	0.022	0.027	2.695	6.263
θ_2	9.662	17.140	1.884	2.934	0.586	1.655
θ_3			0.022	0.027		

Table 41.2: Comparison of standard errors from MIDAS regressions

Differences of this order are not unexpected, however, when different methods are used to calculate the covariance matrix for a nonlinear regression. The Matlab standard errors are based on a numerical approximation to the Hessian at convergence, while those produced by `gretl` are based on a Gauss-Newton Regression, as discussed and recommended in Davidson and MacKinnon (2004, chapter 6).

Underlying methods

The `midasreg` command calls one of several possible estimation methods in the background, depending on the MIDAS specification(s). As shown in Listing 41.2, this is flagged in a line of output immediately preceding the “Dependent variable” line. If the only specification type is U-MIDAS, the method is OLS. Otherwise it is one of three variants of Nonlinear Least Squares.

- Levenberg-Marquardt. This is the back-end for `gretl`'s `nls` command.

⁴The Matlab program includes an additional parameterization not supported by `gretl`, namely a step-function.

⁵Nonlinear results, even for a given software package, are subject to slight variation depending on the compiler used and the exact versions of supporting numerical libraries.

Listing 41.1: Script to replicate results given by Ghysels [\[Download ▼\]](#)

```

set verbose off
open gdp_midas.gdt --quiet

# form the dependent variable
series dy = 100 * ldiff(qgdp)
# form list of high-frequency lagged log differences
list X = payems*
list dXL = hflags(3, 11, hflldiff(X, 100))
# initialize matrix to collect forecasts
matrix FC = {}

# estimation sample
smp1 1985:1 2009:1

print "=== unrestricted MIDAS (umidas) ==="
midasreg dy 0 dy(-1) ; mds1(dXL, 0)
fcast --out-of-sample --static --quiet
FC ~= $fcast

print "=== normalized beta with zero last lag (beta0) ==="
midasreg dy 0 dy(-1) ; mds1(dXL, 2, {1,5})
fcast --out-of-sample --static --quiet
FC ~= $fcast

print "=== normalized beta, non-zero last lag (betan) ==="
midasreg dy 0 dy(-1) ; mds1(dXL, 3, {1,1,0})
fcast --out-of-sample --static --quiet
FC ~= $fcast

print "=== normalized exponential Almon (nealmon) ==="
midasreg dy 0 dy(-1) ; mds1(dXL, 1, {0,0})
fcast --out-of-sample --static --quiet
FC ~= $fcast

print "=== Almon polynomial (almonp) ==="
midasreg dy 0 dy(-1) ; mds1(dXL, 4, 4)
fcast --out-of-sample --static --quiet
FC ~= $fcast

smp1 2009:2 2011:2
matrix my = {dy}
print "Forecast RMSEs:"
printf "  umidas  %.4f\n", fcstats(my, FC[,1])[2]
printf "  beta0   %.4f\n", fcstats(my, FC[,2])[2]
printf "  betan   %.4f\n", fcstats(my, FC[,3])[2]
printf "  nealmon %.4f\n", fcstats(my, FC[,4])[2]
printf "  almonp  %.4f\n", fcstats(my, FC[,5])[2]

```

Listing 41.2: Replication of Ghysels' results, partial output

```

=== normalized beta, non-zero last lag (betan) ===
Model 3: MIDAS (NLS), using observations 1985:1-2009:1 (T = 97)
Using L-BFGS-B with conditional OLS
Dependent variable: dy

```

	estimate	std. error	t-ratio	p-value	
const	0.748578	0.146404	5.113	1.74e-06	***
dy_1	0.248055	0.118903	2.086	0.0398	**

MIDAS list dXL, high-frequency lags 3 to 11

HF_slope	1.72167	0.582076	2.958	0.0039	***
Beta1	0.998501	0.0269479	37.05	1.10e-56	***
Beta2	2.95148	2.93404	1.006	0.3171	
Beta3	-0.0743143	0.0271273	-2.739	0.0074	***

Sum squared resid	28.78262	S.E. of regression	0.562399
R-squared	0.356376	Adjusted R-squared	0.321012
Log-likelihood	-78.71248	Akaike criterion	169.4250
Schwarz criterion	184.8732	Hannan-Quinn	175.6715

```

=== Almon polynomial (almonp) ===
Model 5: MIDAS (NLS), using observations 1985:1-2009:1 (T = 97)
Using Levenberg-Marquardt algorithm
Dependent variable: dy

```

	estimate	std. error	t-ratio	p-value	
const	0.741403	0.146433	5.063	2.14e-06	***
dy_1	0.255099	0.119139	2.141	0.0349	**

MIDAS list dXL, high-frequency lags 3 to 11

Almon0	1.06035	1.53491	0.6908	0.4914
Almon1	0.193615	1.30812	0.1480	0.8827
Almon2	-0.140466	0.299446	-0.4691	0.6401
Almon3	0.0116034	0.0198686	0.5840	0.5607

Sum squared resid	28.66623	S.E. of regression	0.561261
R-squared	0.358979	Adjusted R-squared	0.323758
Log-likelihood	-78.51596	Akaike criterion	169.0319
Schwarz criterion	184.4802	Hannan-Quinn	175.2784

```

Forecast RMSEs:
umidas  0.5424
beta0    0.5650
betan    0.5210
nealmon  0.5642
almonp   0.5329

```

- L-BFGS-B with conditional OLS. L-BFGS is a “limited memory” version of the BFGS optimizer and the trailing “-B” means that it supports bounds on the parameters, which is useful for reasons given below.
- Golden Section search with conditional OLS. This is a line search method, used only when there is just a single hyperparameter to estimate.

Levenberg-Marquardt is the default NLS method, but if the MIDAS specifications include any of the beta variants or normalized exponential Almon we switch to L-BFGS-B, *unless* the user gives the `--levenberg` option. The ability to set bounds on the hyperparameters via L-BFGS-B is helpful, first because the beta parameters (other than the third one, if applicable) must be non-negative but also because one is liable to run into numerical problems (in calculating the weights and/or gradient) if their values become too extreme. For example, we have found it useful to place bounds of -2 and $+2$ on the exponential Almon parameters.

Here’s what we mean by “conditional OLS” in the context of L-BFGS-B and line search: the search algorithm itself is only responsible for optimizing the MIDAS hyperparameters, and when the algorithm calls for calculation of the sum of squared residuals given a certain hyperparameter vector we optimize the remaining parameters (coefficients on base-frequency regressors, slopes with respect to MIDAS terms) via OLS.

Testing for a structural break

The `--breaktest` option can be used to carry out the Quandt Likelihood Ratio (QLR) test for a structural break at the stage of running the final Gauss-Newton regression (to check for convergence and calculate the covariance matrix of the parameter estimates). This can be a useful aid to diagnosis, since non-homogeneity of the data over the estimation period can lead to numerical problems in nonlinear estimation, besides compromising the forecasting capacity of the resulting equation. For example, when this option is given with the command to estimate the “betan” model shown in Listing 41.2, the following result is appended to the standard output:

```
QLR test for structural break -
Null hypothesis: no structural break
Test statistic: chi-square(6) = 35.1745 at observation 2005:2
with asymptotic p-value = 0.000127727
```

Despite the strong evidence for a structural break, in this case the nonlinear estimator appears to converge successfully. But one might wonder if a shorter estimation period could provide better out-of-sample forecasts.

Defining your own MIDAS estimator

As explained above, the `midasreg` command is in effect a “wrapper” for various underlying methods. Some users may wish to undo the wrapping. (This would be required if you wish to introduce any nonlinearity other than that associated with the stock MIDAS parameterizations, or to define your own MIDAS parameterization).

Anyone with ambitions in this direction will presumably be quite familiar with the commands and functions available in `hansl`, `gretl`’s scripting language, so we will not say much here beyond presenting a couple of examples. First we show how the `nls` command can be used, along with the MIDAS-related functions described in section 41.1, to estimate a model with the exponential Almon specification.

```
open gdp_midas.gdt --quiet
series dy = 100 * ldiff(qgdp)
series dy1 = dy(-1)
list X = payems*
```

```
list dXL = hflags(3, 11, hflldiff(X, 100))

smp1 1985:1 2009:1

# initialization via OLS
series mdX = mean(dXL)
ols dy 0 dy1 mdX --quiet
matrix b = $coeff | {0,0}'
scalar p = nelem(dXL)

# convenience matrix for computing gradient
matrix mdXL = {dXL}

# normalized exponential Almon via nls
nls dy = b[1] + b[2]*dy1 + b[3]*mdx
series mdx = mlincomb(dXL, b[4:], 1)
matrix grad = mgradient(p, b[4:], 1)
deriv b = {const, dy1, mdx} ~ (b[3] * mdXL * grad)
param_names "const dy(-1) HF_slope Almon1 Almon2"
end nls
```

Listing 41.3 presents a more ambitious example: we use `GSSmin` (Golden Section minimizer) to estimate a MIDAS model with the “one-parameter beta” specification (that is, the two-parameter beta with θ_1 clamped at 1). Note that while the function named `beta1_SSR` is specialized to the given parameterization, `midas_GNR` is a fairly general means of calculating the Gauss-Newton regression for an ADL(1) MIDAS model, and it could be generalized further without much difficulty.

Plot of coefficients

At times, it may be useful to plot the “gross” coefficients on the lags of the high-frequency series in a MIDAS regression—that is, the normalized weights multiplied by the `HF_slope` coefficient (the γ in 41.2). After estimation of a MIDAS model in the `gretl` GUI this is available via the item **MIDAS coefficients** under the **Graphs** menu in the model window. It is also easily generated via script, since the `$model` bundle that becomes available following the `midasreg` command contains a matrix, `midas_coeffs`, holding these coefficients. So the following is sufficient to display the plot:

```
matrix m = $model.midas_coeffs
plot m
  options with-lp fit=none
  literal set title "MIDAS coefficients"
  literal set ylabel ''
end plot --output=display
```

Caveat: this feature is at present available only for models with a single MIDAS specification.

41.3 Parameterization functions

Here we give some more detail of the MIDAS parameterizations supported by `gretl`.

In general the normalized coefficient or weight i ($i = 1, \dots, p$) is given by

$$w_i = \frac{f(i, \theta)}{\sum_{k=1}^p f(k, \theta)} \quad (41.3)$$

such that the coefficients sum to unity.

Listing 41.3: Manual MIDAS: one-parameter beta specification [\[Download ▼\]](#)

```

set verbose off

function scalar beta1_SSR (scalar th2, const series y,
                          const series x, list L)
    matrix theta = {1, th2}
    series mdx = mlincomb(L, theta, 2)
    # run OLS conditional on theta
    ols y 0 x mdx --quiet
    return $ess
end function

function matrix midas_GNR (const matrix theta, const series y,
                          const series x, list L, int type)
    # Gauss-Newton regression
    series mdx = mlincomb(L, theta, type)
    ols y 0 x mdx --quiet
    matrix b = $coeff
    matrix u = {$uhat}
    matrix mgrad = mgradient(nelem(L), theta, type)
    matrix M = {const, x, mdx} ~ (b[3] * {L} * mgrad)
    matrix V
    set svd on # in case of strong collinearity
    mols(u, M, null, &V)
    return (b | theta) ~ sqrt(diag(V))
end function

/* main */

open gdp_midas.gdt --quiet

series dy = 100 * ldiff(qgdp)
series dy1 = dy(-1)
list dX = ld_payem*
list dXL = hflags(3, 11, dX)

# estimation sample
smpl 1985:1 2009:1

matrix b = {0, 1.01, 100}
# use Golden Section minimizer
SSR = GSSmin(b, beta1_SSR(b[1], dy, dy1, dXL), 1.0e-6)
printf "SSR (GSS) = %.15g\n", SSR
matrix theta = {1, b[1]}' # column vector needed
matrix bse = midas_GNR(theta, dy, dy1, dXL, 2)
bse[4,2] = $nan # mask std error of clamped coefficient
modprint bse "const dy(-1) HF_slope Beta1 Beta2"

```

In the **normalized exponential Almon** case with m parameters the function $f(\cdot)$ is

$$f(i, \theta) = \exp \left(\sum_{j=1}^m \theta_j i^j \right) \quad (41.4)$$

So in the usual two-parameter case we have

$$w_i = \frac{\exp(\theta_1 i + \theta_2 i^2)}{\sum_{k=1}^p \exp(\theta_1 k + \theta_2 k^2)}$$

and equal weighting is obtained when $\theta_1 = \theta_2 = 0$.

In the standard, two-parameter **normalized beta** case we have

$$f(i, \theta) = (i^- / p^-)^{\theta_1 - 1} \cdot (1 - i^- / p^-)^{\theta_2 - 1} \quad (41.5)$$

where $p^- = p - 1$, and $i^- = i - 1$ except at the end-points, $i = 1$ and $i = p$, where we add and subtract, respectively, machine epsilon to avoid numerical problems. This formulation constrains the coefficient on the last lag to be zero—provided that the weights are declining at higher lags, a condition that is ensured if θ_2 is greater than θ_1 by a sufficient margin. The special case of $\theta_1 = \theta_2 = 1$ yields equal weights at all lags. A third parameter can be used to allow a non-zero final weight, even in the case of declining weights. Let w_i denote the normalized weight obtained by using (41.5) in (41.3). Then the modified variant with additional parameter θ_3 can be written as

$$w_i^{(3)} = \frac{w_i + \theta_3}{1 + p\theta_3}$$

That is, we add θ_3 to each weight then renormalize so that the $w_i^{(3)}$ values again sum to unity.

In Eric Ghysels' Matlab code the two beta variants are labeled “normalized beta density with a zero last lag” and “normalized beta density with a non-zero last lag” respectively. Note that while the two basic beta parameters must be positive, the third additive parameter may be positive, negative or zero.

In the case of the plain **Almon polynomial** of order m , coefficient i is given by

$$w_i = \sum_{j=1}^m \theta_j i^{j-1}$$

Note that no normalization is applied in this case, so no additional coefficient should be placed before the MIDAS lags term in the context of a regression.

Analytical gradients

Here we set out the expressions for the analytical gradients produced by the `mgradient` function, and also used internally by the `midasreg` command. In these expressions $f(i, \theta)$ should be understood as referring back to the specific forms noted above for the exponential Almon and beta distributions. The summation \sum_k should be understood as running from 1 to p .

For the normalized exponential Almon case, the gradient is

$$\begin{aligned} \frac{dw_i}{d\theta_j} &= \frac{f(i, \theta) i^j}{\sum_k f(k, \theta)} - \frac{f(i, \theta)}{[\sum_k f(k, \theta)]^2} \sum_k [f(k, \theta) k^j] \\ &= w_i \left(i^j - \frac{\sum_k [f(k, \theta) k^j]}{\sum_k f(k, \theta)} \right) \end{aligned}$$

For the two-parameter normalized beta case it is

$$\begin{aligned}\frac{dw_i}{d\theta_1} &= \frac{f(i, \theta) \log(i^-/p^-)}{\sum_k f(k, \theta)} - \frac{f(i, \theta)}{[\sum_k f(k, \theta)]^2} \sum_k [f(k, \theta) \log(k^-/p^-)] \\ &= w_i \left(\log(i^-/p^-) - \frac{\sum_k [f(k, \theta) \log(k^-/p^-)]}{\sum_k f(k, \theta)} \right) \\ \frac{dw_i}{d\theta_2} &= \frac{f(i, \theta) \log(1 - i^-/p^-)}{\sum_k f(k, \theta)} - \frac{f(i, \theta)}{[\sum_k f(k, \theta)]^2} \sum_k [f(k, \theta) \log(1 - k^-/p^-)] \\ &= w_i \left(\log(1 - i^-/p^-) - \frac{\sum_k [f(k, \theta) \log(1 - k^-/p^-)]}{\sum_k f(k, \theta)} \right)\end{aligned}$$

And for the three-parameter beta, we have

$$\begin{aligned}\frac{dw_i^{(3)}}{d\theta_1} &= \frac{1}{1 + p\theta_3} \frac{dw_i}{d\theta_1} \\ \frac{dw_i^{(3)}}{d\theta_2} &= \frac{1}{1 + p\theta_3} \frac{dw_i}{d\theta_2} \\ \frac{dw_i^{(3)}}{d\theta_3} &= \frac{1}{1 + p\theta_3} - \frac{p(w_i + \theta_3)}{(1 + p\theta_3)^2}\end{aligned}$$

For the (non-normalized) Almon polynomial the gradient is simply

$$\frac{dw_i}{d\theta_j} = i^{j-1}$$

Part III

Technical details

Chapter 42

Gretl and ODBC

Gretl provides a method for retrieving data from databases which support the Open Database Connectivity (ODBC) standard. Most users won't be interested in this, but there may be some for whom this feature matters a lot—typically, those who work in an environment where huge data collections are accessible via a Data Base Management System (DBMS).

In the following section we explain what is needed for ODBC support in gretl. We provide some background information on how ODBC works in section 42.2, and explain the details of getting gretl to retrieve data from a database in section 42.3. Section 42.4 provides some example of usage, and section 42.5 gives some details on the management of ODBC connections.

42.1 ODBC support

The piece of software that bridges between gretl and the ODBC system is a dynamically loaded “plugin”. This is included in the gretl packages for MS Windows and Mac OS X. On other unix-type platforms (notably Linux) you may have to build gretl from source to get ODBC support. This is because the plugin depends on having unixODBC installed, which we cannot assume to be the case on typical Linux systems. To enable the ODBC plugin when building gretl, you must pass the option `--with-odbc` to gretl's `configure` script. In addition, if unixODBC is installed in a non-standard location you will have to specify its installation prefix using `--with-ODBC-prefix`, as in (for example)

```
./configure --with-odbc --with-ODBC-prefix=/opt/ODBC
```

42.2 ODBC base concepts

ODBC is short for *Open DataBase Connectivity*, a group of software methods that enable a *client* to interact with a database *server*. The most common operation is when the client fetches some data from the server. ODBC acts as an intermediate layer between client and server, so the client “talks” to ODBC rather than accessing the server directly (see Figure 42.1).

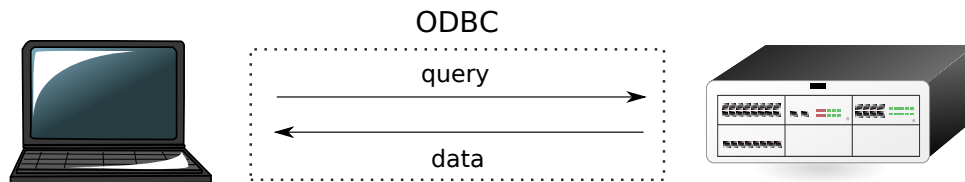


Figure 42.1: Retrieving data via ODBC

For the above mechanism to work, it is necessary that the relevant ODBC software is installed and working on the client machine (contact your DB administrator for details). At this point, the database (or databases) that the server provides will be accessible to the client as a *data source* with a specific identifier (a Data Source Name or DSN); in most cases, a username and a password are required to connect to the data source.

Once the connection is established, the user sends a *query* to ODBC, which contacts the database manager, collects the results and sends them back to the user. The query is almost invariably formulated in a special language used for the purpose, namely SQL.¹ We will not provide here an SQL tutorial: there are many such tutorials on the Net; besides, each database manager tends to support its own SQL dialect so the precise form of an SQL query may vary slightly if the DBMS on the other end is Oracle, MySQL, PostgreSQL or something else.

Suffice it to say that the main statement for retrieving data is the SELECT statement. Within a DBMS, data are organized in *tables*, which are roughly equivalent to spreadsheets. The SELECT statement returns a subset of a table, which is itself a table. For example, imagine that the database holds a table called “NatAccounts”, containing the data shown in Table 42.1.

year	qtr	gdp	consump	tradebal
1970	1	584763	344746.9	-5891.01
1970	2	597746	350176.9	-7068.71
1970	3	604270	355249.7	-8379.27
1970	4	609706	361794.7	-7917.61
1971	1	609597	362490	-6274.3
1971	2	617002	368313.6	-6658.76
1971	3	625536	372605	-4795.89
1971	4	630047	377033.9	-6498.13

Table 42.1: The “NatAccounts” table

The SQL statement

```
SELECT qtr, tradebal, gdp FROM NatAccounts WHERE year=1970;
```

produces the subset of the original data shown in Table 42.2.

qtr	tradebal	gdp
1	-5891.01	584763
2	-7068.71	597746
3	-8379.27	604270
4	-7917.61	609706

Table 42.2: Result of a SELECT statement

Gretl provides a mechanism for forwarding your query to the DBMS via ODBC and including the results in your currently open dataset.

42.3 Syntax

At present we do not offer a graphical interface for ODBC import; this must be done via the command line interface. The two commands used for fetching data via an ODBC connection are `open` and `data`.

The `open` command is used for connecting to a DBMS: its syntax is

```
open dsn=database [user=username] [password=password] --odbc
```

The `user` and `password` items are optional; the effect of this command is to initiate an ODBC connection. It is assumed that the machine gretl runs on has a working ODBC client installed.

¹See <http://en.wikipedia.org/wiki/SQL>.

In order to actually retrieve the data, the `data` command is used. Its syntax is:

```
data series [obs-format=format-string] query=query-string --odbc
```

where:

series is a list of names of gretl series to contain the incoming data, separated by spaces. Note that these series need not exist prior to the ODBC import.

format-string is an optional parameter, used to handle cases when a “rectangular” organisation of the database cannot be assumed (more on this later);

query-string is a string containing the SQL statement used to extract the data.

There should be no spaces around the equals signs in the `obs-format` and `query` fields in the `data` command.

The **query-string** can, in principle, contain any valid SQL statement which results in a table. This string may be specified directly within the command, as in

```
data x query="SELECT foo FROM bar" --odbc
```

which will store into the gretl variable `x` the content of the column `foo` from the table `bar`. However, since in a real-life situation the string containing the SQL statement may be rather long, it may be best to store it in a string variable. For example:

```
string SqlQry = "SELECT foo1, foo2 FROM bar"
data x y query=SqlQry --odbc
```

The observation format specifier

If the optional parameter `obs-format` is absent, as in the above example, the SQL query should return k columns of data, where k is the number of series names listed in the `data` command. It may be necessary to include a `smpl` command before the `data` command to set up the right “window” for the incoming data. In addition, if one cannot assume that the data will be delivered in the correct order (typically, chronological order), the SQL query should contain an appropriate `ORDER BY` clause.

The optional format string is used for those cases when there is no certainty that the data from the query will arrive in the same order as the gretl dataset. This may happen when missing values are interspersed within a column, or with data that do not have a natural ordering, e.g. cross-sectional data. In this case, the SQL statement should return a table with $m + k$ columns, where the first m columns are used to identify the observation or row in the gretl dataset into which the actual data values in the final k columns should be placed. The `obs-format` string is used to translate the first m fields into a string which matches the string gretl uses to identify observations in the currently open dataset. Up to three columns can be used for this purpose ($m \leq 3$).

Note that the strings gretl uses to identify observations can be seen by printing any variable “by observation”, as in

```
print index --byobs
```

(The series named `index` is automatically added to a dataset created via the `newdata` command.)

The format specifiers available for use with `obs-format` are as follows:

%d	print an integer value
%s	print a string value
%g	print a floating-point value

In addition the format can include literal characters to be passed through, such as slashes or colons, to make the resulting string compatible with gretl's observation identifiers.

For example, consider the following fictitious case: we have a 5-days-per-week dataset, to which we want to add the stock index for the Verdurian market;² it so happens that in Verduria Saturdays are working days but Wednesdays are not. We want a column which does *not* contain data on Saturdays, because we wouldn't know where to put them, but at the same time we want to place missing values on all the Wednesdays.

In this case, the following syntax could be used

```
string QRY="SELECT year,month,day,VerdSE FROM AlmeaIndexes"
data y obs-format="%d-%d-%d" query=QRY --odbc
```

The column VerdSE holds the data to be fetched, which will go into the gretl series *y*. The first three columns are used to construct a string which identifies the day. Daily dates take the form YYYY-MM-DD in gretl. If a row from the DBMS produces the observation string 2008-04-01 this will match OK (it's a Tuesday), but 2008-04-05 will not match since it is a Saturday; the corresponding row will therefore be discarded. On the other hand, since no string 2008-04-23 will be found in the data coming from the DBMS (it's a Wednesday), that entry is left blank in our series *y*.

42.4 Examples

Table Consump		Table DATA	
Field	Type	Field	Type
time	decimal(7,2)	year	decimal(4,0)
income	decimal(16,6)	qtr	decimal(1,0)
consump	decimal(16,6)	varname	varchar(16)
		xval	decimal(20,10)

Table 42.3: Example AWM database – structure

Table Consump			Table DATA			
			1970	1	CAN	-517.9085000000
1970.00	424278.975500	344746.944000	1970	2	CAN	662.5996000000
1970.25	433218.709400	350176.890400	1970	3	CAN	1130.4155000000
1970.50	440954.219100	355249.672300	1970	4	CAN	467.2508000000
1970.75	446278.664700	361794.719900	1970	1	COMPR	18.4000000000
1971.00	447752.681800	362489.970500	1970	2	COMPR	18.6341000000
1971.25	453553.860100	368313.558500	1970	3	COMPR	18.3000000000
1971.50	460115.133100	372605.015300	1970	4	COMPR	18.2663000000
...			1970	1	D1	1.0000000000
			1970	2	D1	0.0000000000
			...			

Table 42.4: Example AWM database — data

In the following examples, we will assume that access is available to a database known to ODBC with the data source name "AWM", with username "Otto" and password "Bingo". The database "AWM" contains quarterly data in two tables (see 42.3 and 42.4):

²See <http://www.almeopedia.com/index.php/Verduria>.

The table `Consump` is the classic “rectangular” dataset; that is, its internal organization is the same as in a spreadsheet or econometrics package: each row is a data point and each column is a variable. The structure of the `DATA` table is different: each record is one figure, stored in the column `xval`, and the other fields keep track of which variable it belongs to, for which date.

Listing 42.1: Simple query from a rectangular table

```

nulldata 160
setobs 4 1970:1 --time
open dsn=AWM user=Otto password=Bingo --odbc

string Qry = "SELECT consump, income FROM Consump"
data cons inc query=Qry --odbc

```

Listing 42.1 shows a query for two series: first we set up an empty quarterly dataset. Then we connect to the database using the `open` statement. Once the connection is established we retrieve two columns from the `Consump` table. No observation string is required because the data already have a suitable structure; we need only import the relevant columns.

Listing 42.2: Simple query from a non-rectangular table

```

string S = "select year, qtr, xval from DATA \
           where varname='WLN' ORDER BY year, qtr"
data wln obs-format="%d:%d" query=S --odbc

```

In example 42.2, by contrast, we make use of the observation string since we are drawing from the `DATA` table, which is not rectangular. The SQL statement stored in the string `S` produces a table with three columns. The `ORDER BY` clause ensures that the rows will be in chronological order, although this is not strictly necessary in this case.

42.5 Connectivity details

It may be helpful to supply some details on gretl’s management of ODBC connections. First, when the `open` command is invoked with the `--odbc` option, gretl checks to see if a connection to the specified DSN (Data Source Name) can be established via the ODBC function `SQLConnect`. If not, an error is flagged; if so, the connection is dropped (`SQLDisconnect`) but the DSN details are stored. The stored DSN then remains the implicit source for subsequent invocation of the `data` command, with the `--odbc` option, until a countermanding `open` command is issued.

Each time an ODBC-related `data` command is issued, gretl attempts to re-establish a connection to the given DSN; the connection is dropped once the data transfer is complete.

Listing 42.3: Handling of missing values for a non-rectangular table

```
string foo = "select year, qtr, xval from DATA \
              where varname='STN' AND qtr>1"
data bar obs-format="%d:%d" query=foo --odbc
print bar --byobs
```

Listing 42.3 shows what happens if the rows in the outcome from the SELECT statement do not match the observations in the currently open gretl dataset. The query includes a condition which filters out all the data from the first quarter. The query result (invisible to the user) would be something like

year	qtr	xval
1970	2	7.8705000000
1970	3	7.5600000000
1970	4	7.1892000000
1971	2	5.8679000000
1971	3	6.2442000000
1971	4	5.9811000000
1972	2	4.6883000000
1972	3	4.6302000000
...		

Internally, gretl fills the variable `bar` with the corresponding value if it finds a match; otherwise, NA is used. Printing out the variable `bar` thus produces

Obs	bar
1970:1	
1970:2	7.8705
1970:3	7.5600
1970:4	7.1892
1971:1	
1971:2	5.8679
1971:3	6.2442
1971:4	5.9811
1972:1	
1972:2	4.6883
1972:3	4.6302
...	

Chapter 43

Gretl and T_EX

43.1 Introduction

T_EX — initially developed by Donald Knuth of Stanford University and since enhanced by hundreds of contributors around the world — is the gold standard of scientific typesetting. Gretl provides various hooks that enable you to preview and print econometric results using the T_EX engine, and to save output in a form suitable for further processing with T_EX.

This chapter explains the finer points of gretl’s T_EX-related functionality. The next section describes the relevant menu items; section 43.3 discusses ways of fine-tuning T_EX output; and section 43.4 gives some pointers on installing (and learning) T_EX if you do not already have it on your computer. (Just to be clear: T_EX is not included with the gretl distribution; it is a separate package, including several programs and a large number of supporting files.)

Before proceeding, however, it may be useful to set out briefly the stages of production of a final document using T_EX. For the most part you don’t have to worry about these details, since, in regard to previewing at any rate, gretl handles them for you. But having some grasp of what is going on behind the scenes will enable you to understand your options better.

The first step is the creation of a plain text “source” file, containing the text or mathematics to be typeset, interspersed with mark-up that defines how it should be formatted. The second step is to run the source through a processing engine that does the actual formatting. Typically this a program called `pdflatex` that generates PDF output.¹ (In times gone by it was a program called `latex` that generated so-called DVI (device-independent) output.)

So gretl calls `pdflatex` to process the source file. On MS Windows and Mac OS X, gretl expects the operating system to find the default viewer for PDF output. On GNU/Linux you can specify your preferred PDF viewer via the menu item “Tools, Preferences, General,” under the “Programs” tab.

43.2 T_EX-related menu items

The model window

The fullest T_EX support in gretl is found in the GUI model window. This has a menu item titled “LaTeX” with sub-items “View”, “Copy”, “Save” and “Equation options” (see Figure 43.1).

The first three sub-items have branches titled “Tabular” and “Equation”. By “Tabular” we mean that the model is represented in the form of a table; this is the fullest and most explicit presentation of the results. See Table 43.1 for an example; this was pasted into the manual after using the “Copy, Tabular” item in gretl (a few lines were edited out for brevity).

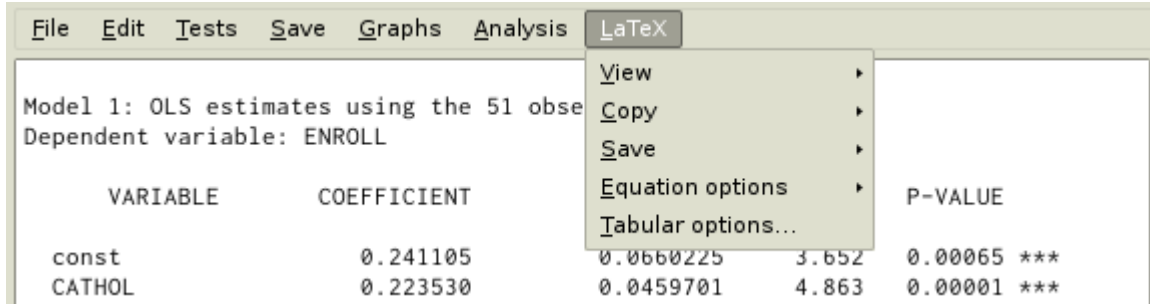
The “Equation” option is fairly self-explanatory — the results are written across the page in equation format, as below:

$$\widehat{\text{ENROLL}} = 0.241105 + 0.223530 \text{ CATHOL} - 0.00338200 \text{ PUPIL} - 0.152643 \text{ WHITE}$$

(0.066022) (0.04597) (0.0027196) (0.040706)

$$T = 51 \quad \bar{R}^2 = 0.4462 \quad F(3, 47) = 14.431 \quad \hat{\sigma} = 0.038856$$

¹Experts will be aware of something called “plain T_EX”, which is processed using the program `tex`. The great majority of T_EX users, however, use the L^AT_EX macros, initially developed by Leslie Lamport. gretl does not support plain T_EX.

Figure 43.1: \LaTeX menu in model window**Table 43.1:** Example of \LaTeX tabular output

Model 1: OLS estimates using the 51 observations 1-51
Dependent variable: ENROLL

Variable	Coefficient	Std. Error	<i>t</i> -statistic	p-value
const	0.241105	0.0660225	3.6519	0.0007
CATHOL	0.223530	0.0459701	4.8625	0.0000
PUPIL	-0.00338200	0.00271962	-1.2436	0.2198
WHITE	-0.152643	0.0407064	-3.7499	0.0005
Mean of dependent variable			0.0955686	
S.D. of dependent variable			0.0522150	
Sum of squared residuals			0.0709594	
Standard error of residuals ($\hat{\sigma}$)			0.0388558	
Unadjusted R^2			0.479466	
Adjusted \bar{R}^2			0.446241	
$F(3, 47)$			14.4306	

(standard errors in parentheses)

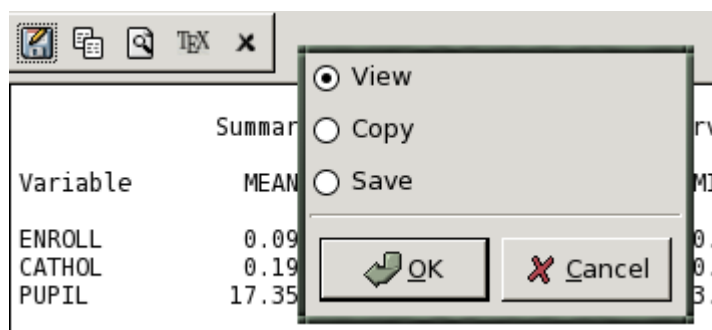
The distinction between the “Copy” and “Save” options (for both tabular and equation) is twofold. First, “Copy” puts the T_EX source on the clipboard while with “Save” you are prompted for the name of a file into which the source should be saved. Second, with “Copy” the material is copied as a “fragment” while with “Save” it is written as a complete file. The point is that a well-formed T_EX source file must have a header that defines the `documentclass` (article, report, book or whatever) and tags that say `\begin{document}` and `\end{document}`. This material is included when you do “Save” but not when you do “Copy”, since in the latter case the expectation is that you will paste the data into an existing T_EX source file that already has the relevant apparatus in place.

The items under “Equation options” should be self-explanatory: when printing the model in equation form, do you want standard errors or *t*-ratios displayed in parentheses under the parameter estimates? The default is to show standard errors; if you want *t*-ratios, select that item.

Other windows

Several other sorts of output windows also have T_EX preview, copy and save enabled. In the case of windows having a graphical toolbar, look for the T_EX button. Figure 43.2 shows this icon (second from the right on the toolbar) along with the dialog that appears when you press the button.

Figure 43.2: T_EX icon and dialog



One aspect of gretl’s T_EX support that is likely to be particularly useful for publication purposes is the ability to produce a typeset version of the “model table” (see section 3.4). An example of this is shown in Table 43.2.

43.3 Fine-tuning typeset output

There are three aspects to this: adjusting the appearance of the output produced by gretl in L^AT_EX preview mode; adjusting the formatting of gretl’s tabular output for models when using the `tabprint` command; and incorporating gretl’s output into your own T_EX files.

Previewing in the GUI

As regards *preview mode*, you can control the appearance of gretl’s output using a file named `gretlpre.tex`, which should be placed in your gretl user directory (see the *Gretl Command Reference*). If such a file is found, its contents will be used as the “preamble” to the T_EX source. The default value of the preamble is as follows:

```
\documentclass[11pt]{article}
\usepackage[utf8]{inputenc}
```

Table 43.2: Example of model table output

OLS estimates			
Dependent variable: ENROLL			
	Model 1	Model 2	Model 3
const	0.2907** (0.07853)	0.2411** (0.06602)	0.08557 (0.05794)
CATHOL	0.2216** (0.04584)	0.2235** (0.04597)	0.2065** (0.05160)
PUPIL	−0.003035 (0.002727)	−0.003382 (0.002720)	−0.001697 (0.003025)
WHITE	−0.1482** (0.04074)	−0.1526** (0.04071)	
ADMEXP	−0.1551 (0.1342)		
<i>n</i>	51	51	51
\bar{R}^2	0.4502	0.4462	0.2956
ℓ	96.09	95.36	88.69

Standard errors in parentheses

* indicates significance at the 10 percent level

** indicates significance at the 5 percent level

```

\usepackage{amsmath}
\usepackage{dcolumn,longtable}
\begin{document}
\thispagestyle{empty}

```

Note that the `amsmath` and `dcolumn` packages are required. (For some sorts of output the `longtable` package is also needed.) Beyond that you can, for instance, change the type size or the font by altering the `documentclass` declaration or including an alternative font package.

In addition, if you wish to typeset gretl output in more than one language, you can set up per-language preamble files. A “localized” preamble file is identified by a name of the form `gretlpre_xx.tex`, where `xx` is replaced by the first two letters of the current setting of the `LANG` environment variable. For example, if you are running the program in Polish, using `LANG=pl_PL`, then gretl will do the following when writing the preamble for a T_EX source file.

1. Look for a file named `gretlpre_pl.tex` in the gretl user directory. If this is not found, then
2. look for a file named `gretlpre.tex` in the gretl user directory. If this is not found, then
3. use the default preamble.

Conversely, suppose you usually run gretl in a language other than English, and have a suitable `gretlpre.tex` file in place for your native language. If on some occasions you want to produce T_EX output in English, then you could create an additional file `gretlpre_en.tex`: this file will be used for the preamble when gretl is run with a language setting of, say, `en_US`.

Command-line options

After estimating a model via a script—or interactively via the gretl console or using the command-line program `gretlcli`—you can use the commands `tabprint` or `eqnprint` to print the model to file in tabular format or equation format respectively. These options are explained in the *Gretl Command Reference*.

If you wish alter the appearance of gretl’s tabular output for models in the context of the `tabprint` command, you can specify a custom row format using the `--format` flag. The format string must be enclosed in double quotes and must be tied to the flag with an equals sign. The pattern for the format string is as follows. There are four fields, representing the coefficient, standard error, *t*-ratio and p-value respectively. These fields should be separated by vertical bars; they may contain a `printf`-type specification for the formatting of the numeric value in question, or may be left blank to suppress the printing of that column (subject to the constraint that you can’t leave all the columns blank). Here are a few examples:

```

--format="%.4f|%.4f|%.4f|%.4f"
--format="%.4f|%.4f|%.3f|"
--format="%.5f|%.4f| |%.4f"
--format="%.8g|%.8g| |%.4f"

```

The first of these specifications prints the values in all columns using 4 decimal places. The second suppresses the p-value and prints the *t*-ratio to 3 places. The third omits the *t*-ratio. The last one again omits the *t*, and prints both coefficient and standard error to 8 significant figures.

Once you set a custom format in this way, it is remembered and used for the duration of the gretl session. To revert to the default formatting you can use the special variant `--format=default`.

Further editing

Once you have pasted gretl’s T_EX output into your own document, or saved it to file and opened it in an editor, you can of course modify the material in any wish you wish. In some cases, machine-generated T_EX is hard to understand, but gretl’s output is intended to be human-readable and

-editable. In addition, it does not use any non-standard style packages. Besides the standard L^AT_EX document classes, the only files needed are, as noted above, the `amsmath`, `dcolumn` and `longtable` packages. These should be included in any reasonably full T_EX implementation.

43.4 Installing and learning T_EX

This is not the place for a detailed exposition of these matters, but here are a few pointers.

So far as we know, every GNU/Linux distribution has a package or set of packages for T_EX, and in fact these are likely to be installed by default. Check the documentation for your distribution. For MS Windows, several packaged versions of T_EX are available: one of the most popular is MiK_T_EX at <http://www.miktex.org/>. For Mac OS X a nice implementation is i_T_EXMac, at <http://itexmac.sourceforge.net/>. An essential starting point for online T_EX resources is the Comprehensive T_EX Archive Network (CTAN) at <http://www.ctan.org/>.

As for learning T_EX, many useful resources are available both online and in print. Among online guides, Tony Roberts' "L^AT_EX: from quick and dirty to style and finesse" is very helpful, at

<http://www.sci.usq.edu.au/staff/robertsa/LaTeX/latexintro.html>

An excellent source for advanced material is *The L^AT_EX Companion* (Goossens *et al.*, 2004).

Chapter 44

Gretl and R

44.1 Introduction

R is, by far, the largest free statistical project.¹ Like gretl, it is a GNU project and the two have a lot in common; however, gretl's approach focuses on ease of use much more than R, which instead aims to encompass the widest possible range of statistical procedures.

As is natural in the free software ecosystem, we don't view ourselves as competitors to R,² but rather as projects sharing a common goal who should support each other whenever possible. For this reason, gretl provides a way to interact with R and thus enable users to pool the capabilities of the two packages.

In this chapter, we will explain how to exploit R's power from within gretl. We assume that the reader has a working installation of R available and a basic grasp of R's syntax.³

Despite several valiant attempts, no graphical shell has gained wide acceptance in the R community: by and large, the standard method of working with R is by writing scripts, or by typing commands at the R prompt, much in the same way as one would write gretl scripts or work with the gretl console. In this chapter, the focus will be on the methods available to execute R commands without leaving gretl.

44.2 Starting an interactive R session

The easiest way to use R from gretl is in interactive mode. Once you have your data loaded in gretl, you can select the menu item "Tools, Start GNU R" and an interactive R session will be started, with your dataset automatically pre-loaded.

A simple example: OLS on cross-section data

For this example we use Ramanathan's dataset `data4-1`, one of the sample files supplied with gretl. We first run, in gretl, an OLS regression of `price` on `sqft`, `bedrms` and `baths`. The basic results are shown in Table 44.1.

Table 44.1: OLS house price regression via gretl

Variable	Coefficient	Std. Error	<i>t</i> -statistic	p-value
const	129.062	88.3033	1.4616	0.1746
sqft	0.154800	0.0319404	4.8465	0.0007
bedrms	-21.587	27.0293	-0.7987	0.4430
baths	-12.192	43.2500	-0.2819	0.7838

¹R's homepage is at <http://www.r-project.org/>.

²OK, who are we kidding? But it's *friendly* competition!

³The main reference for R documentation is <http://cran.r-project.org/manuals.html>. In addition, R tutorials abound on the Net; as always, Google is your friend.

We will now replicate the above results using R. Select the menu item “Tools, Start GNU R”. A window similar to the one shown in figure 44.1 should appear.

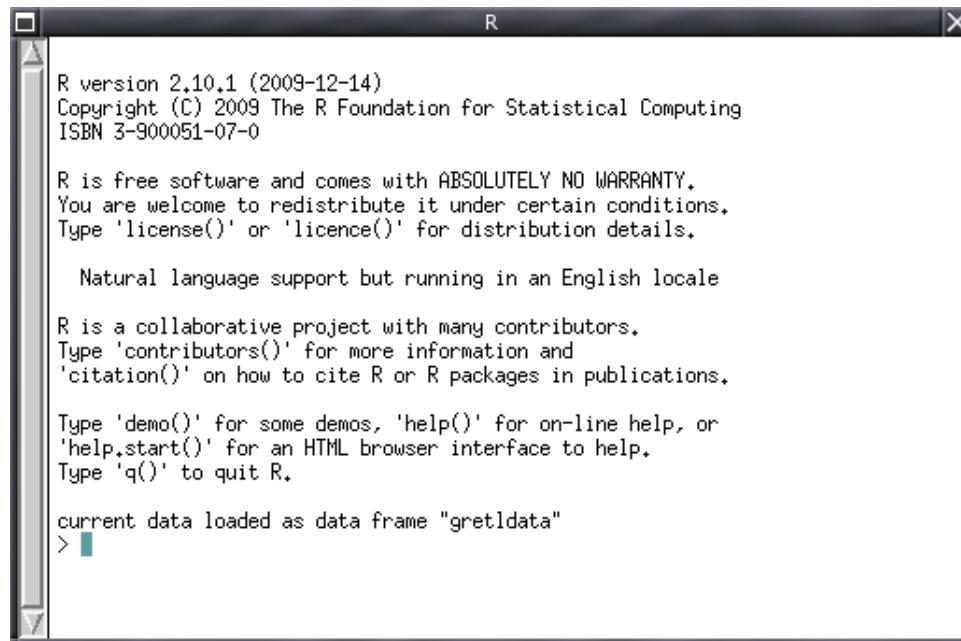


Figure 44.1: R window

The actual look of the R window may be somewhat different from what you see in Figure 44.1 (especially for Windows users), but this is immaterial. The important point is that you have a window where you can type commands to R. If the above procedure doesn't work and no R window opens, it means that gretl was unable to launch R. You should ensure that R is installed and working on your system and that gretl knows where it is. The relevant settings can be found by selecting the “Tools, Preferences, General” menu entry, under the “Programs” tab.

Assuming R was launched successfully, you will see notification that the data from gretl are available. In the background, gretl has arranged for two R commands to be executed, one to load the gretl dataset in the form of a *data frame* (one of several forms in which R can store data) and one to *attach* the data so that the variable names defined in the gretl workspace are available as valid identifiers within R.

In order to replicate gretl's OLS estimation, go into the R window and type at the prompt

```
model <- lm(price ~ sqft + bedrms + baths)
summary(model)
```

You should see something similar to Figure 44.2. Surprise—the estimates coincide! To get out, just close the R window or type `q()` at the R prompt.

Time series data

We now turn to an example which uses time series data: we will compare gretl's and R's estimates of Box and Jenkins' immortal “airline” model. The data are contained in the `bjg` sample dataset. The following gretl code

```
open bjg
arima 0 1 1 ; 0 1 1 ; lg --nc
```

produces the estimates shown in Table 44.2.

```

> model <- lm(price ~ sqft + bedrms + baths)
> summary(model)

Call:
lm(formula = price ~ sqft + bedrms + baths)

Residuals:
    Min       1Q   Median       3Q      Max
-55.533 -16.219  -6.093   22.432   68.703

Coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept) 129.06163   88.30326   1.462 0.174559
sqft         0.15480    0.03194   4.847 0.000675 ***
bedrms      -21.58752   27.02933  -0.799 0.443037
baths       -12.19276   43.25000  -0.282 0.783758
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 40.87 on 10 degrees of freedom
Multiple R-squared:  0.836,    Adjusted R-squared:  0.7868
F-statistic: 16.99 on 3 and 10 DF, p-value: 0.0002986

>

```

Figure 44.2: OLS regression on house prices via R

Table 44.2: Airline model from Box and Jenkins (1976) – selected portion of gretl’s estimates

Variable	Coefficient	Std. Error	<i>t</i> -statistic	p-value
θ_1	-0.401824	0.0896421	-4.4825	0.0000
Θ_1	-0.556936	0.0731044	-7.6184	0.0000
Variance of innovations			0.00134810	
Log-likelihood			244.696	
Akaike information criterion			-483.39	

If we now open an R session as described in the previous subsection, the data-passing mechanism is slightly different. Since our data were defined in gretl as time series, we use an R *time-series* object (*ts* for short) for the transfer. In this way we can retain in R useful information such as the periodicity of the data and the sample limits. The downside is that the names of individual series, as defined in gretl, are not valid identifiers. In order to extract the variable *lg*, one needs to use the syntax `lg <- gretldata[, "lg"]`.

ARIMA estimation can be carried out by issuing the following two R commands:

```
lg <- gretldata[, "lg"]
arima(lg, c(0,1,1), seasonal=c(0,1,1))
```

which yield

```
Coefficients:
      ma1      sma1
    -0.4018  -0.5569
s.e.    0.0896   0.0731

sigma^2 estimated as 0.001348:  log likelihood = 244.7,  aic = -483.4
```

Happily, the estimates again coincide.

44.3 Running an R script

Opening an R window and keying in commands is a convenient method when the job is small. In some cases, however, it would be preferable to have R execute a script prepared in advance. One way to do this is via the `source()` command in R. Alternatively, gretl offers the facility to edit an R script and run it, having the current dataset pre-loaded automatically. This feature can be accessed via the “File, Script Files” menu entry. By selecting “User file”, one can load a pre-existing R script; if you want to create a new script instead, select the “New script, R script” menu entry.

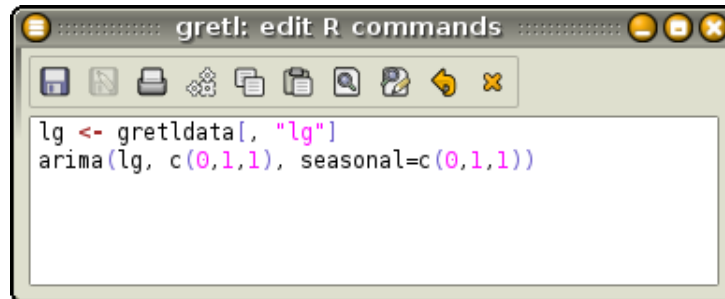


Figure 44.3: Editing window for R scripts

In either case, you are presented with a window very similar to the editor window used for ordinary gretl scripts, as in Figure 44.3.

There are two main differences. First, you get syntax highlighting for R's syntax instead of gretl's. Second, clicking on the Execute button (the gears icon), launches an instance of R in which your commands are executed. Before R is actually run, you are asked if you want to run R interactively or not (see Figure 44.4).

An interactive run opens an R instance similar to the one seen in the previous section: your data will be pre-loaded (if the “pre-load data” box is checked) and your commands will be executed. Once this is done, you will find yourself at the R prompt, where you can enter more commands.

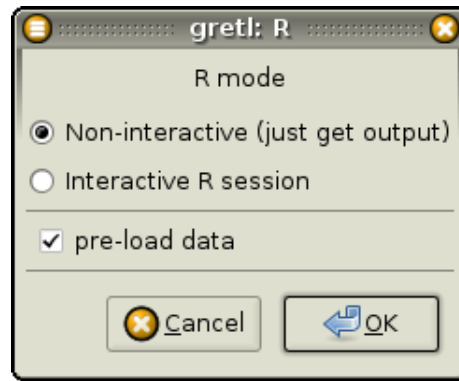


Figure 44.4: Editing window for R scripts

A non-interactive run, on the other hand, will execute your script, collect the output from R and present it to you in an output window; R will be run in the background. If, for example, the script in Figure 44.3 is run non-interactively, a window similar to Figure 44.5 will appear.

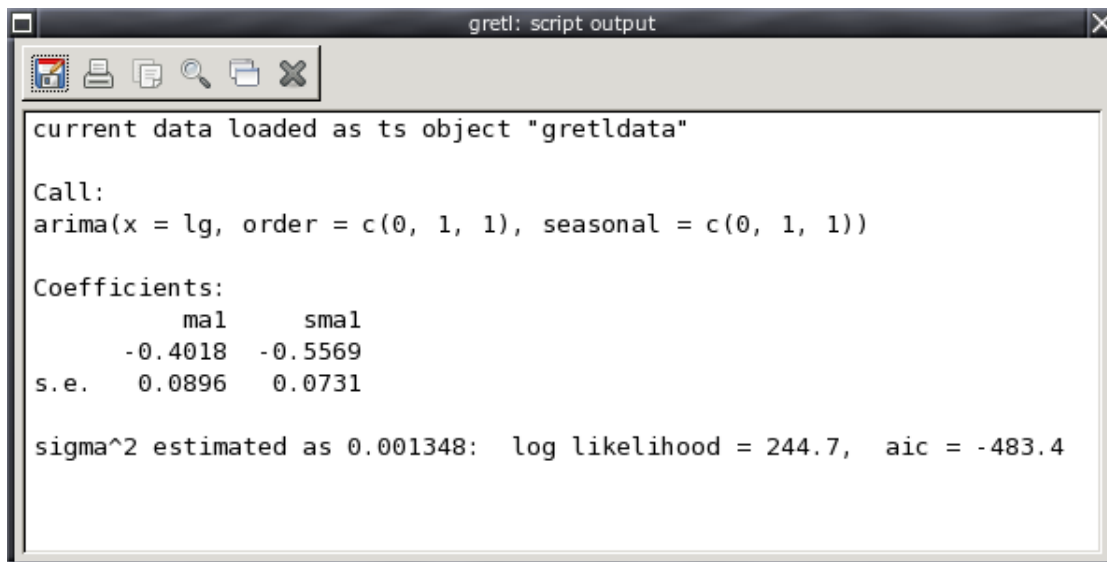


Figure 44.5: Output from a non-interactive R run

44.4 Sending data back and forth

As regards the passing of data between the two programs, so far we have only considered passing series from gretl to R. In order to achieve a satisfactory degree of interoperability, more is needed. In the following sub-sections we see how matrices can be exchanged, and how data can be passed from R back to gretl.

Passing matrices from gretl to R

For passing matrices from gretl to R, you can use the `mwwrite` matrix function described in section 17.7. For example, the following gretl code fragment generates the matrix

$$A = \begin{bmatrix} 3 & 7 & 11 \\ 4 & 8 & 12 \\ 5 & 9 & 13 \\ 6 & 10 & 14 \end{bmatrix}$$

and stores it into the file `mymatfile.mat` in the user's "dotdir" (see section 15.2). Note that writing to this special directory, which is sure to exist and be writable by the user, is mandated by the non-zero value for the third, optional argument to `mwwrite`.

```
matrix A = mshape(seq(3,14),4,3)
err = mwwrite(A, "mymatfile.mat", 1)
```

The recommended R code to import such a matrix is

```
A <- gretl.loadmat("mymatfile.mat")
```

The function `gretl.loadmat`, which is predefined when R is called from gretl, retrieves the matrix from dotdir. (The ".mat" extension for gretl matrix files is not compulsory; you can name these files as you wish.)

It's also possible to take more control over the details of the transfer if you wish. You have the built-in string variable `$dotdir` in gretl, while in R you have the same variable under the name `gretl.dotdir`. To use a location other than `$dotdir` you may (a) omit the third argument to `mwwrite` and supply a full path to the matrix file, and (b) use a more generic approach to reading the file in R. Here's an example:

Gretl side:

```
mwwrite(A, "/path/to/mymatfile.mat")
```

R side:

```
A <- as.matrix(read.table("/path/to/mymatfile.mat", skip=1))
```

Passing data from R to gretl

For passing data in the opposite direction, gretl defines a special function that can be used in the R environment. An R object will be written as a temporary file in `$dotdir`, from where it can be easily retrieved from within gretl.

The name of this function is `gretl.export()`; it takes one required argument, the object to be exported. At present, the objects that can be exported with this method are matrices, data frames and time-series objects. The function creates a text file, by default with the same name as the exported object (plus an appropriate suffix), in gretl's temporary directory. Data frames and time-series objects are stored as CSV files, and can be retrieved by using gretl's `append` command. Matrices are stored in a special text format that is understood by gretl (see section 17.7); the file suffix is in this case `.mat`, and to read the matrix in gretl you must use the `mread()` function.

This function also has an optional second argument, namely a string which specifies a basename for the export file, in case you want to use a name other than that attached to the object within R. As in the default case an appropriate suffix, `.csv` or `.mat`, will be added to the basename.

As an example, we take the airline data and use them to estimate a structural time series model à la [Harvey \(1989\)](#).⁴ The model we will use is the *Basic Structural Model* (BSM), in which a time series is decomposed into three terms:

$$y_t = \mu_t + \gamma_t + \varepsilon_t$$

where μ_t is a trend component, γ_t is a seasonal component and ε_t is a noise term. In turn, the following is assumed to hold:

$$\begin{aligned}\Delta\mu_t &= \beta_{t-1} + \eta_t \\ \Delta\beta_t &= \zeta_t \\ \Delta_s\gamma_t &= \Delta\omega_t\end{aligned}$$

where Δ_s is the seasonal differencing operator, $(1 - L^s)$, and η_t , ζ_t and ω_t are mutually uncorrelated white noise processes. The object of the analysis is to estimate the variances of the noise components (which may be zero) and to recover estimates of the latent processes μ_t (the “level”), β_t (the “slope”) and γ_t .

We will use R’s `StructTS` command and import the results back into gretl. Once the `bjg` dataset is loaded in gretl, we pass the data to R and execute the following script:

```
# extract the log series
y <- gretldata[, "lg"]
# estimate the model
strmod <- StructTS(y)
# save the fitted components (smoothed)
compon <- as.ts(tsSmooth(strmod))
# save the estimated variances
vars <- as.matrix(strmod$coef)

# export into gretl's temp dir
gretl.export(compon)
gretl.export(vars)
```

Running this script via gretl produces minimal output:

```
current data loaded as ts object "gretldata"
wrote /home/cottrell/.gretl/compon.csv
wrote /home/cottrell/.gretl/vars.mat
```

However, we are now able to pull the results back into gretl by executing the following commands, either from the console or by creating a small script:

```
string fname = sprintf("%s/compon.csv", $dotdir)
append @fname
vars = mread("vars.mat", 1)
```

The first command reads the estimated time-series components from a CSV file, which is the format that the passing mechanism employs for series. The matrix `vars` is read from the file `vars.mat`.

After the above commands have been executed, three new series will have appeared in the gretl workspace, namely the estimates of the three components; by plotting them together with the original data, you should get a graph similar to Figure 44.6. The estimates of the variances can be seen by printing the `vars` matrix, as in

```
? print vars
vars (4 x 1)
```

⁴The function package *StucTiSM* is available to handle this class of models natively in gretl.

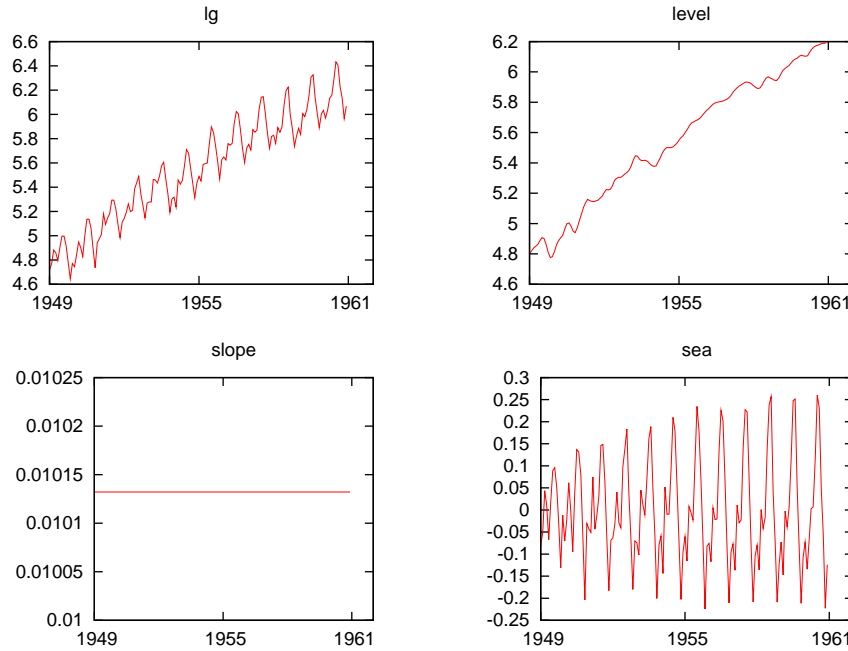


Figure 44.6: Estimated components from BSM

```
0.00077185
0.0000
0.0013969
0.0000
```

That is,

$$\hat{\sigma}_\eta^2 = 0.00077185, \quad \hat{\sigma}_\zeta^2 = 0, \quad \hat{\sigma}_\omega^2 = 0.0013969, \quad \hat{\sigma}_\varepsilon^2 = 0$$

Notice that, since $\hat{\sigma}_\zeta^2 = 0$, the estimate for β_t is constant and the level component is simply a random walk with a drift.

44.5 Interacting with R from the command line

Up to this point we have spoken only of interaction with R via the GUI program. In order to do the same from the command line interface, gretl provides the `foreign` command. This enables you to embed non-native commands within a gretl script.

A “foreign” block takes the form

```
foreign language=R [--send-data[=list]] [--quiet]
... R commands ...
end foreign
```

and achieves the same effect as submitting the enclosed R commands via the GUI in the non-interactive mode (see section 44.3 above). The `--send-data` option arranges for auto-loading of the data present in the gretl session, or a subset thereof specified via a named list. The `--quiet` option prevents the output from R from being echoed in the gretl output.

Using this method, replicating the example in the previous subsection is rather easy: basically, all it takes is encapsulating the content of the R script in a `foreign...end foreign` block; see Listing 44.1.

Listing 44.1: Estimation of the Basic Structural Model – simple [\[Download ▼\]](#)

```

open bjg.gdt

foreign language=R --send-data
  y <- gretldata[, "lg"]
  strmod <- StructTS(y)
  compon <- as.ts(tsSmooth(strmod))
  vars <- as.matrix(strmod$coef)
  gretl.export(compon)
  gretl.export(vars)
end foreign

append @dotdir/compon.csv
rename level lg_level
rename slope lg_slope
rename sea lg_seas

vars = mread("vars.mat", 1)

```

The above syntax, despite being already quite useful by itself, shows its full power when it is used in conjunction with user-written functions. Listing 44.2 shows how to define a gretl function that calls R internally.

Listing 44.2: Estimation of the Basic Structural Model via a function [\[Download ▼\]](#)

```

function list RStructTS(series myseries)
  smpl ok(myseries) --restrict
  sx = argname(myseries)

  foreign language=R --send-data --quiet
    @sx <- gretldata[, "myseries"]
    strmod <- StructTS(@sx)
    compon <- as.ts(tsSmooth(strmod))
    gretl.export(compon)
  end foreign

  append @dotdir/compon.csv
  rename level @sx_level
  rename slope @sx_slope
  rename sea @sx_seas

  list ret = @sx_level @sx_slope @sx_seas
  return ret
end function

# ----- main -----

open bjg.gdt
list X = RStructTS(lg)

```

44.6 Performance issues with R

R is a large and complex program, which takes an appreciable time to initialize itself. In interactive use this not a significant problem, but if you have a gretl script that calls R repeatedly the cumulated start-up costs can become bothersome. To get around this, gretl calls the R shared library by preference; in this case the start-up cost is borne only once, on the first invocation of R code from within gretl.

Support for the R shared library is built into the gretl packages for MS Windows and OS X—but the advantage is realized only if the library is in fact available at run time. If you are building gretl yourself on Linux and wish to make use of the R library, you should ensure (a) that R has been built with the shared library enabled (specify `--enable-R-shlib` when configuring your build of R), and (b) that the `pkg-config` program is able to detect your R installation. We do not link to the R library at build time, rather we open it dynamically on demand. The gretl GUI has an item under the Tools/Preferences menu which enables you to select the path to the library, if it is not detected automatically.

If you have the R shared library installed but want to force gretl to call the R executable instead, you can do

```
set R_lib off
```

44.7 Further use of the R library

Besides improving performance, as noted above, use of the R shared library makes possible a further refinement. That is, you can define functions in R, within a `foreign` block, then call those functions later in your script much as if they were gretl functions. This is illustrated below.

```
set R_functions on
foreign language=R
  plus_one <- function(q) {
    z = q+1
    invisible(z)
  }
end foreign

scalar b=R.plus_one(2)
```

The R function `plus_one` is obviously trivial in itself, but the example shows a couple of points. First, for this mechanism to work you need to enable `R_functions` via the `set` command. Second, to avoid collision with the gretl function namespace, calls to functions defined in this way must be prefixed with “R.”, as in `R.plus_one`. (But please note, this mechanism will not work if you have defined a gretl bundle named R: in that case identifiers beginning with “R.” will be understood as referring to members of the bundle in question.)

Built-in R functions may also be called in this way, once `R_functions` is set on. For example one can invoke R's `choose` function, which computes binomial coefficients:

```
set R_functions on
scalar b = R.choose(10,4)
```

The use of R functions from within gretl is limited by the need for an unambiguous and lossless mapping between R and gretl data-types (both for arguments passed by gretl and for return values generated by R). So far, the following possibilities are supported (see chapter 11 for details on the definition of types on the gretl side):

- The most basic types—real scalars, real matrices and (single) strings—can be pushed in either direction no problem. Since gretl 2023b, row and column names will be preserved when transferring matrices.

- A `series` in gretl can be pushed to R as a vector. If the gretl series is string-valued (see chapter 16), R will receive the string values.
- Gretl's arrays of strings can be pushed to R as vectors of strings, and vice versa.
- Gretl's bundles can be pushed to R as "lists", with tags naming the elements, and R's lists can be retrieved as gretl bundles provided that their elements have a corresponding gretl type and are identified by tags. But this is subject to the restriction that a gretl bundle passed to R cannot contain instances of the gretl `list` type (or arrays of anything other than strings).

Chapter 45

Gretl and Ox

45.1 Introduction


Ox, written by Jurgen A. Doornik (see [Doornik, 2007](#)), is described by its author as “an object-oriented statistical system. At its core is a powerful matrix language, which is complemented by a comprehensive statistical library. Among the special features of Ox are its speed [and] well-designed syntax. . . . Ox comes in two versions: Ox Professional and Ox Console. Ox is available for Windows, Linux, Mac (OS X), and several Unix platforms.” (www.doornik.com)

Ox is proprietary, closed-source software. The command-line version of the program is, however, available free of charge for academic users. Quoting again from Doornik’s website: “The Console (command line) versions may be used freely for academic research and teaching purposes only. . . . The Ox syntax is public, and, of course, you may do with your own Ox code whatever you wish.” If you wish to use Ox in conjunction with gretl please refer to [doornik.com](http://www.doornik.com) for further details on licensing.

As the reader will no doubt have noticed, most other software that we discuss in this Guide is open-source and freely available for all users. We make an exception for Ox on the grounds that it is indeed fast and well designed, and that its statistical library—along with various add-on packages that are also available—has exceptional coverage of cutting-edge techniques in econometrics. The gretl authors have used Ox for benchmarking some of gretl’s more advanced features such as dynamic panel models and state space models.¹

45.2 Ox support in gretl

The support offered for Ox in gretl is similar to that offered for R, as discussed in chapter 44.

 To enable support for Ox, go to the Tools/Preferences/General menu item and look under the Programs tab. Find the entry for the path to the `oxl` executable, that is, the program that runs Ox files (on MS Windows it is called `oxl.exe`). Adjust the path if it’s not already right for your system and you should be ready to go.

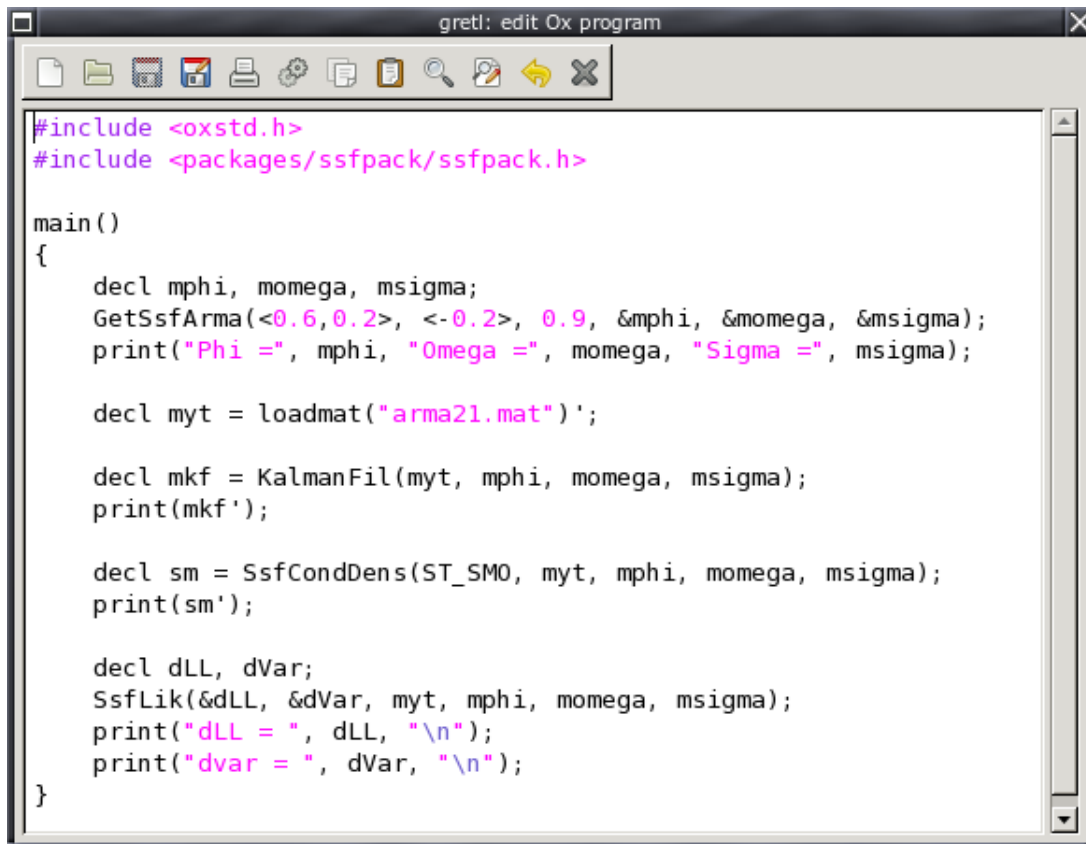
With support enabled, you can open and edit Ox programs in the gretl GUI. Clicking the “execute” icon in the editor window will send your code to Ox for execution. Figures 45.1 and Figure 45.2 show an Ox program and part of its output.

In addition you can embed Ox code within a gretl script using a `foreign` block, as described in connection with R. A trivial example, which simply prints the gretl data matrix within Ox, is shown in Listing 45.1.

The listing illustrates how a matrix can be passed from gretl to Ox. We use the `mwrite` function to write a matrix into the user’s “dotdir” (see section 15.2), then in Ox we use the function `gretl_loadmat` to retrieve the matrix.

How does `gretl_loadmat` come to be defined? When gretl writes out the Ox program corresponding to your `foreign` block it does two things in addition. First, it writes a small utility file named `gretl_io.ox` into your dotdir. This contains a definition for `gretl_loadmat` and also for the function `gretl_export` (see below). Second, gretl interpolates into your Ox code a line which in-

¹For a review of Ox, see [Cribari-Neto and Zarkos \(2003\)](#) and for a (somewhat dated) comparison of Ox with other matrix-oriented packages such as GAUSS, see [Steinhaus \(1999\)](#).



```

#include <oxstd.h>
#include <packages/ssfpack/ssfpack.h>

main()
{
    decl mphi, momega, msigma;
    GetSsfArma(<0.6,0.2>, <-0.2>, 0.9, &mphi, &momega, &msigma);
    print("Phi =", mphi, "Omega =", momega, "Sigma =", msigma);

    decl myt = loadmat("arma21.mat");

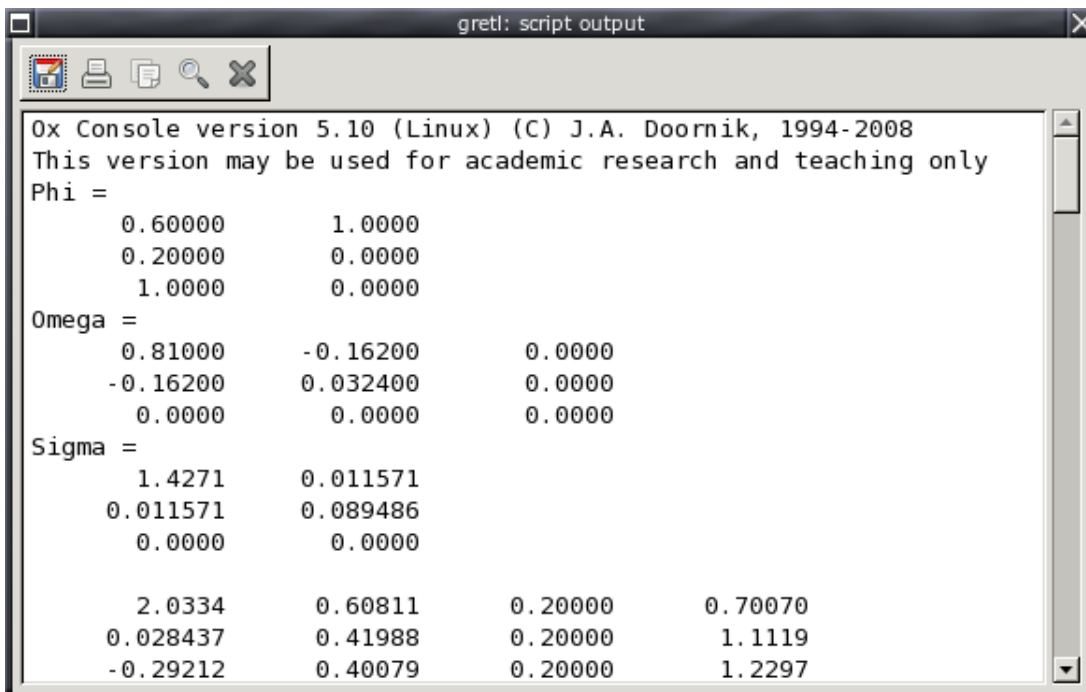
    decl mkf = KalmanFil(myt, mphi, momega, msigma);
    print(mkf');

    decl sm = SsfCondDens(ST_SMO, myt, mphi, momega, msigma);
    print(sm');

    decl dLL, dVar;
    SsfLik(&dLL, &dVar, myt, mphi, momega, msigma);
    print("dLL = ", dLL, "\n");
    print("dvar = ", dVar, "\n");
}

```

Figure 45.1: Ox editing window



```

Ox Console version 5.10 (Linux) (C) J.A. Doornik, 1994-2008
This version may be used for academic research and teaching only
Phi =
    0.60000    1.0000
    0.20000    0.0000
    1.0000    0.0000
Omega =
    0.81000   -0.16200    0.0000
   -0.16200    0.032400   0.0000
    0.0000    0.0000    0.0000
Sigma =
    1.4271    0.011571
    0.011571    0.089486
    0.0000    0.0000

    2.0334    0.60811    0.20000    0.70070
    0.028437    0.41988    0.20000    1.1119
   -0.29212    0.40079    0.20000    1.2297

```

Figure 45.2: Output from Ox

Listing 45.1: Simple example of Ox usage

```

open data4-1
matrix m = {dataset}
mwrite(m, "gretl.mat", 1)

foreign language=Ox
#include <oxstd.h>
main()
{
    decl gmat = gretl_loadmat("gretl.mat");
    print(gmat);
}
end foreign

```

cludes this utility file (it is inserted right after the inclusion of `oxstd.h`, which is needed in all Ox programs). Note that `gretl_loadmat` expects to find the named file in the user's dotdir.

45.3 Illustration: replication of DPD model

Listing 45.2 shows a more ambitious case. This script replicates one of the dynamic panel data models in [Arellano and Bond \(1991\)](#), first using `gretl` and then using `Ox`; we then check the relative differences between the parameter estimates produced by the two programs (which turn out to be reassuringly small). This was last tested using version 9.10 of `Ox` console for Linux.

Unlike the previous example, in this case we pass the dataset from `gretl` to `Ox` as a CSV file in order to preserve the variable names. Note the use of the internal variable `csv_na` to get the right representation of missing values for use with `Ox`—and also note that the `--send-data` option for the `foreign` command is not available in connection with `Ox`.

We get the parameter estimates back from `Ox` using `gretl_export` on the `Ox` side and `mread` on the `gretl` side. The `gretl_export` function takes two arguments, a matrix and a file name. The file is written into the user's dotdir, from where it can be picked up using `mread`. The final portion of the output from Listing 45.2 is shown below:

```

? matrix oxparm = mread("oxparm.mat", 1)
Generated matrix oxparm
? eval abs((parm - oxparm) ./ oxparm)
1.1094e-12
1.6314e-12
1.7885e-13
1.1949e-12
1.8999e-13
1.1359e-13
6.5339e-13
3.1943e-12
1.2108e-12
3.7335e-13
1.7468e-12
3.9536e-12
2.0980e-12

```

Listing 45.2: Estimation of dynamic panel data model via gretl and Ox [\[Download ▼\]](#)

```

open abdata.gdt

# 1-step GMM estimation
dpanel 2 ; n w w(-1) k ys ys(-1) 0 --time-dummies --dpdstyle
matrix parm = $coeff

# Write CSV file for Ox
set csv_na .NaN
store @dotdir/abdata.csv

# Replicate using the Ox DPD package
foreign language=Ox
#include <oxstd.h>
#import <packages/DPD/dpd>

main ()
{
    decl dpd = new DPD();
    dpd.Load("@dotdir/abdata.csv");
    dpd.SetYear("YEAR");

    dpd.Select(DPD::Y_VAR, {"n", 0, 2});
    dpd.Select(DPD::X_VAR, {"w", 0, 1, "k", 0, 0, "ys", 0, 1});
    dpd.Select(DPD::I_VAR, {"w", 0, 1, "k", 0, 0, "ys", 0, 1});

    dpd.Gmm("n", 2, 99); // GMM-type instrument
    dpd.SetDummies(DPD::D_CONSTANT + DPD::D_TIME);
    dpd.SetTest(2, 2); // Sargan, AR 1-2 tests
    dpd.Estimate(); // 1-step estimation
    decl parm = dpd.GetPar();
    gretl_export(parm, "oxparm.mat");

    delete dpd;
}
end foreign

# Compare the results
matrix oxparm = mread("oxparm.mat", 1)
eval abs((parm - oxparm) ./ oxparm)

```

Chapter 46

Gretl and Octave

46.1 Introduction

GNU Octave, written by John W. Eaton and others, is described as “a high-level language, primarily intended for numerical computations.” The program is oriented towards “solving linear and nonlinear problems numerically” and “performing other numerical experiments using a language that is mostly compatible with Matlab.” (www.gnu.org/software/octave) Octave is available in source-code form (naturally, for GNU software) and also in the form of binary packages for MS Windows and Mac OS X. Numerous contributed packages that extend Octave’s functionality in various ways can be found at octave.sf.net.

46.2 Octave support in gretl

The support offered for Octave in gretl is similar to that offered for R (chapter 44). For example, you can open and edit Octave scripts in the gretl GUI. Clicking the “execute” icon in the editor window will send your code to Octave for execution. Figures 46.1 and Figure 46.2 show an Octave script and its output; in this example we use the function `logistic_regression` to replicate some results from [Greene \(2000\)](#).

In addition you can embed Octave code within a gretl script using a `foreign` block, as described in connection with R. A trivial example is shown below: it simply loads and prints the gretl data matrix within Octave, then takes it back to gretl and checks for any difference (there should be none). (Note that in Octave, appending “;” to a line suppresses verbose output; leaving off the semicolon results in printing of the object that is produced, if any.)

```
open data4-1
matrix m = {dataset}
mwrite(m, "gretl.mat", 1)

foreign language=Octave
    gmat = gretl_loadmat("gretl.mat")
    gretl_export(gmat, "octave.mat")
end foreign

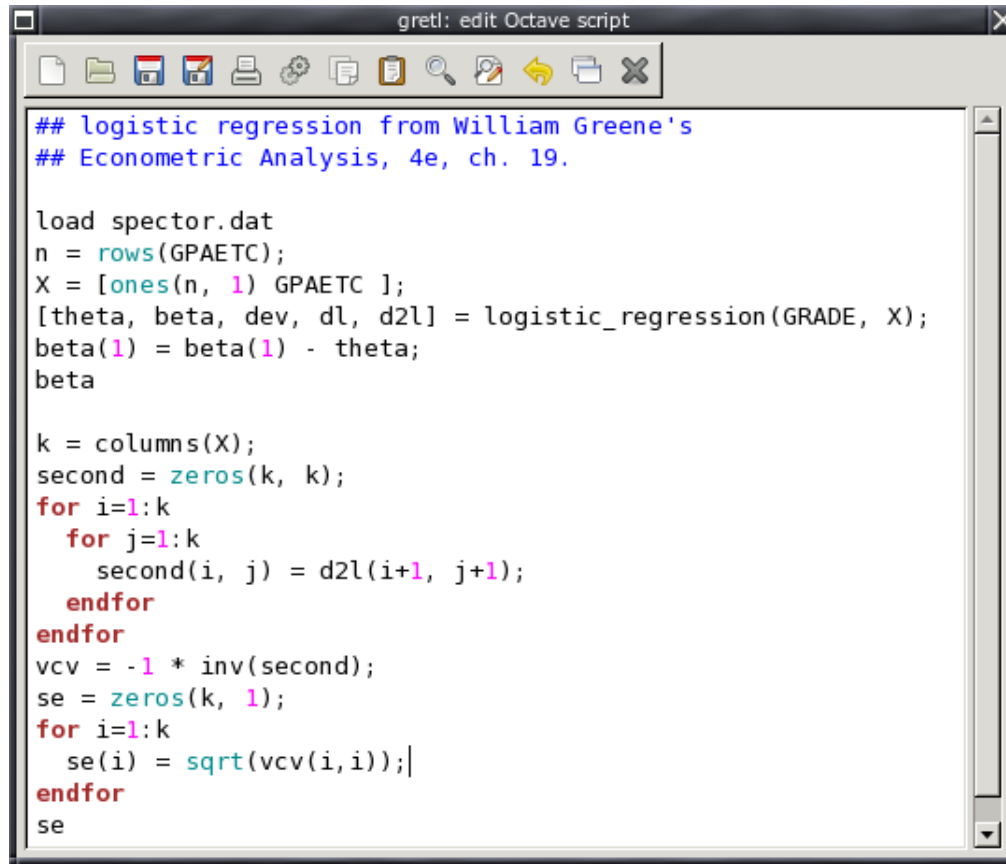
matrix chk = mread("octave.mat", 1)
eval maxr(maxc(abs(m - chk)))
```

The functions `gretl_loadmat` and `gretl_export`, which are predefined when you run Octave from within gretl, have the following signatures:

```
function A = gretl_loadmat(fname, autodot=1)

function gretl_export(X, fname, autodot=1)
```

By default traffic in matrices goes via the user’s “dotdir” (see section 15.2) on the Octave side; that is, the name of this directory is prepended to `filename` for both reading and writing. (This is complementary to use of the `export` and `import` parameters with gretl’s `mwrite` and `mread` functions, respectively.) However, if you wish to take control over the reading and writing locations

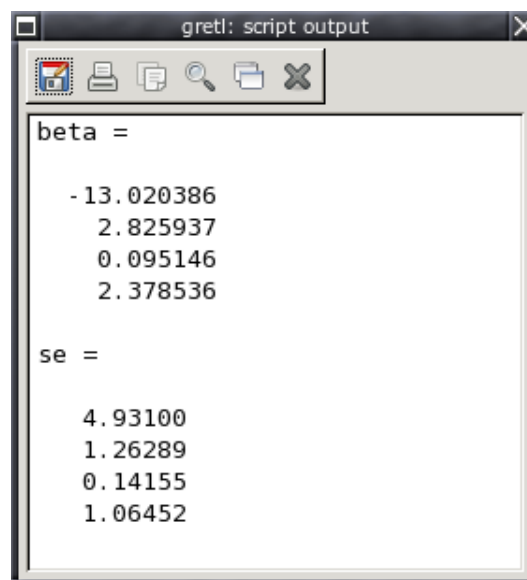
A screenshot of the 'gretl: edit Octave script' window. It features a standard toolbar with icons for file operations (new, open, save, print, etc.) and editing (undo, redo, search). The script content is as follows:

```
## logistic regression from William Greene's
## Econometric Analysis, 4e, ch. 19.

load spector.dat
n = rows(GPAETC);
X = [ones(n, 1) GPAETC ];
[theta, beta, dev, dl, d2l] = logistic_regression(GRADE, X);
beta(1) = beta(1) - theta;
beta

k = columns(X);
second = zeros(k, k);
for i=1:k
    for j=1:k
        second(i, j) = d2l(i+1, j+1);
    endfor
endfor
vcv = -1 * inv(second);
se = zeros(k, 1);
for i=1:k
    se(i) = sqrt(vcv(i,i));
endfor
se
```

Figure 46.1: Octave editing window

A screenshot of the 'gretl: script output' window. It displays the results of the Octave script execution. The output is organized into two sections: 'beta =' and 'se =', each followed by a column vector of four numerical values.

```
beta =

-13.020386
  2.825937
  0.095146
  2.378536

se =

 4.93100
 1.26289
 0.14155
 1.06452
```

Figure 46.2: Output from Octave

you can supply a zero value for `autodot` (or give an absolute path) when calling `gretl_loadmat` and `gretl_export`: in that case the `filename` argument is used as is.

46.3 Illustration: spectral methods

We now present a more ambitious example which exploits Octave's handling of the frequency domain (and also its ability to use code written for MATLAB), namely estimation of the spectral coherence of two time series. For this illustration we require two extra Octave packages from octave.sf.net, namely those supporting spectral functions (`specfun`) and signal processing (`signal`). After downloading the packages you can install them from within Octave as follows (using version numbers as of March 2010):

```
pkg install specfun-1.0.8.tar.gz
pkg install signal-1.0.10.tar.gz
```

In addition we need some specialized MATLAB files made available by Mario Forni of the University of Modena, at http://morgana.unimore.it/forni_mario/matlab.htm. The files needed are `coheren2.m`, `coheren.m`, `coher.m`, `cospec.m`, `crosscov.m`, `crosspec.m`, `crosspe.m` and `spec.m`. These are in a form appropriate for MS Windows. On Linux you could run the following shell script to get the files and remove the Windows end-of-file character (which prevents the files from running under Octave):

```
SITE=http://morgana.unimore.it/forni_mario/MYPROG
# download files and delete trailing Ctrl-Z
for f in \
  coheren2.m \
  coheren.m \
  coher.m \
  cospec.m \
  crosscov.m \
  crosspec.m \
  crosspe.m \
  spec.m ; do
  wget $SITE/$f && \
  cat $f | tr -d '\032' > tmp.m && mv tmp.m $f
done
```

The Forni files should be placed in some appropriate directory, and you should tell Octave where to find them by adding that directory to Octave's `loadpath`. On Linux this can be done via an entry in one's `~/.octaverc` file. For example

```
addpath("~/stats/octave/forni");
```

Alternatively, an `addpath` directive can be written into the Octave script that calls on these files.

With everything set up on the Octave side we now write a `gretl` script (see Listing 46.1) which opens a time-series dataset, constructs and writes a matrix containing two series, and defines a `foreign` block containing the Octave statements needed to produce the spectral coherence matrix. This matrix is exported via `gretl_export` and picked up using `mread`. Finally, we produce a graph from the matrix in `gretl`. In the script this is sent to the screen; Figure 46.3 shows the same graph in PDF format.

Listing 46.1: Estimation of spectral coherence via Octave

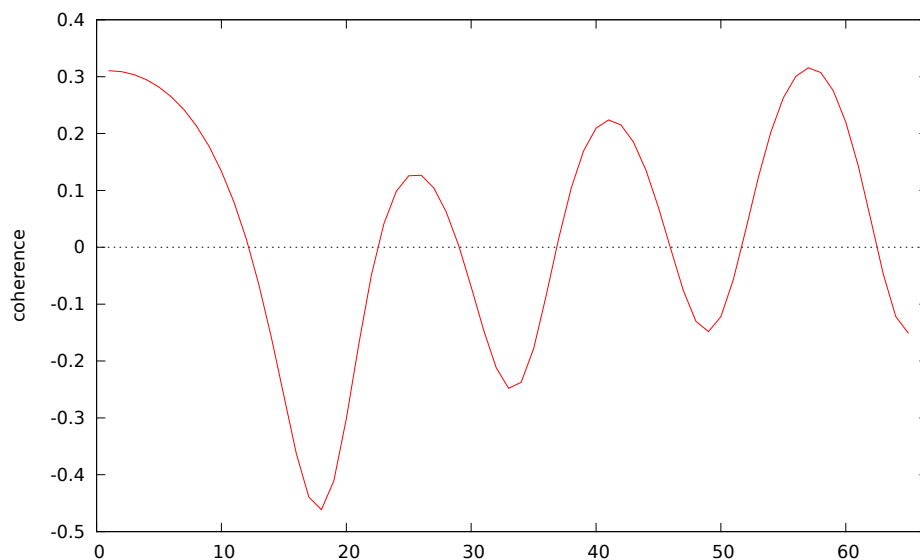
```

open data9-7
matrix xy = {PRIME, UNEMP}
mwrite(xy, "xy.mat", 1)

foreign language=Octave
  pkg load signal
  # uncomment and modify the following if necessary
  # addpath("~/stats/octave/forni");
  xy = gretl_loadmat("xy.mat");
  x = xy(:,1);
  y = xy(:,2);
  # note: the last parameter is the Bartlett window size
  h = coher(x, y, 8);
  gretl_export(h, "h.mat");
end foreign

h = mread("h.mat", 1)
cnameset(h, "coherence")
gnuplot 1 --time-series --with-lines --matrix=h --output=display


```

**Figure 46.3:** Spectral coherence estimated via Octave

Chapter 47

Gretl and Stata

Stata (www.stata.com) is closed-source, proprietary (and expensive) software and as such is not a natural companion to gretl. Nonetheless, given Stata's popularity it is desirable to have a convenient way of comparing results across the two programs, and to that end we provide some support for Stata code under the `foreign` command.

 To enable support for Stata, go to the Tools/Preferences/General menu item and look under the Programs tab. Find the entry for the path to the Stata executable. Adjust the path if it's not already right for your system and you should be ready to go.

The following example illustrates what's available. You can send the current gretl dataset to Stata using the `--send-data` flag. And having defined a matrix within Stata you can export it for use with gretl via the `gretl_export` command: this takes two arguments, the name of the matrix to export and the filename to use; the file is written to the user's "dotdir", from where it can be retrieved using the `mread()` function.¹ To suppress printed output from Stata you can add the `--quiet` flag to the `foreign` block.

Listing 47.1: Comparison of clustered standard errors with Stata [\[Download ▼\]](#)

```
function matrix stata_reorder (matrix se)
  # stata puts the intercept last, but gretl puts it first
  scalar n = rows(se)
  return se[n] | se[1:n-1]
end function

open data4-1
ols 1 0 2 3 --cluster=bedrms
matrix se = $stderr

foreign language=stata --send-data
  regress price sqft bedrms, vce(cluster bedrms)
  matrix vcv = e(V)
  gretl_export vcv "vcv.mat"
end foreign

matrix stata_vcv = mread("vcv.mat", 1)
stata_se = stata_reorder(sqrt(diag(stata_vcv)))
matrix check = se - stata_se
print check
```

In addition you can edit “pure” Stata scripts in the gretl GUI and send them for execution as with native gretl scripts.

Note that Stata coerces all variable names to lower-case on data input, so even if series names in

¹We do not currently offer the complementary functionality of `gretl_loadmat`, which enables reading of matrices written by gretl's `mwrite()` function in Ox and Octave. This is not at all easy to implement in Stata code.

gretl are upper-case, or of mixed case, it's necessary to use all lower-case in Stata. Also note that when opening a data file within Stata via the `use` command it will be necessary to provide the full path to the file.

Chapter 48

Gretl and Python

48.1 Introduction

According to www.python.org, Python is “an easy to learn, powerful programming language. It has efficient high-level data structures and a simple but effective approach to object-oriented programming. Python’s elegant syntax and dynamic typing, together with its interpreted nature, make it an ideal language for scripting and rapid application development in many areas on most platforms.”

Indeed, Python is widely used in a great variety of contexts. Numerous add-on modules are available; the ones likely to be of greatest interest to econometricians include NumPy (“the fundamental package for scientific computing with Python”—see www.numpy.org); SciPy (which builds on NumPy—see www.scipy.org); and Statsmodels (<http://statsmodels.sourceforge.net/>).

48.2 Python support in gretl

The support offered for Python in gretl is similar to that offered for Octave (chapter 46). You can open and edit Python scripts in the gretl GUI. Clicking the “execute” icon in the editor window will send your code to Python for execution. In addition you can embed Python code within a gretl script using a `foreign` block, as described in connection with R.

When you launch Python from within gretl one variable and two convenience functions are pre-defined, as follows.

```
gretl_dotdir
gretl_loadmat(filename, autodot=1)
gretl_export(M, filename, autodot=1)
```

The variable `gretl_dotdir` holds the path to the user’s “dot directory.” The first function loads a matrix of the given `filename` as written by gretl’s `mwrite` function, and the second writes matrix `M`, under the given `filename`, in the format wanted by gretl.

By default the traffic in matrices goes via the dot directory on the Python side; that is, the name of this directory is prepended to `filename` for both reading and writing. (This is complementary to use of the `export` and `import` parameters with gretl’s `mwrite` and `mread` functions, respectively.) However, if you wish to take control over the reading and writing locations you can supply a zero value for `autodot` (or give an absolute path) when calling `gretl_loadmat` and `gretl_export`: in that case the `filename` argument is used as is.

Note that `gretl_loadmat` and `gretl_export` depend on NumPy; they make use of the functions `loadtxt` and `savetxt` respectively. Nonetheless, the presence of NumPy is not an absolute requirement if you don’t need to use these two functions.

48.3 Illustration: linear regression with multicollinearity

Listing 48.1 compares the numerical accuracy of gretl’s `ols` command with that of the function `linalg.lstsq` in NumPy, using the notorious Longley test data which exhibit extreme multicollinearity. Unlike some econometrics packages, NumPy does a good job on these data. The script computes and prints the log-relative error in estimation of the regression coefficients, using

the NIST-certified values as a benchmark;¹ the error values correspond to the number of correct digits (with a maximum of 15). The results will likely differ somewhat by computer architecture and compiler.

Listing 48.1: Comparing regression results with Python [\[Download ▼\]](#)

```

set verbose off

function matrix logrel_err (const matrix est, const matrix true)
  return -log10(abs(est - true) ./ abs(true))
end function

open longley.gdt -q
list LX = prdefl .. year
ols employ 0 LX -q
matrix b_gretl = $coeff

mwrite({employ} ~ {const} ~ {LX}, "alldata.mat", 1)

foreign language=python
  import numpy as np
  X = gretl_loadmat('alldata.mat', 1)
  # NumPy's OLS
  b = np.linalg.lstsq(X[:,1:], X[:,0])[0]
  gretl_export(np.transpose(np.matrix(b)), 'py_b.mat', 1)
end foreign

# NIST's certified coefficient values
matrix b_nist = {-3482258.63459582, 15.0618722713733,
  -0.358191792925910E-01, -2.02022980381683,
  -1.03322686717359, -0.511041056535807E-01,
  1829.15146461355}'

matrix b_numpy = mread("py_b.mat", 1)
matrix E = logrel_err(b_gretl, b_nist) ~ logrel_err(b_numpy, b_nist)
cnameset(E, "gretl python")
printf "Log-relative errors, Longley coefficients:\n\n%#12.5g\n", E
printf "Column means\n\n%#12.5g\n", meanc(E)

```

Output:

Log-relative errors, Longley coefficients:

	gretl	python
	12.844	12.850
	11.528	11.414
	12.393	12.401
	13.135	13.121
	13.738	13.318
	12.587	12.363
	12.848	12.852
Column means		
	12.725	12.617

¹See <http://www.itl.nist.gov/div898/strd/11s/data/Longley.shtml>.

Chapter 49

Gretl and Julia

49.1 Introduction

According to julia-lang.org, Julia is “a high-level, high-performance dynamic programming language for technical computing, with syntax that is familiar to users of other technical computing environments. It provides a sophisticated compiler, distributed parallel execution, numerical accuracy, and an extensive mathematical function library.” Julia is well known for being very fast; however, you should be aware that by default starting Julia takes some time due to Just-in-Time compilation of the input. This fixed cost is well worth bearing if you are asking Julia to perform a big computation, but small jobs are likely to run faster if you use the (Julia-specific) `--no-compile` option with the `foreign` command.¹

49.2 Julia support in gretl

The support offered for Julia in gretl is similar to that offered for Octave (chapter 46). You can open and edit Julia scripts in the gretl GUI. Clicking the “execute” icon in the editor window will send your code to Julia for execution. In addition you can embed Julia code within a gretl script using a `foreign` block, as described in connection with R.

When you launch Julia from within gretl one variable and two convenience functions are pre-defined, as follows.

```
gretl_dotdir  
gretl_loadmat(filename, autodot=true)  
gretl_export(M, filename, autodot=true)
```

The variable `gretl_dotdir` holds the path to the user’s “dot directory.” The first function loads a matrix of the given `filename` as written by gretl’s `mwrite` function, and the second writes matrix `M`, under the given `filename`, in the format wanted by gretl.

By default the traffic in matrices goes via the dot directory on the Julia side; that is, the name of this directory is prepended to `filename` for both reading and writing. (This is complementary to use of the `export` and `import` parameters with gretl’s `mwrite` and `mread` functions, respectively.) However, if you wish to take control over the reading and writing locations you can supply a zero value for `autodot` (or give an absolute path) when calling `gretl_loadmat` and `gretl_export`: in that case the `filename` argument is used as is.

49.3 Illustration

Listing 49.1 shows a minimal example of how to interact with Julia from a gretl script.

Since this is a very small job JIT compilation is not worthwhile; in our testing the script runs almost 4 times faster if the Julia block is opened with

```
foreign language=julia --no-compile
```

This has the effect of passing the option `--compile=no` to the Julia executable.

¹Caveat: it seems that this option is not supported by all builds of Julia.

Listing 49.1: Simple Julia I/O example [\[Download ▼\]](#)

```

set verbose off

matrix A = mnormal(4,4)           # generate a random matrix
mwrite(A, "A", 1)                 # and save it to a file

foreign language=julia           # call Julia
    print("Hi from Julia!\n");    # output a string
    A = gretl_loadmat("A");        # grab the matrix from gretl
    gretl_export(inv(A), "iA.mat"); # and save its inverse
end foreign                       # go back to gretl

matrix iA = mread("iA.mat", 1)    # read the inverse from Julia
matrix check = A * iA             # compute the product
print check                       # print out the check (should be I)

```

Output (good approximation to identity matrix):

Hi from Julia!

check (4 x 4)

1.0000	6.9389e-18	1.6653e-16	1.6653e-16
0.0000	1.0000	0.0000	0.0000
-4.4409e-16	-8.3267e-17	1.0000	-6.6613e-16
-4.4409e-16	-1.3878e-17	-1.1102e-16	1.0000

Chapter 50

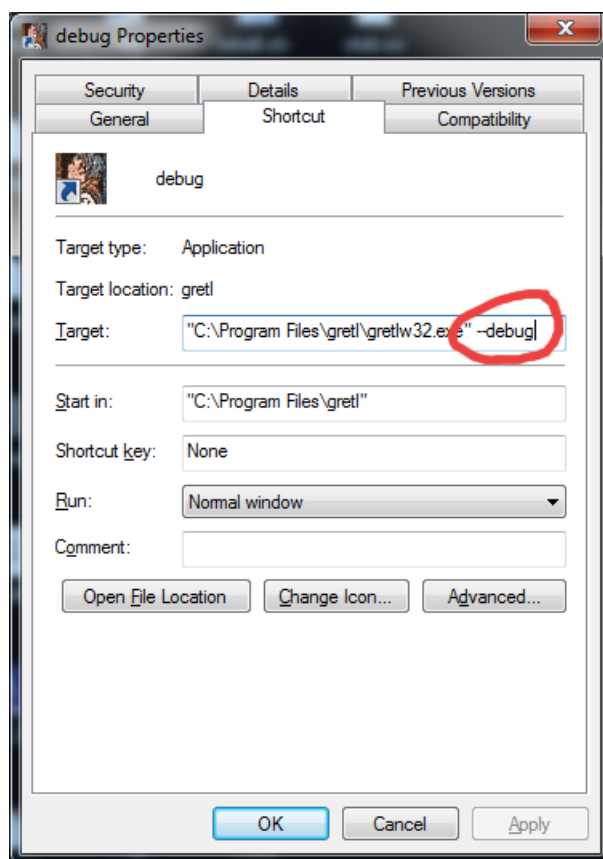
Troubleshooting gretl

50.1 Bug reports

Bug reports are welcome—well, if not exactly welcome then useful and appreciated. Hopefully, you are unlikely to find bugs in the actual calculations done by gretl (although this statement does not constitute any sort of warranty). You may, however, come across bugs or oddities in the behavior of the graphical interface. Please remember that the usefulness of bug reports is greatly enhanced if you can be as specific as possible: what *exactly* went wrong, under what conditions, and on what operating system? If you saw an error message, what precisely did it say?

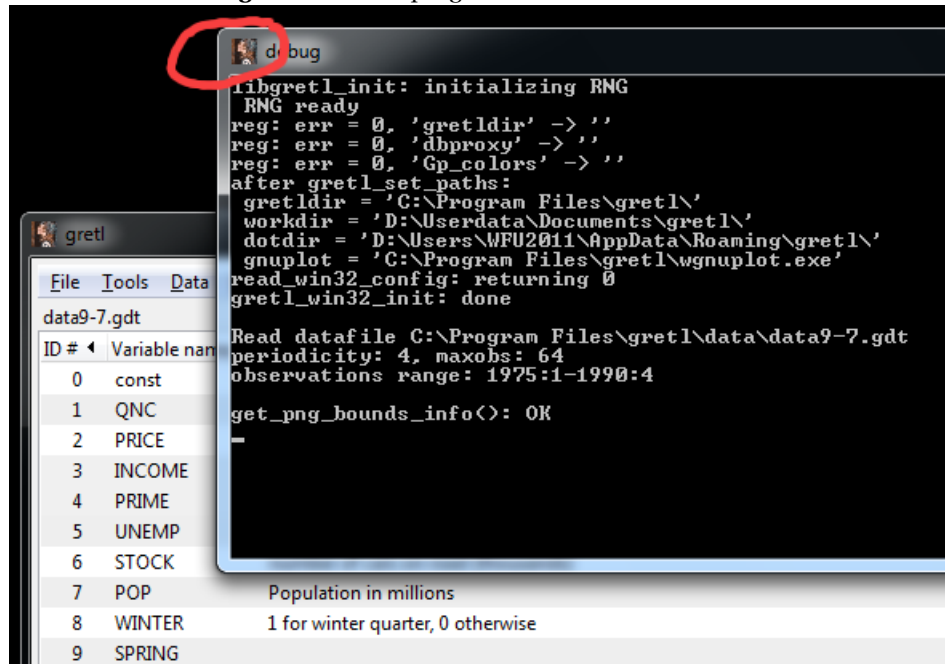
One way of making a bug report more useful is to run the program in such a way that you can see (and copy) any additional information that gets printed to the `stderr` output stream. On Linux and Mac OS X that's just a matter of launching gretl from the command prompt in a terminal window. On MS Windows it's a bit more complicated since `stderr` is by default “invisible.” However, you can quite easily set up a special gretl shortcut that does the job. On the Windows desktop, right-click and select “New shortcut.” In the dialog box that appears, browse to find `gretl.exe` and append the `--debug` flag, as shown in Figure 50.1. Note that there are two dashes before “debug”.

Figure 50.1: Creating a debugging shortcut



When you start gretl in this mode, a “console window” appears as well as the gretl window, and `stderr` output goes to the console. To copy this output, click at the top left of the console window for a menu (Figure 50.2): first do “Select all”, then “Copy.” You can paste the results into Notepad or similar.

Figure 50.2: The program with console window



50.2 Auxiliary programs

As mentioned above, gretl calls some other programs to accomplish certain tasks (gnuplot for graphing, L^AT_EX for high-quality typesetting of regression output, GNU R). If something goes wrong with such external links, it is not always easy for gretl to produce an informative error message. If such a link fails when accessed from the gretl graphical interface, you may be able to get more information by starting gretl from the command prompt rather than via a desktop menu entry or icon. On the X window system, start gretl from the shell prompt in an xterm; on MS Windows, start the program `gretl.exe` from a console window or “DOS box” using the `-g` or `--debug` option flag. Additional error messages may be displayed on the terminal window.

Also please note that for most external calls, gretl assumes that the programs in question are available in your “path”—that is, that they can be invoked simply via the name of the program,¹ Thus if a given program fails, try the experiment of typing the program name at the command prompt, as shown below.

	<i>Graphing</i>	<i>Typesetting</i>	<i>GNU R</i>
X window system	gnuplot	pdflatex	R
MS Windows	wgnuplot.exe	pdflatex	RGui.exe

If the program fails to start from the prompt, it’s not a gretl issue but rather that the program’s home directory is not in your path, or the program is not installed (properly). For details on modifying your path please see the documentation or online help for your operating system or shell.

¹The exception to this rule is the invocation of gnuplot under MS Windows, where a full path to the program is given.

Chapter 51

The command line interface

The gretl package includes the command-line program gretlcli. On Linux it can be run from a terminal window (xterm, rxvt, or similar), or at the text console. Under MS Windows it can be run in a console window (sometimes inaccurately called a “DOS box”). gretlcli has its own help file, which may be accessed by typing “help” at the prompt. It can be run in batch mode, sending output directly to a file (see also the *Gretl Command Reference*).

If gretlcli is linked to the readline library (this is automatically the case in the MS Windows version; also see Appendix B), the command line is recallable and editable, and offers command completion. You can use the Up and Down arrow keys to cycle through previously typed commands. On a given command line, you can use the arrow keys to move around, in conjunction with Emacs editing keystrokes.¹ The most common of these are:

<i>Keystroke</i>	<i>Effect</i>
Ctrl-a	go to start of line
Ctrl-e	go to end of line
Ctrl-d	delete character to right

where “Ctrl-a” means press the “a” key while the “Ctrl” key is also depressed. Thus if you want to change something at the beginning of a command, you *don’t* have to backspace over the whole line, erasing as you go. Just hop to the start and add or delete characters. If you type the first letters of a command name then press the Tab key, readline will attempt to complete the command name for you. If there’s a unique completion it will be put in place automatically. If there’s more than one completion, pressing Tab a second time brings up a list.

Probably the most useful mode for heavy-duty work with gretlcli is batch (non-interactive) mode, in which the program reads and processes a script, and sends the output to file. For example

```
gretlcli -b scriptfile > outputfile
```

Note that *scriptfile* is treated as a program argument; only the output file requires redirection (>). Don’t forget the -b (batch) switch, otherwise the program will wait for user input after executing the script (and if output is redirected, the program will appear to “hang”).

¹Actually, the key bindings shown below are only the defaults; they can be customized. See the [readline manual](#).

Part IV

Appendices

Appendix A

Data file details

A.1 Basic native format

In gretl's basic native data format—for which we use the suffix `gdt`—a dataset is stored in XML (extensible mark-up language). Data files correspond to the simple DTD (document type definition) given in `gretldata.dtd`, which is supplied with the gretl distribution and is installed in the system data directory (e.g. `/usr/share/gretl/data` on Linux.) Such files may be plain text (uncompressed) or gzipped. They contain the actual data values plus additional information such as the names and descriptions of variables, the frequency of the data, and so on.

In a `gdt` file the actual data values are written to 17 significant figures (for generated data such as logs or pseudo-random numbers) or to a maximum of 15 figures for primary data. The C `printf` format `“%. *g”` is used (for `* = 17` or `15`) so that trailing zeros are not printed.

Most users will probably not have need to read or write such files other than via gretl itself, but if you want to manipulate them using other software tools you should examine the DTD and also take a look at a few of the supplied practice data files: `data4-1.gdt` gives a simple example; `data4-10.gdt` is an example where observation labels are included.

A.2 Binary data file format

A native binary format is also available for dataset storage. This format—with suffix `gdtb`—offers *much* faster writing and reading for very large datasets. For small to moderately sized datasets (say, up to a few megabytes) there is little advantage in the binary format and we recommend use of plain `gdt`. Note that `gdtb` files are saved in the endianness of the machine on which they're written and are not portable across platforms of differing endianness, but since almost all machines on which gretl is likely to be run are little-endian this is unlikely to be a serious limitation. The implementation of `gdtb` format can be found in `purebin.c`, in the `plugin` subdirectory of the gretl source tree.

Prior to version 2021b of gretl, `gdtb` files had a different structure, namely a PKZIP file containing an XML component for the metadata plus a binary component for the actual data values. It turned out that this hybrid format did not scale well for datasets with a great deal of metadata. For backward compatibility gretl can still read such old-style files but it doesn't write them any more.

A.3 Native database format

A gretl database has two primary parts: a plain text index file (with filename suffix `.idx`) containing information on the included series, and a binary file (suffix `.bin`) containing the actual data. Two examples of the format for an entry in the `idx` file are shown below:

```
GOM910  Composite index of 11 leading indicators (1987=100)
M 1948.01 - 1995.11  n = 575
currbal Balance of Payments: Balance on Current Account; SA
Q 1960.1 - 1999.4  n = 160
```

The first field is the series name. The second is a description of the series (maximum 128 characters). On the second line the first field is a frequency code: M for monthly, Q for quarterly, A for

annual, B for business-daily (daily with five days per week), D for 7-day daily, S for 6-day daily, U for undated. No other frequencies are accepted at present.

Then comes the starting date (with two digits following the point for monthly data, one for quarterly data, none for annual), a space, a hyphen, another space, the ending date, the string “n = ” and the integer number of observations. In the case of daily data the starting and ending dates should be given in the ISO 8601 form, YYYY-MM-DD. This format must be respected exactly.

Optionally, the first line of the index file may contain a short comment (up to 64 characters) on the source and nature of the data, following a hash mark. For example:

```
# Federal Reserve Board (interest rates)
```

The corresponding binary database file holds the data values, represented as “floats”, that is, single-precision floating-point numbers taking four bytes apiece. The values are packed “by variable”, so that the first n numbers are the observations of variable 1, the next m the observations on variable 2, and so on.

A third file may accompany the `idx` and `bin` files, namely a “codebook” containing a description of the data. If present, this must be plain text, with filename suffix `.cb`, or PDF with suffix `.pdf`.

The components of a gretl database are generally combined in a single file, with `zlib` compression and `.gz` suffix, for distribution. A small program named `gretlzip` can be used to create or unpack such files. See the `utils/dbzip` subdirectory of the gretl source tree.

Appendix B

Building gretl

Here we give instructions detailed enough to allow a user with only a basic knowledge of a Unix-type system to build gretl. These steps were tested on a fresh installation of Debian Etch. For other Linux distributions (especially Debian-based ones, like Ubuntu and its derivatives) little should change. Other Unix-like operating systems such as Mac OS X and BSD would probably require more substantial adjustments.

In this guided example, we will build gretl complete with documentation. This introduces a few more requirements, but gives you the ability to modify the documentation files as well, like the help files or the manuals.

B.1 Installing the prerequisites

We assume that the basic GNU utilities are already installed on the system, together with these other programs:

- some $\text{T}_{\text{E}}\text{X}/\text{L}_{\text{A}}\text{T}_{\text{E}}\text{X}$ system (texlive will do beautifully)
- Gnuplot
- ImageMagick

We also assume that the user has administrative privileges and knows how to install packages. The examples below are carried out using the `apt-get` shell command, but they can be performed with menu-based utilities like `aptitude`, `dselect` or the GUI-based program `synaptic`. Users of Linux distributions which employ rpm packages (e.g. Red Hat/Fedora, Mandriva, SuSE) may want to refer to the [dependencies](#) page on the gretl website.

The first step is installing the C compiler and related basic utilities, if these are not already in place. On a Debian (or derivative) system, these are contained in a bunch of packages that can be installed via the command

```
apt-get install gcc autoconf automake1.9 libtool flex bison gcc-doc \
libc6-dev libc-dev gfortran gettext pkgconfig
```

Then it is necessary to install the “development” (dev) packages for the libraries that gretl uses:

<i>Library</i>	<i>command</i>
GLIB	<code>apt-get install libglib2.0-dev</code>
GTK 3.0	<code>apt-get install libgtk3.0-dev</code>
PNG	<code>apt-get install libpng12-dev</code>
XSLT	<code>apt-get install libxslt1-dev</code>
LAPACK	<code>apt-get install liblapack-dev</code>
FFTW	<code>apt-get install libfftw3-dev</code>
READLINE	<code>apt-get install libreadline-dev</code>
ZLIB	<code>apt-get install zlib1g-dev</code>
XML	<code>apt-get install libxml2-dev</code>
GMP	<code>apt-get install libgmp-dev</code>
CURL	<code>apt-get install libcurl4-gnutls-dev</code>
MPFR	<code>apt-get install libmpfr-dev</code>

It is possible to substitute GTK 2.0 for GTK 3.0. The dev packages for these libraries are necessary to *compile* gretl—you’ll also need the plain, non-dev library packages to *run* gretl, but most of these should already be part of a standard installation. In order to enable other optional features, like audio support, you may need to install more libraries.

☞ The above steps can be much simplified on Linux systems that provide deb-based package managers, such as Debian and its derivatives (Ubuntu, Knoppix and other distributions). The command

```
apt-get build-dep gretl
```

will download and install all the necessary packages for building the version of gretl that is currently present in your APT sources. Technically, this does not guarantee that all the software necessary to build the git version is included, because the version of gretl on your repository may be quite old and build requirements may have changed in the meantime. However, the chances of a mismatch are rather remote for a reasonably up-to-date system, so in most cases the above command should take care of everything correctly.

B.2 Getting the source: release or git

At this point, it is possible to build from the source. You have two options here: obtain the latest released source package, or retrieve the current git version of gretl (git = the version control software currently in use for gretl). The usual caveat applies to the git version, namely, that it may not build correctly and may contain “experimental” code; on the other hand, git often contains bug-fixes relative to the released version. If you want to help with testing and to contribute bug reports, we recommend using git gretl.

To work with the released source:

1. Download the gretl source package from gretl.sourceforge.net.
2. Unzip and untar the package. On a system with the GNU utilities available, the command would be `tar xvfJ gretl-N.tar.xz` (replace N with the specific version number of the file you downloaded at step 1).
3. Change directory to the gretl source directory created at step 2 (e.g. `gretl-2020a`).
4. Proceed to the next section, “Configure and make”.

To work with git you’ll first need to install the git client program if it’s not already on your system. Relevant resources you may wish to consult include the main git website at git-scm.com and instructions specific to gretl: [gretl git basics](#).

When grabbing the git sources *for the first time*, you should first decide where you want to store the code. For example, you might create a directory called `git` under your home directory. Open a terminal window, `cd` into this directory, and type the following commands:

```
git clone git://git.code.sf.net/p/gretl/git gretl-git
```

At this point git should create a subdirectory named `gretl-git` and fill it with the current sources. When you want to *update the source*, this is very simple: just move into the `gretl-git` directory and type

```
git pull
```

Assuming you're now in the `gretl-git` directory, you can proceed in the same manner as with the released source package.

B.3 Configure the source

The next command you need is `./configure`; this is a complex script that detects which tools you have on your system and sets things up. The `configure` command accepts many options; you may want to run

```
./configure --help
```

first to see what options are available. One option you may wish to tweak is `--prefix`. By default the installation goes under `/usr/local` but you can change this. For example

```
./configure --prefix=/usr
```

will put everything under the `/usr` tree.

Note that the recommended location to build gretl is *not* in the source directory. The way to achieve that is quite simple: the invocation of the `configure` script has to take into account the relative path to the source tree. So if your build directory is inside (underneath) the source tree it is

```
../configure
```

while if it is in a parallel tree it would be (something like):

```
../gretl-git/configure
```

If you have a multi-core machine you may want to activate support for OpenMP, which permits the parallelization of matrix multiplication and some other tasks. This requires adding the `configure` flag

```
--enable-openmp
```

By default the gretl GUI is built using version 3.0 of the GTK library, if available, otherwise version 2.0. If you have both versions installed and prefer to use GTK 2.0, use the flag

```
--enable-gtk2
```

In order to have the documentation built, we need to pass the relevant option to `configure`, as in

```
--enable-build-doc
```

But please note that this option will work only if you are using the git source.

☞ In order to build the documentation, there is the possibility that you will have to install some extra software on top of the packages mentioned in the previous section. For example, you may need some extra \LaTeX packages to compile the manuals. Two of the required packages, that not every standard \LaTeX installation include, are typically `pifont.sty` and `appendix.sty`. You could install the corresponding packages from your distribution or you could simply download them from CTAN and install them by hand.

This, for example, if you want to install under `/usr`, with OpenMP support, and also build the documentation, you would do

```
./configure --prefix=/usr \
--enable-openmp \
--enable-build-doc
```

You will see a number of checks being run, and if everything goes according to plan, you should see a summary similar to that displayed in Listing B.1.

Listing B.1: Sample output from `./configure`

Configuration:

```
Installation path:           /usr
Use readline library:       yes
Use gnuplot for graphs:     yes
Use LaTeX for typesetting output: yes
Use libgsf for zip/unzip:   no
sse2 support for RNG:       yes
OpenMP support:             yes
MPI support:                no
AVX support for arithmetic: no
Build with GTK version:     2.0
Build gretl documentation:  yes
Use Lucida fonts:          no
Build message catalogs:    yes
X-12-ARIMA support:         yes
TRAMO/SEATS support:        yes
libR support:               yes
ODBC support:               no
Experimental audio support: no
Use xdg-utils in installation: if DESTDIR not set
LAPACK libraries:
    -llapack -lblas -lgfortran
```

Now type `'make'` to build gretl.

You can also do `'make pdfdocs'` to build the PDF documentation.

☞ If you're using git, it's a good idea to re-run the configure script after doing an update. This is not always necessary, but sometimes it is, and it never does any harm. For this purpose, you may want to write a little shell script that calls configure with any options you want to use.

B.4 Build and install

We are now ready to undertake the compilation proper: this is done by running the `make` command, which takes care of compiling all the necessary source files in the correct order. All you need to do

is type

```
make
```

This step will likely take several minutes to complete; a lot of output will be produced on screen. Once this is done, you can install your freshly baked copy of gretl on your system via

```
make install
```

On most systems, the `make install` command requires you to have administrative privileges. Hence, either you log in as `root` before launching `make install` or you may want to use the `sudo` utility, as in:

```
sudo make install
```

Now try if everything works: go back to your home directory and run gretl

```
cd ~  
gretl &
```

If all is well, you ought to see gretl start, at which point just exit the program in the usual way. On the other hand, there is the possibility that gretl doesn't start and instead you see a message like

```
/usr/local/bin/gretl_x11: error while loading shared libraries:  
libgretl-1.0.so.0: cannot open shared object file: No such file or directory
```

In this case, just run

```
sudo ldconfig
```

The problem should be fixed once and for all.

Appendix C

Numerical accuracy

Gretl uses double-precision arithmetic throughout—except for the multiple-precision plugin invoked by the menu item “Model, Other linear models, High precision OLS” which represents floating-point values using a number of bits given by the environment variable GRETL_MP_BITS (default value 256).

The normal equations of Least Squares are by default solved via Cholesky decomposition, which is highly accurate provided the matrix of cross-products of the regressors, $X'X$, is not very ill conditioned. If this problem is detected, gretl automatically switches to use QR decomposition.

The program has been tested rather thoroughly on the statistical reference datasets provided by NIST (the U.S. National Institute of Standards and Technology) and a full account of the results may be found on the gretl website (follow the link “Numerical accuracy”).

To date, two published reviews have discussed gretl’s accuracy: Giovanni Baiocchi and Walter Di-taso (2003), and Talha Yalta and Yasemin Yalta (2007). We are grateful to these authors for their careful examination of the program. Their comments have prompted several modifications including the use of Stephen Moshier’s *cephes* code for computing p-values and other quantities relating to probability distributions (see netlib.org), changes to the formatting of regression output to ensure that the program displays a consistent number of significant digits, and attention to compiler issues in producing the MS Windows version of gretl (which at one time was slightly less accurate than the Linux version).

Gretl now includes a “plugin” that runs the NIST linear regression test suite. You can find this under the “Tools” menu in the main window. When you run this test, the introductory text explains the expected result. If you run this test and see anything other than the expected result, please send a bug report to cottrell@wfu.edu.

All regression statistics are printed to 6 significant figures in the current version of gretl (except when the multiple-precision plugin is used, in which case results are given to 12 figures). If you want to examine a particular value more closely, first save it (for example, using the `genr` command) then print it using `printf`, to as many digits as you like (see the *Gretl Command Reference*).

Appendix D

Related free software

Gretl's capabilities are substantial, and are expanding. Nonetheless you may find there are some things you can't do in gretl, or you may wish to compare results with other programs. If you are looking for complementary functionality in the realm of free, open-source software we recommend the following programs. The self-description of each program is taken from its website.

- **GNU R** r-project.org: "R is a system for statistical computation and graphics. It consists of a language plus a run-time environment with graphics, a debugger, access to certain system functions, and the ability to run programs stored in script files... It compiles and runs on a wide variety of UNIX platforms, Windows and MacOS." Comment: There are numerous add-on packages for R covering most areas of statistical work.
- **GNU Octave** www.octave.org: "GNU Octave is a high-level language, primarily intended for numerical computations. It provides a convenient command line interface for solving linear and nonlinear problems numerically, and for performing other numerical experiments using a language that is mostly compatible with Matlab. It may also be used as a batch-oriented language."
- **Julia** julialang.org: "Julia is a high-level, high-performance dynamic programming language for technical computing, with syntax that is familiar to users of other technical computing environments. It provides a sophisticated compiler, distributed parallel execution, numerical accuracy, and an extensive mathematical function library."
- **JMulTi** www.jmulti.de: "JMulTi was originally designed as a tool for certain econometric procedures in time series analysis that are especially difficult to use and that are not available in other packages, like Impulse Response Analysis with bootstrapped confidence intervals for VAR/VEC modelling. Now many other features have been integrated as well to make it possible to convey a comprehensive analysis." Comment: JMulTi is a java GUI program: you need a java run-time environment to make use of it.

As mentioned above, gretl offers the facility of exporting data in the formats of both Octave and R. In the case of Octave, the gretl data set is saved as a single matrix, X. You can pull the X matrix apart if you wish, once the data are loaded in Octave; see the Octave manual for details. As for R, the exported data file preserves any time series structure that is apparent to gretl. The series are saved as individual structures. The data should be brought into R using the `source()` command.

In addition, gretl has a convenience function for moving data quickly into R. Under gretl's "Tools" menu, you will find the entry "Start GNU R". This writes out an R version of the current gretl data set (in the user's gretl directory), and sources it into a new R session. The particular way R is invoked depends on the internal gretl variable `Rcommand`, whose value may be set under the "Tools, Preferences" menu. The default command is `RGui.exe` under MS Windows. Under X it is `xterm -e R`. Please note that at most three space-separated elements in this command string will be processed; any extra elements are ignored.

Appendix E

Listing of URLs

Below is a listing of the full URLs of websites mentioned in the text.

Estima (RATS) <http://www.estima.com/>
FFTW3 <http://www.fftw.org/>
Gnome desktop homepage <http://www.gnome.org/>
GNU Multiple Precision (GMP) library <http://gmplib.org/>
CURL library <http://curl.haxx.se/libcurl/>
GNU Octave homepage <http://www.octave.org/>
GNU R homepage <http://www.r-project.org/>
GNU R manual <http://cran.r-project.org/doc/manuals/R-intro.pdf>
Gnuplot homepage <http://www.gnuplot.info/>
Gretl data page http://gretl.sourceforge.net/gretl_data.html
Gretl homepage <http://gretl.sourceforge.net/>
GTK+ homepage <http://www.gtk.org/>
GTK+ port for win32 <https://wiki.gnome.org/Projects/GTK/Win32/>
InfoZip homepage <http://www.info-zip.org/pub/infozip/zlib/>
JMulTi homepage <http://www.jmulti.de/>
JRSOFTWARE <http://www.jrsoftware.org/>
Julia homepage <http://julialang.org/>
Mingw (gcc for win32) homepage <http://www.mingw.org/>
Minpack <http://www.netlib.org/minpack/>
Penn World Table <http://pwt.econ.upenn.edu/>
Readline homepage <http://cnswww.cns.cwru.edu/~chet/readline/rltop.html>
Readline manual <http://cnswww.cns.cwru.edu/~chet/readline/readline.html>
Xmlsoft homepage <http://xmlsoft.org/>

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